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# Mass distribution in the core of MACS J1206

## Robust modeling from an exceptionally large sample of central multiple images

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### ABSTRACT

We present a new strong lensing analysis of the galaxy cluster MACS J1206.2–0847 (MACS 1206), at  $z = 0.44$ , using deep spectroscopy from CLASH-VLT and VLT/MUSE archival data in combination with imaging from the Cluster Lensing and Supernova survey with *Hubble*. MUSE observations enable the spectroscopic identification of 23 new multiply imaged sources, extending the previous compilations by a factor of approximately five. In total, we use the positional measurements of 82 spectroscopic multiple images belonging to 27 families at  $z = 1.0$ – $6.1$  to reconstruct the projected total mass distribution of MACS 1206. Remarkably, 11 multiple images are found within 50 kpc of the brightest cluster galaxy, making this an unprecedented set of constraints for the innermost projected mass distribution of a galaxy cluster. We thus find that, although dynamically relaxed, the smooth matter component (dark matter plus hot gas) of MACS 1206 shows a significant asymmetry, which closely follows the asymmetric distribution of the stellar component (galaxy members and intracluster light). We determine the value of the innermost logarithmic slope of the projected total mass density profile and find it to be close to the canonical Navarro-Frenk-White value. We demonstrate that this quantity is very robust against different parametrizations of the diffuse mass component; however, this is not the case when only one central image is used in the mass reconstruction. We also show that the mass density profile from our new strong lensing model is in very good agreement with dynamical and X-ray measurements at larger radii, where they overlap.

**Key words.** galaxies: clusters: individual: MACS J1206.2–0847 – gravitational lensing: strong – cosmology: observations – dark matter

## 1. Introduction

In recent years, significant efforts have been devoted to observational and theoretical studies of the internal mass structure of galaxy clusters, which host the largest bound dark matter (DM) halos. These studies, particularly those focusing on the central high-density regions, provide stringent tests of the structure formation paradigm, in which cold dark matter (CDM) drives the hierarchical assembly and shape the density profiles of DM halos via dynamical processes over a wide range of scales. Cosmological  $N$ -body high-resolution simulations, where particles are treated as a collisionless fluid, consistently find that the central slope of the 3D mass density profile is  $\rho_{\text{DM}}(r) \propto r^{-\gamma}$ , with  $\gamma \simeq 1$  (Navarro et al. 1996; Moore et al. 1998; Gao et al. 2012), and where there is no evidence of a central core. However, the presence of baryons, which eventually become dominant in real massive clusters at small radii where the brightest cluster galaxy (BCG) resides, complicates this scenario. Baryonic processes, such as adiabatic cooling or heating due to star formation or accretion onto a supermassive black hole, can significantly alter the gravitational potential in the inner regions; as a result the DM mass distribution will dynamically adjust to it. The observational evidence that DM halos on cluster scales seem to have shallow inner slopes from a first systematic study using stellar kinematics and lensing in the strong and weak regime (Sand et al. 2004; Newman et al. 2011, 2013a,b) has stimulated a number of theoretical investigations on the role of the baryons

in shaping cluster cores. Despite recent progress in complex hydrodynamical simulations of clusters, there is still no consensus on the net effect of such feedback mechanisms on the inner density slope (see, e.g., Gnedin et al. 2004; Martizzi et al. 2012; Schaller et al. 2015). In addition, dynamical processes due to infalling galaxies may also play a relevant role in producing a flat central slope (Nipoti et al. 2004; Del Popolo 2012).

Interestingly, the central logarithmic slope  $\gamma$  is also quite sensitive to the physical properties of the DM particles. For example, a nonvanishing self-interaction cross section of DM particles would lead to the formation of a core in the high-density regions, approximately within the central 50 kpc ( $\gamma \simeq 0$ ; e.g., Spergel & Steinhardt 2000; Firmani et al. 2000; Vogelsberger et al. 2012; Macciò et al. 2012). This would have significant implications on the strong lensing cross section of galaxy clusters (see, e.g., Meneghetti et al. 2001). Clearly, an understanding of the baryonic effects is critical in order to turn observational constraints of the innermost DM density profiles into a powerful probe of the nature of DM particles in combination with constraints on the self-interaction cross section from bullet-like cluster mergers (e.g., Markevitch et al. 2004; Harvey et al. 2015). In this regard, the extension of these observational studies to galaxy scale systems is particularly interesting.  $N$ -body simulations predict similarly cuspy profiles given the approximate self-similarity of density profiles across halo masses; however, baryonic effects are expected to vary across the mass spectrum

of DM halos. Observational studies of the inner density profiles of galaxy systems have focused on DM dominated dwarf galaxies, which have consistently revealed a flattening of the central density (Burkert 1995; Swaters et al. 2003; Adams et al. 2014) and field elliptical galaxies, which are instead found to have isothermal total mass profiles (i.e.,  $\rho_{\text{TOT}}(r) \propto r^{-2}$ ) using kinematic and lensing methods, implying a lack of cores for  $\rho_{\text{DM}}(r)$  (Grillo 2012; Sonnenfeld et al. 2012).

In general, the best observational constraints on the cluster density profiles can only be obtained by combining all possible tracers of the total cluster mass distribution, as each tracer is most sensitive in a different radial range and is affected by different astrophysical systematics. These methods are stellar kinematics of the BCG and strong gravitational lensing in the central regions (e.g., Newman et al. 2011); hydrostatic equilibrium of the hot X-ray gas out to  $\sim R_{500}$ ; weak gravitational lensing out to the virial radius,  $R_{200}$ ; and galaxy dynamics at  $R \gtrsim 100$  kpc to well beyond the virial radius, which has recently become feasible with extensive spectroscopic surveys (Biviano et al. 2013). The quality and homogeneity of gravitational lensing data on large samples of clusters have increased dramatically in recent years thanks to dedicated programs with the *Hubble* Space Telescope (HST), particularly with the Cluster Lensing and Supernova survey with *Hubble* (CLASH, Postman et al. 2012), later enhanced with the *Hubble* Frontier Fields program (HFF, Lotz et al. 2017), supplemented by ground-based panoramic high-quality imaging data, especially with Subaru/SupCam (Umetsu et al. 2014; von der Linden et al. 2014).

These studies have shown that the overall total mass density profiles of massive clusters is on average well reproduced by the Navarro-Frenk-White parametrization (NFW, Navarro et al. 1996, 1997), down to  $R \sim 100$  kpc. At lower radii, possibly down to a few kpc, separating the luminous and dark matter contributions becomes increasingly difficult. The most promising approach is indeed the combination of a highly precise strong lensing model, based on a large number of spectroscopically confirmed multiple images, and spatially resolved kinematics of the BCG. The latter can probe the inner cluster potential out to 2–3 effective radii ( $R_e$ ) in clusters at  $z \sim 0.4$  or approximately 50 kpc, whereas strong lensing can robustly probe these small radii ( $R < 50$  kpc) provided that an adequate number of internal multiple images are present, which is the case of the cluster MACS J1206.2–0847 (hereafter MACS 1206), the subject of this study.

The combination of strong lensing and internal kinematics is also not straightforward; a dynamical model for the mass profile from the projected velocity dispersion and density profile requires an estimate of the mass-to-light ratio (e.g., a knowledge of the BCG star formation history and the stellar IMF), as well as an ansatz on the isotropy of the stellar orbits. Therefore, a simple dynamical model may not capture the complexity of the 3D phase space stellar distribution in the inner core and is prone to systematics or degeneracies.

In this paper we present a new, significantly enhanced measurement of the inner total mass distribution of MACS 1206 based on an exceptionally large number of central multiple images identified with CLASH multi-band imaging; this measurement is possible thanks to the unique sensitivity of the Multi Unit Spectroscopic Explorer (MUSE) on the Very Large Telescope. We describe the new spectroscopic confirmation of 73 multiple images combined with previous studies, which provide a sample of 27 background sources multiply lensed into 82 multiple images. A good fraction of these images is found in the inner 100 kpc, enabling a very robust determination of the total mass

density profile down to a few kpc, thus extending and improving previous determinations of the density profiles based on weak lensing, X-ray observations, and galaxy dynamics. In a forthcoming paper we will use these new strong lensing measurements of the total mass to separate the luminous and dark matter contributions, also taking advantage of the internal kinematics of the BCG.

The galaxy cluster MACS 1206, discovered in the ROSAT All Sky Survey (RXC J1206.2–0848, Böhringer et al. 2001), at  $z = 0.44$ , has long been known as a powerful gravitational lens (Borgani & Guzzo 2001; Ebeling et al. 2009). Its mass distribution has been studied as part of the CLASH project, using a wide range of techniques. A strong lensing model exploiting a large number of multiple images (mainly photometrically identified) was first developed by Zitrin et al. (2012), and later revisited by Eichner et al. (2013). The overall cluster mass distribution was further studied through a combination of weak and strong lensing (Umetsu et al. 2012) and galaxy dynamics based on a large redshift sample of cluster members from the CLASH-VLT project (Biviano et al. 2013; Rosati et al. 2014). Further analysis of its gravitational potential and mass distribution have included a combination of methods and multiwavelength data sets (Stock et al. 2015; Sereno et al. 2017). The stellar content of MACS 1206 has also been the subject of a number of studies using spectrophotometric and kinematical information from the CLASH-VLT data set: Presotto et al. (2014) has studied the color and morphological properties of its prominent intracluster light (ICL), detailed investigations of its galaxy populations, and internal structure have been presented in Annunziatella et al. (2014) and Girardi et al. (2015), and more recently in Kuchner et al. (2017).

In this paper, we adopt the standard  $\Lambda$ CDM cosmological model, with  $\Omega_m = 0.3$  with vanishing curvature and  $H_0 = 70 \text{ km s}^{-1}/\text{kpc}$ . Adopting this cosmology, at the cluster redshift ( $z = 0.439$ ) one arcsec corresponds to 5.68 kpc. All the images are oriented with north at top and east to the left, and the angles are measured from the west and oriented counterclockwise.

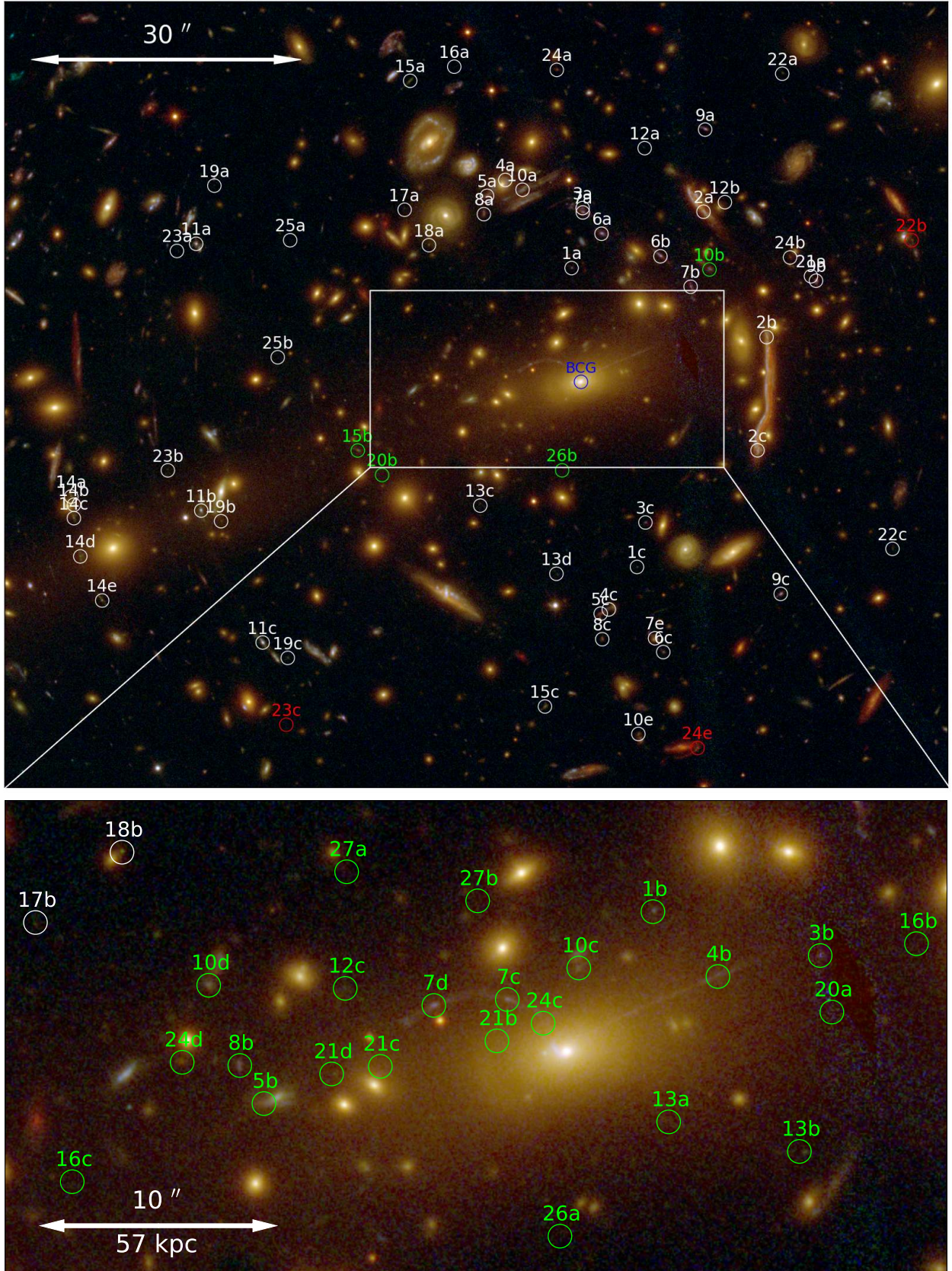
## 2. VLT and HST observations of MACS 1206

HST imaging of the core of the galaxy cluster MACS 1206 was obtained as part of the Cluster Lensing And Supernova survey with *Hubble* (CLASH, Postman et al. 2012), from the UV to the near-IR (16 filters). In Fig. 1, we show the color composite image obtained from the combination of 12 HST filters.

As part of the CLASH-VLT Large Programme (Rosati et al., in prep.), VLT/VIMOS was used to measure redshifts for  $\sim 2700$  sources over an area of  $400 \text{ arcmin}^2$ , spectroscopically confirming 600 galaxy members (Biviano et al. 2013). The spectroscopic catalog was publicly released in March 2014.

### 2.1. MUSE observations

MACS 1206 was also observed with the integral field spectrograph MUSE on the VLT (Bacon et al. 2014) under the GTO programs 095.A-0181(A) and 097.A-0269(A) (P.I. J. Richard) in April–May 2015 and April 2016. The MUSE survey area includes three pointings, one centered on the BCG with a rotation of  $\approx 20^\circ$ , and two with an offset of  $\approx 35''$  towards the east and west. A total of 25 exposures of 1800 s each were obtained covering an effective area of  $2.63 \text{ arcmin}^2$ , of which  $0.5 \text{ arcmin}^2$  have an exposure of 8.5 h and the remaining area  $\approx 4$  h. An offset of  $\approx 0''.5$  and a rotation angle of  $90^\circ$  were applied in different exposures to improve the removal of instrumental signatures and sky subtraction.



**Fig. 1.** Spectroscopically confirmed families of multiple images in MACS 1206 overlaid on a color composite image based on 12 CLASH filters (from optical to near-infrared wavelengths). White and green circles indicate, respectively, the tangential ( $\mu_{\text{tan}} > \mu_{\text{rad}}$ ) and radial ( $\mu_{\text{tan}} < \mu_{\text{rad}}$ ) multiple images (see Eqs. (3) and (4)) used in our strong lensing model (see Table A.1). The three red circles indicate multiple images that are excluded from our models because they might be significantly deflected by massive and angularly close early-type galaxies at distances between those of the galaxy cluster and the sources.

