



Publication Year	2016
Acceptance in OA @INAF	2020-05-27T15:11:02Z
Title	Planck intermediate results. XXX. The angular power spectrum of polarized dust emission at intermediate and high Galactic latitudes
Authors	Planck Collaboration; Adam, R.; Ade, P. A. R.; Aghanim, N.; Arnaud, M.; et al.
DOI	10.1051/0004-6361/201425034
Handle	http://hdl.handle.net/20.500.12386/25245
Journal	ASTRONOMY & ASTROPHYSICS
Number	586



Publication Year	2016
Acceptance in OA@INAF	2020-05-27T15:11:02Z
Title	Planck intermediate results. XXX. The angular power spectrum of polarized dust emission at intermediate and high Galactic latitudes
Authors	Planck Collaboration; Adam, R.; Ade, P. A. R.; Aghanim, N.; Arnaud, M.; et al.
DOI	10.1051/0004-6361/201425034
Handle	http://hdl.handle.net/20.500.12386/25245
Journal	ASTRONOMY & ASTROPHYSICS
Number	586

Planck intermediate results

XXX. The angular power spectrum of polarized dust emission at intermediate and high Galactic latitudes

Planck Collaboration: R. Adam⁸⁰, P. A. R. Ade⁹¹, N. Aghanim⁶⁴, M. Arnaud⁷⁸, J. Aumont^{64,*}, C. Baccigalupi⁹⁰, A. J. Banday^{99,10}, R. B. Barreiro⁷⁰, J. G. Bartlett^{1,72}, N. Bartolo^{33,71}, E. Battaner^{102,103}, K. Benabed^{65,98}, A. Benoit-Lévy^{25,65,98}, J.-P. Bernard^{99,10}, M. Bersanelli^{36,54}, P. Bielewicz^{99,10,90}, A. Bonaldi⁷³, L. Bonavera⁷⁰, J. R. Bond⁹, J. Borrill^{15,94}, F. R. Bouchet^{65,98}, F. Boulanger⁶⁴, A. Bracco⁶⁴, M. Bucher¹, C. Burigana^{53,34,55}, R. C. Butler⁵³, E. Calabrese⁹⁶, J.-F. Cardoso^{79,1,65}, A. Catalano^{80,77}, A. Challinor^{67,74,13}, A. Chamballu^{78,17,64}, R.-R. Chary⁶², H. C. Chiang^{28,7}, P. R. Christensen^{86,40}, D. L. Clements⁶¹, S. Colombi^{65,98}, L. P. L. Colombo^{24,72}, C. Combet⁸⁰, F. Couchot⁷⁵, A. Coulais⁷⁷, B. P. Crill^{72,87}, A. Curto^{6,70}, F. Cuttaia⁵³, L. Danese⁹⁰, R. D. Davies⁷³, R. J. Davis⁷³, P. de Bernardis³⁵, G. de Zotti^{50,90}, J. Delabrouille¹, J.-M. Delouis^{65,98}, F.-X. Désert⁵⁹, C. Dickinson⁷³, J. M. Diego⁷⁰, K. Dolag^{101,83}, H. Dole^{64,63}, S. Donzelli⁵⁴, O. Doré^{72,12}, M. Douspis⁶⁴, A. Ducout^{65,61}, J. Dunkley⁹⁶, X. Dupac⁴³, G. Efstathiou⁶⁷, F. Elsner^{25,65,98}, T. A. Enßlin⁸³, H. K. Eriksen⁶⁸, E. Falgarone⁷⁷, F. Finelli^{53,55}, O. Forni^{99,10}, M. Frailis⁵², A. A. Fraisse²⁸, E. Franceschi⁵³, A. Frejsel⁸⁶, S. Galeotta⁵², S. Galli⁶⁵, K. Ganga¹, T. Ghosh⁶⁴, M. Giard^{99,10}, Y. Giraud-Héraud¹, E. Gjerløw⁶⁸, J. González-Nuevo^{70,90}, K. M. Górski^{72,104}, S. Gratton^{74,67}, A. Gregorio^{37,52,58}, A. Gruppiso⁵³, V. Guillet⁶⁴, F. K. Hansen⁶⁸, D. Hanson^{84,72,9}, D. L. Harrison^{67,74}, G. Helou¹², S. Henrot-Versillé⁷⁵, C. Hernández-Monteagudo^{14,83}, D. Herranz⁷⁰, E. Hivon^{65,98}, M. Hobson⁶, W. A. Holmes⁷², K. M. Huffenberger²⁶, G. Hurier⁶⁴, A. H. Jaffe⁶¹, T. R. Jaffe^{99,10}, J. Jewell⁷², W. C. Jones²⁸, M. Juvela²⁷, E. Keihänen²⁷, R. Keskitalo¹⁵, T. S. Kisner⁸², R. Kneissl^{42,8}, J. Knoche⁸³, L. Knox³⁰, N. Krachmalnicoff³⁶, M. Kunz^{19,64,2}, H. Kurki-Suonio^{27,49}, G. Lagache^{5,64}, J.-M. Lamarre⁷⁷, A. Lasenby^{6,74}, M. Lattanzi³⁴, C. R. Lawrence⁷², J. P. Leahy⁷³, R. Leonardi⁴³, J. Lesgourgues^{97,89,76}, F. Levrier⁷⁷, M. Liguori³³, P. B. Lilje⁶⁸, M. Linden-Vørnle¹⁸, M. López-Caniego⁷⁰, P. M. Lubin³¹, J. F. Macías-Pérez⁸⁰, B. Maffei⁷³, D. Maino^{36,54}, N. Mandolesi^{53,4,34}, A. Mangilli⁶⁵, M. Maris⁵², P. G. Martin⁹, E. Martínez-González⁷⁰, S. Masi³⁵, S. Matarrese^{33,71,46}, P. Mazzotta³⁸, P. R. Meinhold³¹, A. Melchiorri^{35,56}, L. Mendes⁴³, A. Mennella^{36,54}, M. Migliaccio^{67,74}, S. Mitra^{60,72}, M.-A. Miville-Deschênes^{64,9}, A. Moneti⁶⁵, L. Montier^{99,10}, G. Morgante⁵³, D. Mortlock⁶¹, A. Moss⁹², D. Munshi⁹¹, J. A. Murphy⁸⁵, P. Naselsky^{86,40}, F. Nati³⁵, P. Natoli^{34,3,53}, C. B. Netterfield²¹, H. U. Nørgaard-Nielsen¹⁸, F. Novello⁷³, D. Novikov⁶¹, I. Novikov⁸⁶, L. Pagano^{35,56}, F. Pajot⁶⁴, R. Paladini⁶², D. Paoletti^{53,55}, B. Partridge⁴⁸, F. Pasian⁵², G. Patanchon¹, T. J. Pearson^{12,62}, O. Perdereau⁷⁵, L. Perrotta⁸⁰, F. Perrotta⁹⁰, V. Pettorino⁴⁷, F. Piacentini³⁵, M. Piat¹, E. Pierpaoli²⁴, D. Pietrobon⁷², S. Plaszczynski⁷⁵, E. Pointecouteau^{99,10}, G. Polenta^{3,51}, N. Ponthieu^{64,59}, L. Popa⁶⁶, G. W. Pratt⁷⁸, S. Prunet^{65,98}, J.-L. Puget⁶⁴, J. P. Rachen^{22,83}, W. T. Reach¹⁰⁰, R. Rebolo^{69,16,41}, M. Remazeilles^{73,64,1}, C. Renault⁸⁰, A. Renzi^{39,57}, S. Ricciardi⁵³, I. Ristorcelli^{99,10}, G. Rocha^{72,12}, C. Rosset¹, M. Rossetti^{36,54}, G. Roudier^{1,77,72}, B. Rouillé d'Orfeuil⁷⁵, J. A. Rubiño-Martín^{69,41}, B. Rusholme⁶², M. Sandri⁵³, D. Santos⁸⁰, M. Savelainen^{27,49}, G. Savini⁸⁸, D. Scott²³, J. D. Soler⁶⁴, L. D. Spencer⁹¹, V. Stolyarov^{6,74,95}, R. Stompor¹, R. Sudiwala⁹¹, R. Sunyaev^{83,93}, D. Sutton^{67,74}, A.-S. Suur-Uski^{27,49}, J.-F. Sygnet⁶⁵, J. A. Tauber⁴⁴, L. Terenzi^{45,53}, L. Toffolatti^{20,70,53}, M. Tomasi^{36,54}, M. Tristram⁷⁵, M. Tucci¹⁹, J. Tuovinen¹¹, L. Valenziano⁵³, J. Valiviita^{27,49}, B. Van Tent⁸¹, L. Vibert⁶⁴, P. Vielva⁷⁰, F. Villa⁵³, L. A. Wade⁷², B. D. Wandelt^{65,98,32}, R. Watson⁷³, I. K. Wehus⁷², M. White²⁹, S. D. M. White⁸³, D. Yvon¹⁷, A. Zacchei⁵², and A. Zonca³¹

(Affiliations can be found after the references)

Received 19 September 2014 / Accepted 1 December 2014

ABSTRACT

The polarized thermal emission from diffuse Galactic dust is the main foreground present in measurements of the polarization of the cosmic microwave background (CMB) at frequencies above 100 GHz. In this paper we exploit the uniqueness of the *Planck* HFI polarization data from 100 to 353 GHz to measure the polarized dust angular power spectra C_ℓ^{EE} and C_ℓ^{BB} over the multipole range $40 < \ell < 600$ well away from the Galactic plane. These measurements will bring new insights into interstellar dust physics and allow a precise determination of the level of contamination for CMB polarization experiments. Despite the non-Gaussian and anisotropic nature of Galactic dust, we show that general statistical properties of the emission can be characterized accurately over large fractions of the sky using angular power spectra. The polarization power spectra of the dust are well described by power laws in multipole, $C_\ell \propto \ell^\alpha$, with exponents $\alpha^{EE,BB} = -2.42 \pm 0.02$. The amplitudes of the polarization power spectra vary with the average brightness in a way similar to the intensity power spectra. The frequency dependence of the dust polarization spectra is consistent with modified blackbody emission with $\beta_d = 1.59$ and $T_d = 19.6$ K down to the lowest *Planck* HFI frequencies. We find a systematic difference between the amplitudes of the Galactic *B*- and *E*-modes, $C_\ell^{BB}/C_\ell^{EE} = 0.5$. We verify that these general properties are preserved towards high Galactic latitudes with low dust column densities. We show that even in the faintest dust-emitting regions there are no “clean” windows in the sky where primordial CMB *B*-mode polarization measurements could be made without subtraction of foreground emission. Finally, we investigate the level of dust polarization in the specific field recently targeted by the BICEP2 experiment. Extrapolation of the *Planck* 353 GHz data to 150 GHz gives a dust power $\mathcal{D}_\ell^{BB} \equiv \ell(\ell+1)C_\ell^{BB}/(2\pi)$ of $1.32 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ over the multipole range of the primordial recombination bump ($40 < \ell < 120$); the statistical uncertainty is $\pm 0.29 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ and there is an additional uncertainty $(+0.28, -0.24) \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ from the extrapolation. This level is the same magnitude as reported by BICEP2 over this ℓ range, which highlights the need for assessment of the polarized dust signal even in the cleanest windows of the sky.

Key words. cosmic background radiation – cosmology: observations – ISM: structure – ISM: magnetic fields – polarization

* Corresponding author: J. Aumont,
 e-mail: jonathan.aumont@ias.u-psud.fr

1. Introduction

The sky at high Galactic latitude and frequencies above about 100 GHz is dominated by thermal emission from the Galactic interstellar medium, specifically arising from dust grains of about $0.1\,\mu\text{m}$ in size. Asymmetrical dust grains align with the Galactic magnetic field to produce polarized emission. This polarized submillimetre emission has been measured from ground-based and balloon-borne telescopes (e.g., [Hildebrand et al. 1999](#); [Benoît et al. 2004](#); [Ponthieu et al. 2005](#); [Vaillancourt 2007](#); [Matthews et al. 2014](#)). The observed polarization relates to the nature, size, and shape of dust grains and the mechanisms of alignment, discussed for example by [Draine \(2004\)](#) and [Martin \(2007\)](#). It also probes the structure of the Galactic magnetic field, which is an essential component of models of Galactic dust polarization ([Baccigalupi 2003](#); [Fauvet et al. 2011, 2012](#); [O’Dea et al. 2012](#); [Jaffe et al. 2013](#); [Delabrouille et al. 2013](#)).

The polarized emission from dust is also of interest in the context of foregrounds ([Tucci et al. 2005](#); [Dunkley et al. 2009a](#); [Gold et al. 2011](#)) to the cosmic microwave background (CMB). On angular scales between $10'$ and a few tens of degrees, cosmological B -mode polarization signals may be present that were imprinted during the epoch of inflation. The discovery of a primordial B -mode polarization signature is a major scientific goal of many CMB experiments. These include ground-based experiments (ACTPol, [Niemack et al. 2010](#); BICEP2, [BICEP2 Collaboration 2014a](#); Keck-array, [Staniszewski et al. 2012](#); POLARBEAR, [Arnold et al. 2010](#); QUBIC, [Ghribi et al. 2014](#); QUIJOTE, [Rubio-Martín et al. 2010](#); and SPTpol, [Austermann et al. 2012](#)), stratospheric balloon missions (EBEX, [Grainger et al. 2008](#); and SPIDER, [Fraisie et al. 2013](#)), and the ESA *Planck*¹ satellite ([Tauber et al. 2010](#)). Accurate assessment and, if necessary, subtraction of foreground contamination is critical to the measurement of CMB E - and B -mode polarization because the expected signals from inflation and late-time reionization are expected to be small.

Planck has measured the all-sky dust polarization at 353 GHz, where the dust emission dominates over other polarized signals. These data have been presented in a first set of publications in which the focus was on the structure of the Galactic magnetic field and the characterization of dust polarization properties ([Planck Collaboration Int. XIX 2015](#); [Planck Collaboration Int. XX 2015](#); [Planck Collaboration Int. XXI 2015](#); [Planck Collaboration Int. XXII 2015](#)). Here, we use the *Planck* polarized data to compute the C_ℓ^{EE} and C_ℓ^{BB} power spectra of dust polarization over the multipole range $40 < \ell < 600$, on large fractions of the sky away from the Galactic plane. We also investigate dust polarization in sky patches at high Galactic latitude with sizes comparable to those surveyed by ground-based CMB experiments. We derive statistical properties of dust polarization from these spectra, characterizing the shape of the spectra and their amplitude with respect to both the observing frequency and the mean dust intensity of the sky region over which they are computed. We verify that these properties hold in low-column-density patches at high Galactic latitude and we explore statistically the potential existence of “clean” patches on the sky that might be suitable for cosmology.

Our analysis of dust polarization is relevant to the present generation of CMB polarization observations, and to the design of future experiments. It gives a statistical description of Galactic dust polarization, providing input for the modelling of Galactic dust as part of component separation methods and for CMB polarization likelihood analysis parameterization.

The BICEP2 collaboration has recently reported a significant detection of the B -mode power spectrum around the expected angular scale of the recombination bump, namely a few degrees ([BICEP2 Collaboration 2014a,b](#)). Their analysis was based on dust polarization models that predicted subdominant contamination of their B -mode signal by dust polarization. We use information from our detailed analysis of *Planck* polarization data at 353 GHz to assess the potential dust contamination.

The paper is organized as follows. In Sect. 2, we present the *Planck* HFI polarization data used in this work and describe the general properties of the polarization maps in terms of emission components and systematic effects. In Sect. 3, we describe our method for computing the dust C_ℓ^{EE} and C_ℓ^{BB} angular power spectra, including the selected science regions of interest on the sky. We assess and compare the two methods we use to compute the power spectra in Appendix A. In Sect. 4, we present power spectra of dust polarization for multipoles $\ell > 40$, computed with high signal-to-noise ratio (S/N) on large fractions of the sky, and characterize their shape and amplitude. Complementary angular power spectra involving temperature and polarization, C_ℓ^{TE} and C_ℓ^{TB} , and cross-polarization, C_ℓ^{EB} are given in Appendix B. We extend this analysis to smaller sky patches at high Galactic latitude in Sect. 5. In Appendix C we discuss some complementary aspects of this analysis of patches. These results are used specifically in Sect. 5.3 to build a map of the expected dust contamination of the C_ℓ^{BB} power spectrum at 150 GHz and $\ell = 80$. In Sect. 6 we present a study of the polarized dust emission in the vicinity of the BICEP2 region. Systematic effects relating to the *Planck* angular power spectrum estimates are assessed in Appendix D and we discuss the decorrelation of the dust signal between frequencies in Appendix E. Section 7 summarizes the main conclusions and discusses the implications of this work for future CMB experiments².

2. Planck polarization maps

2.1. Planck data

The Planck Collaboration recently released the *Planck* satellite nominal mission temperature data and published a set of papers describing these data and their cosmological interpretation (e.g., [Planck Collaboration I 2014](#); [Planck Collaboration XVI 2014](#)). These results are based on the data from the two instruments on board the satellite (Low Frequency Instrument, LFI, [Mennella et al. 2011](#), and High Frequency Instrument, HFI, [Planck HFI Core Team 2011](#)). The data processing of the nominal mission data (Surveys 1 and 2, 14 months) was summarized in [Planck Collaboration II \(2014\)](#) and [Planck Collaboration VI \(2014\)](#).

Planck HFI measures the linear polarization at 100, 143, 217, and 353 GHz ([Rosset et al. 2010](#)). The properties of the detectors (sensitivity, spectral response, noise properties, beams, etc.) are described in detail in [Lamarre et al. \(2010\)](#) and their in-flight performance is reported in [Planck HFI Core Team \(2011\)](#), [Planck Collaboration VII \(2014\)](#), [Planck Collaboration VIII \(2014\)](#),

¹ *Planck* (<http://www.esa.int/Planck>) is a project of the European Space Agency (ESA) with instruments provided by two scientific consortia funded by ESA member states (in particular the lead countries France and Italy), with contributions from NASA (USA) and telescope reflectors provided by a collaboration between ESA and a scientific consortium led and funded by Denmark.

² While this paper was in preparation three papers have used publicly available polarization information from *Planck* to infer potentially high levels of dust contamination in the BICEP2 field ([Flauger et al. 2014](#); [Mortonson & Seljak 2014](#); [Colley & Gott 2015](#)).

Planck Collaboration IX (2014), and Planck Collaboration X (2014), while Planck Collaboration VI (2014) describes the general processing applied to the data to measure polarization. In this paper, we make use of full-mission (Surveys 1 to 5, 30 months, Planck Collaboration I 2014) polarization maps of *Planck* HFI (internal data release “DX11d”), projected into the HEALPix pixelization scheme (Górski et al. 2005). This is one of the first publications to use these maps, which will be described in the *Planck* cosmology 2015 release.

To compute polarization angular power spectra, we use Q and U maps at 100, 143, 217, and 353 GHz. Specifically, we calculate power spectra using the so-called “Detector-Set” maps (hereafter “DetSets”), constructed using two subsets of polarization sensitive bolometers (PSBs) at a given frequency (see Table 3 in Planck Collaboration VI 2014). Each DetSet polarization map is constructed using data from two pairs of PSBs, with the angle between the two PSBs in a pair being 90° , and the angle between pairs being 45° . In this paper we concentrate on the Q and U maps at 353 GHz. The Stokes Q and U maps at lower frequencies (100, 143, and 217 GHz) are only used to determine the spectral energy distribution (SED) of the dust emission in polarization.

To quantify systematic effects, we also use maps made from other data subsets (Planck Collaboration VI 2014). We use the ring halves (hereafter “HalfRing”), where the approximately 60 circles performed for each *Planck* telescope ring (also called a stable pointing period) are divided into two independent subsets of 30 circles. We use observational years (hereafter “Years”), consisting of Surveys 1 and 2 on the one hand and Surveys 3 and 4 on the other, to build two additional maps with independent noise.

The *Planck* maps we use are in thermodynamic units (K_{CMB}). To characterize the SED of the dust emission in polarization we express the data as the specific intensity (such as that for Stokes I dust emission, $I_d(\nu)$) at the *Planck* reference frequencies, using the conversion factors and colour corrections from Planck Collaboration IX (2014)³. For the average dust SED at intermediate Galactic latitudes, the colour correction factor is 1.12 at 353 GHz (see Table 3 in Planck Collaboration Int. XXII 2015).

In addition to these basic products, a *Planck* CO map from Planck Collaboration XIII (2014), the so-called “type 3” map, and the *Planck* 857 GHz map, are also used in the selection of the large intermediate latitude analysis regions (see Sect. 3.3.1).

2.2. Emission contributions to the *Planck* HFI polarization maps

2.2.1. Polarized thermal dust emission

Thermal dust emission is partially linearly polarized (e.g., Hildebrand et al. 1999; Benoît et al. 2004; Ponthieu et al. 2005; Vaillancourt 2007). It is the dominant polarized foreground

signal in the high frequency *Planck* bands (Tucci et al. 2005; Dunkley et al. 2009b; Fraisse et al. 2009; Fauvet et al. 2011; Planck Collaboration Int. XXII 2015).

