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Authors	Cavuoti, S.; BRESCIA, Massimo; TORTORA, CRESCENZO; Longo, G.; NAPOLITANO, NICOLA ROSARIO; et al.
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Machine-learning-based photometric redshifts for galaxies of the ESO Kilo-Degree Survey data release 2

S. Cavuoti,^{1*} M. Brescia,¹ C. Tortora,¹ G. Longo,² N. R. Napolitano,¹ M. Radovich,³ F. La Barbera,¹ M. Capaccioli,⁴ J. T. A. de Jong,⁵ F. Getman,¹ A. Grado¹ and M. Paolillo²

¹*Astronomical Observatory of Capodimonte – INAF, via Moiariello 16, I-80131, Napoli, Italy*

²*Department of Physics, University Federico II, via Cinthia 6, I-80126 Napoli, Italy*

³*Astronomical Observatory of Padua, vicolo dell’ Osservatorio 5, I-35122 Padova, Italy*

⁴*VSTCen – INAF, via Moiariello 16, I-80131, Napoli, Italy*

⁵*Leiden Observatory, Leiden University, PO Box 9513, NL-2300 RA Leiden, the Netherlands*

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ABSTRACT

We have estimated photometric redshifts (z_{phot}) for more than 1.1 million galaxies of the public European Southern Observatory (ESO) Kilo-Degree Survey (KiDS) data release 2. KiDS is an optical wide-field imaging survey carried out with the Very Large Telescope (VLT) Survey Telescope (VST) and the OmegaCAM camera, which aims to tackle open questions in cosmology and galaxy evolution, such as the origin of dark energy and the channel of galaxy mass growth. We present a catalogue of photometric redshifts obtained using the Multi-Layer Perceptron with Quasi-Newton Algorithm (MLPQNA) model, provided within the framework of the DATA Mining and Exploration Web Application RESOURCE (DAMEWARE). These photometric redshifts are based on a spectroscopic knowledge base that was obtained by merging spectroscopic data sets from the Galaxy and Mass Assembly (GAMA) data release 2 and the Sloan Digital Sky Survey III (SDSS-III) data release 9. The overall 1σ uncertainty on $\Delta z = (z_{\text{spec}} - z_{\text{phot}})/(1 + z_{\text{spec}})$ is ~ 0.03 , with a very small average bias of ~ 0.001 , a normalized median absolute deviation of ~ 0.02 and a fraction of catastrophic outliers ($|\Delta z| > 0.15$) of ~ 0.4 per cent.

Key words: techniques: photometric – galaxies: distances and redshifts – galaxies: photometry.

1 INTRODUCTION

Photometric redshifts (z_{phot}) derived from multiband digital surveys are crucial to a variety of cosmological applications (Scranton et al. 2005; Hennawi et al. 2006; Myers et al. 2006; Giannantonio et al. 2008). In the last few years, a plethora of methods has been developed to estimate z_{phot} (see Hildebrandt et al. 2010), but the advent of a new generation of photometric surveys – to quote just a few, the Panoramic Survey Telescope and Rapid Response System (Pan-STARRS; Kaiser 2004), *Euclid* (Laureijs et al. 2011) and the Kilo-Degree Survey¹ (KiDS; de Jong et al. 2013) – demands higher accuracy (Brescia et al. 2014b).

The evaluation of photometric redshifts requires the mapping of the photometric space into the spectroscopic redshift space. All methods, one way or the other, require the use of a knowledge

base (KB) consisting of a set of templates, and differ mainly in the following aspects: (i) the way in which the KB is constructed (spectroscopic redshifts or, rather, empirically or theoretically derived spectral energy distributions or SEDs); (ii) the adopted interpolation/fitting algorithm. Methods based on the interpolation of a spectroscopic KB are usually labelled as empirical.

