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## Evidence against Anomalous Compositions for Giants in the Galactic Nuclear Star Cluster

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### Abstract

Very strong Sc I lines have recently been found in cool M giants in the Nuclear Star Cluster (NSC) in the Galactic center. Interpreting these as anomalously high scandium abundances in the Galactic center would imply a unique enhancement signature and chemical evolution history for NSCs, and a potential test for models of chemical enrichment in these objects. We present high resolution K-band spectra (NIRSPEC/Keck II) of cool M giants situated in the solar neighborhood and compare them with spectra of M giants in the NSC. We clearly identify strong Sc I lines in our solar neighborhood sample as well as in the NSC sample. The strong Sc I lines in M giants are therefore not unique to stars in the NSC and we argue that the strong lines are a property of the line formation process that currently escapes accurate theoretical modeling. We further conclude that for giant stars with effective temperatures below approximately 3800 K these Sc I lines should not be used for deriving the scandium abundances in any astrophysical environment until we better understand how these lines are formed. We also discuss the lines of vanadium, titanium, and yttrium identified in the spectra, which demonstrate a similar striking increase in strength below 3500 K effective temperature.

*Key words:* Galaxy: center – stars: abundances – stars: late-type

### 1. Introduction

With the advent of high resolution infrared spectroscopy, it has become possible to explore the spectra and composition of stars in the nuclear star cluster (NSC) just a few parsecs from the Galactic center. Several chemical abundance studies have addressed the giants in the Galactic center region and the NSC (see, e.g., Ryde & Schultheis 2015; Rich et al. 2017; Do et al. 2018). Spectroscopy in the Galactic center poses a special challenge, as the high extinction generally at present restricts investigations to the infrared K band. Although there is considerable heritage in the  $1.6\ \mu\text{m}$  H band from, e.g., APOGEE and earlier studies using NIRSPEC/Keck II (e.g., Origlia et al. 2011), one is challenged by the paucity of weak lines suitable for abundance analysis, as well as the presence of molecular bands that cause blends. The cool, luminous, giants of the NSC are easiest to observe, but pose the greatest perils for analysis.

Low resolution studies have advanced a scenario in which the NSC and nuclear disk have abundant metal-rich stars, reaching to  $[\text{Fe}/\text{H}] = +1$  (Do et al. 2015; Feldmeier-Krause et al. 2017). Rich et al. (2017) challenges this picture with new high resolution NIRSPEC spectra in the Galactic center, and finds no stars above  $[\text{Fe}/\text{H}] = +0.6$ . Do et al. (2018) reports high resolution spectra of NSC stars behind AO correction, arguing for extreme enhancements of scandium, vanadium, and yttrium; in some cases, the analysis finds 10 times solar abundance for these elements.

Especially interesting are the strong Sc I lines found in M giants that are discussed in Rich et al. (2017). They suggest non-LTE effects as the cause for them, while Do et al. (2018) argue for extreme overabundance (as much as a factor of 10 compared to iron) of scandium in the NSC. If confirmed, this latter interpretation would be a chemical signature of the

special environment in the Galactic center and potentially very important. There are good reasons to assume that the enrichment and star formation histories might be different in the Galactic center, especially if the NSC has a unique formation history. Large magnetic fields, suppressed star formation, high turbulence, tidal forces, and the deep Galactic center potential well might lead to a very different chemical history for the stellar populations in the Galactic center. Furthermore, one might expect inhomogeneities in the trends with a larger scatter, including outliers due to a possible mixture of populations that in principle might include the disk, inner halo, NSC, nuclear disk, and bulge. A unique scandium abundance trend for the NSC would suggest that the Galactic center and similar environments is a site for a new channel of nucleosynthesis of scandium and possibly other elements. Such a trend might also provide a powerful chemical tag for stars formed in nuclear environments.

Scandium resides between the  $\alpha$ -elements calcium and titanium in the periodic table and is considered an iron-group element. Even titanium is sometimes considered an iron-group element, such as in the discussion of the metal-poor star HD 84937 (Snedden et al. 2016); therefore, scandium can be seen as an intermediate element between the  $\alpha$  elements and the iron-peak group. The precise origin of scandium and its only stable isotope,  $^{45}\text{Sc}$ , seems to be complex and is still a matter of debate. Scandium is produced in the innermost ejected layers of core-collapse SNe (type II) during neon burning and explosive silicon and oxygen burning via the radioactive progenitor  $^{45}\text{Ti}$ , as reviewed by Woosley & Weaver (1995) and Romano et al. (2010), while the contribution from type Ia SNe seems to be negligible (Iwamoto et al. 1999; Clayton 2003). However, the predicted trends of scandium with  $[\text{Fe}/\text{H}]$  disagree even when taking into account metallicity- and mass-dependent yields,

which might be important (Woosley & Weaver 1995; Chieffi & Limongi 2002; Nomoto et al. 2013). Chemical evolution models predict too little scandium production. This could be due to the problems in the stellar yield calculations (see also Romano et al. 2010). It should be noted, however, that although extreme enhancements of individual elements are known in stars of low metallicity, for stars with  $[\text{Fe}/\text{H}] > 0$ , the total metal production is so high that no single supernova event can affect the abundance of a given species, save perhaps for an r-process production event that might result from a neutron star merger. These factors raise the bar significantly for any purported enhancements of metals in stars of high metallicity.