Dust polarization arises from alignment of non-spherical grains with the interstellar magnetic field (e.g., Hildebrand 1988; Draine 2004; Martin 2007). The structure of the dust polarization sky has already been described using maps of the polarization fraction (p) and angle (ψ) derived from the *Planck* HFI 353 GHz data (Planck Collaboration Int. XIX 2015; Planck Collaboration Int. XX 2015). The map of p shows structure on all scales, with polarization fractions ranging from low (less than 1%) to high values (greater than 18%). Planck Collaboration Int. XIX (2015) and Planck Collaboration Int. XX (2015) report an anti-correlation between p and the local dispersion of ψ , which indicates that variations in p arise mainly from depolarization associated with changes in the magnetic field orientation within the beam, rather than from changes in the efficiency of grain alignment.

Planck Collaboration Int. XXII (2015) showed that the SED of polarized dust emission over the four *Planck* HFI frequencies from 100 to 353 GHz is consistent with a modified blackbody emission law of the type $I_d(\nu) \propto \nu^{\beta_d} B_\nu(T_d)$, with spectral index $\beta_d = 1.59$ for $T_d = 19.6 \text{ K}$ ⁴, and where B_ν is the Planck function. About 39% of the sky at intermediate Galactic latitudes was analysed⁵. Among 400 circular patches with 10° radius (equivalent to a sky fraction $f_{\text{sky}}^{\text{eff}} = 0.0076$) the 1σ dispersion of β_d was 0.17 for constant $T_d = 19.6 \text{ K}$. We scale this uncertainty on β_d to larger sky areas by using the factor $(0.0076/f_{\text{sky}}^{\text{eff}})^{0.5}$. This is a conservative choice because this uncertainty includes the effects of noise in the data and so is an upper limit to the true regional variations of β_d on this scale. This polarization spectral index can be compared to variations in the spectral index $\beta_{\text{d,mm}}^I$ for the intensity SED. For that quantity the S/N of the data is higher than for polarization and Planck Collaboration Int. XXII (2015) report a dispersion of 0.07 (1σ) over the same sized circular patches. Planck Collaboration Int. XVII (2014) extend this analysis for intensity to high Galactic latitudes in the southern Galactic cap, using the dust-HI correlation to separate the faint emission of dust from the anisotropies of the cosmic infrared background, and find a dispersion of about 0.10 in $\beta_{\text{d,mm}}^I$. We expect spectral variations to be correlated in polarization and intensity, unless the dust emission has a significant component that is unpolarized.

2.2.2. CMB

The CMB temperature anisotropies have been measured with unprecedented accuracy by the Planck Collaboration (Planck Collaboration I 2014; Planck Collaboration XV 2014), and preliminary *Planck* polarization results have been demonstrated to be in very good agreement with the cosmology inferred from temperature measurements (Planck Collaboration I 2014; Planck Collaboration XVI 2014).

For C_ℓ^{EE} , the ΛCDM concordance model has been shown to be a very good fit to all the available data (including preliminary *Planck* results at $\ell \gtrsim 50$; see Barkats et al. 2014, for a recent compendium). For 353 GHz data at small angular scales

³ The conversion factor from K_{CMB} to MJy sr^{-1} is computed for a standard specific intensity $I_\nu \propto \nu^{-1}$. The colour correction depends on the actual dust SED; it is the scaling factor used to transform from the specific intensity of the dust emission, at the reference frequency, to the *Planck* brightness in MJy sr^{-1} (see Eq. (19) in Planck Collaboration Int. XXII 2015). The conversion factors and the colour corrections are computed via Eq. (32) in Planck Collaboration IX (2014) using the *Planck* HFI filters and the *Planck* UCC software available through the *Planck* Explanatory Supplement (http://www.sciops.esa.int/wikiSI/planckpla/index.php?title=Unit_conversion_and_Color_correction&instance=Planck_Public_PLA); we use the band-average values.

⁴ This spectral index was called $\beta_{\text{d,mm}}^P$ in that paper, but we adopt a more compact notation here.

⁵ More specifically, for the latitude range $10^\circ < |b| < 60^\circ$, with patches contained within the region in Fig. 1 (below) defined by including that with $f_{\text{sky}} = 0.8$ and then removing that with $f_{\text{sky}} = 0.4$.

($\ell \gtrsim 400$), the E -mode CMB polarization is comparable to the power of dust polarization at high Galactic latitudes.

The CMB B -mode power, even for the highest primordial tensor perturbation models, is negligible with respect to the dust polarization at 353 GHz. Since no reliable published CMB polarization maps are available, we have chosen not to remove the CMB polarization from the *Planck* HFI Q and U maps. Nevertheless, because the CMB E -mode polarization is significant with respect to the dust at 353 GHz at high multipoles (and even at lower multipoles for the lower frequencies), when studying the *Planck* HFI bands we subtract the *Planck* best-fit Λ CDM C_ℓ^{EE} model (Col. 2 of Table 2 in [Planck Collaboration XVII 2014](#)) from the dust power spectra, paying the price of an increased error due to sample variance. No CMB is removed in this work when computing the dust C_ℓ^{BB} spectra.

2.2.3. Synchrotron emission

Synchrotron emission is known to be significantly polarized (up to 75% for typical relativistic electron spectra, [Rybicki & Lightman 1979](#)). Since its specific intensity scaling with frequency follows a power law with a spectral index close to -3 ([Gold et al. 2011](#); [Macellari et al. 2011](#); [Fuskeland et al. 2014](#)), synchrotron polarized emission is expected to be subdominant in the *Planck* HFI channels in general and negligible at 353 GHz ([Tucci et al. 2005](#); [Dunkley et al. 2009a](#); [Gold et al. 2011](#); [Fauvet et al. 2011](#); [Fuskeland et al. 2014](#); [Planck Collaboration Int. XXII 2015](#)). Hence, we neither subtract nor mask any synchrotron contribution before estimating the angular power spectra of dust polarization. The justification of this assumption will be demonstrated below by studying the frequency dependence of the polarized dust power between 100 and 353 GHz (but see also Appendix D.4).

2.2.4. Polarized point sources

Radio sources have been shown to have a fractional polarization of a few percent (e.g., [Battye et al. 2011](#); [Massardi et al. 2013](#)). Their contribution to the polarization angular power spectra in the *Planck* HFI bands is expected to be negligible at low and intermediate multipoles ([Battye et al. 2011](#); [Tucci & Toffolatti 2012](#)). Upper limits have been set on the polarization of infrared galaxies, and their contribution to the polarization power spectra is also expected to be negligible (e.g., [Seiffert et al. 2007](#)). However, the brightest of the polarized point sources can be responsible for ringing in the angular power spectra estimation, and therefore need to be masked (see Sect. 3.3.1).

2.2.5. CO emission

The first three carbon monoxide (CO) Galactic emission lines at 115 GHz ($J=1 \rightarrow 0$), 230 GHz ($J=2 \rightarrow 1$), and 345 GHz ($J=3 \rightarrow 2$), contribute significantly to the power in the *Planck* HFI bands at 100, 217, and 353 GHz, respectively ([Planck Collaboration IX 2014](#)). The *Planck* data were used to produce the first all-sky maps of Galactic CO emission ([Planck Collaboration XIII 2014](#)). It is known that CO emission can be intrinsically polarized ([Goldreich & Kylafis 1982](#); [Li & Henning 2011](#)). Furthermore, CO emission can induce spurious polarization because of the differences in spectral transmission at the CO frequencies between *Planck* HFI detectors ([Planck Collaboration IX 2014](#)). For these reasons, we mask CO-emitting regions (Sect. 3.3.1). Outside this mask, as has been

shown in [Planck Collaboration XIII \(2014\)](#) by comparing the *Planck* CO maps to high Galactic latitude ground-based CO observations ([Hartmann et al. 1998](#); [Magnani et al. 2000](#)), the CO emission is negligible in the *Planck* channels (lower than one fourth of each channel noise rms at 95% CL). We will check that our polarization analysis is not contaminated by CO by examining the frequency dependence of the polarized angular power spectra of the dust (see Sect. 4.5).

2.3. Systematics of the *Planck* HFI polarization maps

The first CMB polarization results from *Planck* were presented in [Planck Collaboration I \(2014\)](#) and [Planck Collaboration XVI \(2014\)](#). The EE power spectrum at $\ell > 200$ was found to be consistent with the cosmological model derived from temperature anisotropies. Systematic effects in the data have so far limited the use of *Planck* HFI polarization data on large angular scales. The polarization systematics in the 2013 data were discussed and estimated in [Planck Collaboration VI \(2014\)](#); see the power spectra shown in their Fig. 27). The same data were used in the *Planck* Galactic polarization papers ([Planck Collaboration Int. XIX 2015](#); [Planck Collaboration Int. XX 2015](#); [Planck Collaboration Int. XXI 2015](#); [Planck Collaboration Int. XXII 2015](#)) and there the low brightness regions of the 353 GHz sky were masked.

In this paper, we use a new set of *Planck* polarization maps for which the systematic effects have been significantly reduced. Corrections will be fully described and applied in the *Planck* 2015 cosmology release, as well as the remaining systematic effects that we describe briefly here.

Two main effects have been corrected in the time-ordered data prior to mapmaking. The correction for the nonlinearity of the analogue-to-digital converters was improved, and we have also corrected the data for very long time constants that were not previously identified (see [Planck Collaboration VI 2014](#); [Planck Collaboration X 2014](#)). After these corrections, the main systematic effects over the multipole range $40 < \ell < 600$ relevant to this analysis result from leakage of intensity into polarization maps. Effects arising from polarization angle and polarization efficiency uncertainties have been shown to be second order ([Planck Collaboration VI 2014](#)). The leakage effect can be expressed as

$$\Delta\{Q, U\}_\nu(\hat{n}) = \sum_s \sum_b \gamma_\nu^{s,b} \Gamma_\nu^{b,I \rightarrow \{Q,U\}}(\hat{n}) I_\nu^s(\hat{n}), \quad (1)$$

where ν is the frequency, and $\Gamma_\nu^{b,I \rightarrow \{Q,U\}}$, the leakage pattern for bolometer b , is multiplied by the different s leakage source maps I_ν^s and their associated scaling coefficients $\gamma_\nu^{s,b}$. The leakage patterns are fully determined by the scanning strategy. They represent the cumulative result of all the systematic effects that lead to a leakage of intensity to polarization. In the *Planck* HFI bands, there are three main sources of intensity to polarization leakage: (i) monopole differences between detectors not corrected by data destriping (the intensity source term is constant over the sky); (ii) bolometer inter-calibration mismatch (the source term is the full intensity map, including the CMB dipole and the Galactic emission); and (iii) a dust spectral mismatch term. The spectral bandpass varies from one bolometer to another for a given band. As the bolometer gain is calibrated on the CMB dipole, the differential gains on the dust emission produce the bandpass mismatch term (for which the source term is the dust intensity map).

Results from a global fit of the Q and U maps with these three leakage terms $I_{\nu}^{b,l \rightarrow \{Q,U\}} I_{\nu}^s$ are used to quantify the leakage. This fit yields estimates of the scaling coefficients at each frequency ν in Eq. (1), which allows us to compute angular power spectra of the leakage terms in Sect. 4. We point out that the fit captures any emission in the maps that has a pattern on the sky similar to one of the leakage patterns. These global fit maps are used to assess the level of systematics, but are not removed from the data.

An independent and complementary estimate of systematic effects in the data is provided by the null tests that we can build from the DetSets, HalfRings, and Years data subsets (see Sect. 2.1). These null tests are a good way of determining the level of any systematics other than intensity to polarization leakage. These are pursued in Sect. 4.1 and Appendices C.1 and D.3.

3. Computation of angular power spectra of polarized dust emission

3.1. Methods

We can use the *Planck* data to compute the polarization angular power spectra (C_{ℓ}^{EE} and C_{ℓ}^{BB}) of the polarized dust emission within selected sky regions. Even if the statistical properties of the dust emission on the sky might not be entirely captured by a two-point function estimator, because the scope of this paper is to assess the level of dust in the framework of CMB data analysis, we follow the approximation that is generally made when processing such data, i.e., that a large fraction of the information is contained in power spectra.

On an incomplete sky, a polarization field can be divided into three classes of modes: pure E -modes; pure B -modes; and “ambiguous” modes, which are a mixture of the true E - and B -modes (Bunn et al. 2003).

The ambiguous modes represent a cross-talk between E and B , which is often referred to as “ E -to- B leakage” for the CMB (because for the CMB $C_{\ell}^{EE} \gg C_{\ell}^{BB}$). Methods used to estimate the CMB angular power spectrum for polarization account for and correct analytically for the incomplete sky coverage. However, the presence of the ambiguous modes yields a biased estimate of the variance of the spectra, unless so-called “pure” power spectrum estimators are used (Smith 2006). For dust polarization, the power in E - and B -modes are comparable, and we do not expect a significant variance bias.

The two specific approaches we use are Xpol, our main method, which we describe as a “classical” pseudo- C_{ℓ} estimator⁶ and, for comparison, Xpure, a pure pseudo- C_{ℓ} estimator. Since they give similar results for the present study, as we demonstrate below, the former is chosen as our main method because it is computationally less expensive.

3.1.1. Xpol

Xpol is an extension of the Xspect method (Tristram et al. 2005) to polarization. Xspect computes the pseudo power spectra and corrects them for incomplete sky coverage, filtering effects, and pixel and beam window functions. Correction for incomplete sky coverage is performed using a Master-like algorithm (Hivon et al. 2002), consisting of the inversion of the mode-mode coupling matrix $M_{\ell\ell'}$ that describes the effect of the

partial sky coverage; $M_{\ell\ell'}$ is computed directly from the power spectrum of the mask that selects the data in the analysis region of interest (Sect. 3.3). The HEALPix pixel window functions (Górski et al. 2005) are used to correct for pixelization effects. For the beams we use the *Planck* HFI individual detector beam transfer functions described in Planck Collaboration VII (2014).

Xpol estimates the error bars analytically, without requiring Monte Carlo simulations. Using simulated data comprising inhomogeneous white noise and a Gaussian map with a dust power spectrum, we have checked that this analytical estimate is not biased for multipoles $\ell > 40$. The analytical error bars combine the contributions from instrumental noise and sample variance. The Gaussian approximation of the sample variance is

$$\text{var}(C_{\ell_{\text{bin}}}^{XX}) = \frac{2}{(2\ell_{\text{bin}} + 1)f_{\text{sky}}\Delta\ell_{\text{bin}}} (C_{\ell_{\text{bin}}}^{XX})^2, \quad (2)$$

where $X = \{E, B\}$, f_{sky} is the retained sky fraction (which can be $f_{\text{sky}}^{\text{eff}}$ if the sky field is apodized), and $\Delta\ell_{\text{bin}}$ is the size of the multipole bin ℓ_{bin} . To estimate the error relevant to the polarized dust signal measured within a given region, we subtract quadratically this estimate of the contribution from sample variance. The performance of Xpol on Gaussian simulations that have EE and BB dust-like angular power spectra is presented in Appendix A.

3.1.2. Xpure

Xpure is a numerical implementation of the pure pseudo-spectral approach described and validated in Grain et al. (2009). The method is optimized for computing CMB B -mode power spectra over small sky patches. It uses a suitably chosen sky apodization that vanishes (along with its first derivative) at the edges of the patch in order to minimize the effects of E -to- B leakage. For the estimation of the angular power spectra of the *Planck* data we compute the cross-correlation of two different DetSets. Uncertainties are obtained by performing Monte Carlo inhomogeneous white noise simulations, considering the diagonal terms of the pixel-pixel covariance for the two data sets.

We have applied this algorithm to *Planck* 353 GHz maps and simulations to estimate the B -mode power spectrum of the Galactic thermal dust emission in regions ranging from 1% to 30% of the sky. We have used Xpure here as a cross-check for the robustness of the Xpol method presented in the previous section. Validation and comparison of the performance of the two algorithms is presented in Appendix A on simulations and in Appendix D.1 on application to the data.

3.2. Computing cross-spectra

To avoid a bias arising from the noise, we compute all the *Planck* power spectra from cross-correlations of DetSets maps (see Sect. 2). The noise independence of the two DetSet maps at a given frequency was quantified in Planck Collaboration XV (2014) and the resulting level of noise bias in the cross-power spectra between them has been shown to be negligible. The cross-power spectrum at a given frequency ν is

$$C_{\ell}(\nu \times \nu) \equiv C_{\ell}(D_{\nu}^1 \times D_{\nu}^2), \quad (3)$$

where D_{ν}^1 and D_{ν}^2 are the two independent DetSet 1 and DetSet 2 maps at the frequency ν . The *Planck* cross-band spectrum

⁶ Pseudo- C_{ℓ} estimators compute an estimate of the angular power spectra directly from the data (denoted the “pseudo-power spectrum”) and then correct for sky coverage, beam smoothing, data filtering, etc.

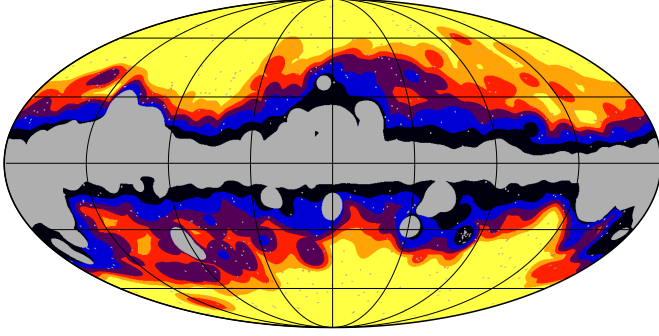


Fig. 1. Masks and complementary selected large regions that retain fractional coverage of the sky f_{sky} from 0.8 to 0.3 (see details in Sect. 3.3.1). The grey is the CO mask, whose complement is a selected region with $f_{\text{sky}} = 0.8$. In increments of $f_{\text{sky}} = 0.1$, the retained regions can be identified by the colours yellow (0.3) to black (0.8), inclusively. Also shown is the (unapodized) point source mask used.

between the frequencies ν and ν' is

$$C_\ell(\nu \times \nu') \equiv \frac{1}{4} \left[C_\ell(D_\nu^1 \times D_{\nu'}^1) + C_\ell(D_\nu^2 \times D_{\nu'}^2) + C_\ell(D_\nu^1 \times D_{\nu'}^2) + C_\ell(D_\nu^2 \times D_{\nu'}^1) \right], \quad (4)$$

or equivalently the cross-spectrum between ν and ν' of the averaged frequency maps $(D_\nu^1 + D_\nu^2)/2$.

As we noted in Sect. 2.2.2, from each computed C_ℓ^{EE} spectrum we subtract the *Planck* best-fit Λ CDM C_ℓ^{EE} model (Planck Collaboration XVI 2014), i.e., the theoretical C_ℓ^{EE} model obtained from the temperature data fit, while C_ℓ^{BB} spectra are kept unaltered.

3.3. Selection of regions

To measure the dust polarization power spectra with high S/N, we select six large regions, the analysis regions of interest at intermediate Galactic latitude, which have effective coverage of the sky from 24 to 72% (see Sect. 3.3.1)⁷. For statistical studies at high Galactic latitude, we compute spectra on a complete set of smaller regions or patches (Sect. 3.3.2), similar in size to the patches observed in typical CMB experiments.

3.3.1. Large regions

For selection of all of the large regions, we used the *Planck* CO map from Planck Collaboration XIII (2014), smoothed to a 5° resolution, to mask the sky wherever the CO line brightness $I_{\text{CO}} \geq 0.4 \text{ K km s}^{-1}$ ⁸. This mask is shown in Fig. 1. The complement to this mask by itself defines a preliminary region that retains a sky fraction $f_{\text{sky}} = 0.8$.

We then mask the sky above successively lower thresholds of I_{857} in the *Planck* 857 GHz intensity map, smoothed to a 5° resolution, chosen such that together with the CO mask we select five more preliminary regions that retain f_{sky} from 0.7 to 0.3 in steps of 0.1. These six regions are shown in Fig. 1.

⁷ Although the selection process is similar to that in Planck Collaboration XV (2014), there are differences in detail.

⁸ We use the CO ($J=1 \rightarrow 0$) type 3 map, which has the highest S/N. At this resolution and for this map, the cut we apply corresponds to $S/N > 8$.

To avoid power leakage, these six masks are then apodized by convolving with a 5° FWHM Gaussian which alters the window function by gradually reducing the signal towards the edges of the retained regions and thus lowers the effective retained sky coverage. The $f_{\text{sky}}^{\text{eff}}$ value is simply defined as the mean sky coverage of the window function map.

Finally, we mask data within a radius $2\sigma_{\text{beam}}$ of point sources selected from the *Planck* Catalogue of Compact Sources (PCCS, Planck Collaboration XXVIII 2014) at 353 GHz. The selected sources have $S/N > 7$ and a flux density above 400 mJy ⁹. Selection of spurious infrared sources in bright dust-emitting regions is avoided by using contamination indicators of infrared cirrus listed in the PCCS description (Planck Collaboration XXVIII 2014). This point-source masking is done to prevent the brightest polarized sources from producing ringing in the power spectrum estimation, while avoiding the removal of dust emitting regions and their statistical contribution to the angular power spectra. The details of this source selection will be presented in the *Planck* 2014 release papers. The edges of the masks around point sources were apodized with a $30'$ FWHM Gaussian, further reducing the retained net effective sky coverage.

In combination these masking and apodization procedures result in six large retained (LR) regions, which we label using the percentage of the sky retained (the net effective fractional sky coverages, $f_{\text{sky}}^{\text{eff}}$, are listed in Table 1), e.g., LR72 for the largest region and LR24 for the smallest.

Table 1 also lists other properties of the regions, including $\langle I_{353} \rangle$, the mean specific intensity at 353 GHz within the region in MJy sr^{-1} , and N_{HI} , the mean HI column density in units of 10^{20} cm^{-2} computed on the LAB HI survey data cube (Kalberla et al. 2005).