The raw data were reduced using the standard calibrations provided by the MUSE pipeline (Weilbacher et al. 2014), version 1.6.2, following the same procedures described in Caminha et al. (2017). For each of the 25 observations we checked the calibrated data-cube and wavelength-collapsed images, but did not find large variations on the observational conditions and final calibration. We then combined all the MUSE PIXELTABLEs, taking into account the positional offset of each observation, into one single data-cube. The final data-cube has a field of view of  $2.63 \text{ arcmin}^2$ , with a spatial sampling of  $0''.2$  in the wavelength range  $[4750\text{--}9350 \text{ \AA}]$ . The seeing, measured from stars in the wavelength-collapsed image of the final data-cube in regions with different exposure times, has a fairly constant value of  $\approx 0''.6$ . To reduce the sky residuals, we applied the Zurich Atmosphere Purge (Soto et al. 2016) using a SExtractor (Bertin & Arnouts 1996) segmentation map to define sky regions.

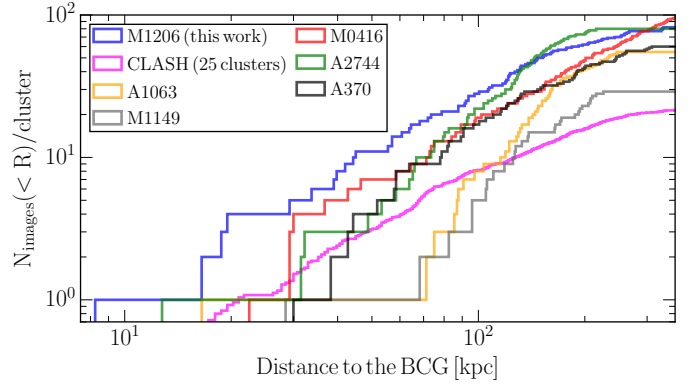
In the next section we describe the identification process of the multiply lensed images needed for the strong lensing model.

## 2.2. Multiple image identification

In keeping with our previous studies, we consider only families of multiple images with secure spectroscopic confirmation in order to avoid any image misidentification and to remove possible degeneracies between the values of the source redshifts and that of the cluster total mass. Incorrect or incomplete information about the multiple images can bias the estimate of the total mass of a lens and suppress the statistical uncertainties (Grillo et al. 2015; Caminha et al. 2016a; Johnson & Sharon 2016) of the strong lensing modeling.

We combine the spectroscopic measurements from CLASH-VLT (Biviano et al. 2013) and MUSE (Delgado-Correal, in prep.) to find the largest possible number of families of multiple images based on their redshift values (see Sect. 2.1). In this remarkable data set, we identify 27 different background sources in the redshift range from 1.01 to 6.06 that are lensed into 85 multiple images. Only four of these images lack a spectroscopic redshift, but their colors, shape, and image parity observed in the HST images ensure their correct association with two spectroscopically confirmed families. The redshift distribution of the multiple images presents a clear overdensity at  $z \approx 1.4$ , containing five galaxies within  $\Delta z = 0.0011$  (see Sect. 4).

In Fig. 1, we show the positions of the 85 multiple images, highlighting radial multiple images, i.e., those that according to our reference model (see Appendix A) have magnification values that are greater in the radial than in the tangential direction, in very good agreement with the observed shapes of the images. To illustrate this exceptionally large number of central multiple images, we show in Fig. 2 the histogram of the cumulative number of spectroscopically confirmed multiple images of MACS 1206, and other galaxy clusters with similar spectroscopic and photometric data, as a function of their projected distance from the BCG. We also show the overall distribution of the CLASH sample from Zitrin et al. (2015), which also includes many photometrically selected multiple images. Within the inner 20 kpc, MACS 1206 has strong lensing constraints from four multiple images, while at most one is usually present in other clusters. At larger radii, MACS 1206 still contains the largest number of multiple image constraints out to  $\approx 200 \text{ kpc}$ . We also note that Abell 1063, which is known to be a very regular and relaxed cluster, presents only one central multiple image, while the



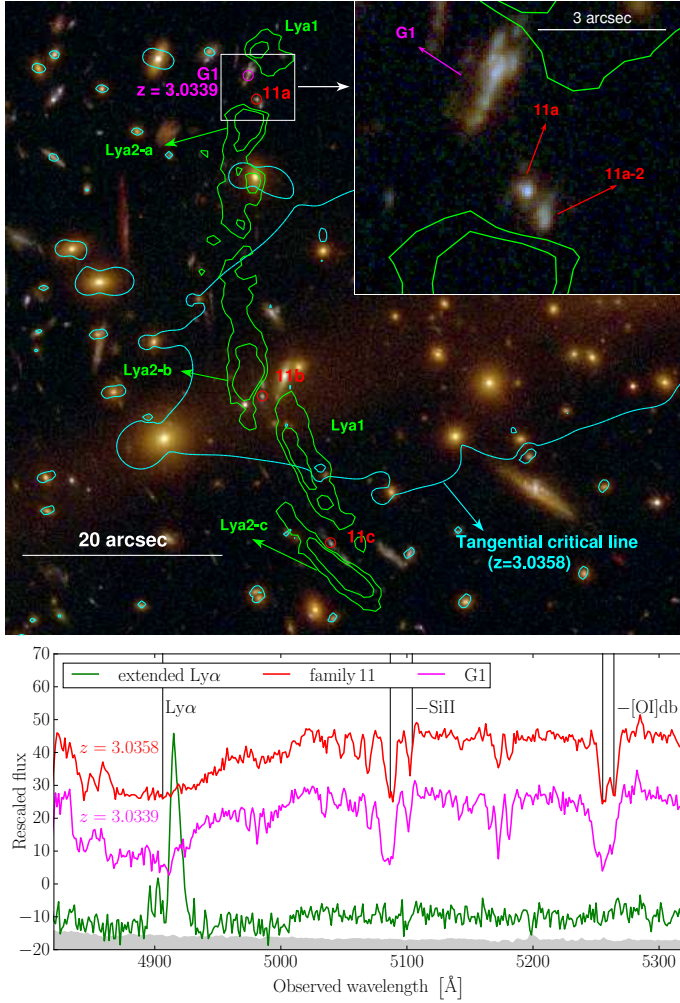
**Fig. 2.** Cumulative distribution of the number of multiple images belonging to spectroscopically confirmed families of MACS 1206 and other clusters with similar MUSE and HST data. For the CLASH study by Zitrin et al. (2015), we consider all multiple images (also those with no spectroscopic information) and the values are renormalized by the number of clusters in that work, only 7 of the 25 clusters present spectroscopically confirmed multiple images within the inner 20 kpc.

merging clusters MACS J0416.1–2403 (hereafter MACS 0416, Balestra et al. 2016) and Abell 2744 have more multiple images in their inner regions.

Interestingly, 10 of the 27 multiply imaged sources are Lyman- $\alpha$  emitters with no detection in the CLASH imaging data (limiting AB mag in  $F814W = 27.7$ ), illustrating the high sensitivity of MUSE to emission lines. We note that Lyman- $\alpha$  emitters with no imaging counterpart have been found with MUSE even in deeper HST imaging, such as in the *Hubble* Frontier Fields (see, e.g., Caminha et al. 2017; Mahler et al. 2017). Although they are very faint, the images of these sources are clearly detected in the MUSE data-cube and their spectroscopic redshifts are secure (see Fig. A.1). We note that the Lyman- $\alpha$  profiles of these images are slightly narrower than those of the objects with clear HST detection, indicating a low level of scattering of the Lyman- $\alpha$  photons.

For each multiple image with HST detection, we carefully measure its position as the luminosity peak in the single band HST images. For each of the families detected only by MUSE, we create a continuum subtracted data-cube and collapse this cube in the wavelength interval of the Lyman- $\alpha$  emission. Then we use the peaks of the emission of the multiple images to measure their positions. In the last column of Table A.1 we indicate for each image whether the position was measured on the HST images and in which filter, or whether the measurement was performed on the MUSE data. In order to reduce the noise in these pseudo-narrowband images, we apply a boxcar smoothing with kernel radius equal to one pixel (i.e.,  $0''.2$ ). The positions of all detected multiple images are shown in Table A.1 and the spectra and small cutouts of the HST color image in Fig. A.1. Here, as in previous works, we conservatively adopt a positional error of  $\sigma^{\text{obs}} = 0''.5$  for the images with HST detection and  $\sigma^{\text{obs}} = 1''$  for images detected only in the MUSE data because of the lower spatial resolution, noisier detection, and extended nature of the Lyman- $\alpha$  emission in some cases. This should also account for large-scale mass perturbations along the line of sight and the limitations of parametric mass models (Jullo et al. 2010; Host 2012).

We noticed that three multiple images, i.e., 22b, 23c, and 24e, are located very close in projection to massive spectroscopically confirmed background galaxies (see Fig. 1), which can introduce significant deflections in addition to that associated with



**Fig. 3.** *Top panel:* Lyman- $\alpha$  extended emission (green contours) associated with the multiple images (red circles) of family 11. The cyan lines show the tangential critical curves at the redshift of family 11 ( $z = 3.0358$ ). A galaxy very close angularly and in redshift ( $z = 3.0339$ ), but singly imaged, is indicated with a magenta circle. *Bottom panel:* red and magenta lines show, respectively, the stacked spectrum of the multiple images of family 11, corrected for the magnification factor and shifted upwards by a factor of +25 (flux units are  $10^{-20} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}$ ), and the spectrum of the singly imaged galaxy. The green line shows the extended Lyman- $\alpha$  continuum-subtracted (to reduce the contamination from ICL) emission, extracted from the innermost green apertures. The magenta and green spectra have been rescaled by arbitrary factors for better visualization. The gray region represents the rescaled variance obtained from the data reduction pipeline.

the cluster. Since the employed lensing software cannot take into account multiplane lensing effects, we decided not to include these multiple images in the reconstruction of the cluster total mass. In the end, our strong lensing models are optimized on the observed positions of 82 multiple images from 27 distinct background sources.

We also briefly comment on a remarkable extended Lyman- $\alpha$  emission associated with family 11 at  $z \approx 3.0$  (IDs 2 and 3 in Zitrin et al. 2012). In the upper panel of Fig. 3, we show the positions of the multiple images 11a/b/c and the contour levels of the extended Lyman- $\alpha$  emission. This consists of two blobs (Ly $\alpha$ 1 and Ly $\alpha$ 2) separated by 18 kpc (at  $z = 3.0358$ , on the source plane), with no continuum emission detected in the MUSE and broadband HST photometric data. The zoom-in panel shows in

detail the region between the two blobs where three compact sources have been detected in the HST imaging: a galaxy named G1 (not multiply lensed), the multiple image 11a with a substructure 11a-2. We note that in this region the Lyman- $\alpha$  emission is suppressed. Deficient emission along the direction of the stellar continuum has also been observed in a Lyman- $\alpha$  blob behind Abell 1063 (Caminha et al. 2016b). The images 11a, 11a-2, and Ly $\alpha$ 2-a are lensed in two additional counter-images located towards the southern region and indicated as 11b/c, 11b/c-2, and Ly $\alpha$ 2-b/c. Instead, the galaxy G1 is outside the region of multiple image formation, while the extended Ly $\alpha$ 1 is only partially multiply lensed, and its counter-image appears crossing the tangential critical line between the images 11b and 11a.

In the bottom panel of Fig. 3, we show the stacked MUSE spectra of the multiple images 11a/b/c corrected for the magnification factor, and also the emission of the single image G1. These two sources present strong absorption features, including Lyman- $\alpha$  revealing a high column-density along the line of sight (see also Zitrin et al. 2012, for the VIMOS spectra of 11a/b/c). The emissions of Ly $\alpha$ 1 and Ly $\alpha$ 2 are similar and do not have strong spatial variation or continuum. In the same panel, we show the stacked continuum subtracted spectrum of the innermost green regions. Using the  $5(3)\sigma$  limiting magnitude in the band  $F606W$  (see Postman et al. 2012), we estimate a lower limit for the equivalent width of Ly $\alpha$ 1 and Ly $\alpha$ 2 of 200(400)  $\text{\AA}$ , which – in combination with the deficient emission around the compact sources – implies that the Lyman- $\alpha$  emission is plausibly generated by fluorescence (Cantalupo et al. 2012). An offset between the ionizing sources and the Lyman- $\alpha$  emission, which in our case is 4.7 kpc between G1 and Ly $\alpha$ 1, and 4.1 kpc between 11a and Ly $\alpha$ 2, has been shown to be relatively common (see, e.g., Rauch et al. 2011; Vanzella et al. 2017). Other Lyman- $\alpha$  emitters behind galaxy clusters have been studied in detail (Patrício et al. 2016; Smit et al. 2017), showing the advantages of using the lensing magnification to explore high- $z$  sources.

### 3. Strong lensing model

In this section, we describe the reconstruction of the total mass distribution of MACS 1206 through a strong lensing analysis. We adopt the same modeling strategy and software (lenstool, Kneib et al. 1996; Jullo et al. 2007) described in Caminha et al. (2016a, 2017); we therefore provide a brief summary here and refer to these previous works for further details.

#### 3.1. Strong gravitational lensing definitions

We use the observed positions of the multiple images as constraints to reconstruct the total mass distribution of MACS 1206. To optimize a model, we minimize the  $\chi^2$  function, defined on the lens plane as

$$\chi^2(\mathbf{\Pi}) := \sum_{j=1}^{N_{\text{fam}}} \sum_{i=1}^{N_{\text{im}}^j} \left( \frac{|\theta_{i,j}^{\text{obs}} - \theta_{i,j}^{\text{pred}}(\mathbf{\Pi})|}{\sigma_{i,j}^{\text{obs}}} \right)^2, \quad (1)$$

where  $\theta^{\text{obs}}$  and  $\theta^{\text{pred}}$  are the multiple image observed and model-predicted positions, respectively;  $N_{\text{fam}}$  is the total number of families of multiple images; and  $N_{\text{im}}^j$  is the number of images associated with family  $j$ . The parameters that characterize a model are given by the vector  $\mathbf{\Pi}$ , and  $\sigma^{\text{obs}}$  is the adopted uncertainty on the observed image positions.

The total magnification,  $\mu$ , of a point-like image located in  $\theta$  is given by

$$\mu^{-1}(\theta) = [1 - \kappa(\theta)]^2 - \gamma^2(\theta), \quad (2)$$

where  $\kappa$  and  $\gamma$  are the convergence and the modulus of the shear, respectively (see, e.g., [Schneider et al. 1992](#)). The shear can be represented as a complex quantity,  $\gamma = \gamma e^{2i\varphi}$ , and the direction of distortion of an observed image is aligned with the phase  $\varphi$  of the shear. The total magnification can be expressed as the product of a tangential ( $\mu_{\text{tan}}$ ) and a radial ( $\mu_{\text{rad}}$ ) term, defined as

$$\mu_{\text{tan}}^{-1}(\theta) = 1 - \kappa(\theta) - \gamma(\theta), \quad (3)$$

$$\mu_{\text{rad}}^{-1}(\theta) = 1 - \kappa(\theta) + \gamma(\theta). \quad (4)$$

### 3.2. Parametric total mass model components

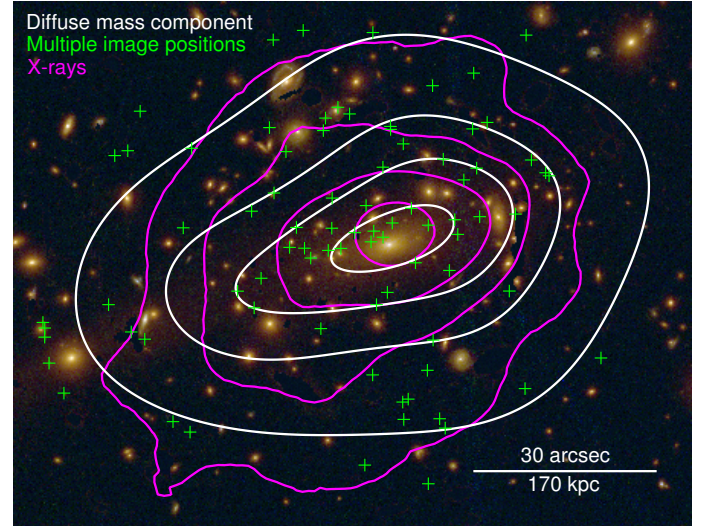
Using multiwavelength observations and different probes, Sereno et al. (2017) have recently proved that MACS 1206 does not show strong deviations from thermal equilibrium and that we are probably observing this cluster in a face-on projection. Given its relaxed state, it is expected that the smooth baryonic component traces the total gravitational potential well, and consequently also traces the dark matter distribution. Moreover, the distributions of the galaxy members and of the ICL suggest that MACS 1206 has a relatively high elongation along a slightly tilted east-west direction (see Fig. 1).