From an observational point of view, scandium seems to behave like a typical  $\alpha$ -element, e.g., enhanced in the thick disk and the Galactic bulge (Battistini & Bensby 2015; Lomaeva 2018). Nissen et al. (2000) and Howes et al. (2016) also find  $[\text{Sc}/\text{Fe}] \approx +0.3$  abundances for halo stars and metal-poor stars toward the bulge; however, their studies have no stars more metal-rich than  $[\text{Fe}/\text{H}] \sim -1.5$ . It is noteworthy that Gratton & Sneden (1991), Prochaska & McWilliam (2000), and Erandes et al. (2018) report a constant  $[\text{Sc}/\text{Fe}] \sim 0$  (and as well for V) for Galactic bulge globular clusters spanning  $-1.5 < [\text{Fe}/\text{H}] < 0.0$ . Smith et al. (2002) report a solar mean scandium abundance for 12 red giants all having subsolar metallicity in the Large Magellanic Cloud (LMC)—an investigation carried out in the K-band.

In the Galactic center, the picture is more complicated. Carr et al. (2000) measured scandium abundance for the cool supergiant star IRS7 located in the Galactic center and found extremely strong Sc I lines as well as V I and Ti I lines. An abundance of  $[\text{Sc}/\text{Fe}] \sim 0.9$  dex is required to fit the strength of the Sc I lines. However, supergiant stars are affected by large velocity fields, depth-dependent turbulence, temperature inhomogeneities, etc., and it is known that fully realistic atmospheres for supergiants remain a challenge.

We have employed high resolution K band spectroscopy to overcome the high and variable extinction toward the NSC (see, e.g., Ryde et al. 2016a; Rich et al. 2017). High resolution, K-band spectroscopy was pioneered in the late 80s by Smith & Lambert (1985, 1986, 1990). With the largest telescopes we can now push further to observe cool M giants, and thus avoid the supergiant stars. However, as we emphasized earlier, even the interpretation of the M giant spectra is challenging. Our aim here is to test whether the strong scandium lines in cool M giants in the NSC are due to either physical effects in the line formation process (Rich et al. 2017) or due to intrinsically high scandium abundances (Do et al. 2018). Toward this aim, we have acquired spectra for a range of solar neighborhood stars, similar to those we have observed in the NSC in Rich et al. (2017), using the same instrument and telescope configuration (NIRSPEC on KECK II). These are used as a benchmark to compare with and we discuss different possible reasons for the strong Sc I lines in the K-band spectra of M giants.

## 2. Observations

The high resolution, K-band spectra have been obtained using the NIRSPEC (McLean 2005; McLean et al. 2007) facility at Keck II, using the  $0''.432 \times 12''$  slit and the NIRSPEC-7 filter, giving the resolving power of  $R \sim 23,000$  needed for accurate abundance determination. Five spectral orders are recorded, covering the wavelength range of

21,000–24,000 Å. However, the wavelength coverage is not complete; there are gaps between the orders.

Apart from the 18 stars observed in the Galactic center, which are presented in Ryde et al. (2016b) and Rich et al. (2017), seven M giants in the solar neighborhood vicinity have been observed using nirspec on Keck II using the configuration described above, on 2017 July 28–29, under program U103NS (PI: Rich). These stars are selected to be of the same spectral type as the stars observed in the NSC. Table 1 provides the basic data for the new observations including the apparent  $K_s$  band magnitudes. For details about the data reduction process, we refer to Rich et al. (2017).

Spectra of three observed solar neighborhood stars are plotted in Figure 1 together with three Galactic center stars from Rich et al. (2017). The stars have been ordered by temperature to illustrate the change in line strengths for scandium, vanadium, and yttrium, which decrease dramatically from 3400 to 3800 K. For scandium, we can illuminate this behavior by investigating the atomic physics in greater depth, something that we cannot yet do for the other features.

## 3. Analysis

### 3.1. The Atomic Structure of Sc I

In addition to the abundance of an element, there are other parameters affecting the line strengths of absorption lines. One is the oscillator strength and another is the population of the lower level. The latter depends strongly on the excitation energy. For most elements, the near-IR transitions appear at high excitation energies, making the level populations lower. This is the case for most iron-group elements such as Fe I, where the lower excitation levels, such as the 4s levels, do not have near-IR transitions. For Sc I, the structure is different, with low excitation transitions  $3d^24s-3d4s4p$  appearing in the K-band.