3.3.2. Small patches at high Galactic latitude

To examine the statistics of the angular power spectra at high Galactic latitude, we also analyse the *Planck* polarization maps within patches with a size similar to those of typical ground-based and balloon-borne CMB experiments (e.g., QUIET Collaboration et al. 2012; Hanson et al. 2013; BICEP2 Collaboration 2014b; Ade et al. 2014; Naess et al. 2014). Specifically, we consider 400 deg^2 circular areas (radius 11.3°) centred on the central pixel positions of the HEALPix $N_{\text{side}} = 8$ grid that have Galactic latitude $|b| > 35^\circ$. This results in 352 such patches. These are apodized with a 2° FWHM Gaussian, which reduces the retained sky fraction to $f_{\text{sky}}^{\text{eff}} = 0.0080$ for each patch. For these small patches, we do not mask point sources as was done in selecting the large regions, since we want to preserve the same $f_{\text{sky}}^{\text{eff}}$ for each mask, nor is the CO mask needed, since we use these masks only on the 353 GHz high Galactic latitude data. We note that for $N_{\text{side}} = 8$, pixels have an area of about 54 deg^2 and characteristic centre-to-centre spacing of about 7.4° . Therefore, this HEALPix grid oversamples the sky relative to this patch size, so that the patches overlap and are not independent.

⁹ This included the brightest point sources in the Large and Small Magellanic Clouds (LMC and SMC). We tested that masking the entirety of the LMC and SMC has no significant effect on the spectra or on the conclusions that we derive from them.

Table 1. Properties of the large retained (LR) science regions described in Sect. 3.3.1.

	LR24	LR33	LR42	LR53	LR63	LR72
f_{sky}	0.3	0.4	0.5	0.6	0.7	0.8
$f_{\text{sky}}^{\text{eff}}$	0.24	0.33	0.42	0.53	0.63	0.72
$\langle I_{353} \rangle / \text{MJy sr}^{-1}$	0.068	0.085	0.106	0.133	0.167	0.227
$N_{\text{HI}} / 10^{20} \text{ cm}^{-2}$	1.65	2.12	2.69	3.45	4.41	6.05
α_{EE}	-2.40 ± 0.09	-2.38 ± 0.07	-2.34 ± 0.04	-2.36 ± 0.03	-2.42 ± 0.02	-2.43 ± 0.02
α_{BB}	-2.29 ± 0.15	-2.37 ± 0.12	-2.46 ± 0.07	-2.43 ± 0.05	-2.44 ± 0.03	-2.46 ± 0.02
$\chi^2_{EE} (\alpha_{EE} = -2.42, N_{\text{d.o.f.}} = 21)$..	26.3	28.1	31.8	38.3	32.7	44.8
$\chi^2_{BB} (\alpha_{BB} = -2.42, N_{\text{d.o.f.}} = 21)$..	18.9	14.0	21.1	22.1	15.4	21.9
$A^{EE} (\ell = 80)$	37.5 ± 1.6	51.0 ± 1.6	78.6 ± 1.7	124.2 ± 1.9	197.1 ± 2.3	328.0 ± 2.8
$\langle A^{BB}/A^{EE} \rangle$	0.49 ± 0.04	0.48 ± 0.03	0.53 ± 0.02	0.54 ± 0.02	0.53 ± 0.01	0.53 ± 0.01

Notes. For each region, f_{sky} is the initial sky fraction, $f_{\text{sky}}^{\text{eff}}$ its value after point source masking and apodization, $\langle I_{353} \rangle$ the mean specific intensity at 353 GHz within the region, in MJy sr⁻¹, and N_{HI} the mean HI column density, in units of 10²⁰ cm⁻² (Kalberla et al. 2005). For the power-law fits in multipole ℓ , we also list the exponents α_{EE} and α_{BB} (Sect. 4.2), the χ^2 of the fits with fixed exponents $\alpha_{EE} = \alpha_{BB} = -2.42$, the value A^{EE} of the fitted \mathcal{D}_ℓ^{EE} amplitude at $\ell = 80$ (in $\mu\text{K}_{\text{CMB}}^2$ at 353 GHz, Sect. 4.3), and the mean of the amplitude ratio $\langle A^{BB}/A^{EE} \rangle$ (see Sect. 4.4).

4. Dust polarized angular power spectra at intermediate Galactic latitude

In this section, we quantify the 353 GHz dust polarization in the power spectrum domain, achieving a high S/N through the use of LR regions. For convenience we present results for \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} , where $\mathcal{D}_\ell \equiv \ell(\ell+1)C_\ell/(2\pi)$.

4.1. Description of the spectra

Using Xpol we have computed \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} from the two DetSets at 353 GHz, as a function of the multipole ℓ in the range 40–600¹⁰. These represent the first measurements of the thermal dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} power spectra on large fractions of the sky for $\ell > 40$ (see Ponthieu et al. 2005; Gold et al. 2011, for earlier related studies).

In Fig. 2 we present the results for $f_{\text{sky}} = \{0.3, 0.5, 0.7\}$. The amplitudes of the spectra increase with increasing f_{sky} because the polarized emission is brighter on average when more sky is retained. We point out that the LR regions presented in Sect. 3.3.1 overlap because they form a nested set. However, the power spectra derived from them are almost independent of each other because each spectrum is dominated by the brightest areas in the corresponding region, namely the parts closest to the Galactic plane and hence the areas in which each LR region differs from those nested inside it.

The \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra are characterized by a power-law dependence on multipole ℓ over the range $\ell = 40$ to 600; furthermore, the slope is similar for different regions that retain from 24 to 63% of the sky.

Figure 2 also shows the \mathcal{D}_ℓ^{EE} power spectrum computed from the Planck 2013 best-fit ΛCDM model of the CMB temperature data (Planck Collaboration XVI 2014), and the much lower expectation for \mathcal{D}_ℓ^{BB} from the CMB model with primordial gravitational waves with amplitude $r = 0.2$. At 353 GHz, the \mathcal{D}_ℓ^{EE} angular power spectra of the dust are about 3–4 orders of magnitude larger than the CMB model at $\ell = 30$, 1–2 orders of magnitude

larger at $\ell = 100$, and about the same order of magnitude as the CMB at $\ell > 300$. At 353 GHz, the \mathcal{D}_ℓ^{BB} angular power spectra for dust are much greater than the CMB model power spectrum for all ℓ values in Fig. 2. The dust power spectra are larger than the $r = 0.2$ CMB spectrum by 4–5 orders of magnitude at $\ell = 30$, and by 3–4 orders of magnitude at $\ell = 100$. At $\ell = 500$, where the lensing of CMB anisotropies is the dominant contribution to the CMB model spectrum, the dust is still 2–3 orders of magnitude higher.

As discussed in Appendix A, we do not expect any significant bias, or E -to- B leakage, from the computation of the dust angular power spectra using Xpol. Figure 2 also includes the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra at 353 GHz, computed from our estimate of the leakage terms from intensity to polarization (discussed in Sect. 2.3), for the same three LR regions. The dust spectra are much higher than the corresponding spectra for the leakage, which represent the main systematic effects over the ℓ range of interest for this work. The largest contamination of the dust signal by leakage is about 3.5% at $\ell = 50$, for both the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra. Because we consider that our estimate of the leakage maps is conservative, we conclude that contamination of the dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} power spectra by systematic effects amounts to a maximum of 4% at $\ell = 50$, and is less at higher multipoles. Therefore, we have not corrected the Planck data for intensity-to-polarization leakage in this work.

Finally, in Fig. 2 we present for the three LR regions the absolute value of the null-test spectra anticipated in Sect. 2.3, here computed from the cross-spectra of the HalfRing/DetSet differences, i.e., $(353_{\text{DS1,HR1}} - 353_{\text{DS1,HR2}})/2 \times (353_{\text{DS2,HR1}} - 353_{\text{DS2,HR2}})/2$. These \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra show a behaviour that is close to what is expected from a white-noise dominated (thus ℓ^2) spectrum. The amplitudes of these error estimates are consistent with the noise expectations; there is no evidence for any effects of systematics.

For completeness, in Appendix B we present a further quantification of the power spectrum of thermal dust emission at 353 GHz via the spectra involving temperature and polarization, \mathcal{D}_ℓ^{TE} and \mathcal{D}_ℓ^{TB} , and the polarization cross-spectrum, \mathcal{D}_ℓ^{EB} .

¹⁰ The spectra are in units of $\mu\text{K}_{\text{CMB}}^2$ at 353 GHz.

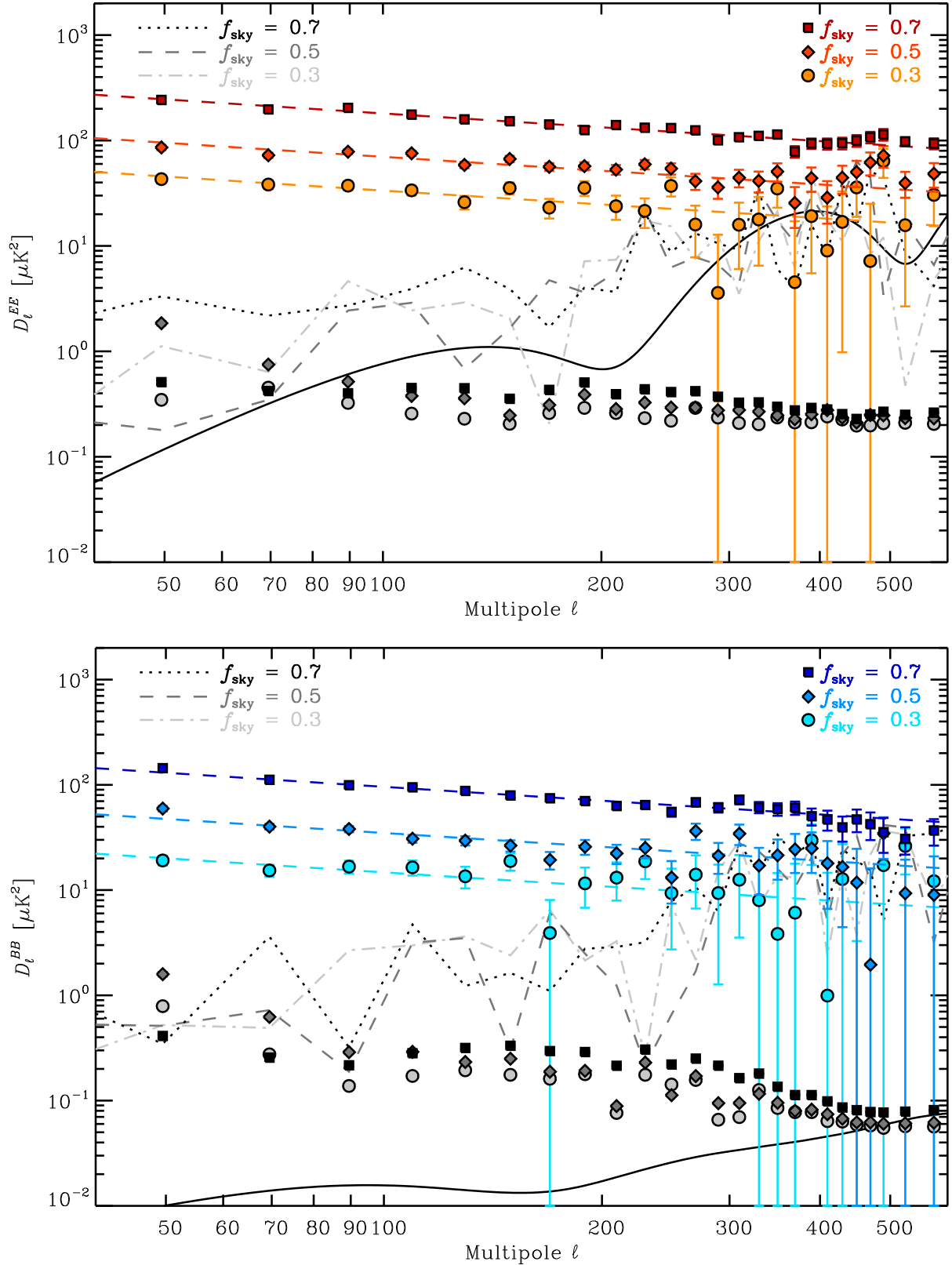


Fig. 2. *Planck* HFI 353 GHz \mathcal{D}_ℓ^{EE} (red, top) and \mathcal{D}_ℓ^{BB} (blue, bottom) power spectra (in $\mu\text{K}_{\text{CMB}}^2$) computed on three of the selected LR analysis regions that have $f_{\text{sky}} = 0.3$ (circles, lightest), $f_{\text{sky}} = 0.5$ (diamonds, medium) and $f_{\text{sky}} = 0.7$ (squares, darkest). The uncertainties shown are $\pm 1\sigma$. The best-fit power laws in ℓ are given for each spectrum as a dashed line of the corresponding colour. The *Planck* 2013 best-fit ΛCDM \mathcal{D}_ℓ^{EE} expectation (Planck Collaboration XVI 2014) and the corresponding $r = 0.2$ \mathcal{D}_ℓ^{BB} CMB model are shown as solid black lines; the rise for $\ell > 200$ is from the lensing contribution. In the lower parts of each panel, the global estimates of the power spectra of the systematic effects responsible for intensity-to-polarization leakage (Sect. 2.3) are shown in different shades of grey, with the same symbols to identify the three regions. Finally, absolute values of the null-test spectra anticipated in Sect. 2.3, computed here from the cross-spectra of the HalfRing/DetSet differences (see text), are represented as dashed-dotted, dashed, and dotted grey lines for the three LR regions.

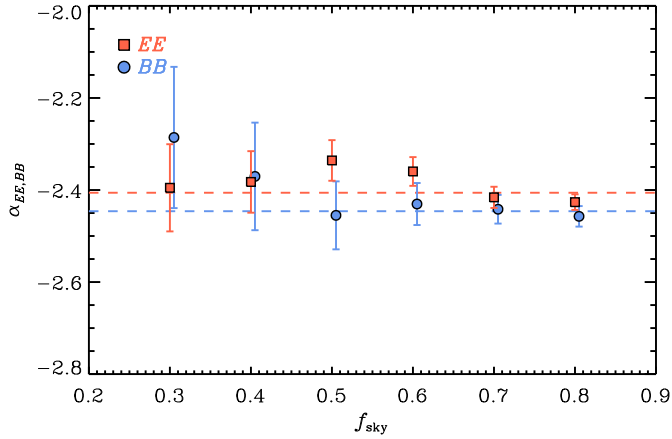


Fig. 3. Best-fit power-law exponents α_{EE} (red squares) and α_{BB} (blue circles) fitted to the 353 GHz dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} power spectra for the different LR regions defined in Sect. 3.3.1, distinguished here with f_{sky} . Although the values in the regions are not quite independent, simple means have been calculated and are represented as red and blue dashed lines.

4.2. Power-law fit

To assess the apparent power-law dependence $C_\ell^{XX} \propto \ell^{\alpha_{XX}}$ quantitatively, we made a χ^2 fit to the spectra at 353 GHz using the form $\mathcal{D}_\ell^{XX} = A^{XX}(\ell/80)^{\alpha_{XX}+2}$, where $X \in \{E, B\}$. For \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} we fit the 22 band-powers in the range $60 < \ell < 500$. For both power spectra we restricted the fit to $\ell > 60$ to avoid a possible bias from systematic effects in the data, and also because the angular power spectra of the dust polarization exhibit more spatial variation than is expected for a Gaussian random field, particularly on large angular scales.

The exponents of the power-law fits, α_{XX} , are plotted in Fig. 3 for each of the six LR regions identified with f_{sky} . All exponents are consistent with constant values of $\alpha_{EE} = -2.41 \pm 0.02$ and of $\alpha_{BB} = -2.45 \pm 0.03$. While there is a slight indication of a steeper slope for \mathcal{D}_ℓ^{BB} than for \mathcal{D}_ℓ^{EE} , hereafter we adopt the mean exponent -2.42 ± 0.02 . This exponent is consistent with the value α_{TT} fitted to the *Planck* 353 GHz dust intensity power spectra in this range of ℓ (Planck Collaboration XV 2014; Planck Collaboration Int. XXII 2015) on similar-sized regions at intermediate Galactic latitude, but slightly flatter than the α_{TT} fitted at higher ℓ and higher frequency (Miville-Deschênes et al. 2007, 2010; Planck Collaboration XV 2014).

For the fits with fixed exponent $\alpha_{EE, BB} = -2.42$, the values of the χ^2 (with number of degrees of freedom, $N_{\text{d.o.f.}} = 21$) are listed in Table 1 for the six LR regions. For the \mathcal{D}_ℓ^{EE} spectra, the χ^2 values range from 26.3 (probability to exceed, PTE = 0.2) to 44.8 (PTE = 0.002), with a trend for a quality of fit that degrades with increasing f_{sky} . For the \mathcal{D}_ℓ^{BB} spectra, the χ^2 values range from 14.0 (PTE = 0.87) to 22.1 (PTE = 0.39), with a trend related to f_{sky} .

Possible explanations for this difference between \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectrum shape descriptions, are the chance correlation between dust and CMB polarization, which is not taken into account in the subtraction of the CMB \mathcal{D}_ℓ^{EE} spectrum, and the increasing S/N degrading the overall quality of the fit when going from \mathcal{D}_ℓ^{BB} to \mathcal{D}_ℓ^{EE} and for \mathcal{D}_ℓ^{EE} from $f_{\text{sky}} = 0.3$ to $f_{\text{sky}} = 0.8$ as the amplitude of the dust polarized signal increases. We stress that while the power law in ℓ is a good general description of the shape of the dust polarized power spectra, a full characterization would have to consider the detailed features that can be seen in Fig. 2.

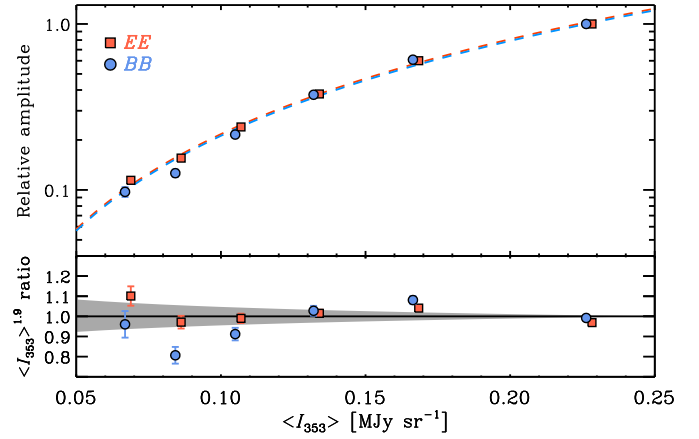


Fig. 4. Amplitude of the dust A^{EE} (red squares) and A^{BB} (blue circles) power spectra, normalized with respect to the largest amplitude for each mode. These are plotted versus the mean dust intensity $\langle I_{353} \rangle$ for the six LR regions (top panel). A power-law fit of the form $A^{XX}(\langle I_{353} \rangle) = K_{XX} \langle I_{353} \rangle^{1.9}$, $X \in \{E, B\}$, is overplotted as a dashed line of the corresponding colour (these almost overlap). The bottom panel presents the ratio of the data and the fitted $\langle I_{353} \rangle^{1.9}$ power law; the range associated with the $\pm 1\sigma$ uncertainty in the power-law exponent of 1.9 is shown in grey. For details see Sect. 4.3.

4.3. Amplitude dependence on $\langle I_{353} \rangle$

Similarly to what has been done for intensity power spectra in, e.g., Gautier et al. (1992) and Miville-Deschênes et al. (2007), we investigate how the amplitude of the dust polarization power spectrum scales with the dust intensity. To quantify the dust emission at 353 GHz, we use the model map derived from a modified blackbody fit to the *Planck* data at $\nu \geq 353$ GHz and IRAS at $\lambda = 100 \mu\text{m}$, presented in Planck Collaboration XI (2014). This map is corrected for zodiacal emission and the brightest extragalactic point sources are subtracted. The Galactic reference offsets of the underlying IRAS and *Planck* data were obtained through a method based on correlation with 21 cm data from the LAB HI survey (Kalberla et al. 2005) integrated in velocity, effectively removing the CIB monopole in the model map. The mean dust intensity, $\langle I_{353} \rangle$, listed for each LR region in Table 1, ranges from 0.068 to 0.227 MJy sr $^{-1}$ for increasing $f_{\text{sky}}^{\text{eff}}$. The mean column density calculated from the LAB survey data is also listed in Table 1, with values ranging from $1.65 \times 10^{20} \text{ cm}^{-2}$ to $6.05 \times 10^{20} \text{ cm}^{-2}$.

For all of the LR regions, we fit the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra with a power law in ℓ , using the fixed exponent $\alpha_{EE, BB} = -2.42$, over the ℓ -ranges defined in Sect. 4.2. The amplitudes A^{EE} derived from these fits are listed in Table 1; the A^{BB} amplitudes can be retrieved from the A^{BB}/A^{EE} ratio. These amplitudes are plotted as a function of $\langle I_{353} \rangle$ in Fig. 4 after normalization by the maximum value found for the largest region (LR72). We fit the empirical dependence of these amplitudes on $\langle I_{353} \rangle$ as a power law of the form $A^{XX}(\langle I_{353} \rangle) = K_{XX} \langle I_{353} \rangle^{\epsilon_{XX}}$ where $X \in \{E, B\}$. The two fitted exponents are quite similar, $\epsilon_{EE} = 1.88 \pm 0.02$ and $\epsilon_{BB} = 1.90 \pm 0.02$. The exponent that we find for polarization is close to the one observed in the diffuse interstellar medium for the dust intensity, consistent with $A_\nu^{TT} \propto \langle I_\nu \rangle^2$, where $\langle I_\nu \rangle$ is the mean value of the dust specific intensity (Miville-Deschênes et al. 2007). Values close to 2 are expected, because we compute angular power spectra, which deal with squared quantities.