Many different implementations of empirical methods exist and we shall recall just a few: (i) polynomial fitting (Connolly et al. 1995); (ii) nearest neighbours (Csabai et al. 2003); (iii) neural networks (D’Abrusco, Longo & Walton 2007; Yéche et al. 2010, and references therein); (iv) support vector machines (Wadadekar 2005); (v) regression trees (Carliles et al. 2010); (vi) Gaussian processes (Way & Srivastava 2006; Bonfield et al. 2010); (vii) diffusion maps (Freeman et al. 2009).

In this paper, we discuss the derivation of photometric redshifts for the galaxies in the KiDS data release 2 (DR2; de Jong et al. 2015). KiDS is a European Southern Observatory (ESO) public survey, based on the Very Large Telescope (VLT) Survey Telescope (VST; Capaccioli & Schipani 2011) with the OmegaCAM camera

*E-mail: stefano.cavuoti@gmail.com; cavuoti@na.astro.it

¹ <http://kids.strw.leidenuniv.nl>

(Kuijken 2011), which will image 1500 deg² in four filters (u , g , r , i), in single epochs per filter. The high spatial resolution of the VST (0.2 arcsec pixel⁻¹), and the photometric depth and area covered make it a front-edge tool for weak gravitational lensing and galaxy evolution studies. The measurement of unbiased and high-quality z_{phot} is a crucial step to pursue many of the scientific goals that have motivated KiDS (de Jong et al. 2015).

We present z_{phot} for a sample of ~ 1.1 million galaxies. These redshifts were derived with the Multi-Layer Perceptron with Quasi-Newton Algorithm (MLPQNA) method, described in detail elsewhere (Brescia et al. 2012, 2013), and hence we refer to those articles for all mathematical and technical details. Recently, this method has also been used to derive a catalogue of z_{phot} for the entire Sloan Digital Sky Survey data release 9 (SDSS DR9; Brescia et al. 2014b). In the PHoto- z Accuracy Testing 1 (PHAT1) contest (Hildebrandt et al. 2010), which blindly compared most existing methods to estimate z_{phot} on a very limited KB (~ 500 objects only), the MLPQNA method proved to be one of the best empirical methods to date (Cavuoti et al. 2012). However, it is worth noticing that in the PHAT1 contest, MLPQNA did not perform as well as many SED fitting methods, because of the very limited KB available. This situation reverses when significantly larger KBs properly sampling the photometric parameter space become available (Brescia et al. 2013, 2014b).

The MLPQNA model is publicly available in the Data Mining and Exploration Web Application Resource infrastructure (DAMEWARE; Brescia et al. 2014a) and has also been implemented in the PhotoRaptor service package (Cavuoti et al. 2015).

The paper is organized as follows. In Section 2, we present the data set, while in Section 3, we describe and discuss the experiments and related outcome. In Section 4, we give a description of the resulting photometric redshift catalogue. Finally, in Section 5, we draw our conclusions and future prospects.

2 THE DATA

The sample of galaxies for which we provide z_{phot} was extracted from the second data release of the public ESO KiDS. A detailed description of all the steps followed to extract the catalogues is given in de Jong et al. (2015). KiDS is a wide-area optical imaging survey in the four filters (u , g , r , i), carried out with the VST and the OmegaCAM camera. The KiDS observation strategy consists of a standard diagonal dithering pattern (five dithers in g , r and i and four in u) in order to minimize the effect of the inter-CCD gaps in the OmegaCAM science array. Therefore, the final footprint of each single tile is slightly larger than the nominal 1 deg² (de Jong et al. 2015).

The data-processing procedure used is based on the Astro-WISE (AW) optical pipeline (McFarland et al. 2013). After the first basic data reduction steps (such as cross-talk, de-biasing and overscan correction, flat-fielding, illumination correction, de-fringing, pixel masking, satellite-track removal and background subtraction), the pipeline performs photometric and astrometric calibrations.