Figure 2 shows the energy level diagrams for Sc I and Fe I, respectively, plotted with the same vertical energy scale. The dashed line shows the ionization energy for each atom. As can be seen, there is a significant difference in the excitation of the near-IR lines, where Sc I originates at much lower energies, around 1.5 eV, compared to Fe I at 3.6 and 6.1 eV. At temperatures of 3500–4500 K in the line-forming atmospheric depths, as for the stars in the current study, the Boltzmann factor,  $e^{-\Delta E/k_b T}$ , gives a difference of 3 orders of magnitudes comparing the two different excitation energies and in this case the different atoms, which means a difference of 3 orders of magnitude for relative level population. Note, however, that the abundance difference between iron and scandium in a solar mixture of gas is more than 4 orders of magnitude. A further implication is, as noted early by Smith & Lambert (1985, 1990), that non-LTE effects should be smaller for high excitation lines, which are formed in deeper, warmer layers of the stellar atmosphere and lines from the dominant stage of ionization. Non-LTE effects could thus affect low excitation lines from neutral species in M giants. It would, therefore, not be unexpected if non-LTE effects should plague the Sc abundances derived from our low excitation Sc I lines.

### 3.2. Atomic Data of Sc I Lines

In general, there is a lack of experimental atomic data for near-IR transitions.<sup>6</sup> In response to this need, we have initiated

<sup>6</sup> <https://www.nature.com/news/nailing-fingerprints-in-the-stars-1.14239>

**Table 1**  
Compiled Data for Both the Observed Stars and Stars Used for Comparisons in This Paper

Star	Obs. Date	$K_s$	R.A. [h:m:s]	Decl. [d:m:s]	$T_{\text{eff}}$ [K]	$\log g$	[Fe/H]	$\xi_{\text{micro}}$ [km s $^{-1}$ ]	[Sc/Fe]
2M17584888–2351011	2017 Jul 30	6.49	17:58:48.89	–23:51:01.17	3652	1.44	0.27	2.0	0.80
2M18103303–1626220	2017 Jul 29	6.51	18:10:33.04	–16:26:22.06	3436	0.79	0.27	2.2	0.77
2M18191551–1726223	2017 Jul 29	6.56	18:19:15.51	–17:26:22.35	3596	1.16	0.21	2.0	0.54
2M18550791+4754062	2017 Jul 30	7.63	18:55:07.92	47:54:06.22	3915	1.40	–0.27	2.0	0.37
2M19122965+2753128	2017 Jul 29	6.60	19:12:29.66	27:53:12.83	3263	0.25	0.27	2.4	0.58
2M19411424+4601483	2017 Jul 30	7.69	19:41:14.25	46:01:48.14	3935	1.41	–0.37	2.0	0.43
2M21533239+5804499	2017 Jul 29	6.58	21:53:32.40	58:04:49.94	3708	1.17	0.29	2.0	0.16
$\alpha$ Boo	...	–2.91	14:15:39.67	19:10:56.67	4286	1.66	–0.52	1.7	0.16
GC 7688	...	11.00	17:45:42.17	–29:00:54.99	4150	1.78	–0.08	1.8	0.13
GC 11025	...	10.41	17:45:37.13	–29:00:14.39	3400	0.69	0.27	2.3	1.27
GC 11473	...	11.74	17:45:42.64	–29:00:10.23	3550	1.13	0.64	2.0	0.37

**Note.** We assume solar abundances of  $A(\text{Fe}) = 7.45$  (Grevesse et al. 2007) and  $A(\text{Sc}) = 3.04$  (Pehlivan Rhodin et al. 2017).

a program to provide accurate and vetted near-IR atomic data for stellar spectroscopy. Scandium is one of the elements covered. Being an odd element, scandium has a nonzero nuclear spin of  $I = 5/2$  allowing for hyperfine structure (HFS). In recent works, we have measured the oscillator strengths and HFS of Sc I (Pehlivan et al. 2015; van Deelen 2017). The oscillator strengths are derived using the radiative and lifetime method, and the uncertainties are 0.03 dex for the lines used in the present study. Since the HFS is a result of the interaction between the nuclear and electronic angular momenta, the effect is larger for electrons close to the nucleus. Unpaired s-electrons are thus expected to show the largest HFS.

The states responsible for the transitions used in the present study,  $3d^24s-3d4s4p$ , involve an unpaired 4s-electron, making the HFS of the lines used large. This is indeed what is observed in the laboratory measurements. The HFS-data used in the present study are derived from fitting Fourier Transform Spectroscopy measurements (van Deelen 2017).