Although the data points roughly follow this $\langle I_{353} \rangle^{1.9}$ dependence, the empirical law fails to fully describe individual dust amplitudes (e.g., the estimate is off by about 20% for \mathcal{D}_ℓ^{BB} on

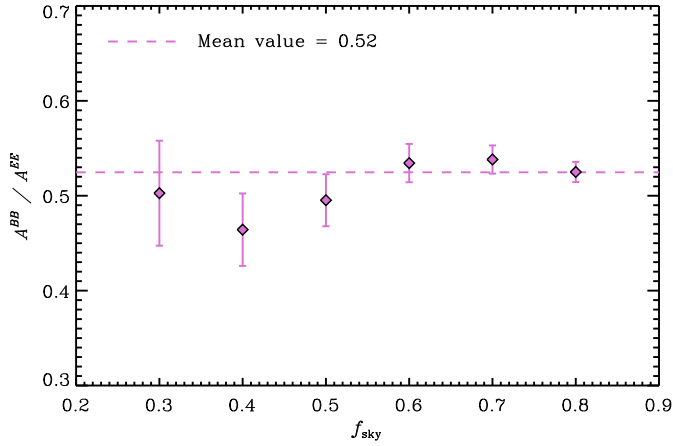


Fig. 5. Ratio of the amplitudes of the \mathcal{D}_ℓ^{BB} and \mathcal{D}_ℓ^{EE} dust power spectra at 353 GHz for the different LR regions defined in Sect. 3.3.1, distinguished here with f_{sky} . The mean value $\langle A^{BB}/A^{EE} \rangle = 0.52$ is plotted as a dashed line.

LR33). The scaling can help to assess the order of magnitude of the dust polarization level on a specific region, but is not a substitute for actually characterizing the polarized angular power spectra.

4.4. Amplitude of \mathcal{D}_ℓ^{BB} relative to \mathcal{D}_ℓ^{EE}

We examine the ratio of the amplitudes of the fitted power laws found in Sect. 4.3. The A^{BB}/A^{EE} ratios are listed in Table 1, and are plotted for different values of f_{sky} in Fig. 5. For all of the LR regions, we observe more power in the \mathcal{D}_ℓ^{EE} dust spectrum than in \mathcal{D}_ℓ^{BB} . All ratios are consistent with a value of $A^{BB}/A^{EE} = 0.52 \pm 0.03$, significantly different from unity, over various large fractions of the intermediate latitude sky.

This result is not taken into account in existing models of polarized microwave dust emission that have been developed to test component separation methods. For example, we have computed the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra over the LR regions for the *Planck* Sky Model (Delabrouille et al. 2013) and the model of O’Dea et al. (2012); for both models and all LR regions we find a ratio A^{BB}/A^{EE} close to 1. However, these two models are based on a very simplified picture of the Galactic magnetic field geometry and assumptions on how the polarized emission depends on it. Further insight into the structure of the dust polarization sky is required to account for the observed ratio.

4.5. Amplitude dependence on frequency

Finally, we explore the frequency dependence of the amplitude of the angular power spectra. We compute the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} angular power spectra from the *Q* and *U* DetSet maps at 100, 143, 217, and 353 GHz (see Sect. 3.2). From these four sets of polarization maps, we compute ten power spectra: 100×100 ; 100×143 ; 100×217 ; 100×353 ; 143×143 ; 143×217 ; 143×353 ; 217×217 ; 217×353 ; and 353×353 .

The ten angular cross-power spectra are consistent with a power law in ℓ , with the exponent $\alpha_{EE,BB} = -2.42$ measured at 353 GHz (Sect. 4.2). Therefore, to each of these spectra we fit the amplitudes of a power-law function that has a fixed exponent $\alpha_{EE,BB} = -2.42$, in the range $40 < \ell < 500$, for \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} . As an illustration of the quality of the fit, for the smallest region (LR24, $f_{\text{sky}} = 0.3$) the averages and dispersions of

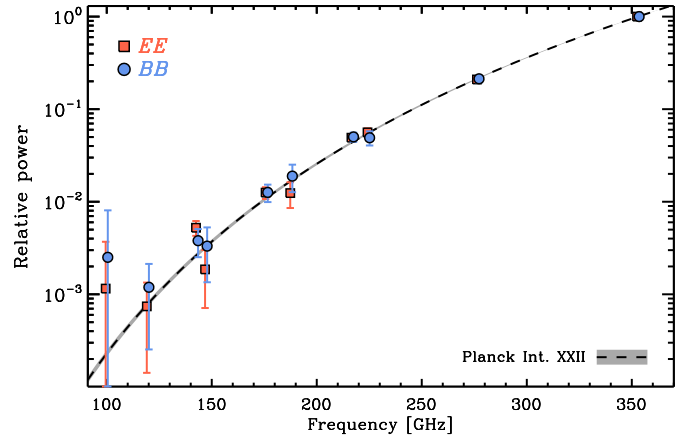


Fig. 6. Frequency dependence of the amplitudes $A^{EE,BB}$ of the angular power spectra, relative to 353 GHz (see details in Sect. 4.5). Results for \mathcal{D}_ℓ^{EE} (red squares) and \mathcal{D}_ℓ^{BB} (blue circles) for the smallest region, LR24. These include evaluations from cross-spectra involving polarization data at two frequencies, plotted at the geometric mean frequency. The square of the adopted relative SED for dust polarization, which is a modified blackbody spectrum with $\beta_d = 1.59$ and $T_d = 19.6$ K, is shown as a black dashed line. The $\pm 1\sigma$ uncertainty area from the expected dispersion of β_d , 0.03 for the size of LR24 as inferred from Planck Collaboration Int. XXII (2015) (see Sect. 2.2.1), is shown in grey.

the χ^2 (21 degrees of freedom) of the fits are $\chi_{EE}^2 = 13.4 \pm 8.2$ and $\chi_{BB}^2 = 12.8 \pm 6.9$ for the ten cross-frequency spectra.

To compare the frequency dependence of the results of the fits to that expected from the SED for dust polarization from Planck Collaboration Int. XXII (2015), we converted the fitted amplitudes $A^{EE,BB}$ from $\mu\text{K}_{\text{CMB}}^2$ to units of $(\text{MJy sr}^{-1})^2$, taking into account the *Planck* colour corrections¹¹. For all regions, we examined the frequency dependence by plotting the amplitudes normalized to unity at 353 GHz versus the effective frequency¹². A representative example is shown in Fig. 6 for the smallest region, LR24 ($f_{\text{sky}} = 0.3$).

For all of the LR regions the frequency dependence found is in good agreement with the square of the adopted dust SED, which is a modified blackbody spectrum having $\beta_d = 1.59$ and $T_d = 19.6$ K (Planck Collaboration Int. XXII 2015). We note that no fit was performed at this stage and that the square of the adopted dust SED goes through the 353 GHz data point. However, if we fit the amplitude of the dust frequency dependence, with fixed β_d and T_d , the χ^2 ($N_{\text{d.o.f.}} = 9$) is 13.1 for *EE* (PTE = 0.16) and 3.2 for *BB* (PTE = 0.96). This good agreement supports the assumption made in the present work about the faintness of the synchrotron and CO emission at high Galactic latitude (see Sect. 2.2). The residuals to the fit do not show any evidence for excess power at 100 GHz, which might arise from polarized synchrotron emission. This result is consistent with the study of synchrotron polarization at high Galactic latitudes by Fuskeland et al. (2014), and confirmed in Appendix D.4. Furthermore, we do not see any excess at either 100 or 217 GHz, such as could arise from leakage and/or

¹¹ Conversion factors were computed as described in Sect. 2.1, here using colour corrections corresponding to a dust modified blackbody spectrum with $\beta_d = 1.59$ and $T_d = 19.6$ K.

¹² For a cross-spectrum between data at frequency ν_1 and frequency ν_2 , the effective frequency is taken for convenience as the geometric mean $\nu_{\text{eff}} \equiv \sqrt{\nu_1 \nu_2}$.

polarization associated with CO line emission in these bands (Sect. 2.2.5).

5. Statistical study of the dust power spectra at high Galactic latitudes

In Sect. 4, statistical properties of dust polarization were derived from angular power spectra computed with the *Planck* 353 GHz data on large fractions of the sky ($f_{\text{sky}}^{\text{eff}}$ from 24% to 72%). Most of the CMB experiments target fields at high Galactic latitude with a smaller size than this. So now we evaluate the dust B -mode power in such patches.

We perform a statistical analysis computing the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} power spectra of the 353 GHz *Planck* polarization data for high Galactic latitude circular patches of size 400 deg^2 , similar to the size of the fields observed in ground-based and balloon-borne CMB polarization experiments (see Sect. 3.3.2). We verify that the empirical scaling law of the power spectra amplitudes as a function of the mean intensity, derived in Sect. 4.3, holds on small independent fractions of the sky that are not nested.

5.1. Data processing

We compute the dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} angular power spectra at 353 GHz from the cross-spectra of the two DetSets with independent noise in this channel, using Xpol on all of the 352 high Galactic latitude ($|b| > 35^\circ$) patches defined in Sect. 3.3.2. As shown in Appendix A, we do not expect any significant cut-sky leakage from E polarization to B polarization for the dust in such patches. The \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra are computed in the range $40 < \ell < 370$, using top-hat binning in the intervals defined between multipoles 40, 70, 110, 160, 220, 290, and 370.

To each of the 352 \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra we fit the power law in ℓ presented in Sect. 4.2 over the range $40 < \ell < 370$ with a slope fixed to $\alpha_{EE,BB} = -2.42$ in order to compute the amplitudes $A^{EE,BB}$ and their associated errors. Since we are interested in quantifying the possible contamination by dust polarization for ground-based CMB experiments, here we express the amplitude of the fitted power laws at the position of the recombination bump at $\ell = 80$ ($A_{\ell=80}^{EE,BB} = A^{EE,BB} \times 80^{-0.42}$). In Appendix C.1, using a null test, we show that the potential systematic effects in the data do not affect the computation of the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectrum amplitudes.

5.2. Results

For patches covering 1% or more of the sky, we do not observe any significant departure in the shapes of the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra from the results presented in Sect. 4.2, even if a large dispersion of the power-law exponent (attributable to the low S/N for some patches) is observed. The $\mathcal{D}_\ell^{BB}/\mathcal{D}_\ell^{EE}$ ratios are on average consistent with what has been derived on the larger LR regions in Sects. 4.4. These ratios are presented in Appendix C.2.

The fitted dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} amplitudes (A^{EE} and A^{BB}) at $\ell = 80$ are presented in Fig. 7 in units of $\mu\text{K}_{\text{CMB}}^2$ at 353 GHz and as a function of the mean dust intensity $\langle I_{353} \rangle$ of each patch.

We see a clear correlation of the dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} amplitudes with $\langle I_{353} \rangle$. The data points are consistent with the same $\langle I_{353} \rangle$ dependence of the scaling law found in Sect. 4.3, $A^{EE,BB} \propto \langle I_{353} \rangle^{1.9}$, indicating that this empirical law also applies in the faintest regions of the sky and holds reasonably well for the description of the amplitudes for any approximately 1% patch of the sky at latitudes above 35° .

The amplitudes of the two empirical scaling laws are adjusted to the data points by computing the median over all the patches of $A^{EE,BB}/\langle I_{353} \rangle^{1.9}$. The amplitudes that we derive from Fig. 7 are in agreement with the amplitudes reported for the LR regions in Sect. 4.3 and Table 1.

The dust brightness $\langle I_{353} \rangle$ in the cleanest 400 deg^2 patches ($\langle I_{353} \rangle$ down to $0.038 \text{ MJy sr}^{-1}$) is about a factor of 2 lower than the value listed in Table 1 for the LR24 region ($0.068 \text{ MJy sr}^{-1}$). Applying the empirical scaling derived in Sect. 4.3, the expected level of the dust polarization angular power spectrum is a factor of $(0.068/0.038)^{1.9} = 3$ higher on 24% of the sky than on the faintest patches.

A dispersion around this empirical power law for the patches is observed. The shaded regions in Fig. 7 show the expected scatter in this relation coming from the noise, together with Gaussian sample variance. The former is computed from *Planck* inhomogeneous noise Monte Carlo simulations presented in Appendix C.1 and the latter is computed given the $f_{\text{sky}}^{\text{eff}}$ and the binning used to determine the spectra (see Sect. 5.1). Thus, the general trend of the dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} amplitudes among these patches follows the empirical scaling in $\langle I_{353} \rangle$, but the inhomogeneous nature of the polarized dust emission, including variations in magnetic field orientation and grain alignment, is responsible for the large dispersion around it, larger than expected for a stationary Gaussian process plus instrumental noise.

Even at low $\langle I_{353} \rangle$, the statistical error on the \mathcal{D}_ℓ^{BB} amplitude at $\ell = 80$ for such small patches is at least $7.5 \mu\text{K}_{\text{CMB}}^2 (3\sigma)$.

5.3. Optimizing the search for a primordial B -mode signal at the recombination peak

In Sect. 5.1 the 353 GHz A^{BB} amplitudes were obtained for the 352 patches of 400 deg^2 at Galactic latitudes $|b| > 35^\circ$. These amplitudes are expressed at $\ell = 80$, the approximate position of the maximum of the CMB tensor B -mode recombination peak. In order to extrapolate these amplitudes to 150 GHz, an observing frequency typical of CMB experiments searching for B -modes, we use the dust SED of Planck Collaboration Int. XXII (2015) presented in Sect. 2.2.1, which is a modified blackbody spectrum with $\beta_d = 1.59 \pm 0.17$ and $T_d = 19.6 \text{ K}$. The conversion factor from the *Planck* 353 GHz band to the 150 GHz central frequency for this extrapolation, taking into account the *Planck* colour corrections and the statistical uncertainty of β_d , is $0.0395^{+0.0045}_{-0.0035}$ in the SED, and this squared in \mathcal{D}_ℓ^{BB} .

These extrapolated estimates are divided by the value of the $r = 1$ primordial tensor CMB \mathcal{D}_ℓ^{BB} spectrum at $\ell = 80$, $6.71 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$, to express the estimated power in units that we denote r_d . Because the CMB primordial tensor B -mode power scales linearly with r ¹³, a value $r_d = 0.1$ would mean that the expected contamination from dust at $\ell = 80$ is equal to the amplitude of the primordial tensor CMB \mathcal{D}_ℓ^{BB} for $r = 0.1$. For each of these estimates we also compute $\sigma(r_d)$, the quadratic sum of the fit errors on A^{BB} and the above uncertainty from the extrapolation to 150 GHz. We note that the fitted amplitudes A^{BB} for five of these patches are negative¹⁴, but are consistent with $r_d = 0$ at 1σ . The r_d values vary from -0.17 to more than 10 and $\sigma(r_d)$ ranges from as small as 5.6×10^{-2} to larger than 10. Taking the smallest value of $\sigma(r_d)$ we see that *Planck* measurements of the dust \mathcal{D}_ℓ^{BB} spectra for such small patches have, at best, a statistical uncertainty of $0.17 (3\sigma)$ in r_d units.

¹³ This spectrum does not include the CMB lensing B -mode signal, which would become dominant even at $\ell = 80$ for a very low r .

¹⁴ Negative values can arise in cross-spectra, as computed here.

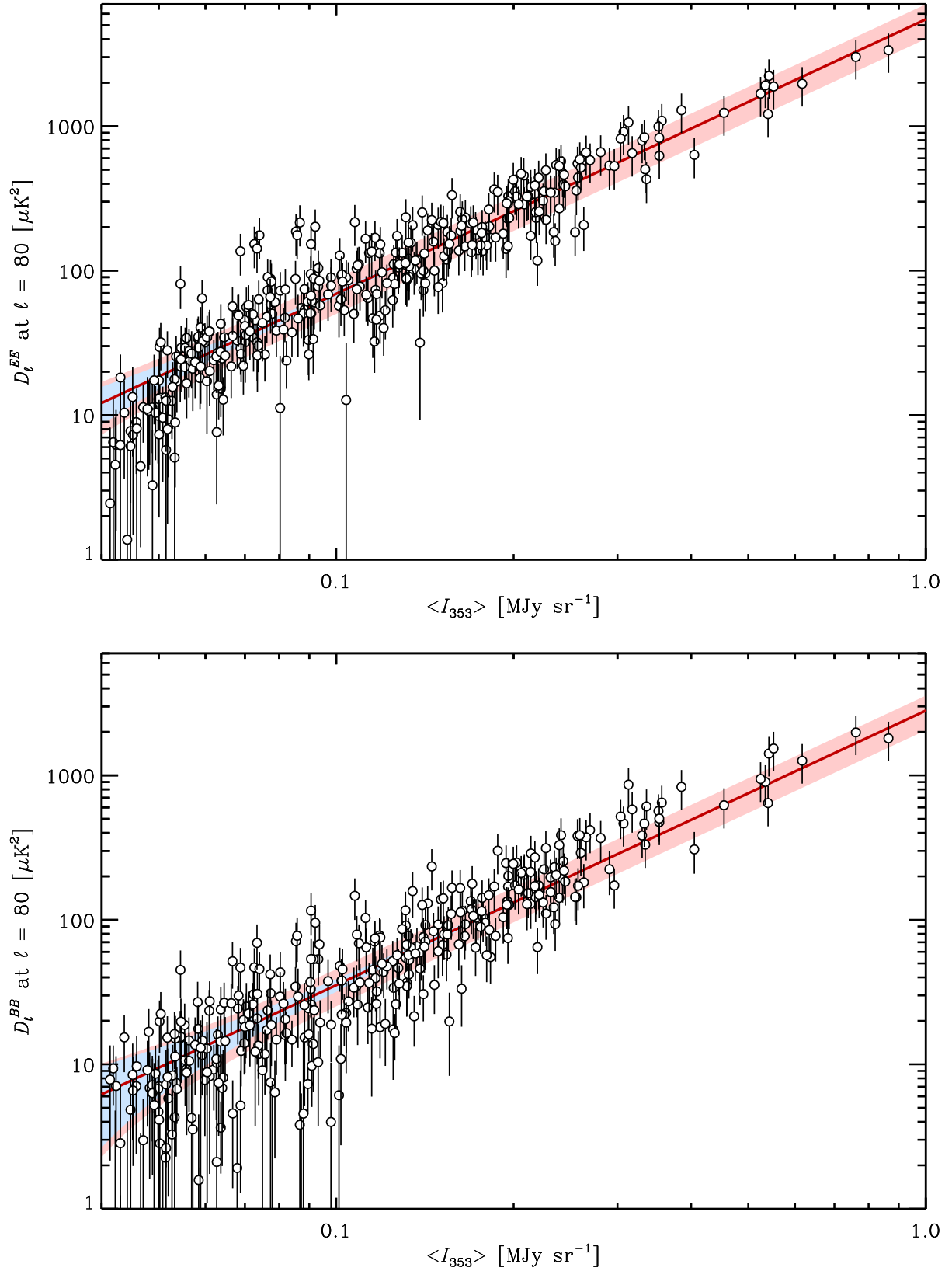


Fig. 7. Fitted dust \mathcal{D}_ℓ^{EE} (top panel) and \mathcal{D}_ℓ^{BB} (bottom panel) amplitudes (A^{EE} and A^{BB}) at $\ell = 80$, in μK^2 for the 400 deg^2 patches as a function of their mean $\langle I_{353} \rangle$. The empirical scaling law, $A^{EE, BB} \propto \langle I_{353} \rangle^{1.9}$, adjusted in amplitude to the data points, is overplotted as a red line. The $\pm 3\sigma$ statistical error on this relation from Monte Carlo simulations of *Planck* inhomogeneous noise (see Appendix C.1) is represented as a light blue shaded area and the total $\pm 3\sigma$ error, including statistical noise plus Gaussian sample variance, is represented as a light red shaded area. Points are computed for all 352 patches, but we note that, as described in Sect. 3.3.2, the patches overlap and so their properties are not independent.