Motivated by this regularity, we divide the cluster total mass distribution into two terms: 1) a smooth component accounting for the mass in the form of principally dark matter, but also hot-gas and ICL; and 2) the clumpy component of the total mass of the galaxy members. Moreover, to account for the possible presence of massive structures in the outer regions of the cluster ( $\geq 300$  kpc), we include an external shear term parametrized by its intensity  $\gamma_{\text{ext}}$  and orientation  $\theta_{\text{ext}}$ .

#### 3.2.1. Selection of cluster members

For the clumpy component of the total mass distribution, we first select the spectroscopically confirmed galaxy members. They are defined as the galaxies that provide a velocity dispersion value lower than  $\Delta_v = 2919 \text{ km s}^{-1}$  in the cluster rest frame ( $z = 0.439$ , [Girardi et al. 2015](#); this corresponds to a redshift range of  $z = 0.425\text{--}0.453$ ). Within the HST field of view, this criterion is satisfied by 114 galaxies with measured magnitudes brighter than 24 in the *F160W* filter. In order to select galaxy members with no spectroscopic information, we employ the method described in [Grillo et al. \(2015\)](#), which uses the HST photometry in 13 different filters to define the color-space region where the spectroscopic members are located. The distance from this region of each galaxy with no spectroscopic measurement is then converted into the probability of belonging (or not) to the cluster.

From our previous analyses of the clusters MACS 0416 ([Grillo et al. 2015](#); [Caminha et al. 2017](#)), MACS J1149.5+2223 ([Grillo et al. 2016](#)), and Abell S1063 ([Caminha et al. 2016a](#)) and from tests performed in MACS 1206 where we compared the cluster membership based on the first VIMOS-only measurements with the additional MUSE data, we can conclude that this methodology results in a low contamination of  $\approx 5\%$  and a completeness of  $\approx 95\%$ . Using this method, we selected 147 additional photometric members in the HST/WFC3 field of view, with *F160W* magnitudes brighter than 24. Moreover, to account for bright and massive galaxies that do not satisfy



**Fig. 4.** Cluster members of MACS 1206 used in the strong lensing models. Galaxies that do not satisfy the selection criteria described in Sect. 3.2.1 have been masked out of the original HST image using the SExtractor segmentation map. The white lines show the contour levels of the reconstructed surface mass density of the diffuse mass components only (obtained by removing the surface mass density of the cluster member halos from that of the total), corresponding to the values of  $[1.0, 1.5, 2.0, 3.0] \times 10^{15} M_{\odot} \text{ Mpc}^{-2}$ . The magenta lines show the isocontours of the 0.5–7 keV *Chandra* X-ray detection. The green crosses indicate the positions of the multiple images shown with white and green circles in Fig. 1.

the strict dynamical selection criterion, we relaxed the velocity dispersion limit to  $\Delta_v = 4000 \text{ km s}^{-1}$  for galaxies with stellar mass values higher than  $10^{10} M_{\odot}$  (following the scaling relation  $\log_{10}(M_{\star}/M_{\odot}) = 20.16 - 0.475 \times F160W$  derived from the SED fitting analysis presented in Delgado-Correal, in prep.), thus adding four extra spectroscopically confirmed members. In conclusion, the final cluster member catalog used in our strong lens model contains 265 galaxies,  $\approx 45\%$  of which have spectroscopic confirmation. Cluster members included in this sample are shown in the background HST image of Fig. 4 by masking out all the other detected sources.

As in [Caminha et al. \(2016a\)](#), we adopt for each cluster member a truncated dual pseudo-isothermal elliptical mass distribution with vanishing ellipticity and core radius. This model is described by two parameters, the central velocity dispersion ( $\sigma_{v,i}^{\text{gals}}$ ) and a truncation radius ( $r_{\text{cut},i}^{\text{gals}}$ ) (see, e.g., [Elíasdóttir et al. 2007](#); [Suyu & Halkola 2010](#)). In order to reduce the number of free parameters describing the 265 cluster members, we use a constant total mass-to-light ratio given by

$$\sigma_{v,i}^{\text{gals}} = \sigma_v^{\text{gals}} \left( \frac{L_i}{L_0} \right)^{0.25}, \quad r_{\text{cut},i}^{\text{gals}} = r_{\text{cut}}^{\text{gals}} \left( \frac{L_i}{L_0} \right)^{0.5}, \quad (5)$$

where  $L_0$  is a reference luminosity, that we associate with the BCG ( $\text{mag}_{F160W} = 17.2$ ), while the two normalizations  $\sigma_v^{\text{gals}}$  and  $r_{\text{cut}}^{\text{gals}}$  are free to vary in the modeling and describe the cluster members.

#### 3.2.2. Diffuse mass distribution

In order to probe systematics originated from the modeling assumptions on the cluster total mass parametrization, we consider two different models to describe the smooth dark matter component. Firstly, we adopt a parametric model given

by a pseudo-isothermal elliptical mass distribution (PIEMD, [Kassiola & Kovner 1993](#)). The projected mass distribution of this model is parametrized in terms of its center ( $x_0$  and  $y_0$ ), an effective velocity dispersion  $\sigma_v$ , a core radius  $r_{\text{core}}$ , an ellipticity  $\varepsilon \equiv (a^2 - b^2)/(a^2 + b^2)$  (where  $a$  and  $b$  are the major and minor axes), and its orientation  $\theta$ . The expression of the projected mass density  $\Sigma$  is given by

$$\Sigma(R) = \frac{\sigma_v^2}{2G} \left( R^2(\varepsilon) + r_{\text{core}}^2 \right)^{-1/2}. \quad (6)$$

The parameter  $r_{\text{core}}$  accounts for a finite value of the density  $\Sigma$  at the origin, i.e., if  $r_{\text{core}} \neq 0$ , it follows that  $\Sigma$  does not change for small values of  $R$ . Moreover, if  $r_{\text{core}}$  is sufficiently large, the profile will be flat in its inner regions, departing from a cuspy mass distribution.

We also use the well-established NFW profile ([Navarro et al. 1996, 1997](#)) to model the smooth mass component.  $N$ -body simulations show that this model describes well the spherically averaged dark matter distribution of halos in equilibrium. The NFW profile is parametrized by a characteristic density ( $\rho_s$ ) and a scale radius ( $r_s$ ). In this model, the concentration parameter is defined as  $c_{200} \equiv r_{200}/r_s$ , where  $r_{200}$  is the radius of the sphere inside which the mean cluster density is 200 times the critical density of the Universe at the cluster redshift. The expression for the 2D projected density and the derivation of the lensing quantities can be found in [Bartelmann \(1996\)](#), [Wright & Brainerd \(2000\)](#), [Golse & Kneib \(2002\)](#), or [Meneghetti et al. \(2003\)](#).

In order to account for variations in the central slope, an extension of the 3D NFW density profile, known as the generalized NFW model (see, e.g., [Zhao 1996](#); [Jing & Suto 2000](#); [Wyithe et al. 2001](#)), is defined as

$$\rho_{\text{gNFW}}(r) = \frac{\rho_s}{(r/r_s)^{\gamma_{\text{gNFW}}} (1 + r/r_s)^{3-\gamma_{\text{gNFW}}}}, \quad (7)$$

where if  $\gamma_{\text{gNFW}} = 1$  the original NFW model is recovered, and  $\gamma_{\text{gNFW}} < 1$  or  $\gamma_{\text{gNFW}} > 1$  correspond, respectively, to shallower or steeper 3D profiles in the core.

In the *lenstool* code, the ellipticity of the NFW and gNFW models is introduced in the lens potential ( $\varepsilon_{\text{pot}}$ ) and not in the projected mass. This approximation allows a fast computation of the deflection angle across the image plane; however, it presents some limitations for relatively high values of the ellipticity. Basically, for ellipticity higher than 0.5, the associated projected mass has a nonphysical dumbbell shape and negative values along the minor axis (see, e.g., [Golse & Kneib 2002](#); [D  met-Montoya et al. 2012](#)). Indeed, in our strong lensing models that use the NFW and gNFW,  $\varepsilon_{\text{pot}}$  reaches values on the order of 0.5. However, we use these parametrizations only for the sake of comparison with our reference model based on the PIEMD model, where the ellipticity is introduced in the projected mass distribution.

### 3.3. Optimizing the strong lensing model

In order to find the parametrization of the total mass distribution that best reproduces the multiple image positions, we begin by adopting one single PIEMD profile to represent the diffuse component, as discussed in Sect. 3.2.2, which has six free parameters. In addition to that, the galaxy members and the external shear add two more free parameters each, for a total of ten free parameters. We note that this parametrization is very similar to that adopted in [Eichner et al. \(2013\)](#); see Sect. 4.1, who used a very different set of multiple images, many of which

were based on photometric information alone. The results from this first model, named P1, are shown in Table 1. We adopt a flat prior for all free parameters in the lens models presented in this work. The model P1 yields a root mean square (rms) difference ( $\Delta_{\text{rms}}$ ) between the model-predicted and observed positions of 2''04. Although this value is comparable to previous strong lensing models of MACS J1206 ([Zitrin et al. 2012](#); [Eichner et al. 2013](#), who used a significantly smaller set of spectroscopically confirmed families), it cannot reproduce the observed multiplicity and positional configuration of families 12, 17, 18, 21, and 26. Moreover, we find that multiple images located in the northern region of the cluster have a slightly larger offset between the model-predicted and observed positions ( $\Delta$ ), suggesting an underlying asymmetry in the mass distribution.

We also note that the exceptionally large number of radially elongated images (27 out of 85) is suggestive of a projected mass distribution with high-order asymmetries, i.e., more complex than an elliptically symmetric distribution. Using numerical simulations, [Torri et al. \(2004\)](#) have shown that following the evolution of a cluster in cosmic time, the cross-section of radial arc formation can be boosted by a factor of 10 in the presence of asymmetries in the cluster core (see their Figs. 5 and 11). This is in agreement with recent studies of FF clusters based on deep MUSE spectroscopy, e.g., MACS 0416 ([Caminha et al. 2017](#)), Abell 2744 ([Mahler et al. 2017](#)), MACS 1149 ([Grillo et al. 2016](#); [Treu et al. 2016](#)), and Abell 370 ([Lagattuta et al. 2017](#)). [Biviano et al. \(2013\)](#) and [Sereno et al. \(2017\)](#) have shown that MACS 1206 is a fairly relaxed cluster; however, the remarkably asymmetric shape of its ICL ([Presotto et al. 2014](#)) and the distribution of the galaxy members (see Fig. 4) reveal a large degree of asymmetry of the overall mass distribution.

In an attempt to correctly reproduce the multiplicity of all multiple images, we then consider another model including an extra circular pseudo-isothermal profile whose center and core radius are left free to vary across the field of view. This model has now 14 free parameters and is named P2 (see Table 1). We find that the second diffuse halo makes the total mass distribution more elongated towards the north direction, while the main diffuse halo remains centered at  $\approx 0''.7$  from the BCG. This model has a  $\Delta_{\text{rms}}$  value of 1''.37 and can reproduce the multiplicity of most of the multiple images, except for family 26. However, this value of  $\Delta_{\text{rms}}$  is significantly higher than the typical subarcsecond average residuals obtained in recent studies using similar high-quality data sets, which combine HST and MUSE observations.

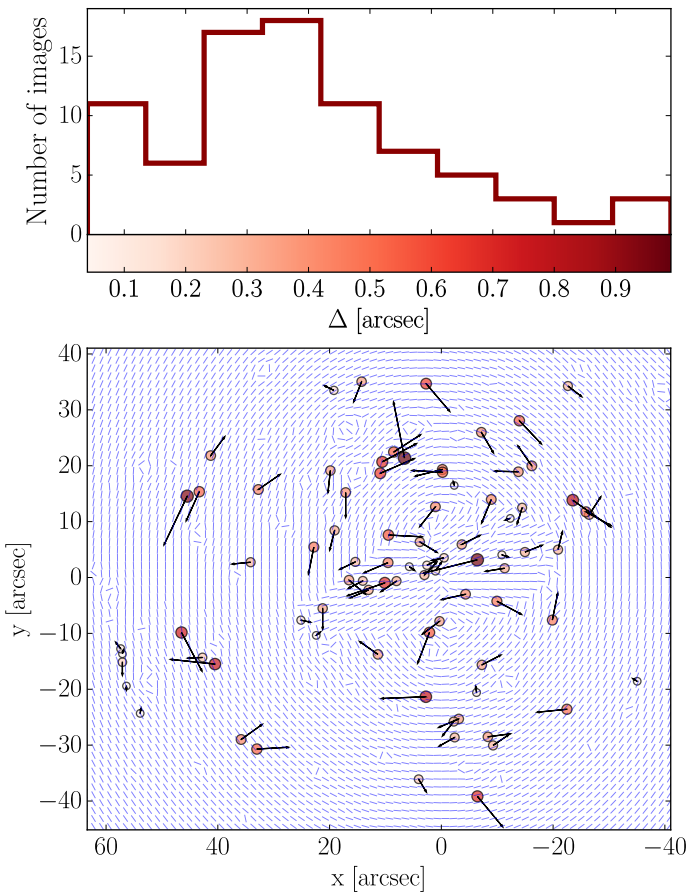
We therefore include a third circular halo in the parametrization of the total mass distribution, leading to 18 free parameters (model P3). In this case, the value of  $\Delta_{\text{rms}}$  reduces significantly to 0''.56 and the multiplicity of all multiple images can be reproduced correctly. We note that the multi-mass components introduced here should not be associated with extra dark matter halos, but rather to extra asymmetries or high-order multipoles that a single parametric profile cannot account for. Numerical simulations have shown that asymmetries in the mass distribution have a significant impact on the strong lensing properties of galaxy clusters ([Meneghetti et al. 2003, 2007](#)).

We further investigate the complexity of the cluster mass distribution by considering a model P3 $\varepsilon$  in which the ellipticity and orientation of the extra components are also free to vary, adding four more free parameters in the modeling. This model reproduces the positions of the observed multiple images with a  $\Delta_{\text{rms}}$  value of 0''.44, a reduction of  $\approx 27\%$  when compared to P3. In the top panel of Fig. 5, we show the distribution of the offset of each multiple image. In the bottom image, the circles

**Table 1.** Summary of the best fit models of MACS 1206 and comparison with previous works on other clusters using only spectroscopically confirmed families of multiple images.

Model ID	N. par.	d.o.f.	$\Delta_{\text{rms}} ["]$	$\chi^2_{\text{min}}$	BIC	AIC	Description
P1	10	100	2.04	819	1023	996	One elliptical PIEMD halo, 265 members and external shear
P2	14	96	1.37	394	616	579	Same as P1, but with a second circular PIEMD halo
P3	18	92	0.56	62.6	304	256	Same as P2, but with a third circular PIEMD halo
P3 $\epsilon$	22	88	0.44	41.0	301	242	Same as P3, but $\epsilon$ and $\theta$ values of all halos are free to vary (reference)
N3 $\epsilon$	22	85	0.40	33.3	294	235	Same as P3 $\epsilon$ , but the central halo is a pseudo-elliptical NFW
G3 $\epsilon$	23	84	0.40	33.3	299	237	Same as P3 $\epsilon$ , but the central halo is a pseudo-elliptical gNFW
P4	22	88	0.53	52.4	313	254	Same as P3, but with a fourth circular PIEMD halo
P3 $\epsilon$ BCG	25	82	0.44	40.0	315	247	Same as P3, but with BCG parameters free to vary
Abell S1063	17	41	0.32	16.8	–	–	Updated model from <a href="#">Caminha et al. (2016a)</a> and <a href="#">Karman et al. (2017)</a>
MACS J0416	26	104	0.59	143	–	–	Model by <a href="#">Caminha et al. (2017)</a>
Abell 2744	30	78	0.67	133	–	–	Model with the “gold constraints” by <a href="#">Mahler et al. (2017)</a>

**Notes.** Summary of the strong lensing models and their global results. Columns show the model IDs, the number of optimized parameters (N. par.) and degrees of freedom (d.o.f.), the best fit positional  $\Delta_{\text{rms}}$ , the value of the reference  $\chi^2_{\text{min}}$ , the Bayesian Information Criterion ([Schwarz 1978](#)), the Akaike information criterion ([Akaike 1974](#)), and a short description of each model. For the definitions of these quantities, we refer to [Caminha et al. \(2016a\)](#).