### 3.3. Analyzing the Effect of Temperature and HFS

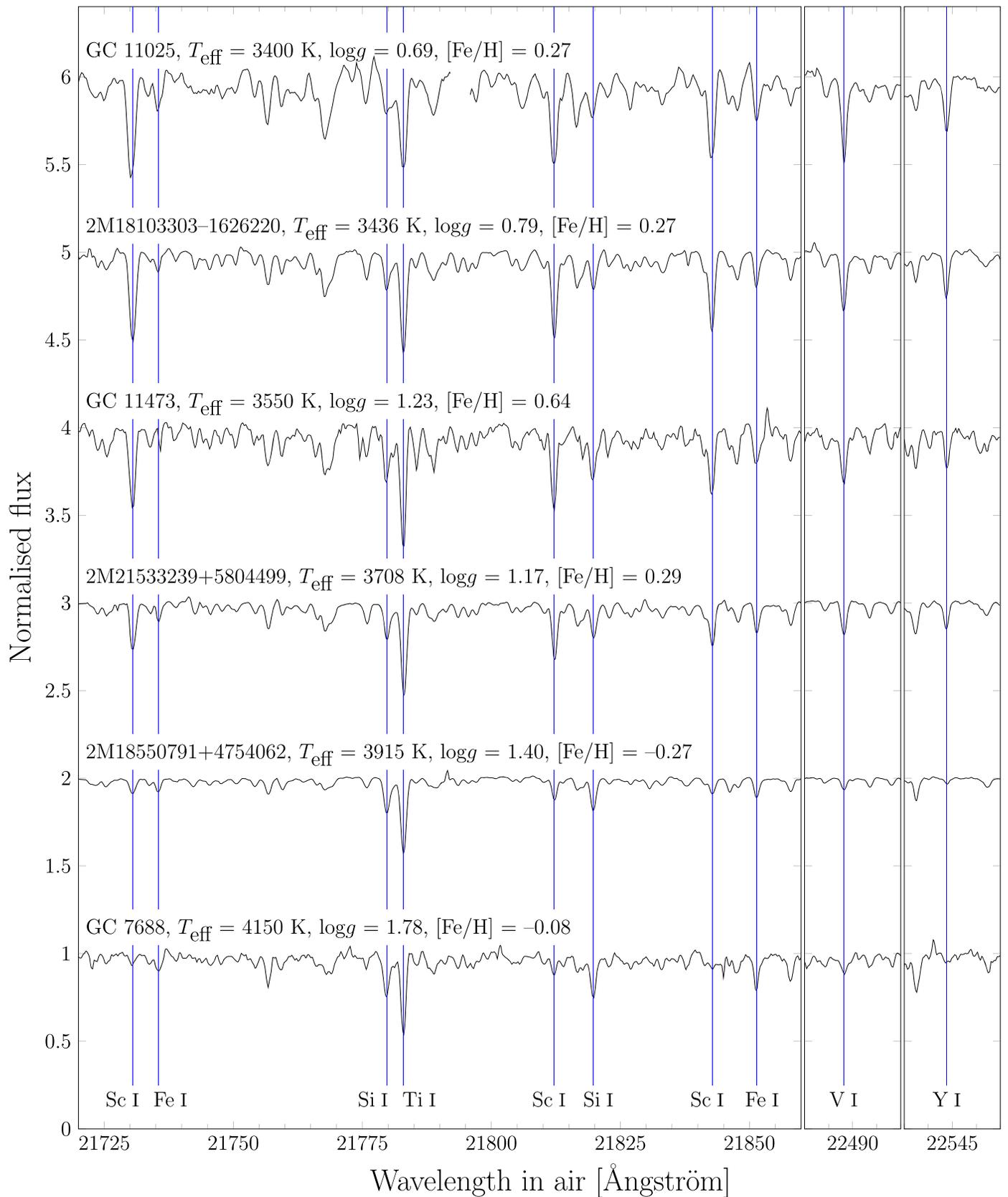
We model theoretical line formation of spectral Sc I lines to explore the effects of both temperature and HFS, using the BSYN and EQWIDTH codes based on routines from the MARCS model atmosphere code (Gustafsson et al. 2008). We use one-dimensional (1D) MARCS atmosphere models, which are hydrostatic model photospheres in spherical geometry, computed assuming LTE, chemical equilibrium, homogeneity, and conservation of the total flux (radiative plus convective, the convective flux being computed using the mixing-length recipe). The resulting line strength measured in equivalent width is plotted against temperature in Figure 3. For the spectral line based on a single atomic level transition, we use the measured oscillator strength from Pehlivan et al. (2015). For the HFS-based spectral line, we use the combined work of Pehlivan et al. (2015) and van Deelen (2017). The fact that the HFS spectral line is a combination of many weak lines means that the spectral line does not saturate in the classical sense of a spectral line based on a single atomic transition, and thus can form a much stronger line.

Using the same code and model assumptions, we further derive scandium abundances for a given spectral Sc I line having an equivalent width of 300 mÅ, which is presented in Figure 4.