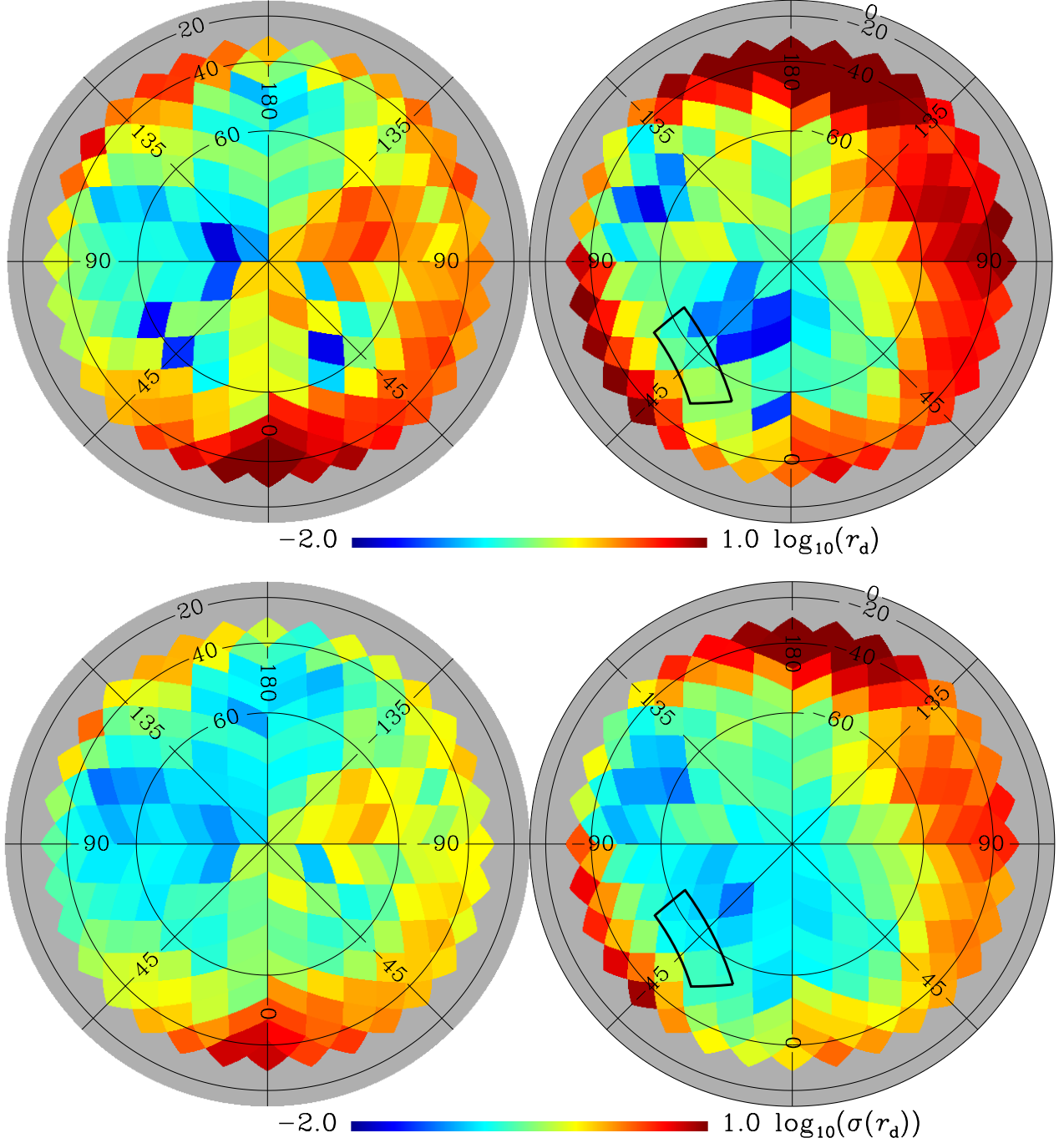


Fig. 8. *Top:* map in orthographic projection of the 150 GHz \mathcal{D}_ℓ^{BB} amplitudes at $\ell = 80$, computed from the *Planck* 353 GHz data, extrapolated to 150 GHz, and normalized by the CMB expectation for tensor-to-scalar ratio $r = 1$. The colours represent the estimated contamination from dust in r_d units (see details in Sect. 5.3). The logarithm of the absolute value of r_d for a 400 deg^2 patch is presented in the pixel on which the patch is centred. As described in Sect. 3.3.2, the patches overlap and so their properties are not independent. The northern (southern) Galactic hemisphere is on the *left* (*right*). The thick black contour outlines the approximate BICEP2 deep-field region (see Sect. 6). *Bottom:* associated uncertainty, $\sigma(r_d)$.

To reveal the spatial dependence over the high latitude sky, a map of the absolute value of r_d is shown in Fig. 8. Each computed value of r_d is given in a pixel at the position of the centre of each of the 352 patches defined in Sect. 3.3.2 on an $N_{\text{side}} = 8$ HEALPix map. The accompanying map of $\sigma(r_d)$ is also presented.

We can see in Fig. 8 that there is a high latitude region in the southern Galactic hemisphere for which r_d is quite low. This region is also associated with a small estimated uncertainty. For example, the six HEALPix $N_{\text{side}} = 8$ pixels numbered 741,

742, 754, 755, 762, and 763 (in the HEALPix “ring” ordering scheme) have $r_d = 0.053 \pm 0.096$, 0.027 ± 0.098 , -0.062 ± 0.052 , -0.020 ± 0.127 , 0.057 ± 0.122 , and -0.031 ± 0.121 , respectively. These pixels are located around Galactic coordinates $l = -30^\circ$, $b = -70^\circ$.

We stress that the expectation for this low level of dust contamination is valid only for these particular patches, including their positions, sizes, shapes, and apodizations. In addition, because we found the amplitudes of the dust \mathcal{D}_ℓ^{BB} spectra associated with these patches based on a power-law fit, our

estimate does not take into account possible features in the power spectra that might alter the precise value of dust contamination. Nevertheless, there are clearly some patches that appear to be “optimal,” i.e., cleaner than the others. It needs to be emphasized, however, that finding the cleanest areas of the polarized sky for primordial B -mode searches cannot be accomplished accurately using the *Planck* total intensity maps alone.

6. BB angular power spectrum of dust in the BICEP2 field

In this section, we use the *Planck* data and the results presented above to assess the dust polarization in the field observed by the BICEP2 experiment (BICEP2 Collaboration 2014a,b). As above, finding \mathcal{D}_ℓ^{BB} at 150 GHz involves two steps, measuring the power spectrum at 353 GHz and then extrapolating the amplitude to 150 GHz.

6.1. An approximation to the observed BICEP2 field

To define a field similar to and representative of the actual BICEP2 field, we carried out the following steps (at the HEALPix $N_{\text{side}} = 2048$ pixelization): (i) we constructed a mask M by filling the inside of the BICEP2 deep-field outline¹⁵ with 1 and the outside with 0; (ii) we took the complement of this mask, $M' = 1 - M$; (iii) inside M' we computed the distance to the border using the HEALPix “iprocess_mask” procedure; (iv) we smoothed this “distance map” with a 7.5 FWHM Gaussian; (v) we apodized, computing the 7.5 FWHM Gaussian weight from the distance map to obtain M'' ; and (vi) we took the complement of M'' to be our definition of the BICEP2 field (i.e., $M_{B2} = 1 - M''$). The resulting field, which in the rest of this paper we will refer to as M_{B2} , has $f_{\text{sky}}^{\text{eff}} = 0.017$ (689 deg²) and $\langle I_{353} \rangle = 0.060$ MJy sr⁻¹. Its $f_{\text{sky}}^{\text{eff}}$ is larger than the BICEP2 373 deg² deep-field region, but M_{B2} is similar to the BICEP2 inverse noise variance map presented in BICEP2 Collaboration (2014a), even if it extends further in declination but less in right ascension. In Appendix D.2 we show that the main results in this section do not depend significantly on the definition of this field. However, we note that the various applications of filtering in the BICEP2 pipeline mean that their observed spatial modes are a subset of those present within their nominal observed region.

6.2. Statistical estimate of the dust B-mode level in the BICEP2 field

We have seen in Sect. 5.2 that the dust \mathcal{D}_ℓ^{BB} spectra amplitudes statistically follow an empirical scaling law of the mean dust intensity $\langle I_{353} \rangle$ for the patch on which they are computed. We can use this scaling law to assess the most probable dust \mathcal{D}_ℓ^{BB} value for M_{B2} . For this field, which has a mean dust intensity of $\langle I_{353} \rangle = 0.060$ MJy sr⁻¹, the expected value at 353 GHz is $(13.4 \pm 0.26) \mu\text{K}_{\text{CMB}}^2$ at $\ell = 80$, taking into account the uncertainty on the fitted $\langle I_{353} \rangle^{1.9}$ amplitude from Sect. 4.3.

In order to extrapolate this value to the BICEP2 observing frequency, 150 GHz, we proceed as in Sect. 5.3, using the same typical dust SED from Planck Collaboration Int. XXII (2015). For patches the size of M_{B2} the expected dispersion of β_d (Sect. 2.2.1) is 0.11, which introduces an uncertainty in

the extrapolation. The extrapolation, unlike in that section, is made to 150 GHz taking into account the BICEP2 bandpass¹⁶. The conversion factor from the *Planck* 353 GHz band to the 150 GHz BICEP2 band, taking into account both *Planck* and BICEP2 colour corrections, as well as the statistical error on β_d , is thus $0.0408^{+0.0046}_{-0.0036}$ in the SED, and therefore this value squared in \mathcal{D}_ℓ^{BB} .

The resulting expected dust \mathcal{D}_ℓ^{BB} amplitude at 150 GHz is $2.23^{+0.55}_{-0.45} \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ at $\ell = 80$. The uncertainty quoted here applies to the most probable value for patches with a similar $\langle I_{353} \rangle$, but it ignores the intrinsic dispersion around this value (see Sect. 5.2). Therefore, a direct measurement of the dust \mathcal{D}_ℓ^{BB} spectrum in M_{B2} is required to complete the assessment of its polarized dust level.

In Sect. 5.3, we have localized the \mathcal{D}_ℓ^{BB} amplitudes from the analysis of patches on a map. The pixels falling inside the approximate BICEP2 deep-field region shown in Fig. 8 give a mean value of $r_d = 0.207$, i.e., an expected dust power of $\mathcal{D}_\ell^{BB} = 1.39 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ at 150 GHz and $\ell = 80$; we note that in this region the *Planck* estimate of the dust contamination is significantly higher, by a factor of about 2, than it is in some more optimal patches. Nevertheless, a more accurate estimate of the dust \mathcal{D}_ℓ^{BB} polarization amplitude in the BICEP2 observed field requires the direct computation of the angular power spectrum on a similar region.

6.3. BB angular power spectrum of dust in the BICEP2 field

We now compute the \mathcal{D}_ℓ^{BB} spectrum of the dust at 150 GHz on M_{B2} presented in Sect. 6.1, using the *Planck* 353 GHz data. For this purpose, we compute the 353 GHz \mathcal{D}_ℓ^{BB} spectrum by cross-correlating the two DetSets that have independent noise at this frequency in the three ℓ -bins defined by the intervals between multipoles 40, 120, 250, and 400. The ℓ -bin sizes were increased with respect to the previous sections in order to increase the S/N, especially around the range of the CMB recombination bump. Appendix D.1 confirms that the result does not depend on the method of computing the power spectrum.

This power spectrum is extrapolated to 150 GHz as in Sect. 6.2, with an extrapolation uncertainty estimated from the inferred dispersion of β_d . Our final estimate of the \mathcal{D}_ℓ^{BB} spectrum is presented in Fig. 9, together with its 1σ error budget. For the first bin, $\ell = 40$ –120, the expected level of dust polarized \mathcal{D}_ℓ^{BB} , as extrapolated to 150 GHz, is $1.32 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ (Fig. 9). The statistical error, estimated from Monte Carlo simulations of inhomogeneous *Planck* noise (presented in Appendix A for this particular binning), is $\pm 0.29 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$, so that the dust \mathcal{D}_ℓ^{BB} spectrum is statistically detected at 4.5σ in this broad ℓ bin.

In order to assess the potential contribution from systematics, we have computed the dust \mathcal{D}_ℓ^{BB} spectrum on M_{B2} on different subsets of the data and performed null tests, which are presented in Appendix D.3. In this lowest bin of ℓ , we do not observe any departure from what is allowed by noise. Nevertheless, we stress that below the noise level our cross-spectra could be subject to a positive or negative bias due to systematic effects. For example, if instead of taking the DetSets cross-spectra (as we have done throughout this paper) we take the mean value computed from the DetSets, HalfRings, and Years cross-spectra (presented in Appendix D.3), the statistical significance of our measurement is decreased from 4.5σ to 3.6σ .

¹⁵ <http://bicepkeck.org> This outline encloses the effective 373 deg² of deep integration (87 nK-degrees, BICEP2 Collaboration 2014b).

¹⁶ <http://bicepkeck.org>

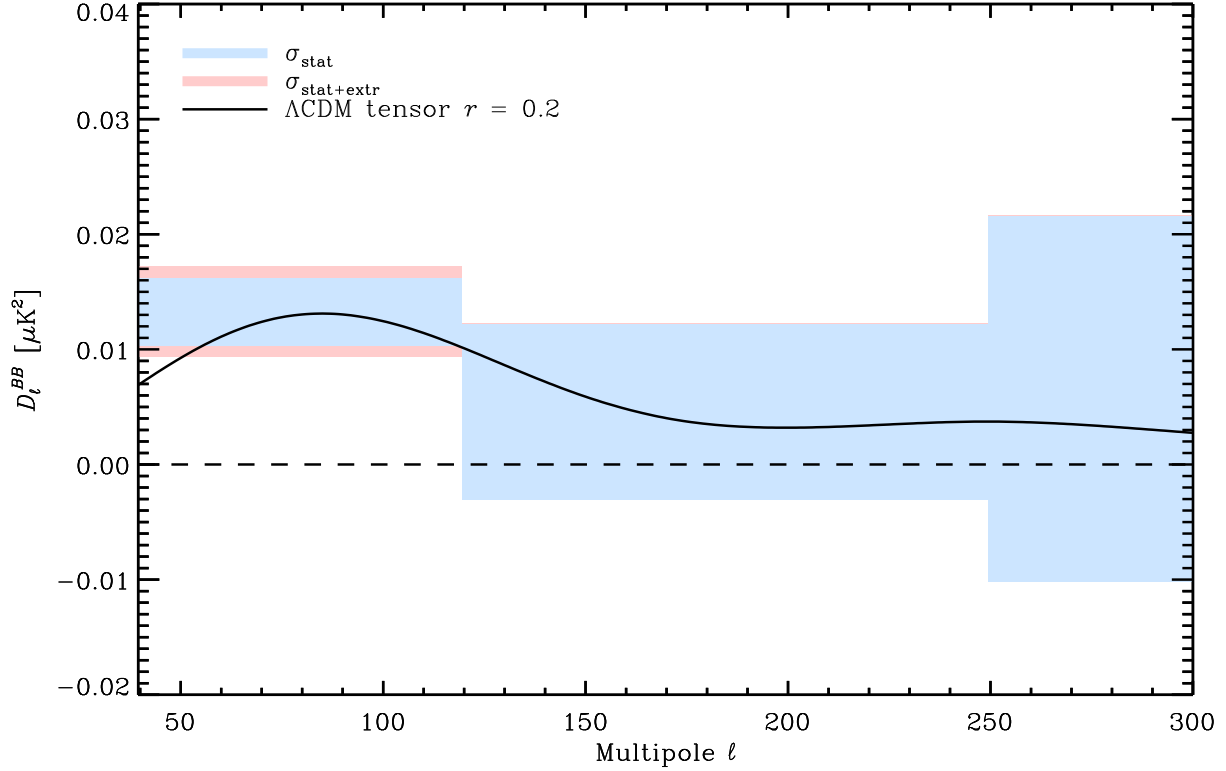


Fig. 9. *Planck* 353 GHz \mathcal{D}_ℓ^{BB} angular power spectrum computed on M_{B2} defined in Sect. 6.1 and extrapolated to 150 GHz (box centres). The shaded boxes represent the $\pm 1\sigma$ uncertainties: blue for the statistical uncertainties from noise; and red adding in quadrature the uncertainty from the extrapolation to 150 GHz. The *Planck* 2013 best-fit Λ CDM \mathcal{D}_ℓ^{BB} CMB model based on temperature anisotropies, with a tensor amplitude fixed at $r = 0.2$, is overplotted as a black line.

The uncertainty coming from the M_{B2} definition (presented in Appendix D.2) is $0.04 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ for this bin, thus much less than the statistical error. For this reason, it is not added to the error budget. However, the spectral extrapolation to 150 GHz adds an additional uncertainty $(+0.28, -0.24) \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$ to the estimated power in M_{B2} , added in quadrature in Fig. 9.

The expected value in this lowest- ℓ bin from direct computation of the \mathcal{D}_ℓ^{BB} power spectrum on M_{B2} , as shown in Fig. 9, is lower than (but consistent with) the statistical expectation from the analysis of the 352 high Galactic latitude patches presented in Sects. 5.2 and 6.2. This indicates that M_{B2} is not one of the outliers of Fig. 7 and therefore its dust B -mode power is well represented by its mean dust intensity through the empirical scaling law $\mathcal{D} \propto \langle I_{353} \rangle^{1.9}$.

These values of the \mathcal{D}_ℓ^{BB} amplitude in the ℓ range of the primordial recombination bump are of the same magnitude as those reported by BICEP2 Collaboration (2014b). Our results emphasize the need for a dedicated joint analysis of the B -mode polarization in this region incorporating all pertinent observational details of the *Planck* and BICEP2 data sets, which is in progress.

6.4. Frequency dependence

We complement the power spectrum analysis of the 353 GHz map with *Planck* data at lower frequencies. As in the analysis in Sect. 4.5, we compute the frequency dependence of the BB power measured by *Planck* at HFI frequencies in the BICEP2 field, using the patch M_{B2} as defined in Sect. 6.1.

We compute on M_{B2} the *Planck* \mathcal{D}_ℓ^{BB} auto- and cross-power spectra from the three *Planck* HFI bands at 100, 143, 217, and 353 GHz, using the two DetSets with independent noise at each

frequency, resulting in ten angular power spectra (100×100 , 100×143 , 100×217 , 100×353 , 143×143 , 143×217 , 143×353 , 217×217 , 217×353 , and 353×353), constructed by combining the cross-spectra as presented in Sect. 3.2. We use the same multipole binning as in Sect. 6.3. To each of these \mathcal{D}_ℓ^{BB} spectra, we fit the amplitude of a power law in ℓ with a fixed exponent $\alpha_{BB} = -0.42$ (see Sect. 4.2). In Fig. 10 we plot these amplitudes as a function of the effective frequency from 143 to 353 GHz, in units of sky brightness squared, as in Sect. 4.5. Data points at effective frequencies below 143 GHz are not presented, because the dust polarization is not detected at these frequencies. An upper limit on the synchrotron contribution at 150 GHz from the *Planck* LFI data is given in Appendix D.4.

We can see that the frequency dependence of the amplitudes of the *Planck* HFI \mathcal{D}_ℓ^{BB} spectra is in very good agreement with a squared dust modified blackbody spectrum having $\beta_d = 1.59$ and $T_d = 19.6$ K (Planck Collaboration Int. XXII 2015). We note that this emission model was normalized only to the 353 GHz point and that no global fit has been performed. Nevertheless, the χ^2 value from the amplitudes relative to this model is 4.56 ($N_{\text{d.o.f.}} = 7$). This shows that dust dominates in the specific M_{B2} region defined where these cross-spectra have been computed. This result emphasizes the need for a dedicated joint *Planck*-BICEP2 analysis.

7. Conclusions

We have presented the first nearly all-sky statistical analysis of the polarized emission from interstellar dust, focussing mostly on the characterization of this emission as a foreground contaminant at frequencies above 100 GHz. Our quantitative analysis of

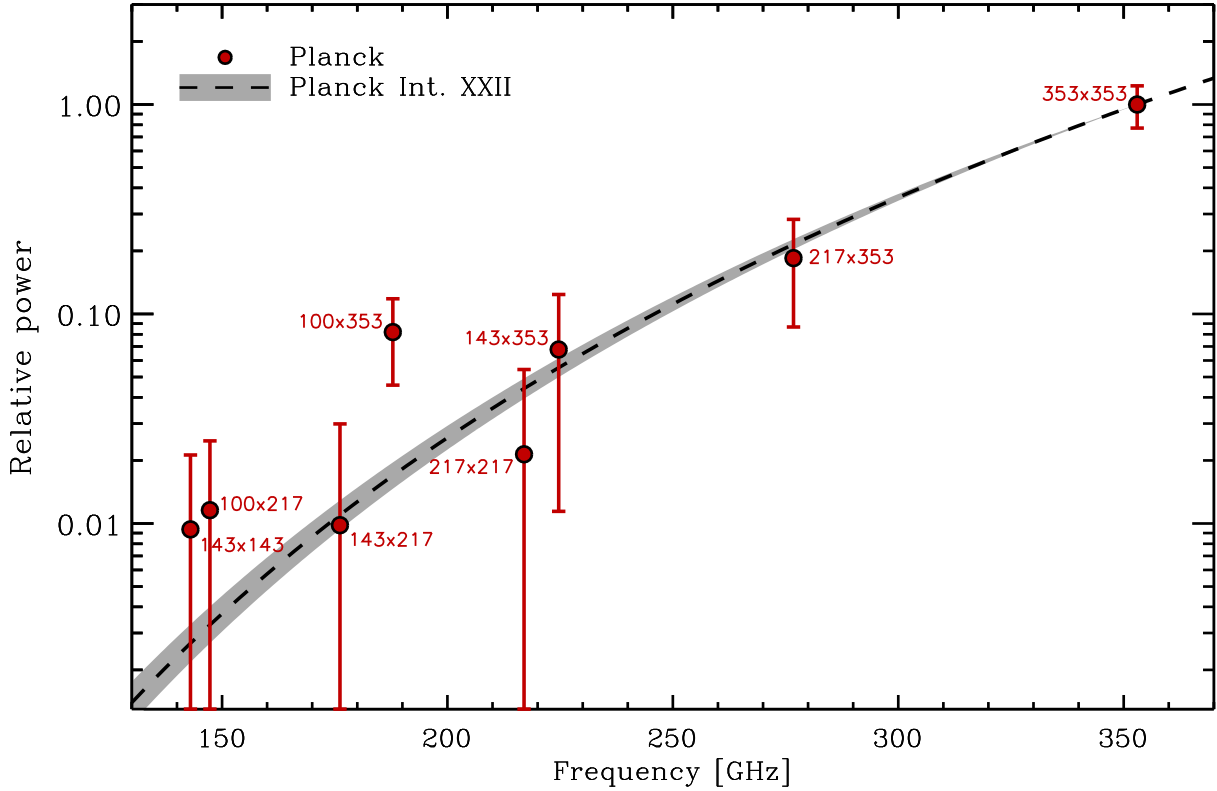


Fig. 10. Frequency dependence of the amplitude A^{BB} of the angular power spectrum \mathcal{D}_ℓ^{BB} computed on M_{B2} defined in Sect. 6.1, normalized to the 353 GHz amplitude (red points); amplitudes for cross-power spectra are plotted at the geometric mean frequency. The square of the adopted dust SED, a modified blackbody spectrum with $\beta_d = 1.59$ and $T_d = 19.6$ K, is overplotted as a black dashed line, again normalized to the 353 GHz point. The $\pm 1\sigma$ error area arising from the expected dispersion of β_d , 0.11 for the M_{B2} patch size (Sect. 2.2.1), is shown in light grey.

the angular dependence of the dust polarization relies on measurements at 353 GHz of the C_ℓ^{EE} and C_ℓ^{BB} (alternatively \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB}) angular power spectra for multipoles $40 < \ell < 500$. At this frequency only two polarized components are present: dust emission; and the CMB, which is subdominant in this multipole range. We have found that the statistical, spatial, and spectral distribution properties can be represented accurately by a simple model over most of the sky, and for all frequencies at which *Planck* HFI measures polarization.