Source extraction is based on a task provided in the AW environment, KiDS-CAT (de Jong et al. 2015), based on algorithms developed for the software 2DPHOT (La Barbera et al. 2008). KiDS-CAT automatically performs a seeing assessment of the image, using best-quality stars in the image, and subsequently optimizes the configuration files of SEXTRACTOR (Bertin & Arnouts 1996) to perform the source extraction in the individual bands. In this process, besides the photometric flag provided by SEXTRACTOR, detected sources are

also flagged according to their proximity to star spikes and haloes (IMAFLAGS_ISO flag), which are identified in the KiDS images through a dedicated masking procedure (de Jong et al. 2015; see also Huang et al. in preparation).

In order to derive our photometric redshifts, we used the multi-band source catalogues, which rely on the double-image mode of SEXTRACTOR. These catalogues are based on source detection in the r -band images. While magnitudes are measured in all filters, the star-galaxy separation, as well as the source positional and shape parameters, are based on the r -band data only. The choice of the r band as a reference is motivated by the fact that it is observed under the best seeing conditions (~ 0.7 arcsec seeing FWHM, on average), and therefore it typically has the best image quality, thus providing the most reliable source positions and shapes. Aperture photometry in the four bands within several aperture radii, together with MAG_AUTO, shape parameters and flags, are available from SEXTRACTOR and KiDS-CAT. In the final catalogue, in order to maximize the sample with the z_{phot} estimates available, we have retained $\sim 10^7$ sources with the r -band SEXTRACTOR flag $\text{FLAGS}_r < 4$ and rejected $\sim 2 \times 10^5$ objects having close and bright companion sources, affected by bad pixels or originally blended with other objects; see Bertin & Arnouts (1996) for a detailed description of extraction flags. The limiting magnitudes of KiDS catalogues² at the 1σ level are

$$\begin{aligned} \text{MAGAP}_{4,u} &= 25.17, & \text{MAGAP}_{6,u} &= 24.74, \\ \text{MAGAP}_{4,g} &= 26.03, & \text{MAGAP}_{6,g} &= 25.61, \\ \text{MAGAP}_{4,r} &= 25.89, & \text{MAGAP}_{6,r} &= 25.44, \\ \text{MAGAP}_{4,i} &= 24.53, & \text{MAGAP}_{6,i} &= 24.06. \end{aligned}$$

KiDS DR2 contains 148 tiles observed in all filters during the first two years of operations. From the original catalogue of ~ 18 million sources, the star-galaxy separation leaves ~ 10 million galaxies, of which ~ 6 million have null IMAFLAGS_ISO in all the filters (i.e. they are observed in unmasked regions). Out of these, we succeeded in estimating z_{phot} for 1 142 992 sources (see Section 4 for details).

In order to build the needed spectroscopic KB, the KiDS galaxy sample was matched with two independent spectroscopic surveys: the Galaxy and Mass Assembly (GAMA) and the SDSS. The final spectroscopic sample was obtained by merging data from GAMA data release 2 (112k new redshifts in the first three years; Driver et al. 2011, Liske et al. in preparation) and SDSS-III DR9 (Ahn et al. 2012, 2014; Bolton et al. 2012; Chen et al. 2012). The redshift distribution of the mixed catalogue is shown in Fig. 1.

GAMA observes galaxies out to $z = 0.5$ and $r < 19.8$ (r -band Petrosian magnitude), by reaching a spectroscopic completeness of 98 per cent for the main survey targets. It also provides information about the quality of the redshift determination by using the probabilistically defined normalized redshift quality scale nQ . The redshifts with $nQ > 2$ are the most reliable (Driver et al. 2011; Hopkins et al. 2013).

For SDSS-III, we used the low z (LOWZ) and constant mass (CMASS) samples of the Baryon Oscillation Sky Survey (BOSS). The BOSS project aims to obtain spectra (redshifts) for 1.5 million luminous galaxies up to $z \sim 0.7$. The LOWZ sample consists of galaxies with $0.15 < z < 0.4$ with colours similar to those of luminous red galaxies (LRGs) at $z \gtrsim 0.4$. Objects were selected by

² We use the MAGAP_4 and MAGAP_6 magnitudes, measured within circular apertures of 4 and 6 arcsec of diameter, respectively. These magnitudes are provided within the produced z_{phot} catalogue.