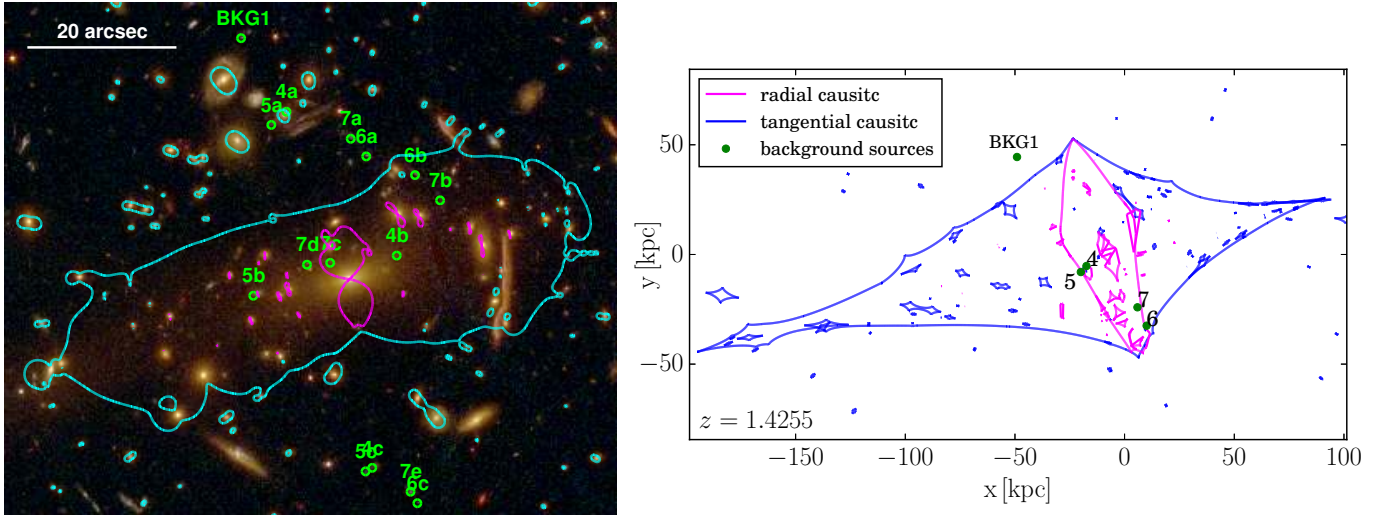
**Fig. 5.** Offset between the observed and model-predicted (model ID P3 $\epsilon$  in Table 1) positions of the multiple images in MACS 1206. Darker hues of red correspond to larger offsets. In the *top panel*, the histogram shows the distribution of the absolute values of the differences ( $\Delta$ ). In the *bottom panel*, the circles indicate the observed positions of the multiple images, and the arrows point towards the model-predicted positions. For the sake of clarity, the arrow lengths are ten times larger than the values of the corresponding offsets. The blue sticks represent the shear orientation on a regular grid (see Sect. 3.1) for a source at  $z_{\text{src}} = 1.4$ .

indicate the observed positions of the multiple images and the arrows point towards the model predicted positions with sizes ten times the offset values. The blue lines indicate the direction

of the distortion (see Sect. 3.1), which is in excellent agreement with the observed orientations of the gravitational arcs (tangential and radial) in Fig. 1. As expected, there is a mild correlation between the directions of the offsets and the distortion. Since the model P3 $\epsilon$  can reproduce very well the positions of all multiple images with a relatively low number of free parameters, given the number of constraints, we use it as our reference model to study the total mass distribution of MACS 1206. The best fit parameters and confidence levels are quoted in Table A.2. The inspection of the covariance between the parameters shows all the expected degeneracies in parametric lens models. Particularly, the external shear parameters show a mild degeneracy with the ellipticity and orientation of the second and third diffuse halos, however not with the central one.

In order to explore the sensitivity of our modeling to specific parametrizations, we also use the NFW and gNFW models to describe the central diffuse component, N3 $\epsilon$  and G3 $\epsilon$  respectively, where  $\gamma_{\text{gNFW}}$  is fixed to one in the former and left free to vary in the latter. In these models we keep the same PIEMD parametrization for the second and third diffuse halos as in the reference model P3 $\epsilon$ . The slope value  $\gamma_{\text{gNFW}}$  of the central diffuse component is not necessarily similar to the slope of the cluster total mass distribution ( $\gamma_{\text{gNFW}}^{\text{total}}$ ), represented in our parametrization as the sum of the diffuse components (generally more than one) and the galaxy members. We find that these two best fit models have similar mass distributions, yielding a  $\Delta_{\text{rms}}$  of 0''.40. Indeed, the reconstructed best fit values are very similar and  $\gamma_{\text{gNFW}}^{\text{halo}}$  is 1.06, making the two models virtually the same. Regarding the limitation of the pseudo-elliptical NFW model, the estimated values from the MCMC sampling are  $\epsilon_{\text{NFW}} = 0.44^{+0.09}_{-0.07}$  and  $\epsilon_{\text{gNFW}} = 0.45^{+0.08}_{-0.08}$  (95% confidence level), reaching the limit of  $\approx 0.5$  mentioned in Sect. 3.2.2. These two models are used only for the sake of comparison with our reference P3 $\epsilon$  model, since the high values of  $\epsilon_{\text{NFW}}$  might lead to nonphysical projected mass distributions.

We investigated whether further increasing the complexity of the cluster total mass distribution reduces the value of  $\Delta_{\text{rms}}$ . We did that by letting the velocity dispersion and cut-radius of the BCG free to vary, i.e., not following the other member total mass-to-light scaling relation. Despite these extra free parameters, we find that the  $\Delta_{\text{rms}}$  does not change and all other best fit parameters remain well within 68% confidence levels, thus not justifying this extra complexity in the mass modeling. We also



**Fig. 6.** Critical curves and caustics of the reference model P3 $\epsilon$  for a source at  $z_{\text{src}} = 1.4255$  (the mean redshift values of the sources). *Left panel:* tangential (cyan) and radial (magenta) critical lines on the image plane. The green circles show the observed positions of the multiple images belonging to the four families within  $\Delta z \leq 0.0011$ . BKG1 is a background galaxy not multiply lensed by MACS 1206. *Right panel:* tangential (cyan) and radial (magenta) caustics on the source plane, and the reconstructed positions of the background sources.

find that by including a fourth diffuse component, whose best fitting position is at  $\approx 30''$  southeast from the BCG, we cannot improve the overall fit of the multiple image positions. Similarly, negligible differences are found if we adopt nonzero ellipticities for the cluster members, fixing them to the values measured from the *F160W* band. Finally, we verify that by including the three multiple images 22b, 23c, and 24e (marked in red in Fig. 1), located near massive background galaxies, the value of  $\Delta_{\text{rms}}$  of the reference model increases to  $0''.71$ .

#### 4. Mass distribution of MACS1206

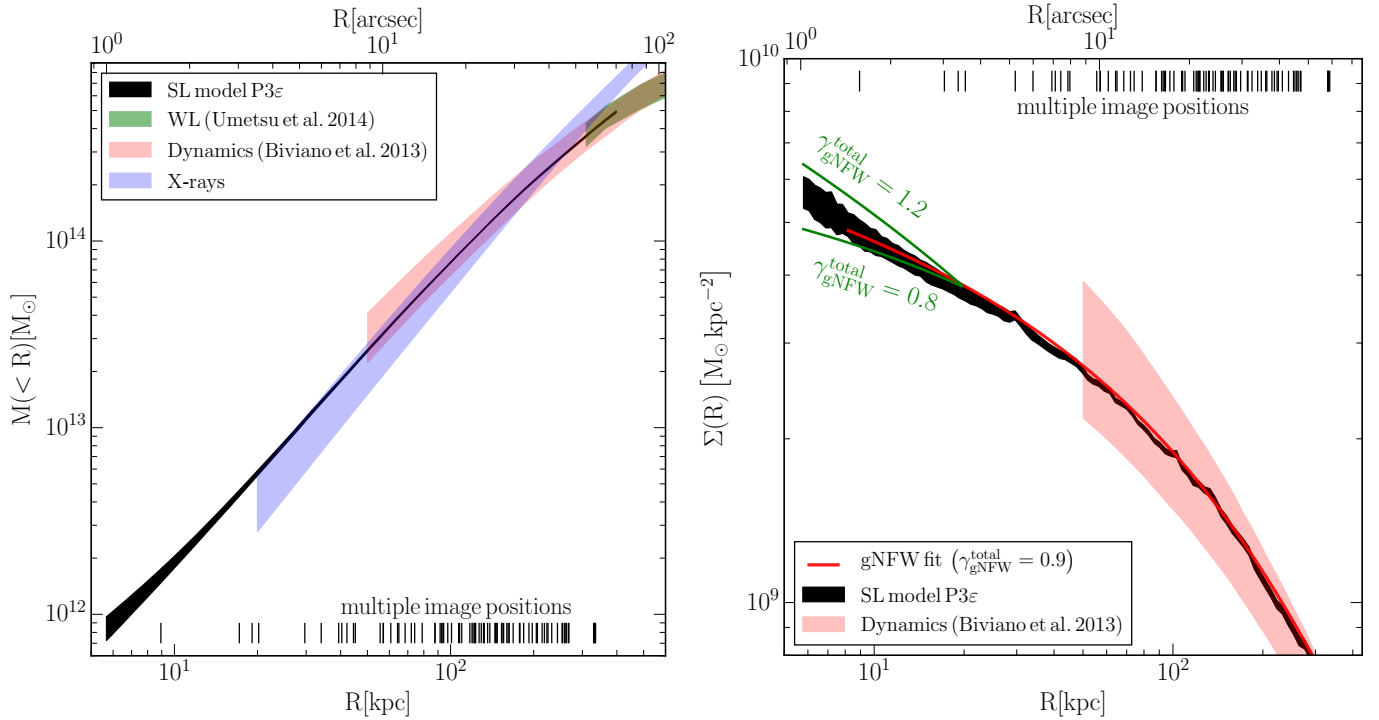
In Fig. 4, we show the surface mass density contours associated with the diffuse component of the mass distribution of our reference model. Owing to the inclusion of the three diffuse halos, the overall distribution is clearly asymmetric. However, this distribution is smooth and presents only one pronounced peak close to the BCG. We also note that the diffuse 2D mass component resembles the spatial distribution of the stellar component (ICL and galaxy members), as well as the hot X-ray gas. Interestingly, the simulated galaxy cluster *Hera* (Meneghetti et al. 2017), extracted from high-resolution *N*-body simulations (Planelles et al. 2014), presents a morphology similar to that of MACS 1206 (see Fig. 1 in Meneghetti et al. 2017), which indicates that such asymmetric structures might not be rare in the population of massive clusters.

As mentioned above, numerical simulations have suggested that such asymmetric mass distributions increase the likelihood that radial arcs will form and large radial caustics will be created. To illustrate this, we show in Fig. 6 the radial critical lines for sources at  $z = 1.4255$  (corresponding to the aforementioned background source overdensity) and the respective caustics on the source plane from our reference strong lensing model. We also indicate the positions of the five background sources located in the narrow redshift range  $[1.4248-1.4259]$ . Source BKG1 is not multiply lensed, while the other sources have different multiple-image configurations on the image plane. These five sources are relatively close in projection (within  $\approx 100$  kpc) and might be associated with a group in an early stage of formation at  $z \approx 1.4$ .

In Fig. 7, we show the cumulative total mass profile of our reference model P3 $\epsilon$ . To compute the 95% confidence level region, we extract 200 random models from the MCMC and create total mass maps with a spatial resolution of  $0''.05$ . For each map, we compute the mass within different radii and the 2.3rd and 97.7th percentiles from the distribution of the 200 measurements. The vertical lines locate the positions of the multiple images, i.e., the region with strong lensing constraints, from  $R \approx 9$  kpc out to  $R \approx 300$  kpc from the BCG center. The colored regions show the total mass profiles obtained from galaxy member dynamics (Biviano et al. 2013), X-ray hydrostatic analysis (see Sect. 4.2), and weak gravitational lensing (not combining with strong lensing, Umetsu et al. 2014). Although these independent measurements are valid only at large radii and cannot be extrapolated to the inner regions ( $R < 50$  kpc), the agreement with our strong lensing mass reconstruction in the overlapping radial range is remarkable.

In the right panel of Fig. 7, we show the total surface mass density profile (95% confidence level) and compare it with the results from Biviano et al. (2013). We find that one single gNFW profile accurately represents the radial profile of the total mass distribution down to  $R = 8$  kpc (solid red curve), where the contribution of the BCG halo starts to become significant. The recovered gNFW parameters are  $\rho_s = (1.9 \pm 0.3) \times 10^6 M_\odot \text{kpc}^{-3}$ ,  $r_s = (300 \pm 3) \text{kpc}$ , and  $\gamma_{\text{gNFW}}^{\text{total}} = 0.91 \pm 0.04$  (at 68% confidence level), corresponding to a concentration of  $c \approx 5.1 \pm 0.2$ . These values are in very good agreement with those obtained from the dynamical analysis (see Table 3 of Biviano et al. 2013), and show that the radial total mass distribution does not strongly deviate from a NFW profile, since  $\gamma_{\text{gNFW}}^{\text{total}}$  is close to one. In the same panel, we illustrate two gNFW profiles with slopes of 1.2 and 0.8, with the same  $r_s$  value and  $\rho_s$  rescaled in order to have the same  $\Sigma(R)$  at 20 kpc. We remark that the measurement of the total mass density profile in projection, within circular apertures, and superposing several diffuse components might also be consistent with profiles different from a gNFW profile.

We also performed a test to investigate possible systematic effects on the determination of the slope of the total projected mass profile when only a limited number of strong lensing constraints is used, or available, in the inner regions. In Fig. 8, we



**Fig. 7.** Comparison of different independent projected total mass determinations in MACS 1206. The black region represents the results at the 95% confidence level of our strong lensing analysis (reference model P3 $\epsilon$ ). At the 68% confidence level, the dynamical (Biviano et al. 2013), weak-lensing (Umetsu et al. 2014), and X-ray (see Sect. 4.2) total mass estimates are shown in red, green, and blue, respectively. The vertical lines indicate the projected radial distances from the cluster center of the multiple images presented in this work. The cumulative projected total mass profile is shown in the left panel. In the right panel we show the projected total surface mass density profile and the red line is a fit using a gNFW model. The green lines show two different gNFW profiles, with values of  $\gamma_{\text{gNFW}}^{\text{total}}$  equal to 0.8 and 1.2, normalized at  $R = 20$  kpc.

compare the density profile obtained with the P3 $\epsilon$  and G3 $\epsilon$  models using the full set of 82 multiple images with that obtained with the P3 $\epsilon$  model when only one multiple image within 70 kpc (in red) is considered. As discussed above, the latter configuration reproduces the most common set of constraints available on the CLASH or Frontier Field clusters, e.g., Abell 1063 and MACS J1149 (see Fig. 2). We note that the determination of the density profile using the new large set of central multiple images in MACS 1206 is very robust against different models (P3 $\epsilon$  and G3 $\epsilon$  are shown), whereas the model based on only one central image underestimates the inner slope of the total density profile.