- The angular power spectra C_ℓ^{EE} and C_ℓ^{BB} at 353 GHz are well fit by power laws in ℓ with exponents consistent with $\alpha_{EE,BB} = -2.42 \pm 0.02$, for sky fractions ranging from 24% to 72% for the LR regions used.
- The amplitudes of \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} in the LR regions vary with mean dust intensity at 353 GHz, $\langle I_{353} \rangle$, roughly as $\langle I_{353} \rangle^{1.9}$.
- The frequency dependence of the dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} from 353 GHz down to 100 GHz, obtained after removal of the \mathcal{D}_ℓ^{EE} prediction from the *Planck* best-fit CMB model (Planck Collaboration XVI 2014), is accurately described by the modified blackbody dust emission law derived in Planck Collaboration Int. XXII (2015), with $\beta_d = 1.59$ and $T_d = 19.6$ K.
- The ratio between the amplitudes of the two polarization power spectra is $C_\ell^{BB}/C_\ell^{EE} = 0.53$, which is not consistent with the simplest theoretical models.
- Dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra computed for 352 high Galactic latitude 400 deg² patches satisfy the above general properties at 353 GHz and have the same frequency dependence.

We have shown that the *Planck* determination of the 353 GHz dust polarization properties is unaffected by systematic errors for $\ell > 40$. This enables us to draw the following conclusions relevant for CMB polarization experiments aimed at the detection of primordial CMB tensor *B*-modes.

- Extrapolating the *Planck* 353 GHz \mathcal{D}_ℓ^{BB} spectra computed on the 400 deg² circular patches at high Galactic latitude to 150 GHz shows that we expect significant contamination by dust over most of the high Galactic latitude sky in the ℓ range of interest for detecting a primordial \mathcal{D}_ℓ^{BB} spectrum.
- Even for the cleanest of these regions, the *Planck* statistical error on the estimate of \mathcal{D}_ℓ^{BB} amplitude at $\ell = 80$ for such small regions is at best 0.17 (3σ) in units of r_d .
- Our results show that subtraction of polarized dust emission will be essential for detecting primordial *B*-modes at a level of $r = 0.1$ or below.
- There is a significant dispersion of the polarization \mathcal{D}_ℓ^{BB} amplitude for a given dust total intensity. Choices of the cleanest areas of the polarized sky cannot be made accurately using the *Planck* total intensity maps alone.
- At present, component separation, or template cleaning, can best be done with the *Planck* HFI 353 GHz data, but the accuracy of such cleaning is limited by *Planck* noise in small fields. Ground-based or balloon-borne experiments should include dust channels at high frequency. Alternatively, if they intend to rely on the *Planck* data to remove the dust emission, they should optimize the integration time and area so as to have a similar S/N level for the CMB and dust power spectra.

Turning specifically to the part of the sky mapped by the BICEP2 experiment, our analysis of the M_{B2} region indicates the following results.

- Over the multipole range $40 < \ell < 120$, the *Planck* 353 GHz \mathcal{D}_ℓ^{BB} power spectrum extrapolated to 150 GHz yields a value $1.32 \times 10^{-2} \mu K_{\text{CMB}}^2$, with statistical error $\pm 0.29 \times 10^{-2} \mu K_{\text{CMB}}^2$ and a further uncertainty $(+0.28, -0.24) \times 10^{-2} \mu K_{\text{CMB}}^2$ from the extrapolation. This value is comparable in magnitude to the BICEP2 measurements at these multipoles that correspond to the recombination bump.
- The frequency dependence of \mathcal{D}_ℓ^{BB} across the *Planck* bands is consistent with the typical SED of dust polarization (Planck Collaboration Int. XXII 2015).
- Assessing the dust contribution to the *B*-mode power measured by the BICEP2 experiment requires a dedicated joint analysis with *Planck*, incorporating all pertinent observational details of the two data sets, such as masking, filtering, and colour corrections.
- We have identified regions in which the dust polarization \mathcal{D}_ℓ^{BB} amplitude may be significantly lower, by about a factor of 2, than in the BICEP2 observing region.

Acknowledgements. The development of *Planck* has been supported by: ESA; CNES and CNRS/INSU-IN2P3-INP (France); ASI, CNR, and INAF (Italy); NASA and DoE (USA); STFC and UKSA (UK); CSIC, MICINN, J.A., and RES (Spain); Tekes, AoF, and CSC (Finland); DLR and MPG (Germany); CSA (Canada); DTU Space (Denmark); SER/SSO (Switzerland); RCN (Norway); SFI (Ireland); FCT/MCTES (Portugal); and PRACE (EU). A description of the Planck Collaboration and a list of its members, including the technical or scientific activities in which they have been involved, can be found at http://www.rssd.esa.int/index.php?project=PLANCK&page=Planck_Collaboration. Some of the results in this paper have been derived using the HEALPix package. The research leading to these results has received funding from the European Research Council under the European Union's Seventh Framework Programme (FP7/2007-2013) / ERC grant agreement No. 267934.

References

- Ade, P. A. R., Akiba, Y., Anthony, A. E., et al. 2014, *Phys. Rev. Lett.*, **113**, 021301
- Arnold, K., Ade, P. A. R., Anthony, A. E., et al. 2010, in SPIE Conf. Ser., 7741
- Austermann, J. E., Aird, K. A., Beall, J. A., et al. 2012, in SPIE Conf. Ser., 8452
- Baccigalupi, C. 2003, *New Astron. Rev.*, **47**, 1127
- Barkats, D., Aikin, R., Bischoff, C., et al. 2014, *ApJ*, **783**, 67
- Battye, R. A., Browne, I. W. A., Peel, M. W., Jackson, N. J., & Dickinson, C. 2011, *MNRAS*, **413**, 132
- Benoît, A., Ade, P., Amblard, A., et al. 2004, *A&A*, **424**, 571
- BICEP2 Collaboration 2014a, *ApJ*, **792**, 62
- BICEP2 Collaboration 2014b, *Phys. Rev. Lett.*, **112**, 241101
- Bunn, E. F., Zaldarriaga, M., Tegmark, M., & de Oliveira-Costa, A. 2003, *Phys. Rev. D*, **67**, 023501
- Colley, W. N., & Gott, III, J. R. 2015, *MNRAS*, **447**, 2034
- Delabrouille, J., Betoule, M., Melin, J.-B., et al. 2013, *A&A*, **553**, A96
- Draine, B. T. 2004, in *The Cold Universe*, Saas-Fee Advanced Course 32 (Springer), eds. A. W. Blain, F. Combes, B. T. Draine, D. Pfenniger, & Y. Revaz, 213
- Dunkley, J., Amblard, A., Baccigalupi, C., et al. 2009a, in AIP Conf. Ser. 1141, eds. S. Dodelson, D. Baumann, A. Cooray, et al., 222
- Dunkley, J., Komatsu, E., Nolte, M. R., et al. 2009b, *ApJS*, **180**, 306
- Fauvet, L., Macías-Pérez, J. F., Aumont, J., et al. 2011, *A&A*, **526**, A145
- Fauvet, L., Macías-Pérez, J. F., & Désert, F. X. 2012, *Astropart. Phys.*, **36**, 57
- Flauger, R., Hill, J. C., & Spergel, D. N. 2014, *J. Cosmol. Astropart. Phys.*, **8**, 39
- Fraisse, A. A., Brown, J.-A. C., Dobler, G., et al. 2009, in AIP Conf. Ser. 1141, eds. S. Dodelson, D. Baumann, A. Cooray, et al., 265
- Fraisse, A. A., Ade, P. A. R., Amiri, M., et al. 2013, *J. Cosmol. Astropart. Phys.*, **4**, 47
- Fuskeland, U., Wehus, I. K., Eriksen, H. K., & Naess, S. K. 2014, *ApJ*, **790**, 104
- Gautier, III, T. N., Boulanger, F., Perault, M., & Puget, J. L. 1992, *AJ*, **103**, 1313
- Ghribi, A., Aumont, J., Battistelli, E. S., et al. 2014, *J. Low Temp. Phys.*, **176**, 698
- Gold, B., Odegard, N., Weiland, J. L., et al. 2011, *ApJS*, **192**, 15
- Goldreich, P., & Kylafis, N. D. 1982, *ApJ*, **253**, 606
- Górski, K. M., Hivon, E., Banday, A. J., et al. 2005, *ApJ*, **622**, 759
- Grain, J., Tristram, M., & Stomp, R. 2009, *Phys. Rev. D*, **79**, 123515
- Grainger, W., Aboobaker, A. M., Ade, P., et al. 2008, ASP Conf. Ser., 7020
- Hanson, D., Hoover, S., Crites, A., et al. 2013, *Phys. Rev. Lett.*, **111**, 141301
- Hartmann, D., Magnani, L., & Thaddeus, P. 1998, *ApJ*, **492**, 205
- Hildebrand, R. H. 1988, *Roy. Astron. Quant. J.*, **29**, 327
- Hildebrand, R. H., Dotson, J. L., Dowell, C. D., Schleuning, D. A., & Vaillancourt, J. E. 1999, *ApJ*, **516**, 834
- Hivon, E., Górski, K. M., Netterfield, C. B., et al. 2002, *ApJ*, **567**, 2
- Jaffe, T. R., Ferrière, K. M., Banday, A. J., et al. 2013, *MNRAS*, **431**, 683
- Kalberla, P. M. W., Burton, W. B., Hartmann, D., et al. 2005, *A&A*, **440**, 775
- Lamarre, J., Puget, J., Ade, P. A. R., et al. 2010, *A&A*, **520**, A9
- Li, H.-B., & Henning, T. 2011, *Nature*, **479**, 499
- Macellari, N., Pierpaoli, E., Dickinson, C., & Vaillancourt, J. E. 2011, *MNRAS*, **418**, 888
- Magnani, L., Hartmann, D., Holcomb, S. L., Smith, L. E., & Thaddeus, P. 2000, *ApJ*, **535**, 167
- Martin, P. G. 2007, in EAS Pub. Ser. 23, eds. M.-A. Miville-Deschênes, & F. Boulanger, 165
- Massardi, M., Burke-Spolaor, S. G., Murphy, T., et al. 2013, *MNRAS*, **436**, 2915
- Matthews, T. G., Ade, P. A. R., Angilè, F. E., et al. 2014, *ApJ*, **784**, 116
- Mennella, A., Butler, R. C., Curto, A., et al. 2011, *A&A*, **536**, A3
- Miville-Deschênes, M.-A., Lagache, G., Boulanger, F., & Puget, J.-L. 2007, *A&A*, **469**, 595
- Miville-Deschênes, M.-A., Martin, P. G., Abergel, A., et al. 2010, *A&A*, **518**, L104
- Mortonson, M. J., & Seljak, U. 2014, *JCAP*, **10**, 035
- Naess, S., Hasselfield, M., McMahon, J., et al. 2014, *J. Cosmol. Astropart. Phys.*, **10**, 7
- Niemack, M. D., Ade, P. A. R., Aguirre, J., et al. 2010, in SPIE Conf. Ser., 7741
- O'Dea, D. T., Clark, C. N., Contaldi, C. R., & MacTavish, C. J. 2012, *MNRAS*, **419**, 1795
- Planck Collaboration I. 2014, *A&A*, **571**, A1
- Planck Collaboration II. 2014, *A&A*, **571**, A2
- Planck Collaboration VI. 2014, *A&A*, **571**, A6
- Planck Collaboration VII. 2014, *A&A*, **571**, A7
- Planck Collaboration VIII. 2014, *A&A*, **571**, A8
- Planck Collaboration IX. 2014, *A&A*, **571**, A9
- Planck Collaboration X. 2014, *A&A*, **571**, A10
- Planck Collaboration XI. 2014, *A&A*, **571**, A11
- Planck Collaboration XIII. 2014, *A&A*, **571**, A13
- Planck Collaboration XV. 2014, *A&A*, **571**, A15
- Planck Collaboration XVI. 2014, *A&A*, **571**, A16
- Planck Collaboration XVII. 2014, *A&A*, **571**, A17
- Planck Collaboration XXVIII. 2014, *A&A*, **571**, A28
- Planck Collaboration Int. XVII. 2014, *A&A*, **566**, A55
- Planck Collaboration Int. XIX. 2015, *A&A*, **576**, A104
- Planck Collaboration Int. XX. 2015, *A&A*, **576**, A105
- Planck Collaboration Int. XXI. 2015, *A&A*, **576**, A106
- Planck Collaboration Int. XXII. 2015, *A&A*, **576**, A107
- Planck HFI Core Team 2011, *A&A*, **536**, A4
- Ponthieu, N., Macías-Pérez, J. F., Tristram, M., et al. 2005, *A&A*, **444**, 327
- QUIET Collaboration, Araujo, D., Bischoff, C., et al. 2012, *ApJ*, **760**, 145
- Rosset, C., Tristram, M., Ponthieu, N., et al. 2010, *A&A*, **520**, A13
- Rubiño-Martín, J. A., Rebolo, R., Tucci, M., et al. 2010, in *Highlights of Spanish Astrophysics V*, ed. J. M. Diego, L. J. Goicoechea, J. I. González-Serrano, & J. Gorgas, 127
- Rybicki, G. B., & Lightman, A. P. 1979, *Radiative processes in Astrophysics* (Wiley-Interscience)
- Seiffert, M., Borys, C., Scott, D., & Halpern, M. 2007, *MNRAS*, **374**, 409
- Smith, K. M. 2006, *New Astron. Rev.*, **50**, 1025
- Staniszewski, Z., Aikin, R. W., Amiri, M., et al. 2012, *J. Low Temp. Phys.*, **167**, 827
- Tassis, K., & Pavlidou, V. 2014, *MNRAS*, submitted [[arXiv:1410.8136](https://arxiv.org/abs/1410.8136)]
- Tauber, J. A., Mandolesi, N., Puget, J.-L., et al. 2010, *A&A*, **520**, A1
- Tristram, M., Macías-Pérez, J. F., Renault, C., & Santos, D. 2005, *MNRAS*, **358**, 833
- Tucci, M., & Toffolatti, L. 2012, *Adv. Astron.*, **2012**, 624987
- Tucci, M., Martínez-González, E., Vielva, P., & Delabrouille, J. 2005, *MNRAS*, **360**, 935
- Vaillancourt, J. E. 2007, in EAS Pub. Ser., 23, eds. M.-A. Miville-Deschênes, & F. Boulanger, 147

- ¹ APC, AstroParticule et Cosmologie, Université Paris Diderot, CNRS/IN2P3, CEA/Irfu, Observatoire de Paris, Sorbonne Paris Cité, 10 rue Alice Domon et Léonie Duquet, 75205 Paris Cedex 13, France
- ² African Institute for Mathematical Sciences, 6–8 Melrose Road, Muizenberg, Cape Town, South Africa
- ³ Agenzia Spaziale Italiana Science Data Center, via del Politecnico snc, 00133 Roma, Italy
- ⁴ Agenzia Spaziale Italiana, viale Liegi 26 Roma, Italy
- ⁵ Aix Marseille Université, CNRS, LAM (Laboratoire d'Astrophysique de Marseille) UMR 7326, 13388 Marseille, France
- ⁶ Astrophysics Group, Cavendish Laboratory, University of Cambridge, J J Thomson Avenue, Cambridge CB3 0HE, UK
- ⁷ Astrophysics & Cosmology Research Unit, School of Mathematics, Statistics & Computer Science, University of KwaZulu-Natal, Westville Campus, Private Bag X54001, 4000 Durban, South Africa
- ⁸ Atacama Large Millimeter/submillimeter Array, ALMA Santiago Central Offices, Alonso de Cordova 3107, Vitacura, Casilla 763 0355 Santiago, Chile
- ⁹ CITA, University of Toronto, 60 St. George St., Toronto, ON M5S 3H8, Canada
- ¹⁰ CNRS, IRAP, 9 Av. colonel Roche, BP 44346, 31028 Toulouse Cedex 4, France
- ¹¹ CRANN, Trinity College, Dublin, Ireland
- ¹² California Institute of Technology, Pasadena, California, USA
- ¹³ Centre for Theoretical Cosmology, DAMTP, University of Cambridge, Wilberforce Road, Cambridge CB3 0WA, UK
- ¹⁴ Centro de Estudios de Física del Cosmos de Aragón (CEFCA), Plaza San Juan, 1, planta 2, 44001 Teruel, Spain
- ¹⁵ Computational Cosmology Center, Lawrence Berkeley National Laboratory, Berkeley, California, USA
- ¹⁶ Consejo Superior de Investigaciones Científicas (CSIC), Madrid, Spain
- ¹⁷ DSM/Irfu/SPP, CEA-Saclay, 91191 Gif-sur-Yvette Cedex, France
- ¹⁸ DTU Space, National Space Institute, Technical University of Denmark, Elektrovej 327, 2800 Kgs. Lyngby, Denmark
- ¹⁹ Département de Physique Théorique, Université de Genève, 24 Quai E. Ansermet, 1211 Genève 4, Switzerland
- ²⁰ Departamento de Física, Universidad de Oviedo, Avda. Calvo Sotelo s/n, Oviedo, Spain
- ²¹ Department of Astronomy and Astrophysics, University of Toronto, 50 Saint George Street, Toronto, Ontario, Canada
- ²² Department of Astrophysics/IMAPP, Radboud University Nijmegen, PO Box 9010, 6500 GL Nijmegen, The Netherlands
- ²³ Department of Physics & Astronomy, University of British Columbia, 6224 Agricultural Road, Vancouver, British Columbia, Canada
- ²⁴ Department of Physics and Astronomy, Dana and David Dornsife College of Letter, Arts and Sciences, University of Southern California, Los Angeles, CA 90089, USA
- ²⁵ Department of Physics and Astronomy, University College London, London WC1E 6BT, UK
- ²⁶ Department of Physics, Florida State University, Keen Physics Building, 77 Chieftan Way, Tallahassee, Florida, USA
- ²⁷ Department of Physics, Gustaf Hållströmin katu 2a, University of Helsinki, Helsinki, Finland
- ²⁸ Department of Physics, Princeton University, Princeton, New Jersey, USA
- ²⁹ Department of Physics, University of California, Berkeley, California, USA
- ³⁰ Department of Physics, University of California, One Shields Avenue, Davis, California, USA
- ³¹ Department of Physics, University of California, Santa Barbara, California, USA
- ³² Department of Physics, University of Illinois at Urbana-Champaign, 1110 West Green Street, Urbana, Illinois, USA
- ³³ Dipartimento di Fisica e Astronomia G. Galilei, Università degli Studi di Padova, via Marzolo 8, 35131 Padova, Italy
- ³⁴ Dipartimento di Fisica e Scienze della Terra, Università di Ferrara, via Saragat 1, 44122 Ferrara, Italy
- ³⁵ Dipartimento di Fisica, Università La Sapienza, P.le A. Moro 2, Roma, Italy
- ³⁶ Dipartimento di Fisica, Università degli Studi di Milano, via Celoria, 16 Milano, Italy
- ³⁷ Dipartimento di Fisica, Università degli Studi di Trieste, via A. Valerio 2, Trieste, Italy
- ³⁸ Dipartimento di Fisica, Università di Roma Tor Vergata, via della Ricerca Scientifica 1, Roma, Italy
- ³⁹ Dipartimento di Matematica, Università di Roma Tor Vergata, via della Ricerca Scientifica 1, Roma, Italy
- ⁴⁰ Discovery Center, Niels Bohr Institute, Blegdamsvej 17, Copenhagen, Denmark
- ⁴¹ Dpto. Astrofísica, Universidad de La Laguna (ULL), 38206 La Laguna, Tenerife, Spain
- ⁴² European Southern Observatory, ESO Vitacura, Alonso de Cordova 3107, Vitacura, Casilla 19001 Santiago, Chile
- ⁴³ European Space Agency, ESAC, Planck Science Office, Camino bajo del Castillo, s/n, Urbanización Villafranca del Castillo, Villanueva de la Cañada, Madrid, Spain
- ⁴⁴ European Space Agency, ESTEC, Keplerlaan 1, 2201 AZ Noordwijk, The Netherlands
- ⁴⁵ Facoltà di Ingegneria, Università degli Studi e-Campus, via Isimbardi 10, 22060 Novedrate (CO), Italy
- ⁴⁶ Gran Sasso Science Institute, INFN, viale F. Crispi 7, 67100 L'Aquila, Italy
- ⁴⁷ HGSFP and University of Heidelberg, Theoretical Physics Department, Philosophenweg 16, 69120 Heidelberg, Germany
- ⁴⁸ Haverford College Astronomy Department, 370 Lancaster Avenue, Haverford, Pennsylvania, USA
- ⁴⁹ Helsinki Institute of Physics, Gustaf Hållströmin katu 2, University of Helsinki, Helsinki, Finland
- ⁵⁰ INAF–Osservatorio Astronomico di Padova, Vicolo dell'Osservatorio 5, Padova, Italy
- ⁵¹ INAF–Osservatorio Astronomico di Roma, via di Frascati 33, Monte Porzio Catone, Italy
- ⁵² INAF–Osservatorio Astronomico di Trieste, via G.B. Tiepolo 11, Trieste, Italy
- ⁵³ INAF/IASF Bologna, via Gobetti 101, Bologna, Italy
- ⁵⁴ INAF/IASF Milano, via E. Bassini 15, Milano, Italy
- ⁵⁵ INFN, Sezione di Bologna, via Irnerio 46, 40126 Bologna, Italy
- ⁵⁶ INFN, Sezione di Roma 1, Università di Roma Sapienza, Piazzale Aldo Moro 2, 00185 Roma, Italy
- ⁵⁷ INFN, Sezione di Roma 2, Università di Roma Tor Vergata, via della Ricerca Scientifica 1, Roma, Italy
- ⁵⁸ INFN/National Institute for Nuclear Physics, via Valerio 2, 34127 Trieste, Italy
- ⁵⁹ IPAG: Institut de Planétologie et d'Astrophysique de Grenoble, Université Grenoble Alpes, CNRS, IPAG, 38000 Grenoble, France
- ⁶⁰ IUCAA, Post Bag 4, Ganeshkhind, Pune University Campus, 411 007 Pune, India
- ⁶¹ Imperial College London, Astrophysics group, Blackett Laboratory, Prince Consort Road, London, SW7 2AZ, UK
- ⁶² Infrared Processing and Analysis Center, California Institute of Technology, Pasadena, CA 91125, USA
- ⁶³ Institut Universitaire de France, 103 Bd Saint-Michel, 75005 Paris, France
- ⁶⁴ Institut d'Astrophysique Spatiale, CNRS (UMR 8617) Université Paris-Sud 11, Bâtiment 121, Orsay, France
- ⁶⁵ Institut d'Astrophysique de Paris, CNRS (UMR 7095), 98bis Boulevard Arago, 75014 Paris, France
- ⁶⁶ Institute for Space Sciences, Bucharest-Magurale, Romania
- ⁶⁷ Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK
- ⁶⁸ Institute of Theoretical Astrophysics, University of Oslo, Blindern, Oslo, Norway
- ⁶⁹ Instituto de Astrofísica de Canarias, C/Vía Láctea s/n, La Laguna, Tenerife, Spain