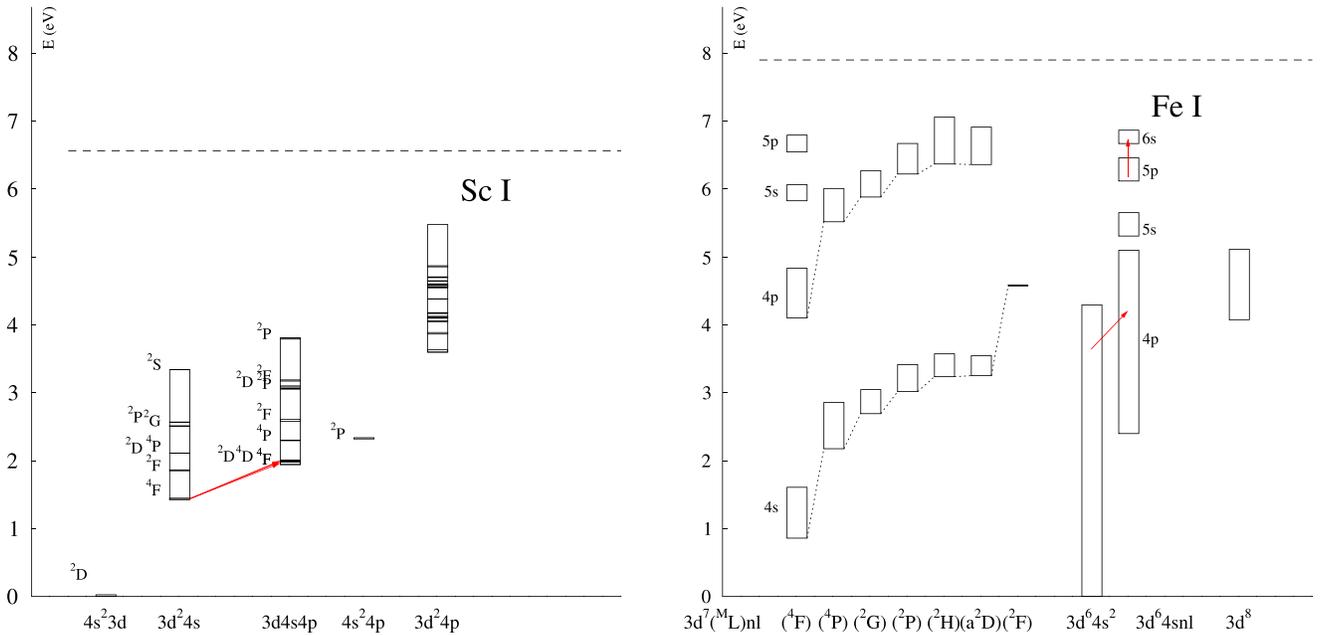
### 3.4. Accurate Stellar Parameters

The stellar parameters of the seven solar neighborhood stars presented here are obtained from the APOGEE Data Release 14 (Blanton et al. 2017; Majewski et al. 2017; Abolfathi et al. 2018). The stellar parameters have been determined using the APOGEE stellar parameters and chemical abundance pipeline (ASPCAP; García Pérez et al. 2016) and then calibrated using photometric effective temperatures, asteroseismic surface gravities, as well as stellar clusters (Holtzman et al. 2018). Jönsson et al. (2018) evaluate the performance of ASPCAP by comparing the stellar parameters and abundances derived to those of high resolution optical studies of giants. The typical uncertainties found in  $T_{\text{eff}}$ ,  $\log g$  and [Fe/H] are in the order of  $\sim 100$  K,  $\sim 0.2$  dex, and  $\sim 0.1$  dex, respectively. Similar uncertainties are found in Schultheis et al. (2017) by comparing to other spectroscopic results for bulge giants in Baade’s Window. However, since both of these comparisons were made for mainly stars with  $T_{\text{eff}} > 3800$  K (Schultheis et al. 2017 have two cooler comparison stars), these results cannot strictly be extrapolated to our much cooler M giants.

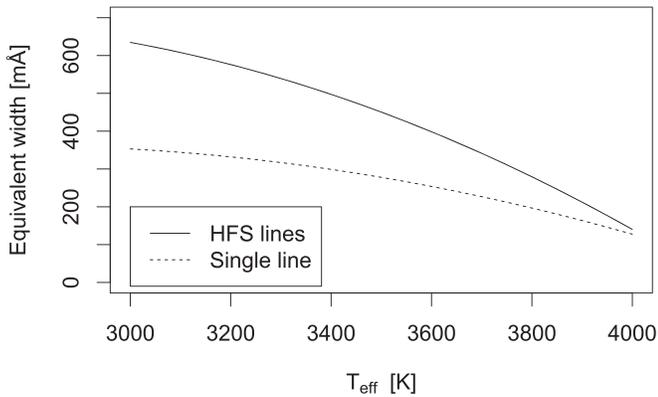
Since  $T_{\text{eff}}$  is the parameter with the greatest influence on the derived Sc abundance (see Section 3.1 and Figures 3, 5, and 6), we go on evaluating the ASPCAP accuracy of this parameter further. Table 2 shows a comparison of the effective temperature measured by APOGEE and the photometric  $T_{\text{eff}}$  based on the  $J - K_S$  versus  $T_{\text{eff}}$  relation from Houdashelt et al. (2000). In addition, we queried the *Gaia* DR2 database and found *Gaia* temperature estimates for seven of our objects. The temperatures from *Gaia* DR2 were determined by using the  $G_{\text{BP}} - G$  and  $G_{\text{RP}} - G$  colors as inputs together with a training set of different labels from different spectroscopic surveys such as APOGEE, RAVE, LAMOST, and the *Kepler* Input Catalog. For a more detailed description of the *Gaia* DR2 temperatures, we refer to Andrae et al. (2018). The mean difference between the spectroscopic and photometric temperatures from Houdashelt et al. (2000) is  $\sim 50$  K with a standard deviation of 240 K. The mean difference between APOGEE and *Gaia* is  $\sim 90$  K with a standard deviation of 185 K. We can conclude that the spectroscopic temperatures of our cool M giants derived from APOGEE are consistent with those of photometric measurements and *Gaia*’s estimated temperatures, and hence are expected not to show any large systematic uncertainties that in turn would skew our abundance analysis.