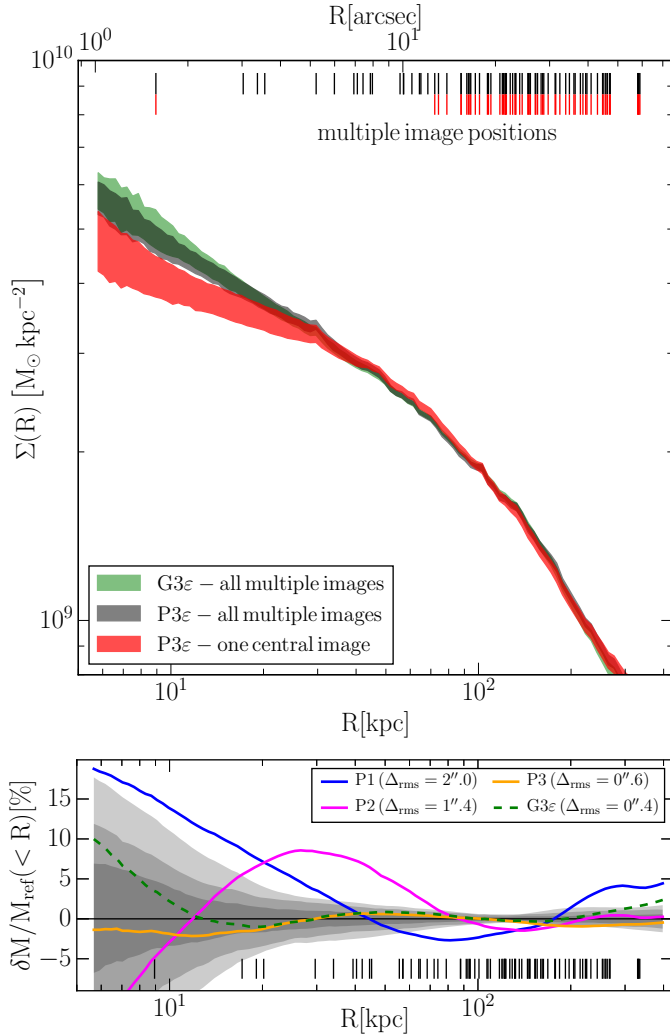
#### 4.1. Comparison with previous strong lensing analyses

Strong lensing analyses of MACS 1206 have been presented in Zitrin et al. (2012) and Eichner et al. (2013). The two studies used a similar set of approximately 50 multiple images belonging to 12 single background sources. This provides a relatively large number of constraints; however, their identification and distances were based largely on CLASH photometric redshifts, since only three multiply lensed sources had a spectroscopic redshifts from CLASH-VLT at that time. As discussed in our previous strong lensing analysis of the Frontier Field clusters, which take advantage of large sets of spectroscopically confirmed multiple images (Caminha et al. 2016a, 2017; Grillo et al. 2016; Lagattuta et al. 2017; Mahler et al. 2017), the use of multiple image systems identified on the basis of their photometric properties is prone to intrinsic systematics in the reconstruction of the internal structure of the mass distribution and in magnification measurements. Nonetheless, the use of a large

number of photometric multiple images is often enough to recover the circularized mass density profiles.

Indeed, previous analyses obtained a relatively high value for  $\Delta_{\text{rms}}$ : Zitrin et al. (2012) found  $\Delta_{\text{rms}} = 1''.8$ , while Eichner et al. (2013) found  $\Delta_{\text{rms}} = 0''.85$ , after removing two misidentified multiple images belonging to two families. Both these studies used only one elliptical profile to describe the smooth mass component. On the other hand, the total projected mass within 100 kpc of  $(8 \pm 1) \times 10^{13} M_{\odot}$  reported in Zitrin et al. (2012) and  $(7.11 \pm 0.04) \times 10^{13} M_{\odot}$  in Eichner et al. (2013) are in very good agreement (given the statistical and systematic errors) with the value of the study presented here of  $(7.25 \pm 0.02) \times 10^{13} M_{\odot}$ . The large set of spectroscopic multiple images used in our new analysis enables the determination of the asymmetric shape of the smooth mass component (as shown in Fig. 4), but also a robust determination of the mass component due to the subhalo population.

We note that the 27 multiple image families spectroscopically confirmed by MUSE contains four with previously known redshifts and seven families for which only photometric information was available (see Table 2 in Eichner et al. 2013, which updated the list from Zitrin et al. 2012). We were not able to confirm only one photometric family from Eichner et al. (2013; their ID 5). When comparing the new spectroscopic measurements with their model predicted redshifts, we find an error of  $\approx 10\%$ , which is larger than the photometric redshift error ( $\approx 5\%$ ). We also note that the purity of the cluster member catalog adopted in our new analysis, based on the highly complete sample of MUSE redshifts, is significantly higher than previous studies where member galaxies were selected from the cluster



**Fig. 8.** Comparison of the total mass density profiles of MACS 1206 obtained from strong lensing models with different cluster mass parametrizations and sets of multiple images. The vertical lines indicate the projected radial distances from the cluster center of the multiple images presented in this work (in black) and a subset of them (in red). *Upper panel:* gray and green regions show, respectively, the profiles for the reference model P3 $\epsilon$  and model G3 $\epsilon$ . The red region shows the profile with the same cluster mass parametrization as for the reference model, obtained by excluding all multiple images within 70 kpc in projection of the cluster center except the innermost one. The errors correspond to the 95% confidence level and are estimated from 200 different models extracted from the corresponding MCMCs. *Bottom panel:* radial profiles of the relative difference in the cumulative projected total mass values obtained from the reference model P3 $\epsilon$  and other models with different cluster mass parametrizations ( $\delta M = M_{\text{ref}} - M_i$ ), all employing the full set of multiple images. The gray regions show the statistical errors at the 68%, 95% and 99.8% confidence levels of the reference model.

red sequence. This further contributes to the accuracy and precision of our new model.

#### 4.2. The hydrostatic mass distribution of MACS1206

The hydrostatic mass profile shown in Fig. 7 is based on an archival *Chandra* ACIS-I observation (ObsId 3277). We have reprocessed it with a standard pipeline based on CIAO 4.9 (Fruscione et al. 2006) and CALDB 4.7.4 to create a new events-2 file which includes filtering for grade, status, bad pixels, and

time intervals for anomalous background levels. We obtain a cumulative good time interval of 22.9 ks. To recover the hydrostatic mass profile, we assume that the hydrostatic equilibrium holds between the intracluster medium and the gravitational potential, and that both have a spherically symmetric distribution (e.g., Ettori et al. 2013). Then we combine the gas density, temperature, and a parametrized dark matter distribution following the backward method described in Ettori et al. (2013). The gas density profile has been recovered from the geometrical deprojection of the X-ray surface brightness profile extracted from the exposure-corrected image in the 0.7–2 keV energy range (see Fig. 4). This energy range has been chosen to maximize the signal-to-noise ratio. All the point sources detected with the CIAO routine wavdetect have been masked. A background defined locally in the same exposure by selecting three circular regions of 2' radius, and between 6' and 8' from the peak of the cluster's emission, has been used to correct both the surface brightness profile and the spectra extracted in four independent spatial bins, by requiring  $\sim 3000$  net counts in the 0.6–7 keV band in each bin. The spectral fitting has been performed with Xspec 12.9 (Arnaud 1996), using a thermal component (apec) with 3 degrees of freedom (normalization, temperature and metallicity), absorbed by a Galactic column density  $n_H$  fixed to the local value of  $4.35 \times 10^{20} \text{ cm}^{-2}$  (Kalberla et al. 2005), and at the nominal redshift of 0.439. A NFW functional form for the gravitational potential is adopted with two free parameters (normalization and  $R_{200}$ ). These parameters are constrained by performing a grid-based search for a minimum in the distribution of the  $\chi^2$  evaluated by comparing the observed spectral temperature profile (also considering the relative errors) and the one predicted from the inversion of the hydrostatic equilibrium equation in which the observed gas density profile is used (for further details see Ettori et al. 2010). At each radius, we associate a symmetric error on the mass profile that represents the range of values allowed from the  $1\sigma$  statistical uncertainties on the two free parameters (i.e., as defined from the region enclosed within  $\Delta\chi^2 = 2.3$ ). The projected cumulative X-ray mass profile is shown in Fig. 7 and found to be in general good agreement with other determinations. It is important to note that this comparison should be limited to the radial range in which the ICM properties are properly constrained. In the present case, the profile of the hydrostatic mass density profile can be extended down to  $4'' = 23 \text{ kpc}$  radius, where the temperature can be determined. Moreover, a clear tension between *Chandra* ACIS and *XMM-Newton* EPIC spectral measurements is observed in MACS 1206 at  $r > 500 \text{ kpc}$ , as shown in Donahue et al. (2014; see their Fig. 3). This systematic difference is partially due to residual mismatches in the cross-calibration of the two instruments (see Schellenberger et al. 2015) and has been observed to be particularly significant ( $\sim 20\%$  and above) in high-temperature ( $T > 10 \text{ keV}$ ) systems such as MACS 1206. As a result of these significant uncertainties in the X-ray spectral analysis, we conclude that the hydrostatic mass in MACS 1206 is presently well constrained only over the radial range between  $\sim 20 \text{ kpc}$  and  $500 \text{ kpc}$ , with the relatively shallow archival *Chandra* data.

#### 5. Conclusions

In this work, we have presented a new strong lensing analysis of the galaxy cluster MACS 1206, based on the identification of 23 new spectroscopically confirmed multiply lensed sources, using deep MUSE archival observations in combination with CLASH imaging. With the new measurements, we have

confirmed seven multiple image families which were previously identified with photometric information alone, and four with previously CLASH-VLT (VIMOS) redshift measurements. In total, we therefore used 27 spectroscopic families at  $z = 1.0\text{--}6.1$ , lensed into 82 multiple images as constraints for our strong lensing model. As in previous studies exploiting MUSE and HST observations, these sources are largely low-luminosity Lyman- $\alpha$  emitters at  $z > 3$ , including extended Lyman- $\alpha$  halos. Remarkably, this study has revealed an exceptional number of central multiple images, which, within the inner 20 kpc, is approximately a factor of 4 larger than in any other known cluster to date. As a result, this spectroscopic data set has allowed us to obtain a very robust estimate of the inner slope of the projected total mass density profile and a detailed reconstruction of the inner projected mass distribution, which has been shown to be challenging when using photometrically selected multiple images (Limousin et al. 2016). We summarize our results as follows:

- We model the total mass distribution with a clumpy component associated with the galaxy member halos, which are reliably identified with MUSE spectroscopy, and a smooth component tracing the cluster contribution at larger radial scales. We find that the model that best fits this large number of multiple images requires significant asymmetry, departing from the elliptical parametrization usually adopted for the diffuse component of a cluster mass distribution. To reproduce this more complex mass distribution, we add extra components in the parametrization of the total mass distribution, significantly improving the overall fit when compared to a model with a single diffuse elliptical halo. With this optimized model, we are able to reproduce the observed image positions with a  $\Delta_{\text{rms}}$  of 0".44, in keeping with previous high precision lens models based on CLASH/HFF data supplemented with MUSE spectroscopy. The resulting projected mass distribution closely follows the asymmetric distribution of the galaxy members and the ICL, as well as the intra-cluster gas (see Fig. 4).
- We believe that this exceptional number of central multiple images is due to such an asymmetric inner mass distribution, as corroborated by numerical simulations of forming massive clusters. The direct inspection of the radial caustics in MACS 1206 reveals indeed that they are unusually wide, thus favoring the formation of a large number of radial images. Based on their radial and tangential magnifications from our reference model, we find that  $\sim 30\%$  of the 82 multiple images are classified as “radial arcs”.
- The large number of constraints in the inner 50 kpc leads to a determination of the projected total mass density profile that is very robust against different parametrizations of the diffuse mass component. We find that systematic errors due to the adopted parametrization are comparable with the statistical errors (a few percent at  $R \gtrsim 50$  kpc), while the accuracy in the mass determination remains within 10% (at 95% confidence level) down to  $R = 10$  kpc. We fit the azimuthally averaged projected total density profile with a gNFW model and find a central slope of  $\gamma_{\text{gNFW}}^{\text{total}} = 0.91 \pm 0.04$ , close to the canonical NFW.
- Using the same reference model parametrization, we test the robustness of the inner slope determination by keeping only one central image within  $R < 70$  kpc, which is the typical case in other clusters. Interestingly, we find that in this case the best fit inner profile is no longer stable against different parametrizations and might lead to significant biases on the

innermost slope measurements, especially in lenses with irregular mass distribution in the core.

The determination of the total mass distribution with unprecedented accuracy in the inner core of MACS 1206 opens the opportunity to accurately measure the dark matter profile by separating the baryonic contribution (see, e.g., Bonamigo et al. 2017). We will address this central issue in a forthcoming paper, taking advantage of the internal kinematics of the BCG, which provides a strong independent constraint on the gravitational potential in the innermost regions. We also plan to investigate the conditions of the formation of radial arcs with the state-of-the-art  $N$ -body and hydrodynamical simulations of clusters. Moreover, the increased number of strong lensing constraints presented in this work makes MACS 1206 an interesting study case for strong lensing cosmography (Jullo et al. 2010; Caminha et al. 2016a; Acebron et al. 2017). The strong lensing maps (lens convergence, shear, and magnification), as well as the configuration files of the `lenstool` software, are publicly available<sup>1</sup>.

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<sup>1</sup> All the files can be found at the link: <http://www.fe.infn.it/ugbcaminha/>

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## Appendix A: Multiple images

In Table A.1, we present relevant information about the multiple images used in our strong lensing model. In Fig. A.1, we show the MUSE spectra around relevant spectral features used to determine the redshift of multiple images and the corresponding

image cutouts for multiple images. The median values and the 68%, 95%, and 99.7% confidence levels of the free parameters of the model P3 $\epsilon$ , as determined from the MCMC analyses, are shown in Table A.2.