- ⁷⁰ Instituto de Física de Cantabria (CSIC-Universidad de Cantabria), Avda. de los Castros s/n, Santander, Spain
- ⁷¹ Istituto Nazionale di Fisica Nucleare, Sezione di Padova, via Marzolo 8, 35131 Padova, Italy
- ⁷² Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, California, USA
- ⁷³ Jodrell Bank Centre for Astrophysics, Alan Turing Building, School of Physics and Astronomy, The University of Manchester, Oxford Road, Manchester, M13 9PL, UK
- ⁷⁴ Kavli Institute for Cosmology Cambridge, Madingley Road, Cambridge, CB3 0HA, UK
- ⁷⁵ LAL, Université Paris-Sud, CNRS/IN2P3, Orsay, France
- ⁷⁶ LAPTh, Univ. de Savoie, CNRS, BP110, 74941 Annecy-le-Vieux, France
- ⁷⁷ LERMA, CNRS, Observatoire de Paris, 61 Avenue de l'Observatoire, Paris, France
- ⁷⁸ Laboratoire AIM, IRFU/Service d'Astrophysique – CEA/DSM – CNRS – Université Paris Diderot, Bât. 709, CEA-Saclay, 91191 Gif-sur-Yvette Cedex, France
- ⁷⁹ Laboratoire Traitement et Communication de l'Information, CNRS (UMR 5141) and Télécom ParisTech, 46 rue Barrault, 75634 Paris Cedex 13, France
- ⁸⁰ Laboratoire de Physique Subatomique et de Cosmologie, Université Joseph Fourier Grenoble I, CNRS/IN2P3, Institut National Polytechnique de Grenoble, 53 rue des Martyrs, 38026 Grenoble Cedex, France
- ⁸¹ Laboratoire de Physique Théorique, Université Paris-Sud 11 & CNRS, Bâtiment 210, 91405 Orsay, France
- ⁸² Lawrence Berkeley National Laboratory, Berkeley, California, USA
- ⁸³ Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, 85741 Garching, Germany
- ⁸⁴ McGill Physics, Ernest Rutherford Physics Building, McGill University, 3600 rue University, Montréal, QC, H3A 2T8, Canada
- ⁸⁵ National University of Ireland, Department of Experimental Physics, Maynooth, Co. Kildare, Ireland
- ⁸⁶ Niels Bohr Institute, Blegdamsvej 17, Copenhagen, Denmark
- ⁸⁷ Observational Cosmology, Mail Stop 367-17, California Institute of Technology, Pasadena, CA, 91125, USA
- ⁸⁸ Optical Science Laboratory, University College London, Gower Street, London, UK
- ⁸⁹ SB-ITP-LPPC, EPFL, 1015 Lausanne, Switzerland
- ⁹⁰ SISSA, Astrophysics Sector, via Bonomea 265, 34136 Trieste, Italy
- ⁹¹ School of Physics and Astronomy, Cardiff University, Queens Buildings, The Parade, Cardiff, CF24 3AA, UK
- ⁹² School of Physics and Astronomy, University of Nottingham, Nottingham NG7 2RD, UK
- ⁹³ Space Research Institute (IKI), Russian Academy of Sciences, Profsoyuznaya Str, 84/32, 117997 Moscow, Russia
- ⁹⁴ Space Sciences Laboratory, University of California, Berkeley, California, USA
- ⁹⁵ Special Astrophysical Observatory, Russian Academy of Sciences, Nizhnij Arkhyz, Zelenchukskiy region, 369167 Karachai-Cherkessian Republic, Russia
- ⁹⁶ Sub-Department of Astrophysics, University of Oxford, Keble Road, Oxford OX1 3RH, UK
- ⁹⁷ Theory Division, PH-TH, CERN, 1211, Geneva 23, Switzerland
- ⁹⁸ UPMC Univ. Paris 6, UMR7095, 98bis Boulevard Arago, 75014 Paris, France
- ⁹⁹ Université de Toulouse, UPS-OMP, IRAP, 31028 Toulouse Cedex 4, France
- ¹⁰⁰ Universities Space Research Association, Stratospheric Observatory for Infrared Astronomy, MS 232-11, Moffett Field, CA 94035, USA
- ¹⁰¹ University Observatory, Ludwig Maximilian University of Munich, Scheinerstrasse 1, 81679 Munich, Germany
- ¹⁰² University of Granada, Departamento de Física Teórica y del Cosmos, Facultad de Ciencias, Granada, Spain
- ¹⁰³ University of Granada, Instituto Carlos I de Física Teórica y Computacional, Granada, Spain
- ¹⁰⁴ Warsaw University Observatory, Aleje Ujazdowskie 4, 00-478 Warszawa, Poland

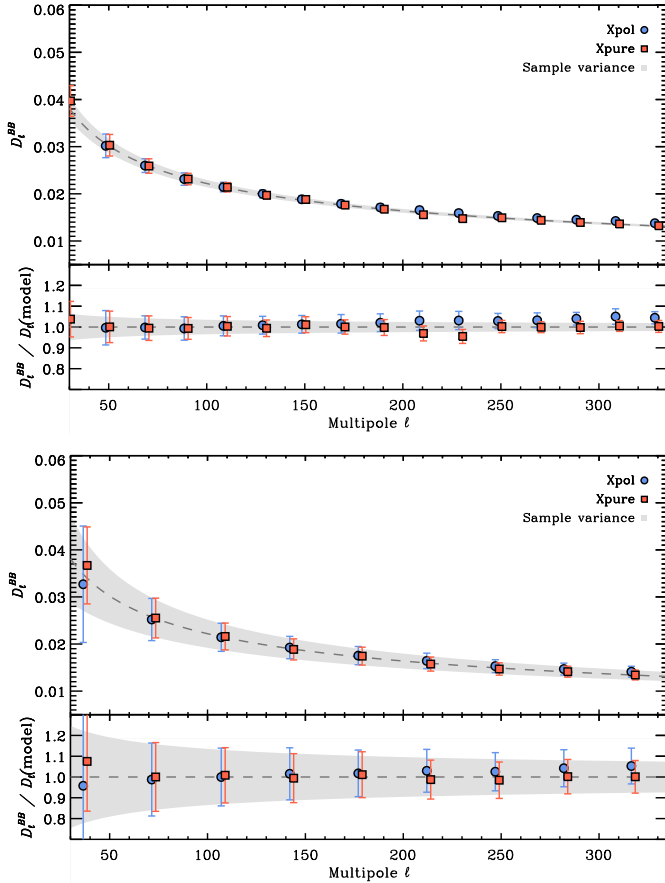


Fig. A.1. Upper parts of both panels: performance of the Xpol (blue points, see Sect. 3.1.1) and Xpure (red squares, see Sect. 3.1.2) algorithms on the \mathcal{D}_ℓ^{BB} power spectrum for Gaussian simulations of the dust polarization in the LR24 region (top panel, defined in Sect. 3.3.1) and in M_{B2} (bottom panel, defined in Sect. 6.1). The signal input power spectrum is shown as a dashed grey line and its associated sample variance as a light grey shaded area. Lower parts of both panels: relative discrepancy with respect to the input power spectrum.

Appendix A: Power spectrum estimator performance

Using Xpol (see Sect. 3.1.1) we have estimated the dust polarization \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} angular power spectrum, not on the full sky, but on particular cuts of the sky, such as the LR24 region defined in Sect. 3.3.1 and the much smaller M_{B2} patch defined in Sect. 6.1. To validate the performance of Xpol on such cuts we compare the results of this algorithm to those from Xpure (see Sect. 3.1.2), using simulated data in both cases.

Simulating the dust polarization for assessment of the performance of polarization angular power spectra estimators is an important issue. One either relies on statistically isotropic, Gaussian simulations with polarization power spectra similar to those of the dust, or alternatively one uses non-Gaussian, anisotropic simulations. The problem in the first case is that the hypotheses of Gaussianity and statistical isotropy might apply only partially to a dust polarization map. The problem in the second case is that one has to produce a non-Gaussian and anisotropic simulation, which has a defined *input* angular power spectrum, in order to be able to characterize what is retrieved in the output. In this section, we will use statistically isotropic, Gaussian simulations to explore the performance of our algorithms for recovering the dust polarization angular power spec-

tra on a given masked sky. This choice is motivated by the fact that cosmologists have tended to make this assumption when analysing the CMB anisotropies from a sky contaminated by non-Gaussian and anisotropic processes.

We generated 1000 full sky Q and U Gaussian map simulations from C_ℓ^{EE} and C_ℓ^{BB} power spectra having $C_\ell^{EE,BB} \propto \ell^{-2.42}$, the typical dust power spectrum shape that we measured in Sect. 4.2. Additionally, we gave to these spectra the B/E amplitude hierarchy that we have measured in Sect. 4.4, i.e., $C_\ell^{BB} = 0.53C_\ell^{EE}$. For each of these simulated dust polarized signal Q and U maps, we computed the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} angular power spectra on the cut sky LR24 region and the much smaller M_{B2} patch. We note that the structure in the simulations is driven by the assumed power spectra and the random phases drawn for each mode and is not correlated with the geometry of the mask.

The results are shown in Fig. A.1. For each region, we give the \mathcal{D}_ℓ^{BB} angular power spectra recovered by Xpol and Xpure from the simulations, together with the input power spectrum and the sample variance associated with each region.

We can see that for both methods there is no overall bias in the recovered \mathcal{D}_ℓ^{BB} angular power spectra, demonstrating that there is no substantial leakage from E to B . At multipoles above 40, the recovered values agree with the input values and the maximum excursions (5%) seen in some bins are consistent with the expected accuracy for this number of simulations. Moreover, Xpol and Xpure give very similar results in terms of the mean value and uncertainty. In the multipole bin $\ell \simeq 40$ on M_{B2} the small offsets for both Xpol and Xpure (−4% and 8%, respectively) might be hinting at a limitation of the estimation procedure in this multipole bin because of the size of the patch.

A related comparative assessment of the two methods on actual *Planck* data is presented in Appendix D.1.

Appendix B: Complementary dust spectra at 353 GHz: \mathcal{D}_ℓ^{TE} , \mathcal{D}_ℓ^{TB} , and \mathcal{D}_ℓ^{EB}

Using the same procedure as described in Sects. 3 and 4 for the dust polarized angular power spectra for the LR regions at intermediate Galactic latitude, we have computed the 353 GHz dust spectra involving temperature and polarization, \mathcal{D}_ℓ^{TE} and \mathcal{D}_ℓ^{TB} , and the cross-spectrum for polarization, \mathcal{D}_ℓ^{EB} . This completes the entire set of polarization-related power spectra. Spectra such as \mathcal{D}_ℓ^{TB} and \mathcal{D}_ℓ^{EB} necessarily vanish for cosmic fields that satisfy statistical isotropy and parity invariance. However, the emission from our Galaxy satisfies neither of these and so the \mathcal{D}_ℓ^{TB} and \mathcal{D}_ℓ^{EB} spectra are generally expected to be non-zero.

In Fig. B.1 we present the \mathcal{D}_ℓ^{TE} results for $f_{\text{sky}} = \{0.3, 0.5, 0.7\}$; we note that the *Planck* best-fit CMB \mathcal{D}_ℓ^{TE} power spectrum was removed, as in Sect. 3.2. Again, the amplitudes of the spectra increase with increasing f_{sky} because the polarized emission is brighter on average when more sky is retained. The amplitudes of the spectra are about a factor of 3 higher than those reported for \mathcal{D}_ℓ^{EE} in Fig. 2. For the largest region there is evidence of a power-law dependence on multipole ℓ over the range $\ell = 40$ to 600, with a slope compatible with that found for \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} in Sect. 4.2 ($\alpha_{TE} = -2.37, -2.43$, and -2.47 for $f_{\text{sky}} = 0.3, 0.5$, and 0.7 , respectively). The fact that the slopes of the spectra are similar to those found in Sect. 4.2 for the dust polarization and in *Planck Collaboration Int. XXII (2015)* for dust intensity, indicates that the TE cross-correlation is dominated by the dust correlations in this multipole range, and not by the other components in the intensity maps (e.g., CIB or point

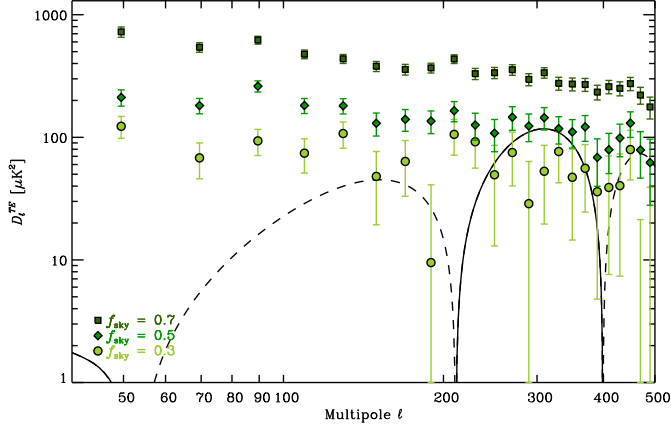


Fig. B.1. *Planck* HFI 353 GHz \mathcal{D}_ℓ^{TE} power spectra (in $\mu\text{K}_{\text{CMB}}^2$) computed on three of the selected LR analysis regions that have $f_{\text{sky}} = 0.3$ (circles, lightest), $f_{\text{sky}} = 0.5$ (diamonds, medium), and $f_{\text{sky}} = 0.7$ (squares, darkest). The uncertainties plotted here are $\pm 1\sigma$. The *Planck* 2013 best-fit ΛCDM \mathcal{D}_ℓ^{TE} expectation (Planck Collaboration XVI 2014) is shown as the black curve, solid where positive, dashed where negative.

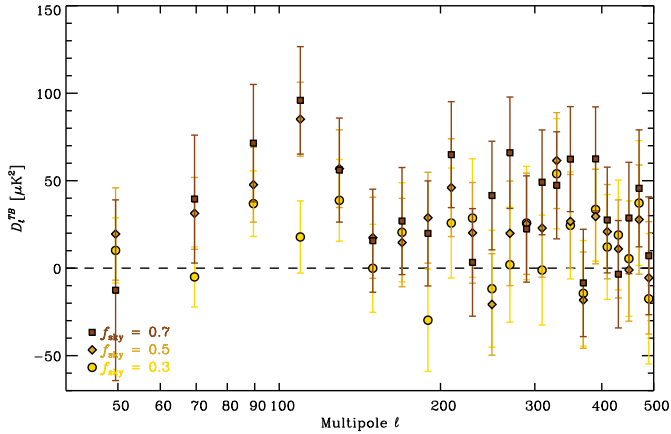


Fig. B.2. *Planck* HFI 353 GHz \mathcal{D}_ℓ^{TB} power spectra (in $\mu\text{K}_{\text{CMB}}^2$) computed on three of the selected LR analysis regions that have $f_{\text{sky}} = 0.3$ (circles, lightest), $f_{\text{sky}} = 0.5$ (diamonds, medium), and $f_{\text{sky}} = 0.7$ (squares, darkest). The uncertainties plotted here are $\pm 1\sigma$.

sources). We also show the \mathcal{D}_ℓ^{TE} power spectrum computed from the *Planck* 2013 best-fit ΛCDM model of the CMB temperature data (Planck Collaboration XVI 2014). As in Fig. 2 for \mathcal{D}_ℓ^{EE} , the CMB model is below the 353 GHz angular power spectra at low ℓ and about the same order of magnitude at $\ell > 300$.

Similarly, the results for \mathcal{D}_ℓ^{TB} are shown in Fig. B.2, but now on a linear scale. For the two largest regions ($f_{\text{sky}} = 0.5$ and 0.7), we detect a significant signal in the range $\ell = 60$ – 130 that increases with the sky area. In the same multipole range, the dust is only marginally detected for the $f_{\text{sky}} = 0.3$ region. At lower and higher ℓ , the individual binned measurements of \mathcal{D}_ℓ^{TB} on all the regions are compatible with zero.

Finally, we show the results for \mathcal{D}_ℓ^{EB} in Fig. B.3. There is a marginal detection of the \mathcal{D}_ℓ^{EB} spectrum in the range $\ell = 60$ – 130 for the $f_{\text{sky}} = 0.7$ mask. For the other masks and at other multipoles, the \mathcal{D}_ℓ^{EB} spectra are compatible with zero.

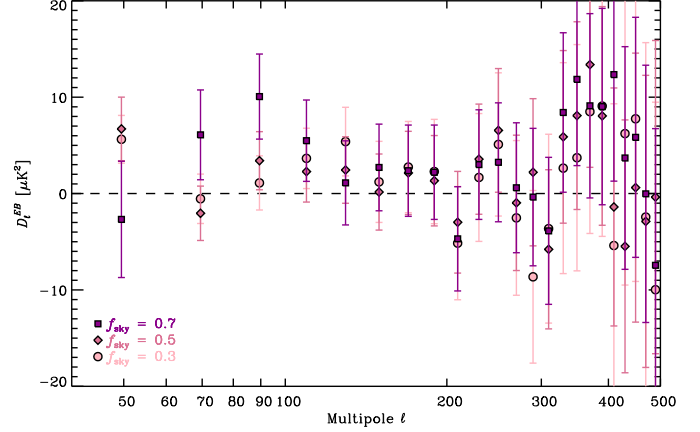


Fig. B.3. *Planck* HFI 353 GHz \mathcal{D}_ℓ^{EB} power spectra (in $\mu\text{K}_{\text{CMB}}^2$) computed on three of the selected LR analysis regions that have $f_{\text{sky}} = 0.3$ (circles, lightest), $f_{\text{sky}} = 0.5$ (diamonds, medium), and $f_{\text{sky}} = 0.7$ (squares, darkest). The uncertainties plotted here are $\pm 1\sigma$.