**Figure 1.** Six M giant stars plotted together with increasing temperature from top to bottom with blue vertical lines identifying lines of interest. The normalized fluxes have been translated upward with integer values for presentation. The stars are a mix of three Galactic center stars (GC 7688, GC 11025, and GC 11473) and three solar neighborhood stars (2M18103303–1626220, 2M18550791+4754062, and 2M21533239+5804499). The spectra show striking strong scandium, vanadium, and yttrium lines in the cooler stars, even though the stars are located in widely different environments. As temperatures increase to 3900 K and beyond, the neutral lines of scandium, vanadium, and yttrium begin to vanish, presumably due to ionization.



**Figure 2.** Energy level diagrams for Sc I and Fe I, respectively. The vertical energy scale is the same, and the dashed line shows the ionization energy. The observed lines are marked with red arrows. Note that the near-IR Sc I lines are located at significantly lower excitation energies compared to the near-IR Fe I lines.

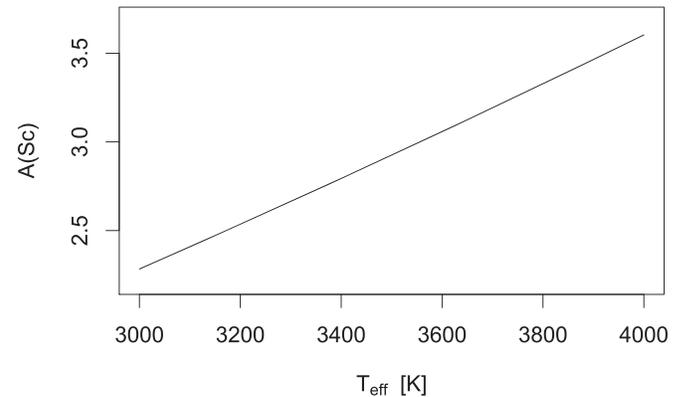


**Figure 3.** Equivalent width of a Sc I line as a function of temperature depends on whether the Sc I line is considered to be a combination of many small lines due to hyperfine structure (HFS) or if the line is considered to be a singular atomic level transition. Notice how at high temperature the two analyses converge, but at cooler temperatures the HFS of the line enables the spectral line feature to become considerably stronger compared to basing the analysis on a singular atomic level transition. The metallicity and scandium abundance is assumed to be solar, and the surface gravity is assumed to follow isochrone relations with changing temperatures. Non-LTE and 3D effects are not considered.

For  $\alpha$  Boo the *Gaia* FGK benchmark stars parameters are used (Jofré et al. 2014, 2015; Heiter et al. 2015) with uncertainties in  $T_{\text{eff}}$ ,  $\log g$  and  $[\text{Fe}/\text{H}]$  being 35 K, 0.09 dex and 0.08 dex, respectively.

The stellar parameters of the three Galactic center stars have been determined by Rich et al. (2017). The  $T_{\text{eff}}$  is determined from the strength of the CO bandhead in low resolution, K-band spectra (Schultheis et al. 2016). The uncertainties in  $T_{\text{eff}}$ ,  $\log g$ , and  $[\text{Fe}/\text{H}]$  are in the order of  $\sim 150$  K,  $\sim 0.3$  dex, and  $\sim 0.2$  dex, respectively.

For determination of microturbulence, we look to the abundance investigations of M giants in the solar neighborhood based on high resolution near-IR spectra (Smith & Lambert 1985; Smith et al. 1989; Smith & Lambert 1990), and for red

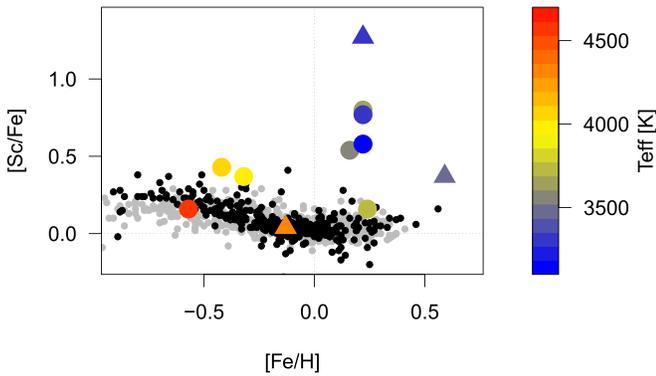


**Figure 4.** This plot assumes a Sc I line with a fixed equivalent width of 300 mÅ, as might be the situation when analyzing an observed spectrum. Plotted is the number density abundance of scandium as a function of temperature derived from this Sc I line. The plot shows how cooler temperatures counteract higher abundances when modeling such a feature. Note that a temperature difference of 100 K corresponds to an abundance difference of more than 0.1 dex. The metallicity is assumed to be solar, and the surface gravity is assumed to follow isochrone relations with varying temperature. Non-LTE and 3D effects are not considered.