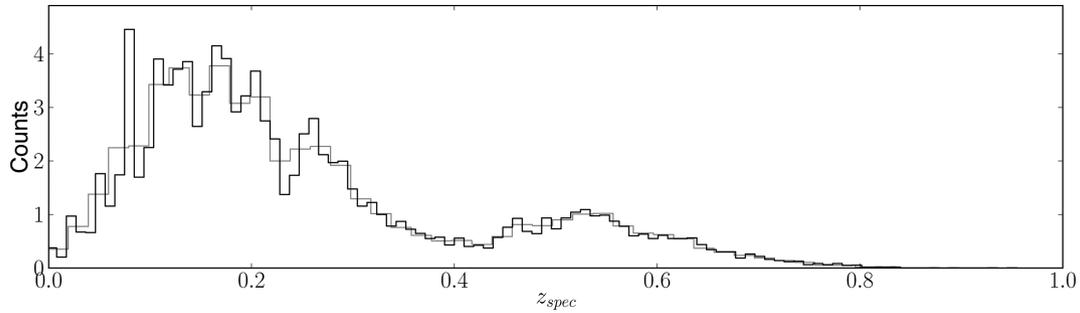


Figure 1. Spectroscopic redshift distribution of objects included in the training set (black line) and test set (grey line) normalized to the splitting rate.

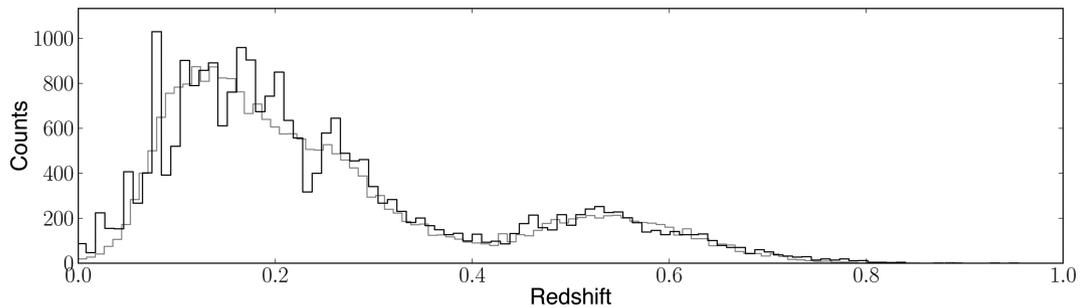


Figure 2. Redshift distribution of objects included in the blind test set, spectroscopic (black line) and photometric (grey line).

applying suitable cuts on magnitudes and colours with the aim of extending the SDSS LRG sample towards fainter magnitudes/higher redshifts (e.g. Ahn et al. 2012; Bolton et al. 2012).

The CMASS sample contains three times more galaxies than the LOWZ sample, and was designed to select galaxies in the range $0.4 < z < 0.8$. The rest-frame colour distribution of the CMASS sample is significantly broader than that of the LRG sample, and thus the CMASS sample contains a nearly complete sample of massive galaxies down to $\log M_*/M_\odot \sim 11.2$. The faintest galaxies are at $r = 19.5$ in the LOWZ sample and at $i = 19.9$ in the CMASS sample.

Our spectroscopic sample is therefore dominated by galaxies from GAMA (46, 603 versus 1, 618 from SDSS) at low- z ($z \lesssim 0.4$), while SDSS galaxies dominate the higher redshift regime (out to $z \sim 0.7$), with $r < 22$.

3 EXPERIMENTS AND DISCUSSION

Dealing with machine-learning-supervised methods, it is common practice to select and use the available KB to build a minimum of three disjoint data subsets: (i) a data set to train the method looking for the correlation hidden in the photometric information among the input features necessary to perform the regression (known as the training set); (ii) a validation set to be used to check and verify the training performance against a loss of generalization capabilities (a phenomenon also known as overfitting); (iii) finally, a test set needed to blindly evaluate the overall performances of the model with data samples never submitted to the model previously.