**Table A.1.** Information on spectroscopically identified multiple images in MACS 1206.

ID	RA	Dec	$z_{\text{MUSE}}$	$z_{\text{previous}}^a$	$\mu_{\text{tot}}$	$\mu_{\text{tan}}/\mu_{\text{rad}}$	Comments
1a	181.550916	-8.797422	1.0121	—	$10.2^{+0.6}_{-0.7}$	$1.48^{+0.05}_{-0.06}$	HST/F606W
1b	181.549604	-8.799294	1.0121	—	$6.5^{+0.7}_{-0.6}$	$0.67^{+0.06}_{-0.05}$	HST/F606W
1c	181.548870	-8.806655	1.0121	—	$3.4^{+0.1}_{-0.1}$	$1.27^{+0.02}_{-0.02}$	HST/F606W
2a	181.546790	-8.795680	1.0369	1.0348	$6.9^{+0.2}_{-0.2}$	$3.19^{+0.10}_{-0.10}$	HST/F105W
2b	181.544819	-8.799553	1.0369	1.0336	$3.0^{+0.3}_{-0.2}$	$2.16^{+0.15}_{-0.12}$	HST/F105W
2c	181.545102	-8.803052	1.0369	1.0336	$6.9^{+0.2}_{-0.2}$	$2.18^{+0.13}_{-0.12}$	HST/F105W
3a	181.550570	-8.795568	1.0433	—	$5.2^{+0.2}_{-0.2}$	$1.56^{+0.03}_{-0.03}$	HST/F606W
3b	181.547611	-8.799811	1.0433	—	$5.1^{+0.3}_{-0.3}$	$0.77^{+0.06}_{-0.05}$	HST/F606W
3c	181.548607	-8.805281	1.0433	—	$6.1^{+0.3}_{-0.3}$	$2.42^{+0.16}_{-0.15}$	HST/F606W
4a	181.552987	-8.794699	1.4248	—	$6.9^{+0.7}_{-0.6}$	$2.31^{+0.32}_{-0.27}$	MUSE
4b	181.548830	-8.800057	1.4248	—	$7.4^{+1.5}_{-1.2}$	$0.09^{+0.02}_{-0.02}$	MUSE
4c	181.549752	-8.807965	1.4248	—	$3.9^{+0.2}_{-0.1}$	$1.46^{+0.04}_{-0.03}$	MUSE
(4c)	181.554126	-8.801587	—	—	$2.2^{+0.2}_{-0.2}$	$0.48^{+0.04}_{-0.03}$	blended with gal.
5a	181.553557	-8.795189	1.4254	—	$5.8^{+0.4}_{-0.4}$	$1.46^{+0.13}_{-0.12}$	HST/F110W
5b	181.554237	-8.801552	1.4254	—	$2.0^{+0.1}_{-0.1}$	$0.74^{+0.03}_{-0.04}$	HST/F110W
5c	181.550005	-8.808098	1.4254	—	$3.8^{+0.1}_{-0.1}$	$1.45^{+0.04}_{-0.04}$	HST/F110W
6a	181.549979	-8.796362	1.4255	—	$18.3^{+2.1}_{-1.6}$	$2.60^{+0.13}_{-0.13}$	HST/F606W
6b	181.548139	-8.797058	1.4255	$2.1743^b$	$27.5^{+2.6}_{-2.4}$	$3.76^{+0.37}_{-0.39}$	HST/F606W
6c	181.548050	-8.809283	1.4255	—	$3.2^{+0.1}_{-0.1}$	$1.55^{+0.03}_{-0.02}$	HST/F606W
7a	181.550563	-8.795704	1.4257	—	$9.8^{+0.7}_{-0.7}$	$2.04^{+0.07}_{-0.06}$	HST/F606W
7b	181.547193	-8.797998	1.4257	—	$6.2^{+0.4}_{-0.3}$	$1.19^{+0.05}_{-0.05}$	HST/F606W
7c	181.551339	-8.800328	1.4257	—	$3.9^{+0.6}_{-0.5}$	$0.29^{+0.03}_{-0.03}$	HST/F606W
7d	181.552213	-8.800398	1.4257	—	$5.3^{+0.6}_{-0.5}$	$0.22^{+0.02}_{-0.02}$	HST/F606W
7e	181.548307	-8.808856	1.4257	—	$3.4^{+0.1}_{-0.1}$	$1.57^{+0.03}_{-0.03}$	HST/F606W
8a	181.553657	-8.795756	1.4864	—	$6.0^{+0.3}_{-0.4}$	$1.56^{+0.07}_{-0.06}$	HST/F110W
8b	181.554524	-8.801104	1.4864	—	$3.1^{+0.2}_{-0.1}$	$0.87^{+0.04}_{-0.05}$	HST/F110W
8c	181.549957	-8.808887	1.4864	—	$3.5^{+0.1}_{-0.1}$	$1.49^{+0.05}_{-0.04}$	HST/F110W
9a	181.546741	-8.793144	1.9600	—	$6.8^{+0.3}_{-0.3}$	$3.42^{+0.14}_{-0.11}$	HST/F606W
9b	181.543273	-8.797812	1.9600	—	$6.4^{+0.4}_{-0.4}$	$3.71^{+0.29}_{-0.24}$	HST/F606W
9c	181.544378	-8.807486	1.9600	—	$5.1^{+0.4}_{-0.3}$	$2.71^{+0.10}_{-0.07}$	HST/F606W
10a	181.552450	-8.795001	2.5393	2.5398	$9.4^{+0.7}_{-0.7}$	$1.41^{+0.06}_{-0.05}$	HST/F606W
10b	181.546604	-8.797465	2.5393	—	$5.9^{+0.2}_{-0.3}$	$0.92^{+0.04}_{-0.04}$	HST/F606W
10c	181.550487	-8.799957	—	—	$1.7^{+0.2}_{-0.2}$	$0.39^{+0.02}_{-0.02}$	HST/F606W
10d	181.554894	-8.800160	—	—	$4.9^{+0.3}_{-0.3}$	$0.92^{+0.06}_{-0.06}$	HST/F606W
10e	181.548827	-8.811813	—	—	$3.0^{+0.1}_{-0.1}$	$1.61^{+0.05}_{-0.04}$	HST/F606W
11a	181.562654	-8.796672	3.0358	3.0363	$4.6^{+0.2}_{-0.2}$	$3.13^{+0.12}_{-0.08}$	HST/F606W
11b	181.562495	-8.804911	3.0358	3.0371	$4.3^{+0.4}_{-0.3}$	$4.10^{+0.24}_{-0.23}$	HST/F606W
11c	181.560573	-8.808988	3.0358	3.0372	$7.5^{+0.5}_{-0.4}$	$5.26^{+0.37}_{-0.35}$	HST/F606W

**Notes.** The magnification values, and their 68% confidence level errors, are computed using the reference model P3 $\epsilon$ . IDs in brackets are model predicted multiple images with no identification in the MUSE and HST data, therefore not used in the modeling. <sup>(\*)</sup> Multiple images nearby background galaxies that are not used in the strong lensing models. <sup>(a)</sup> Spectroscopic redshifts from CLASH-VLT with VIMOS (Zitrin et al. 2012). <sup>(b)</sup> The redshift of the multiple image 6b is reported with quality flag 2, i.e. reliability of 80%, in the public catalogue by Biviano et al. (2013).

Table A.1. continued.

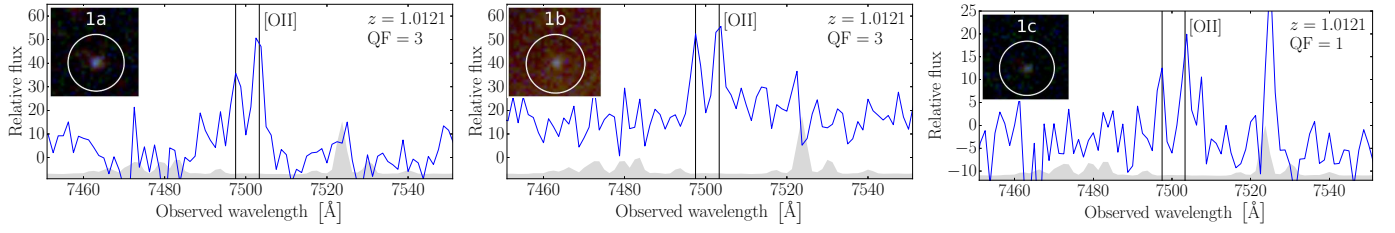
ID	RA	Dec	$z_{\text{MUSE}}$	$z_{\text{previous}}^a$	$\mu_{\text{tot}}$	$\mu_{\text{tan}}/\mu_{\text{rad}}$	Comments
12a	181.548632	-8.793717	3.3890	—	$15.5^{+1.1}_{-1.2}$	$4.32^{+0.32}_{-0.28}$	MUSE
12b	181.546121	-8.795387	3.3890	—	$7.2^{+0.5}_{-0.5}$	$3.13^{+0.22}_{-0.20}$	MUSE
12c	181.553268	-8.800197	3.3890	—	$4.2^{+0.3}_{-0.3}$	$0.28^{+0.03}_{-0.02}$	MUSE
(12d)	181.551478	-8.800081	—	—	$1.5^{+0.1}_{-0.1}$	$0.58^{+0.05}_{-0.04}$	blended with gal., low $\mu$
(12e)	181.547097	-8.812472	—	—	$3.1^{+0.1}_{-0.1}$	$1.72^{+0.04}_{-0.04}$	outside MUSE FoV
13a	181.549416	-8.801768	3.3961	—	$5.9^{+1.7}_{-1.0}$	$0.18^{+0.04}_{-0.03}$	MUSE
13b	181.547859	-8.802115	3.3961	—	$14.4^{+2.1}_{-2.0}$	$0.24^{+0.04}_{-0.03}$	MUSE
13c	181.553770	-8.804759	3.3961	—	$6.8^{+0.7}_{-0.6}$	$1.26^{+0.08}_{-0.07}$	MUSE
13d	181.551389	-8.806864	3.3961	—	$12.0^{+1.1}_{-1.0}$	$2.05^{+0.14}_{-0.13}$	MUSE
(13e)	181.554500	-8.788383	—	—	$2.9^{+0.1}_{-0.1}$	$1.67^{+0.03}_{-0.03}$	outside MUSE FoV
14a	181.566558	-8.804480	3.7531	—	$6.2^{+0.6}_{-0.6}$	$3.93^{+0.34}_{-0.30}$	HST/F625W
14b	181.566475	-8.804733	3.7531	—	$3.2^{+0.5}_{-0.4}$	$4.10^{+0.34}_{-0.31}$	HST/F625W
14c	181.566475	-8.805147	3.7531	—	$7.5^{+0.8}_{-0.7}$	$5.44^{+0.42}_{-0.40}$	HST/F625W
14d	181.566275	-8.806328	3.7531	—	$6.5^{+1.0}_{-0.8}$	$8.36^{+0.99}_{-0.87}$	HST/F625W
14e	181.565591	-8.807690	3.7531	—	$7.2^{+0.6}_{-0.4}$	$6.21^{+0.25}_{-0.23}$	HST/F625W
15a	181.555962	-8.791635	3.7611	—	$4.2^{+0.1}_{-0.1}$	$2.44^{+0.10}_{-0.10}$	HST/F606W
15b	181.557600	-8.803056	3.7611	—	$4.5^{+0.6}_{-0.4}$	$0.67^{+0.13}_{-0.10}$	HST/F606W
15c	181.551748	-8.810964	—	—	$3.8^{+0.1}_{-0.1}$	$1.70^{+0.06}_{-0.07}$	HST/F606W
16a	181.554584	-8.791202	3.7617	—	$4.1^{+0.1}_{-0.1}$	$1.99^{+0.06}_{-0.05}$	MUSE
16b	181.546465	-8.799671	3.7617	—	$2.1^{+0.1}_{-0.1}$	$0.35^{+0.02}_{-0.02}$	MUSE
16c	181.556520	-8.802471	3.7617	—	$2.7^{+0.2}_{-0.1}$	$0.61^{+0.07}_{-0.05}$	MUSE
(16d)	181.550432	-8.811056	—	—	$3.7^{+0.1}_{-0.1}$	$1.60^{+0.05}_{-0.05}$	MUSE edge
17a	181.556136	-8.795620	3.8224	—	$8.3^{+0.7}_{-0.6}$	$2.22^{+0.18}_{-0.14}$	MUSE
17b	181.556958	-8.799422	3.8224	—	$8.7^{+0.9}_{-0.9}$	$2.44^{+0.16}_{-0.19}$	MUSE
(17c)	181.547557	-8.798385	—	—	$3.0^{+0.3}_{-0.3}$	$0.30^{+0.03}_{-0.03}$	low $\mu$
(17d)	181.550041	-8.813393	—	—	$2.8^{+0.1}_{-0.1}$	$1.49^{+0.05}_{-0.04}$	outside MUSE FoV
18a	181.555376	-8.796714	4.0400	—	$17.0^{+2.5}_{-2.0}$	$3.02^{+0.39}_{-0.29}$	HST/F814W
18b	181.555927	-8.798595	4.0400	—	$3.8^{+0.4}_{-0.4}$	$1.56^{+0.11}_{-0.09}$	HST/F814W
(18c)	181.549137	-8.798385	—	—	$2.8^{+0.1}_{-0.1}$	$1.54^{+0.04}_{-0.04}$	blended with gal., low $\mu$
19a	181.562084	-8.794875	4.0520	—	$3.9^{+0.1}_{-0.1}$	$2.58^{+0.06}_{-0.06}$	HST/F814W
19b	181.561873	-8.805239	4.0520	—	$8.1^{+0.7}_{-0.6}$	$5.27^{+0.57}_{-0.61}$	HST/F814W
19c	181.559788	-8.809463	4.0520	—	$7.3^{+0.5}_{-0.4}$	$4.82^{+0.36}_{-0.31}$	HST/F814W
20a	181.547472	-8.800476	4.0553	—	$9.0^{+2.7}_{-1.8}$	$0.08^{+0.02}_{-0.02}$	MUSE
20b	181.556839	-8.803813	4.0553	—	$3.9^{+0.3}_{-0.2}$	$0.65^{+0.10}_{-0.09}$	MUSE
(20c)	181.555448	-8.790286	—	—	$3.5^{+0.1}_{-0.1}$	$1.54^{+0.04}_{-0.04}$	MUSE edge
(20d)	181.551634	-8.810099	—	—	$4.5^{+0.2}_{-0.2}$	$1.96^{+0.05}_{-0.05}$	MUSE edge
21a	181.543431	-8.797674	4.0718	—	$3.6^{+0.2}_{-0.1}$	$1.88^{+0.10}_{-0.10}$	MUSE
21b	181.551462	-8.800814	4.0718	—	$2.0^{+0.8}_{-0.4}$	$0.10^{+0.04}_{-0.03}$	MUSE
21c	181.552850	-8.801115	4.0718	—	$1.6^{+0.2}_{-0.2}$	$0.28^{+0.02}_{-0.02}$	MUSE
21d	181.553430	-8.801204	4.0718	—	$2.2^{+0.2}_{-0.2}$	$0.23^{+0.02}_{-0.01}$	MUSE
(21e)	181.550064	-8.791270	—	—	$5.8^{+0.3}_{-0.3}$	$2.60^{+0.09}_{-0.07}$	outside MUSE FoV
22a	181.544328	-8.791418	4.2913	—	$6.6^{+0.4}_{-0.3}$	$4.74^{+0.23}_{-0.21}$	HST/F105W
22b*	181.540282	-8.796562	4.2913	—	—	—	close to bkg. galaxy
22c	181.540884	-8.806094	4.2913	—	$7.0^{+0.5}_{-0.4}$	$4.67^{+0.24}_{-0.20}$	HST/F105W
23a	181.563252	-8.796893	4.7293	—	$5.8^{+0.3}_{-0.3}$	$4.08^{+0.24}_{-0.15}$	MUSE
23b	181.563537	-8.803670	4.7293	—	$6.3^{+0.5}_{-0.4}$	$5.22^{+0.61}_{-0.52}$	MUSE
23c*	181.559832	-8.811526	4.7293	—	—	—	close to bkg. galaxy
24a	181.551378	-8.791300	5.6984	—	$6.4^{+0.4}_{-0.3}$	$2.67^{+0.10}_{-0.09}$	HST/F105W
24b	181.544085	-8.797094	5.6984	—	$3.7^{+0.2}_{-0.2}$	$1.63^{+0.09}_{-0.09}$	HST/F105W
24c	181.550911	-8.800607	5.6984	—	$0.39^{+0.03}_{-0.04}$	$0.53^{+0.04}_{-0.07}$	MUSE
24d	181.555210	-8.801066	5.6984	—	$4.4^{+0.4}_{-0.3}$	$0.34^{+0.02}_{-0.03}$	HST/F105W
24e*	181.546977	-8.812247	—	5.7030	—	—	close to bkg. galaxy
25a	181.559714	-8.796562	5.7927	—	$8.8^{+0.5}_{-0.5}$	$4.35^{+0.19}_{-0.16}$	MUSE
25b	181.560102	-8.800177	5.7927	—	$9.0^{+0.7}_{-0.7}$	$3.74^{+0.34}_{-0.31}$	MUSE
(25c)	181.553429	-8.813652	—	—	$3.2^{+0.1}_{-0.1}$	$1.90^{+0.09}_{-0.08}$	outside MUSE FoV
26a	181.550711	-8.803112	6.0106	—	$25.2^{+9.9}_{-5.2}$	$0.23^{+0.04}_{-0.04}$	MUSE
26b	181.551211	-8.803668	6.0106	—	$46.9^{+11}_{-7.6}$	$0.22^{+0.07}_{-0.05}$	MUSE
(26c)	181.553742	-8.786102	—	—	$2.6^{+0.1}_{-0.1}$	$1.54^{+0.03}_{-0.03}$	outside MUSE FoV
27a	181.553251	-8.798825	6.0601	—	$13.8^{+1.7}_{-1.3}$	$0.43^{+0.05}_{-0.05}$	MUSE
27b	181.551691	-8.799167	6.0601	—	$4.8^{+0.8}_{-0.6}$	$0.71^{+0.06}_{-0.06}$	MUSE
(27c)	181.546863	-8.814885	—	—	$2.6^{+0.1}_{-0.1}$	$1.43^{+0.03}_{-0.04}$	outside MUSE FoV