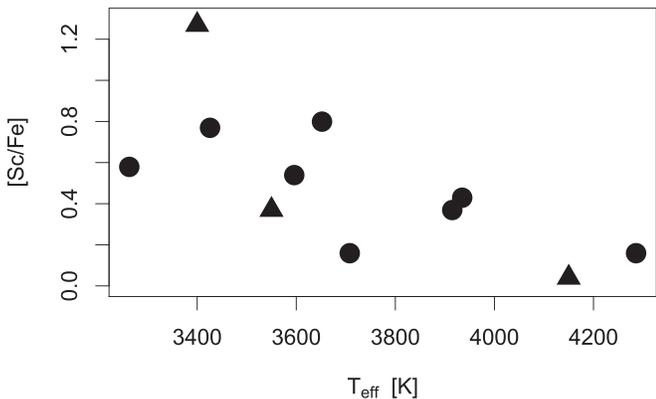
giants in the LMC (Smith et al. 2002). The microturbulence was found by demanding that abundances from lines from a few atomic species be independent of strength, with values from 2 to 3 km s $^{-1}$  for M giants. A more recent detailed analysis of spectra of five red giant stars by Smith et al. (2013) is used to provide an empirical relation described by Rich et al. (2017) for estimating microturbulence for our stars. The microturbulence values used are listed in Table 1.

### 3.5. Scandium Abundance Determination

To determine the scandium abundance of the analyzed stars, we find best fitting synthetic spectra based on radiative transfer and line formation calculated for a given model atmosphere (MARCS atmosphere models in spherical geometry; Gustafsson



**Figure 5.**  $[\text{Sc}/\text{Fe}]$  vs.  $[\text{Fe}/\text{H}]$  for stars in the solar neighborhood (disks) and Galactic center (triangles), colored by their effective temperature. Shown also are the scandium abundances derived from local disk giants from Lomaeva (Lomaeva 2018) as black dots and the scandium abundances derived from disk dwarfs by Battistini & Bensby (2015) as gray dots. Note how the derived  $[\text{Sc}/\text{Fe}]$  abundance ratio increases drastically as the stars becomes cooler, while the stars near 4000 K and above are more in agreement with both Lomaeva (Lomaeva 2018) and Battistini & Bensby (2015).



**Figure 6.**  $[\text{Sc}/\text{Fe}]$  vs.  $T_{\text{eff}}$  for stars in the solar neighborhood (disks) and Galactic center (triangles). Notice that both populations follow approximately the same trend. This plot shows that the derived scandium abundance simply increases with lower temperatures, suggesting that the derived “abundances” are spurious, being systematically in error, perhaps due to an incomplete model of the line formation.

**Table 2**

Comparison of Effective Temperatures between APOGEE, Photometric Temperature, and Those of the *Gaia* DR2 Release

Star	$T_{\text{eff}}^{\text{APOGEE}}$	$T_{\text{eff}}^{\text{photometric}}$	$T_{\text{eff}}^{\text{Gaia}}$
2M17584888–2351011	3652	3673	...
2M18103303–1626220	3436	3350	3282
2M18191551–1726223	3596	3191	3297
2M18550791+4754062	3915	3870	4000
2M19122965+2753128	3263	3402	3286
2M19411424+4601483	3935	4238	4048
2M21533239+5804499	3708	3451	3423

et al. 2008), assuming the fundamental stellar parameters shown in Table 1. We use the code Spectroscopy Made Easy (SME) for synthesizing model spectra and finding the best fit to the observed spectra using  $\chi^2$  minimization (Valenti & Piskunov 1996, 2012).

We use four neutral scandium (Sc I) features seen in the spectra of the analyzed stars for determining scandium abundances. The approximate wavelength in air of these features are 21730, 21812, 21842, and 22394 Å, where the first

three are visible in the spectra plotted in Figure 1. Due to hyperfine splitting of neutral scandium, the four spectral features consist of a total of 59 scandium lines, making the analysis robust against saturation effects that could otherwise be suspected due to the strength of the spectral features.

The determined scandium abundances are shown in Table 1 and plotted in Figure 5 as a function of  $[\text{Fe}/\text{H}]$  and in Figure 6 as a function of temperature. The uncertainties in  $[\text{Sc}/\text{Fe}]$  are on the order of  $\sim 0.1$  dex, assuming that the model assumptions hold.

## 4. Results and Discussion

### 4.1. Observed Spectra

Our central result is given in Figure 1, which shows an array of our NSC K band spectra interleaved with our identically observed local giants of similar spectral type (i.e., very similar stellar parameters). It is clear from this figure that the M giant spectra are overall quite similar, even taking into account the small differences in stellar parameters. This similarity extends to many of the atomic lines as well. At first glance, the plot suggests that the scandium abundance simply increases with lower temperature; this begins to point toward an explanation other than a true enhancement in scandium abundance, such as being unable to accurately model the line formation. Similar enhancements for vanadium and yttrium are also clear; both of these lines strengthen dramatically below 3600 K. We can conclude based only on empirical grounds that there is room for only very small differences in the abundances of these elements between stars in the Nuclear Cluster Stars and stars in the solar neighborhood. In particular, the scandium abundance is very unlikely to be anomalously elevated in the Galactic center NSC, as asserted in Do et al. (2018).