In this work, the validation process was embedded into the training phase, by applying the standard leave-one-out k -fold cross-validation mechanism (Geisser 1975). We would like to stress that none of the objects included in the training (and validation) sample

was included in the test sample and only the test data were used to generate the statistics and scatter plots.

We created training and test samples with relative sizes of 60 per cent (36 222 objects) and 40 per cent (24 150 objects) by randomly drawing without replacement from the KB. The histogram in Fig. 1 shows the distribution of the KB as a function of z_{spec} in both the training and test sets, while in Fig. 2 the distribution of z_{spec} and z_{phot} in the blind test set is shown. As can be seen, the three distributions are in almost perfect agreement.

The results were evaluated using a standard set of statistical indicators applied to the quantity $\Delta z = (z_{\text{spec}} - z_{\text{phot}})/(1 + z_{\text{spec}})$:

- (i) the bias, defined as the mean value of the residuals Δz ;
- (ii) the standard deviation (σ) of the residuals;
- (iii) the *NMAD* of the residuals, defined as $NMAD(\Delta z) = 1.48 \times \text{median}(|\Delta z|)$.

As input photometric parameters (or features), we used the MAGAP_4 and MAGAP_6 aperture magnitudes (u, g, r, i), a choice that was based on our past experience, as almost always this combination leads to the best performances (Brescia et al. 2013, 2014b). However, it needs to be emphasized that an improvement in the performances of a machine-learning method can be expected from an exhaustive exploration of the parameter space through feature selection (see Polsterer et al. 2014). However, this approach is usually too demanding in terms of computing time.

MLPQNA z_{phot} are in excellent agreement with z_{spec} , as we show in Figs 3 and 4, where the results of the experiment are summarized. The upper panel of Fig. 3 shows the predicted photometric redshift estimates versus the spectroscopic redshift values for all objects in the blind test set. In the lower panel of Fig. 3, z_{spec} is plotted versus the residuals Δz . The underpopulated redshift bins, visible