Appendix C: Notes on the analysis of the high Galactic latitude patches

C.1. Assessment of *Planck* polarization systematic uncertainties

To assess the level of systematic effects in the results presented in Sect. 5, we use a null-test analysis (see also Appendix D.3). We repeated the statistical analysis for the 353 GHz \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} cross-spectra on the high-Galactic latitude patches. The steps of the analysis are exactly the same as in Sect. 5.1, except that instead of using the 353 GHz $353_{\text{DS1}} \times 353_{\text{DS2}}$ cross-power spectra, we use the $(353_{\text{DS1,HR1}} - 353_{\text{DS1,HR2}})/2 \times (353_{\text{DS2,HR1}} - 353_{\text{DS2,HR2}})/2$ half-difference cross-spectra. These cross-spectra are expected to be consistent with zero for uncorrelated noise and subdominant systematics.

The computed dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} amplitudes $A_\ell^{EE,BB}$ (at $\ell = 80$ computed on each of these patches) for the null-test spectra, in $\mu\text{K}_{\text{CMB}}^2$ at 353 GHz, are shown in Fig. C.1 as a function of $\langle I_{353} \rangle$. We also report in this figure the expected noise level computed from Monte Carlo simulations of *Planck* inhomogeneous white noise.

We can see that the fitted amplitudes for the null-test spectra on the 352 high Galactic latitude patches are scattered around zero, without any obvious bias, for the entire range of $\langle I_{353} \rangle$; this is the expectation for half-difference cross-spectra. Taking into account the individual error bars, there is no patch that has a null-test spectrum amplitude inconsistent with the $\pm 3\sigma$ range of the instrumental noise dispersion.

We thus conclude from this analysis that the results presented in Sect. 5 are not significantly affected by instrumental systematics.

C.2. Dust B-mode amplitudes compared to E-mode

In Sect. 5, we computed the 353 GHz dust \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} amplitudes on the 352 high Galactic latitude patches defined in Sect. 3.3.2. We present in Fig. C.2 the ratio of the amplitudes of these spectra, A_ℓ^{BB}/A_ℓ^{EE} as a function of the mean dust intensity $\langle I_{353} \rangle$ of the patch on which it was computed.

These ratios are scattered around the inverse noise variance weighted $\langle A_\ell^{BB}/A_\ell^{EE} \rangle = 0.52 \pm 0.19$ value. This value is consistent with the one computed in Sect. 4.4 on the LR regions. Nevertheless, it can be seen from Fig. C.2 that there are patches

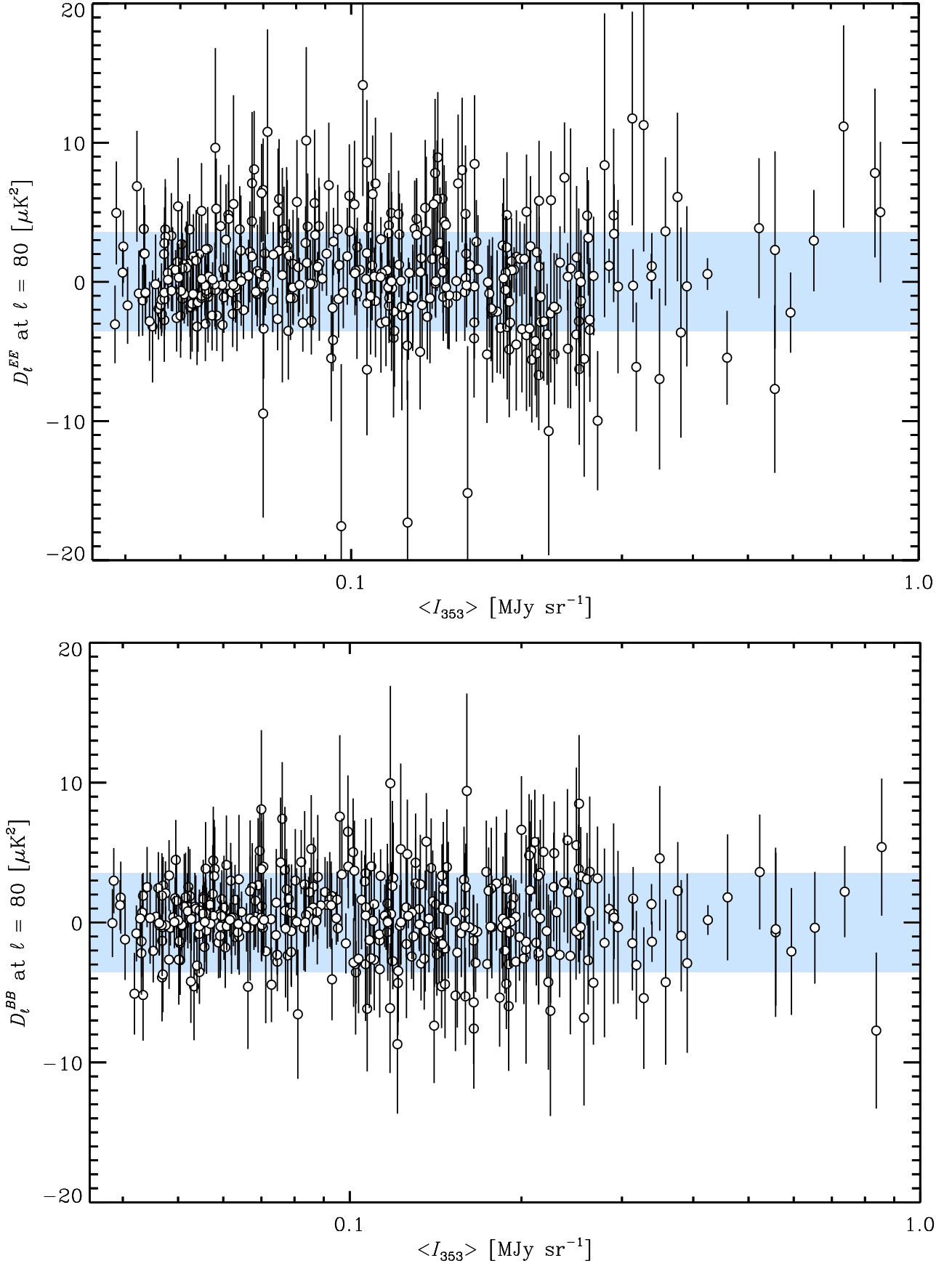


Fig. C.1. *Top:* same as Fig. 7, but instead of computing the \mathcal{D}_ℓ^{EE} (*top panel*) and \mathcal{D}_ℓ^{BB} (*bottom panel*) spectra from the 353 GHz cross-correlation between DetSet1 and DetSet2, we compute them from the cross-correlation between the HalfRing half-differences for each detector set, i.e., $(353_{\text{DS1,HR1}} - 353_{\text{DS1,HR2}})/2 \times (353_{\text{DS2,HR1}} - 353_{\text{DS2,HR2}})/2$. The 3σ expectations from *Planck* inhomogeneous white-noise Monte Carlo simulations are represented as light blue shaded areas.

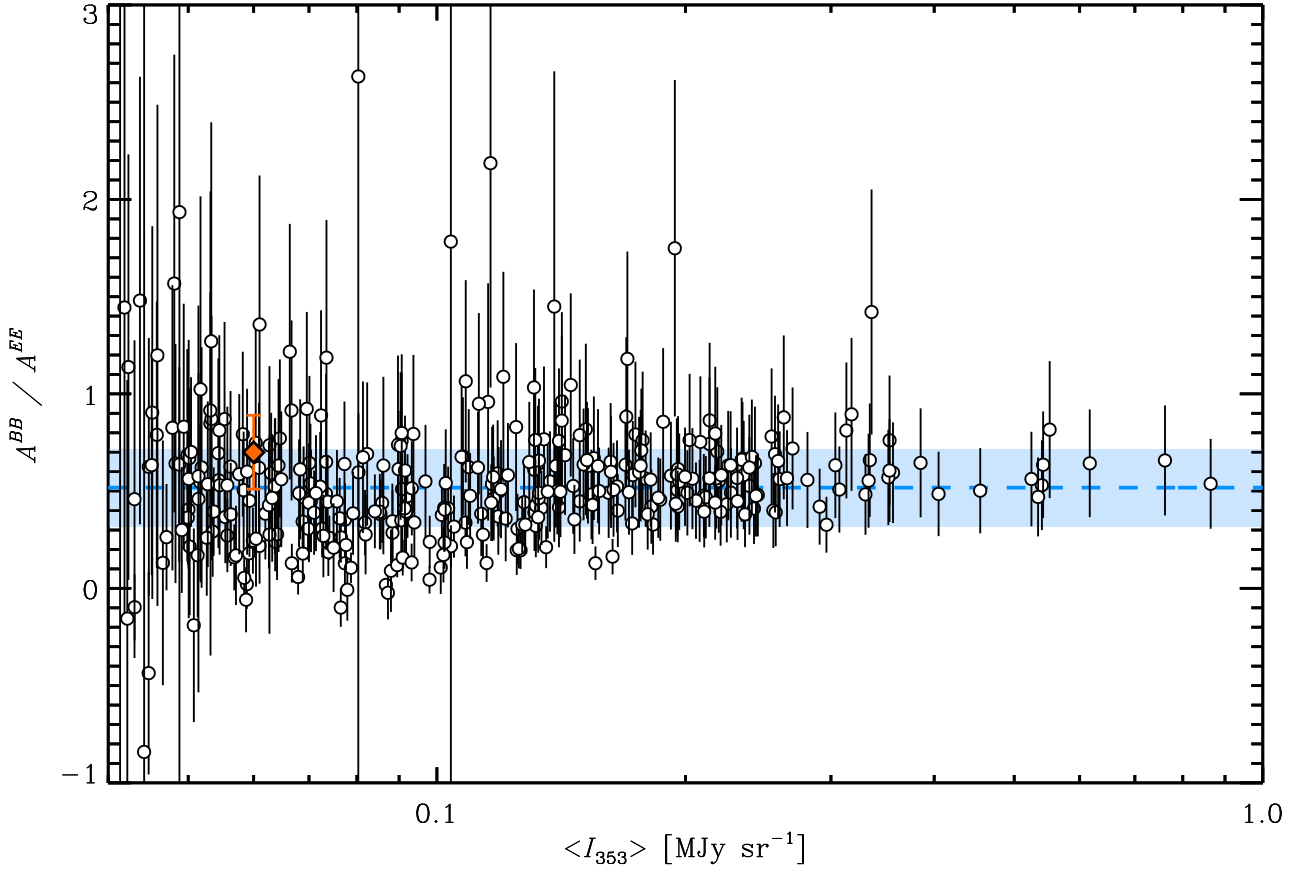


Fig. C.2. Ratio of the dust A^{BB} and A^{EE} angular power spectra amplitudes computed on the 352 patches at high Galactic latitudes (described in Sect. 5, circles), as a function of the mean dust intensity $\langle I_{353} \rangle$ of the patch. The mean value, $\langle A^{BB}/A^{EE} \rangle = 0.51 \pm 0.18$ here, is represented as a dashed-blue line and the associated $\pm 1\sigma$ dispersion as a light blue shaded area. The A^{BB}/A^{EE} ratio for the M_{B2} spectra presented in Sect. 6.3 is shown as an orange diamond.

with a significantly different A^{BB}/A^{EE} ratio, e.g., some smaller values for $\langle I_{353} \rangle$ in the range 0.08–0.1 MJy sr $^{-1}$.

We additionally report in Fig. C.2 the A^{BB}/A^{EE} value determined for the M_{B2} spectra computed in Sect. 6.3. The A^{EE} and A^{BB} amplitudes are computed as they are in Sect. 5, fitting a power law in ℓ to the \mathcal{D}_ℓ^{EE} and \mathcal{D}_ℓ^{BB} spectra with a fixed exponent $\alpha_{EE,BB} = -2.42$. Thus, for M_{B2} , we find that under these assumptions $A^{BB}/A^{EE} = 0.70 \pm 0.19$. This value is higher than the average for such fields, but consistent with the mean expected value.

Appendix D: Systematic effects relating to the power spectrum estimate in the BICEP2 field

D.1. Dust \mathcal{D}_ℓ^{BB} spectrum measurements in the BICEP2 field using Xpol and Xpure

We present in Fig. D.1 the difference of the \mathcal{D}_ℓ^{BB} power spectra computed by Xpol and Xpure in M_{B2} ($\mathcal{D}_\ell^{BB,Xpure} - \mathcal{D}_\ell^{BB,Xpol}$). The processing is the same as described in Sect. 6.3.

The Xpol and Xpure angular power spectra are consistent with each other in all three ℓ bins. The maximum difference observed is in the $\ell = 40$ –120 bin, where the Xpure spectrum is 10% higher than the Xpol spectrum presented in Sect. 6.3. Moreover, the Xpol recovered error bars and the Xpure error bars from Monte Carlo simulations of *Planck* inhomogeneous noise, also presented in Fig. D.1, are consistent.

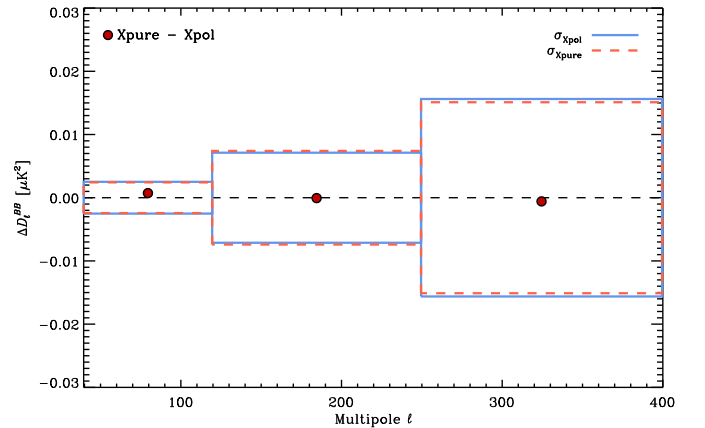


Fig. D.1. Xpol minus Xpure *Planck* 353 GHz \mathcal{D}_ℓ^{BB} angular power spectrum differences extrapolated to 150 GHz, computed from the cross-DetSets on M_{B2} (red circles). The blue boxes represent the $\pm 1\sigma$ errors computed using Xpol from the data on M_{B2} , while the dashed orange boxes are the Xpure $\pm 1\sigma$ errors coming from Monte Carlo simulations of *Planck* noise.

We conclude from this comparison that the results presented in Sect. 6.3 do not depend significantly on the method used for estimating the dust \mathcal{D}_ℓ^{BB} spectrum.

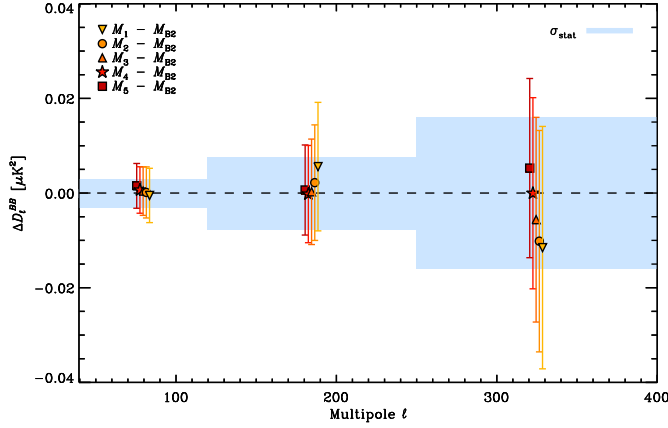


Fig. D.2. *Planck* 353 GHz \mathcal{D}_ℓ^{BB} angular power spectrum differences extrapolated to 150 GHz, determined from the spectra computed on the M_{1-5} regions presented in Appendix D.2 and the spectrum computed on M_{B2} . \mathcal{D}_ℓ^{BB} difference values for the five regions are shown using colours from yellow (for M_1) to dark red (for M_5). As in Fig. 9, the blue boxes represent the statistical uncertainties from noise associated with the M_{B2} spectrum. They are centred on zero because we compute spectrum differences here.

D.2. Impact of uncertainties in the specification of the BICEP2 field

Our estimation of the dust \mathcal{D}_ℓ^{BB} angular power spectrum in M_{B2} can depend on the detailed definition of the field. To explore the dependence of our results on the extent and specification of our approximation of the BICEP2 field, we repeat our computation of the dust \mathcal{D}_ℓ^{BB} power spectrum on the 353 GHz data extrapolated to 150 GHz, as in Sect. 6.3, for slight variations in the definition of this field.

For this purpose, we start from the mask M defined in Sect. 6.1, which consists of zeros and ones. We increase its size (with a smoothing and a cut) in order to have an outline that extends exactly 1° further in every direction. This defines M_5^b (“b” for binary, since it contains zeros and ones like M). We then decrease the size of M_5^b (with smoothing and cut) by exactly 1° in every direction to obtain M_4^b . After that M_4^b is shrunk in the same way to obtain M_3^b and we proceed iteratively down to M_1^b . Then to each M_i^b mask we apply exactly the same procedure for apodizing that we applied to M to produce M_{B2} in Sect. 6.1 to yield the final M_i field. The effective area ($f_{\text{sky}}^{\text{eff}} 4\pi$) is 805 deg^2 for M_5 , 677 deg^2 for M_4 , 564 deg^2 for M_3 , 460 deg^2 for M_2 , and 365 deg^2 for M_1 . We note that because of the forward and backward smoothing, M_{B2} defined in Sect. 6.1 is similar, but not exactly equal to M_4 .

We compute the 353 GHz \mathcal{D}_ℓ^{BB} power spectrum on all five fields using Xpo1 and extrapolate the results to 150 GHz with the frequency dependence from Planck Collaboration Int. XXII (2015), as in Sect. 6.3. We show in Fig. D.2 the difference between these spectra and the \mathcal{D}_ℓ^{BB} spectrum computed on M_{B2} presented in Sect. 6.3. We also show the error budget for M_{B2} , centred on zero because we are looking at differences between power spectra.

The recovered scatter is very low in the bin with $\ell = 40\text{--}120$ (the standard deviation of the mean value among the fields is $0.04 \times 10^{-2} \mu\text{K}_{\text{CMB}}^2$), much lower than the statistical uncertainty in this particular bin. In the two other bins, the scatter is more important, but still consistent with the statistical uncertainty.

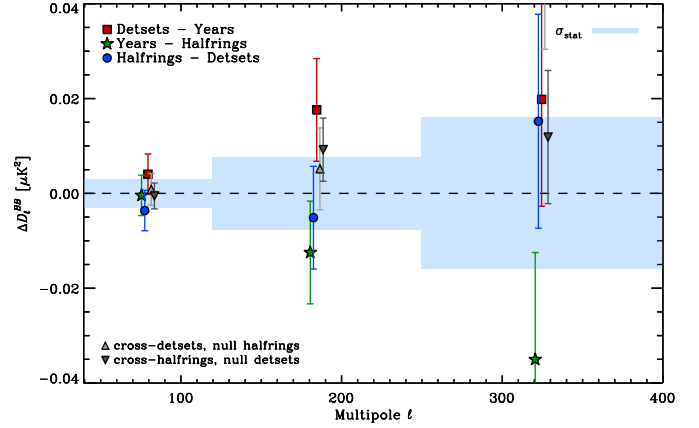


Fig. D.3. *Planck* 353 GHz \mathcal{D}_ℓ^{BB} angular power spectrum differences extrapolated to 150 GHz, computed from the following cross-spectra differences: DetSets minus Years (red squares); Years minus HalfRings (green stars); and HalfRings minus DetSets (blue circles). We also show the null test performed using the cross-DetSets spectra of the HalfRing half-differences (light grey triangle) and the cross-HalfRings of the DetSet half-differences (dark grey reversed triangle) at 353 GHz. As in Fig. 9, the blue boxes represent the statistical uncertainties from noise; these are centred on zero because we do not expect any signal for these null tests.

We conclude from this analysis that the main result presented in Sect. 6.3 does not depend on our precise definition of M_{B2} .

D.3. Assessment of the Planck HFI systematics in the BICEP2 field

To assess the potential contribution of systematic effects to the dust 353 GHz \mathcal{D}_ℓ^{BB} spectrum computed on M_{B2} , we repeat the analysis presented in Sect. 6.3 on null tests coming from subtracting different *Planck* 353 GHz data subsets.

The cross-DetSets, cross-HalfRings, and cross-Years spectra are computed for the 353 GHz data extrapolated to 150 GHz. The differences of these cross-spectra (DetSets minus Years, Years minus HalfRings, and HalfRings minus DetSets) are presented in Fig. D.3. In the first ℓ bin ($\ell = 40\text{--}120$), the three differences of the dust \mathcal{D}_ℓ^{BB} power spectra are consistent with zero, given the statistical uncertainty. They exhibit a dispersion consistent with what is expected from statistical noise. In the other bins the dispersion is larger, but still consistent with the noise. We conclude that the systematic errors are subdominant.

In addition to these data cuts, we create null-test \mathcal{D}_ℓ^{BB} spectra on M_{B2} from the four data subsets at 353 GHz involving detector sets and ring halves. We compute the cross-DetSet spectra between their two HalfRing half-differences $(353_{\text{DS1,HR1}} - 353_{\text{DS1,HR2}})/2 \times (353_{\text{DS2,HR1}} - 353_{\text{DS2,HR2}})/2$ and the cross-HalfRings between the two DetSet half-differences $(353_{\text{DS1,HR1}} - 353_{\text{DS2,HR1}})/2 \times (353_{\text{DS1,HR2}} - 353_{\text{DS2,HR2}})/2$. These null-test spectra are also shown in Fig. D.3. We can see that these spectra are consistent with zero in all the ℓ bins, given the statistical and systematic uncertainties.

We list in Table D.1 the χ^2 values for the null hypothesis, as well as the PTE for these null tests (plus additional values not presented in Fig. D.3). All these tests are consistent with the null hypothesis.