**Table A.2.** Median parameter values and confidence levels for the reference lens model.

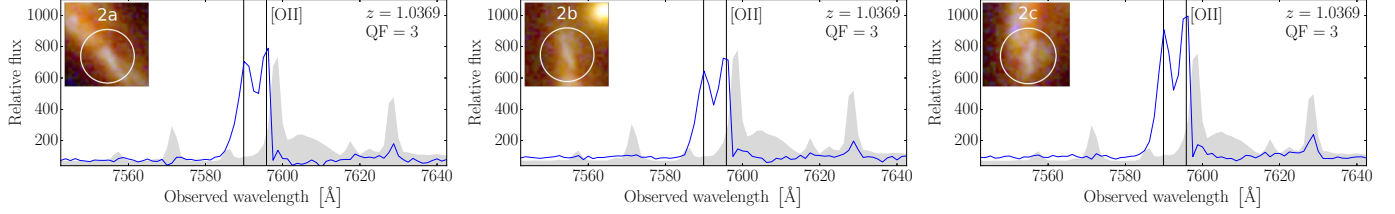
	Median	68% CL	95% CL	99.7% CL
Main diffuse mass component				
$x_1$ (")	-0.5	+0.5 -0.6	+1.0 -1.2	+1.4 -1.8
$y_1$ (")	0.4	+0.3 -0.3	+0.5 -0.6	+0.8 -1.0
$\varepsilon_1$	0.68	+0.04 -0.04	+0.09 -0.08	+0.14 -0.12
$\theta_1$ (deg)	19.1	+1.2 -1.1	+2.6 -2.3	+4.8 -3.5
$r_{\text{core},1}$ (")	6.0	+0.7 -0.8	+1.3 -1.7	+1.9 -2.5
$\sigma_{v1}$ (km s <sup>-1</sup> )	951	+63 -79	+115. -161	+159 -243
Second diffuse mass component				
$x_2$ (")	8.6	+1.2 -1.1	+2.8 -2.2	+5.1 -3.0
$y_2$ (")	4.4	+1.0 -0.9	+2.3 -1.9	+3.7 -3.1
$\varepsilon_2$	0.44	+0.14 -0.15	+0.27 -0.28	+0.37 -0.37
$\theta_2$ (deg)	113.5	+5.0 -4.0	+12.4 -7.3	+23.0 -10.4
$r_{\text{core},2}$ (")	15.7	+2.4 -1.8	+5.9 -3.0	+10.0 -4.0
$\sigma_{v2}$ (km s <sup>-1</sup> )	863	+59 -55	+121 -110	+183 -168
Third diffuse mass component				
$x_3$ (")	-26.3	+1.6 -1.6	+3.6 -3.4	+6.0 -6.2
$y_3$ (")	-8.0	+0.9 -0.9	+1.9 -1.8	+3.1 -2.7
$\varepsilon_3$	0.27	+0.09 -0.09	+0.18 -0.18	+0.31 -0.25
$\theta_3$ (deg)	-18.9	+14.0 -19.4	+23.0 -37.0	+30.2 -51.5
$r_{\text{core},3}$ (")	12.1	+2.9 -2.4	+6.4 -4.4	+10.6 -6.1
$\sigma_{v3}$ (km s <sup>-1</sup> )	667	+65 -55	+144 -101	+229 -140
External shear				
$\gamma_{\text{ext}}$	0.12	+0.02 -0.02	+0.03 -0.03	+0.05 -0.05
$\theta_{\text{ext}}$ (deg)	101.5	+2.3 -2.1	+4.9 -4.1	+8.0 -6.1
Galaxy members				
$r_{\text{cut}}^{\text{gals}}$ (")	3.3	+1.3 -0.9	+3.3 -1.7	+7.1 -2.1
$\sigma_v^{\text{gals}}$ (km s <sup>-1</sup> )	342	+39 -36	+86 -68	+141 -97

**Notes.** Angles are measured from west to north. The values of all velocity dispersions ( $\sigma_v$ ) are corrected by the factor  $\sqrt{2/3}$  as described in the lenstool manual (see <http://projets.lam.fr/projects/lenstool/wiki/PIEMD>).

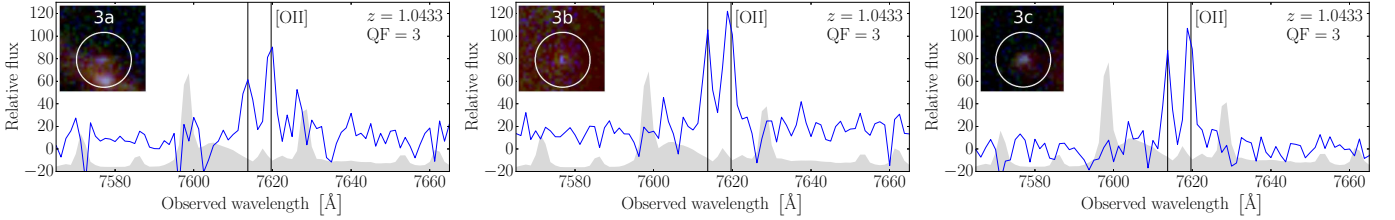
### Family 1:



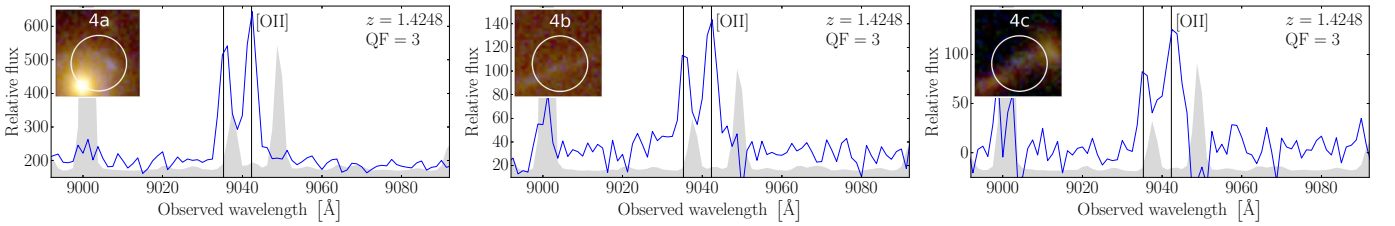
### Family 2:



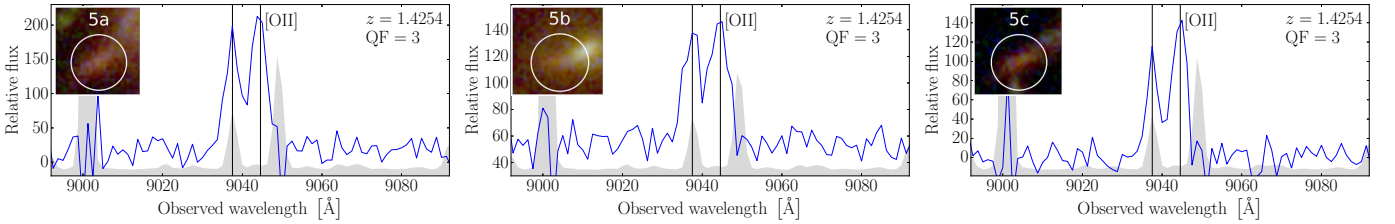
### Family 3:



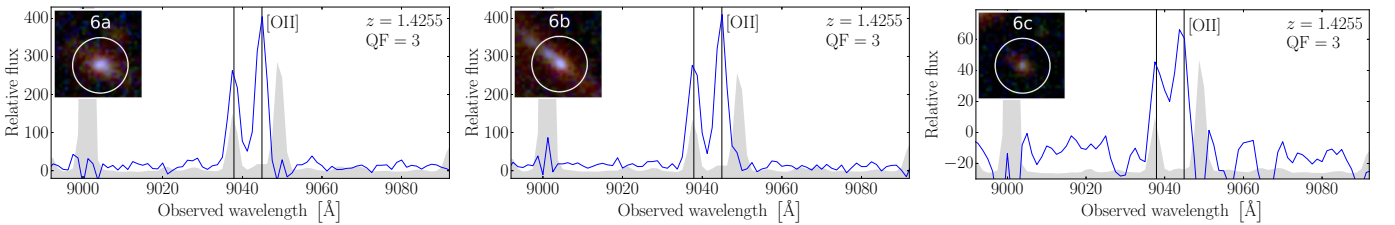
### Family 4:



### Family 5:

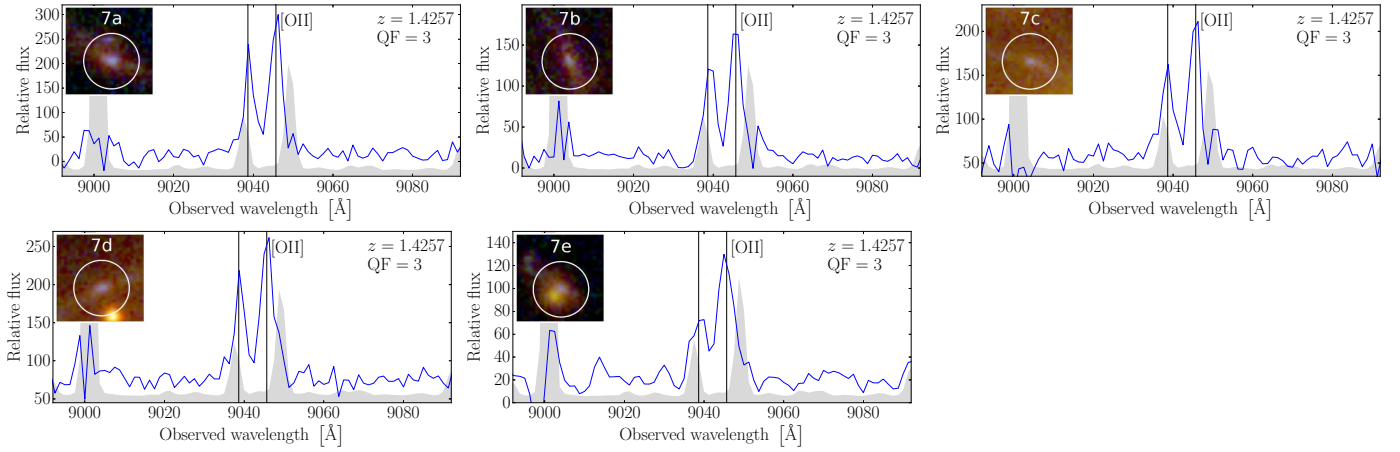


### Family 6:

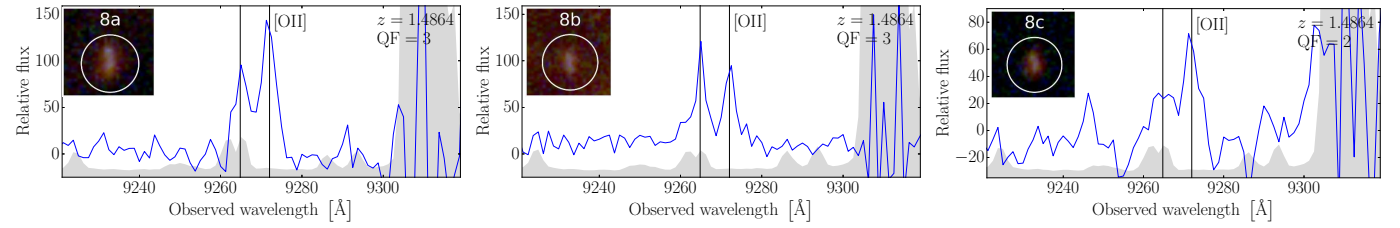


**Fig. A.1.** MUSE data of multiply lensed background sources of MACS 1206. The vertical black lines indicate the positions of the emission lines based on the best estimate of the systemic redshift. The gray area shows the rescaled variance obtained from the data reduction pipeline; the flux is given in units of  $10^{-20} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ Å}^{-1}$ . The image cutouts in each panel have  $2''$  across and are extracted from the CLASH color image. The white circles show the HST counterparts or are centered at the position of the MUSE emission in the cases of no apparent counterparts.

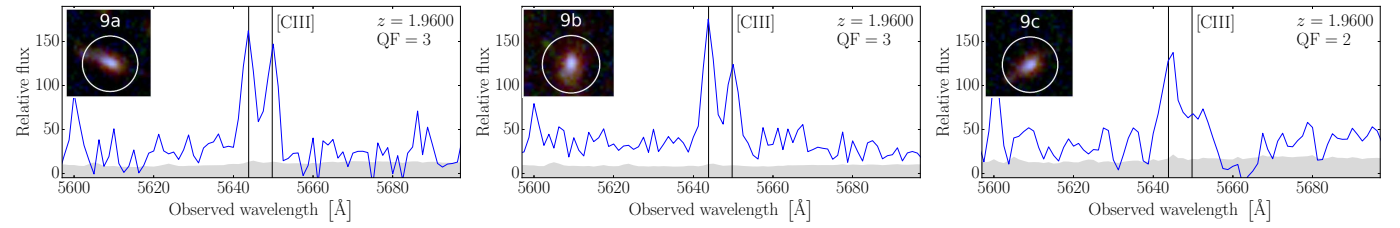
## Family 7:



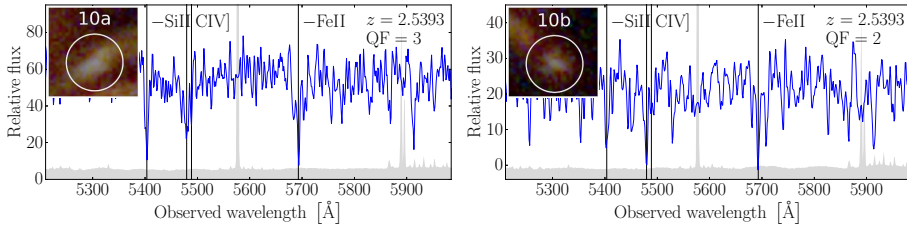
## Family 8:



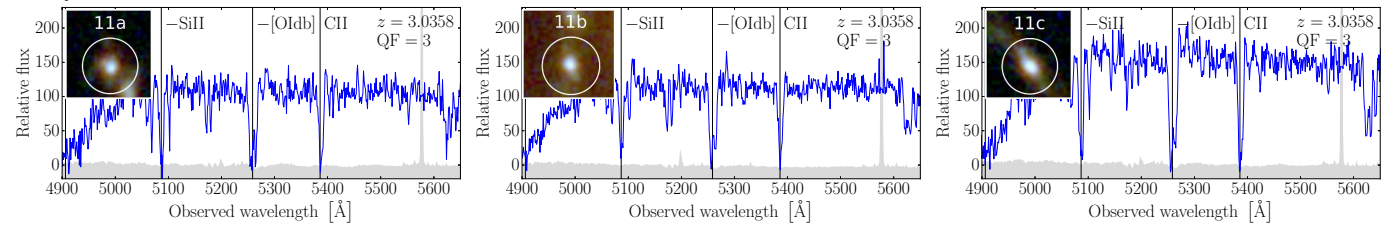
## Family 9:



## Family 10:



## Family 11:



## Family 12:

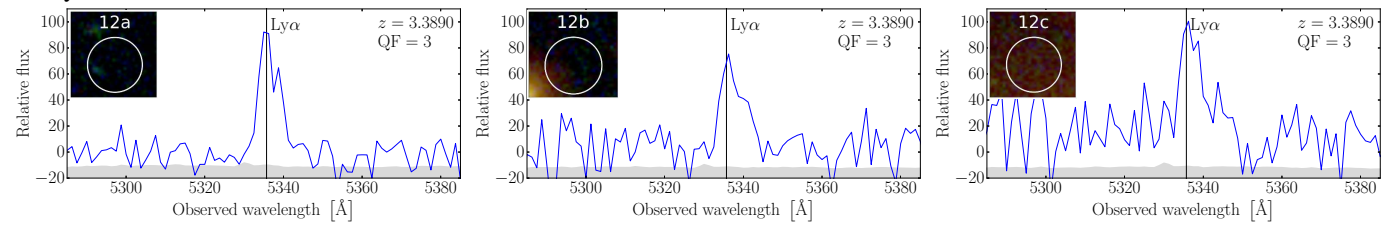
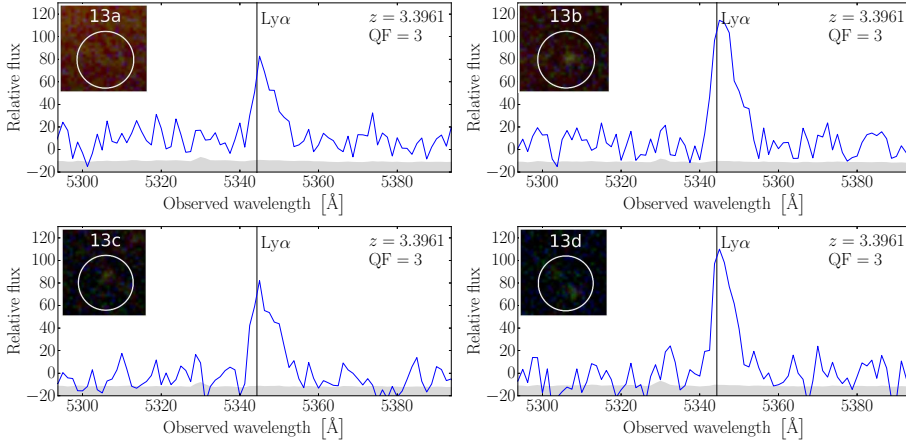
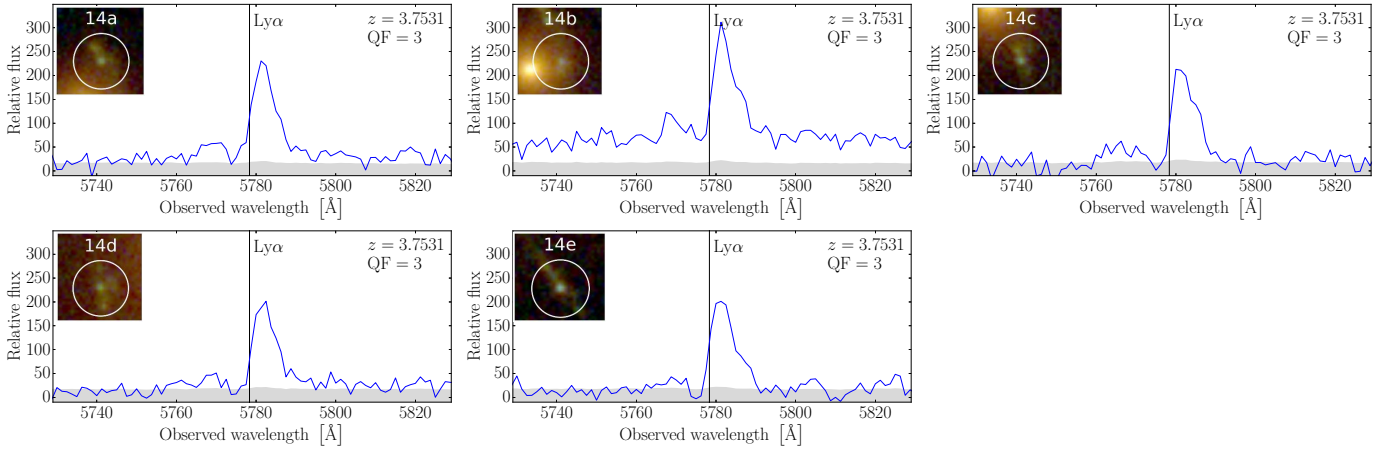


Fig. A.1. continued.

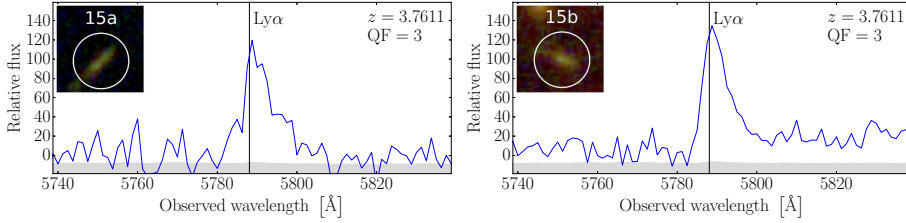
**Family 13:**



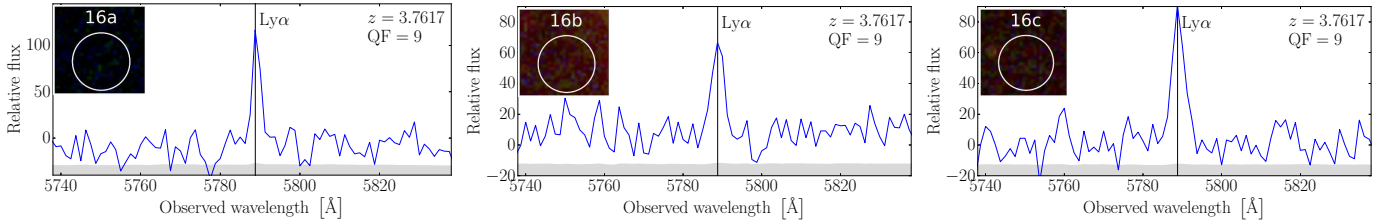
**Family 14:**



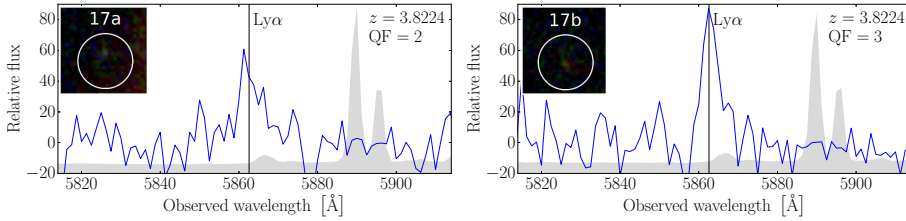
**Family 15:**



**Family 16:**

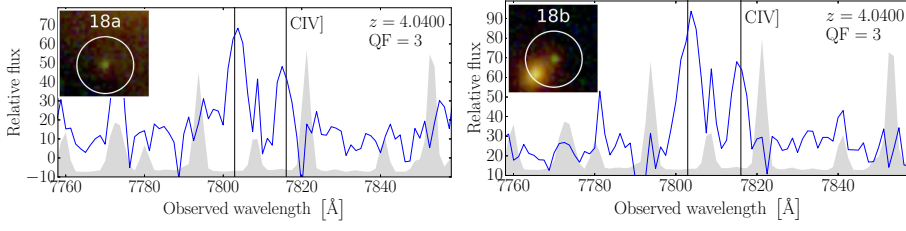


**Family 17:**

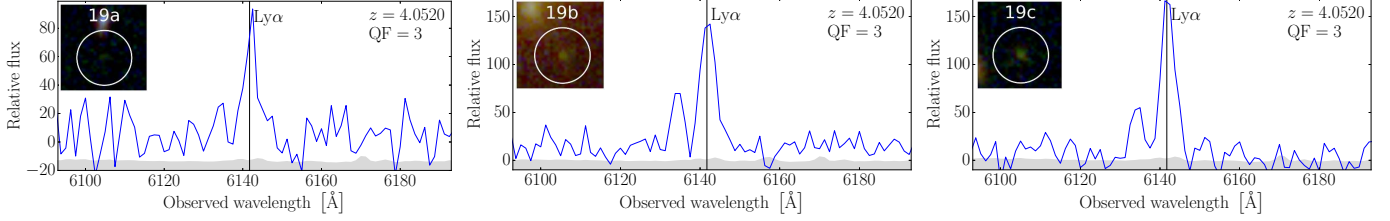


**Fig. A.1.** continued.

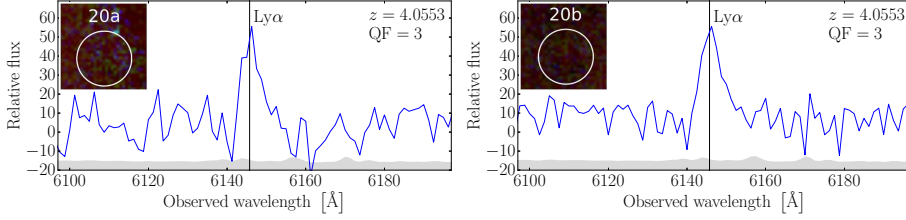
## Family 18:



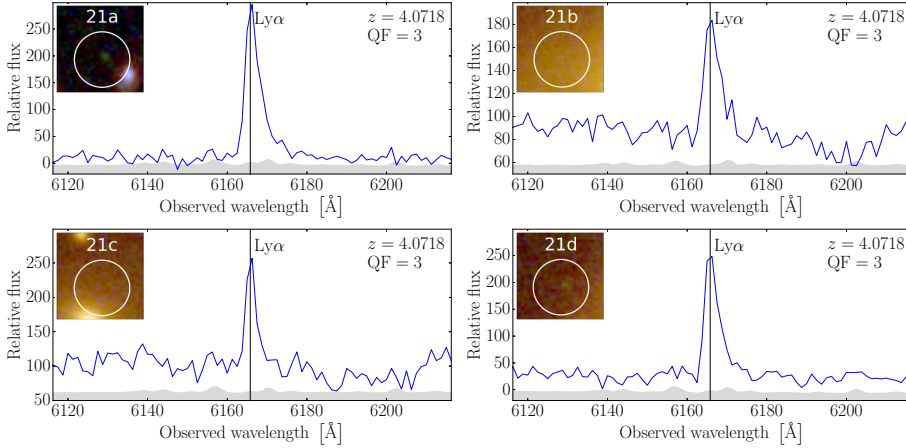
## Family 19:



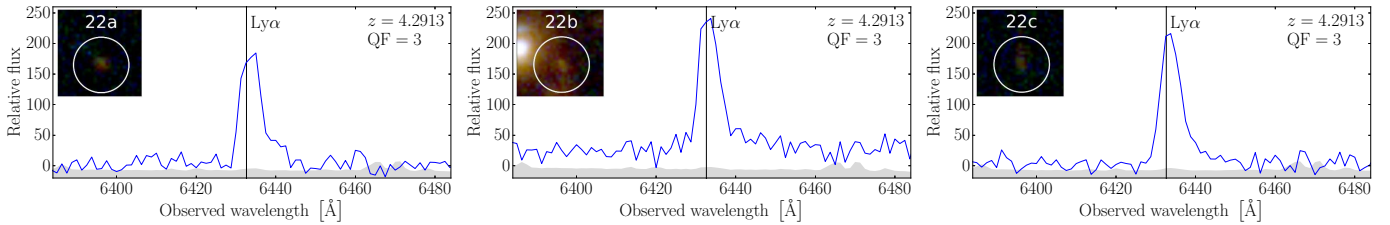
## Family 20:



## Family 21:



## Family 22:



## Family 23:

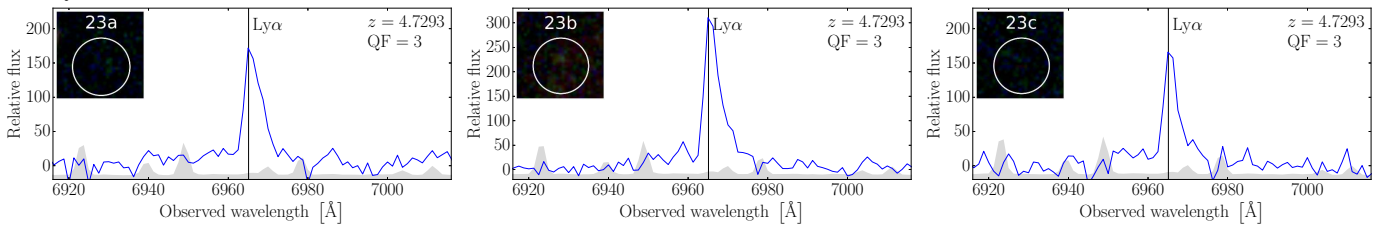
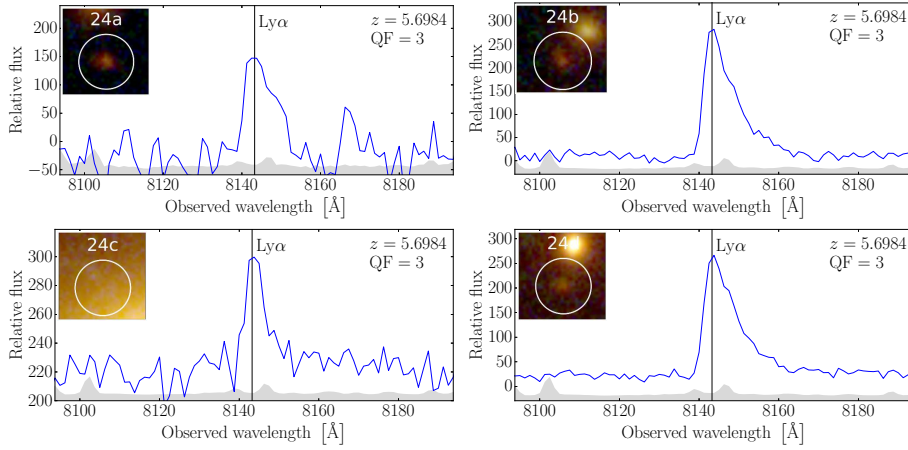
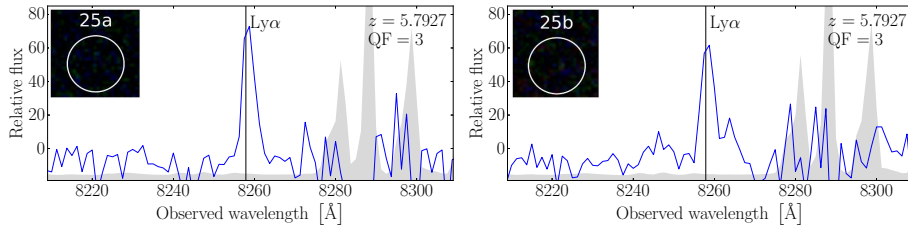


Fig. A.1. continued.

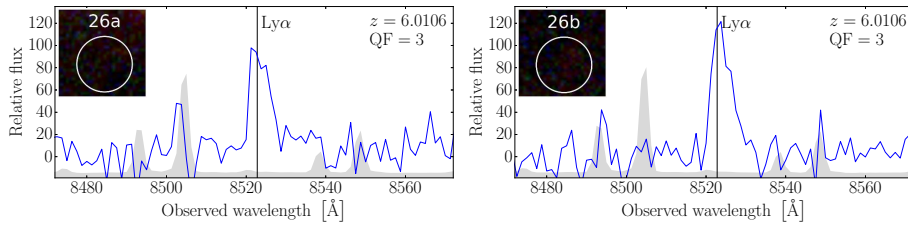
**Family 24:**



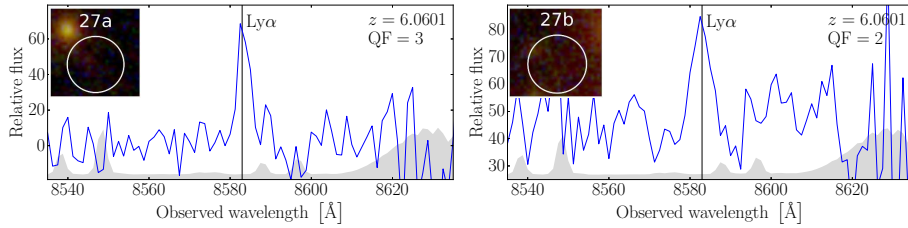
**Family 25:**



**Family 26:**



**Family 27:**



**Fig. A.1.** continued.