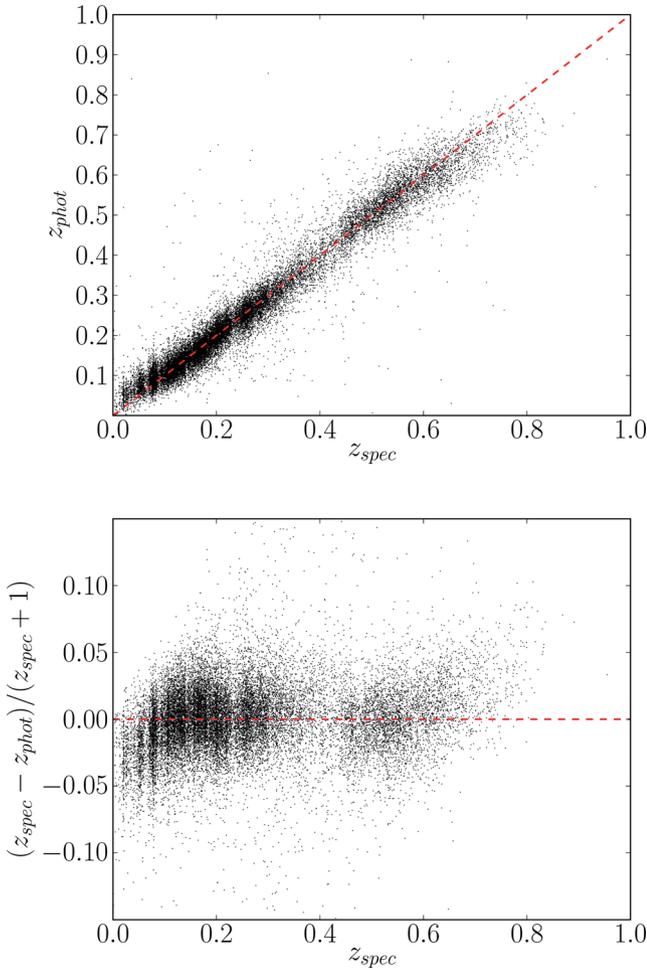


Figure 3. Upper panel: spectroscopic versus photometric redshifts for objects of the blind test set. Lower panel: spectroscopic redshift versus $(z_{\text{spec}} - z_{\text{phot}})/(1 + z_{\text{spec}})$ for the same objects.

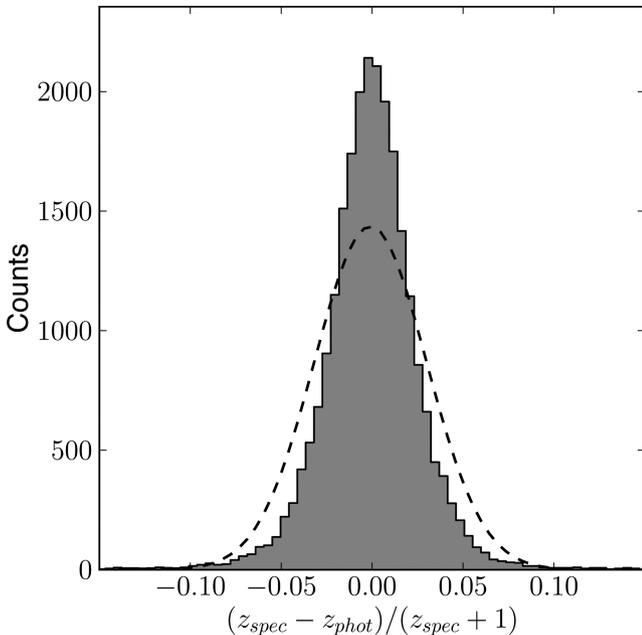


Figure 4. Histogram of $(z_{\text{spec}} - z_{\text{phot}})/(1 + z_{\text{spec}})$ for objects of the blind test set. The dashed line represents the Gaussian fit to the distribution.

in Fig. 3, reflect the distribution of the spectroscopic sample, which is less populated at redshifts ~ 0.22 and ~ 0.42 (see Figs 1 and 2).

In Fig. 4, we show the distribution of residuals, which has a kurtosis of 1.8 and a skewness of 7.07×10^{-16} (i.e. a leptokurtic and symmetric distribution), as already found in the SDSS DR9 case by applying the same method (Brescia et al. 2014b). In other words, the distribution reveals an overdensity of objects in its central region (i.e. objects with a small error), which also reflects the very low percentage of outliers and a low *NMAD* value (see below).

Overall, we find a bias of 9.9×10^{-4} , a standard deviation of 0.0305 and a *NMAD* of 0.021. The σ_{68} (i.e. the range in which 68 per cent of the residuals fall) is 0.022, smaller than the standard deviation, as has to be expected from a leptokurtic distribution. Moreover, our method leads to a very small fraction of outliers (i.e. less than 0.39 per cent and 3.30 per cent using the $|\Delta z| > 0.15$ and $|\Delta z| > 2\sigma$ criteria, respectively). If we refer to the sample of objects with *IMAFLAGS_ISO* = 0, the bias, standard deviation and *NMAD* become 0.00072, 0.0288 and 0.0207, respectively, while the fraction of outliers is 0.32 and 3.26 per cent. Thus, although the present approach is immune to systematic effects in photometry, we find a small improvement in the statistics when the sources in the masked regions are removed from the analysis.

4 PHOTOMETRIC CATALOGUE

To produce the final z_{phot} catalogue, we initially considered the multisource KiDS catalogue (i.e. sources detected in the *r* band and measured in all KiDS bands). However, it is important to underline that all empirical z_{phot} prediction methods suffer from a poor capability to extrapolate outside the range of distributions imposed by the training sample. In the literature, several approaches have been proposed to extend the applicability test of empirical methods outside the boundaries of the parameter space properly sampled by the spectroscopic KB (see Vanzella et al. 2004; Hoyle et al. 2015). While useful in some cases, this artificial augmentation of the KB introduces a further level of complexity and leads to statistical biases, which are difficult to evaluate and control.

In the available spectroscopic KB, we found that ~ 99 per cent of the KB objects fall within the following region of the parameter space:

$$\begin{aligned} \text{MAGAP}_{4,u} &\leq 25.1, & \text{MAGAP}_{6,u} &\leq 24.7, \\ \text{MAGAP}_{4,g} &\leq 24.5, & \text{MAGAP}_{6,g} &\leq 24.0, \\ \text{MAGAP}_{4,r} &\leq 22.2, & \text{MAGAP}_{6,r} &\leq 22.0, \\ \text{MAGAP}_{4,i} &\leq 21.5, & \text{MAGAP}_{6,i} &\leq 21.0. \end{aligned}$$

Hence, to produce the final z_{phot} catalogue, we have removed all the objects that do not match the above criteria in more than one band. The choice to retain objects with only one band not matching the above criteria was dictated by the need to maximize the number of objects with a redshift estimate and supported by the well-tested robustness of the MLPQNA method against non-detections or missing data (Cavuoti et al. 2012). In Table 1, we report the statistical indicators evaluated for two groups of objects: those having all data points falling within the above region (clean objects) and those with only one band falling outside of it (contaminated objects). It appears evident that for a one-band failure there is only a small decrease of performance.

However, in order to keep track of this effect, we include a z_{phot} quality flag in the catalogue, set to 1 for best quality (i.e. clean) and to 0 for worse quality (i.e. contaminated) objects.

Table 1. Statistical indicators computed for two different subsets of the blind test set. The clean set includes only data for which the photometry falls within the limits listed in Section 4. The contaminated subset includes objects that fall outside those limits in only one band.

Subset	$ bias $	σ	$NMAD$	Outliers (per cent) $ \Delta z > 0.15$	Outliers (per cent) $ \Delta z > 2\sigma$
Clean	0.0011	0.0303	0.0212	0.38	3.13
Contaminated	0.0003	0.0339	0.0223	0.47	5.80

The final z_{phot} catalogue consists of 1 142 992 objects (699 155 objects have all IMAFLAGS_ISO = 0 and 710 127 with best quality).

5 CONCLUSIONS

In this work, we applied the MLPQNA neural network to the ESO KiDS DR2 photometric galaxy data, using a KB derived from the SDSS and GAMA spectroscopic samples, to produce a catalogue of photometric redshifts based on optical photometric data only. We obtained an overall 1σ uncertainty on $\Delta z = (z_{\text{spec}} - z_{\text{phot}})/(1 + z_{\text{spec}})$ of 0.0305 with a very small average bias of 9.9×10^{-4} , a low $NMAD$ of 0.021, and a low fraction of outliers (0.39 per cent above the standard limit of 0.15).

The trained network was then used to process all galaxies in the data set that populate a parameter space similar to that defined by the SDSS+GAMA spectroscopic sample, producing z_{phot} estimates for about 1.1 million KiDS galaxies. The catalogue will be made available on the CDS VizieR facility.

Deriving photometric redshifts is an essential task when dealing with large samples of galaxies, such as that expected from the KiDS photometric survey. These redshifts are currently being used by the KiDS collaboration for a variety of studies regarding the evolution of galaxy stellar masses, integrated colours, colour gradients and structural parameters with redshift (Napolitano et al. in preparation). The characterization of how completeness and biases of the photo- z catalogue affect the final scientific goals is therefore postponed to later works. This type of study will allow us to better constrain the processes leading to the (mass) growth of galaxies in the last half of the current age of the Universe.

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