### 4.2. Derived Scandium Abundances

Figure 5 shows our derived scandium abundances in the form of the  $[\text{Sc}/\text{Fe}]$  trend versus metallicity, i.e., the  $[\text{Fe}/\text{H}]$  abundances. We show our seven M giants in the solar neighborhood together with  $\alpha$ -Boo and three M giants in the NSC (from Rich et al. 2017), colored as a function of effective temperature. As a background trend, we also plot the  $[\text{Sc}/\text{Fe}]$  abundance trends found for the solar neighborhood, determined from optical Sc II lines from Jönsson et al. (2017) and Lomaeva (2018) for K giant spectra and from Battistini & Bensby (2015) for dwarf star spectra; these trends follow approximately that of a typical  $\alpha$ -like element in the solar neighborhood, with elevated  $[\text{Sc}/\text{Fe}]$  at  $[\text{Fe}/\text{H}] < -0.5$  and a gentle decline toward Solar  $[\text{Sc}/\text{Fe}]$ . It is evident that these well-established trends are very different from our derived  $[\text{Sc}/\text{Fe}]$  values based on Sc I lines in our M giant spectra. Our derived abundance ratio determined for  $\alpha$ -Boo do agree with the general trend. It is evident that two giants with the highest temperature (from both the NSC and Local giants) fall exactly on the general trend even though their abundances are 0.5 dex apart. All of the cooler stars fall above the trend, and it is evident that the coolest stars are 0.5–1.3 dex above the trend, with the coolest stars showing the most extreme derived  $[\text{Sc}/\text{Fe}]$  “abundance” values.

Indeed, the most striking feature seen in Figure 6 is how our derived  $[\text{Sc}/\text{Fe}]$  “abundance” ratios increase dramatically with decreasing  $T_{\text{eff}}$  leading to anomalously high scandium abundances of up to 1.3 dex for the cooler stars ( $T_{\text{eff}} < 3800$  K), while

the warmer stars show more normal [Sc/Fe]. There is no astrophysical basis for the scandium abundance to depend on the *temperatures* of the stars, and therefore we can safely conclude that the derived abundances for the cooler stars are either plagued with very large systematic uncertainties or based on assumptions in the abundance determination that are not valid. This calls for a discussion of the physical processes involved.

We note that Smith et al. (2002) did not derive any anomalously high scandium abundances from their high resolution, near-IR spectra of 12 M giants in the LMC with effective temperatures in the range of 3600–4000 K and metallicities between  $-1.1$  and  $-0.3$  dex. The Sc I line they used at 23404.8 Å, which is not included in our wavelength range, is measured to have equivalent widths in the range of 70–650 mÅ. This is comparable to the equivalent widths of similar lines we find for our stars in the same temperature range. Apart from scandium, Smith et al. (2002) also derived the abundances of sodium, titanium, and iron, all from neutral lines. The [Na/Fe] and [Ti/Fe] abundance trends decrease with iron slightly below the disk trends, which is to be expected for the LMC. However, their [Sc/Fe] trend does not show such a depletion, possibly indicating higher-than-expected scandium abundances derived. Finally, Smith et al. (2002) find that the scandium abundance determination is very temperature sensitive with an uncertainty of almost 0.2 dex for a shift in 100 K in the effective temperature, which agrees with the modeled temperature sensitivity that we find to be above 0.1 dex, as discussed earlier in Section 3.3.

#### 4.3. Understanding the Strong Scandium Lines

As already noted in the discussion of spectral lines in M giants in the NSC (Rich et al. 2017), the Sc I lines observed in the K-band are indeed stronger than expected from an LTE spectral synthesis analysis for a reasonable scandium abundance. In this context, it is therefore of interest to consider possible processes and properties of these scandium lines that might be responsible for these anomalously high line strengths.

In LTE and for unblended, weak lines, i.e., lines that are not saturated, the observed line strengths are directly proportional to the atomic line strengths (Einstein A coefficients or  $\log gf$ -values) and the number density abundance ( $A_{\text{element}} = \log N_{\text{element}}[\text{cm}^{-3}]$ ) of the element causing the spectral line. In order to derive the abundance, it is therefore vital with a well determined  $\log gf$ -value. We therefore use the recent laboratory measurements of Pehlivan et al. (2015) for all our lines. This ensures a minimum uncertainty due to the intrinsic line strengths of the Sc I lines.

The strength of saturated lines can, on the other hand, also be very sensitive to the assumed microturbulence (see, e.g., Gray 2005), leading to large uncertainties in the derived abundances. However, having an odd nuclear spin, the scandium lines are subdivided into many components due to the HFS. In the case of our Sc I lines, the HFS has the effect of delaying the onset of saturation (since the strong line feature consists of many weak lines), but also to change the appearance of the line. Furthermore, the pressure broadening effect should be smaller on the components compared to an equally strong single line. We have, therefore, taken into account the HFS in our synthesis, successfully reproducing the line profile. Furthermore, our modeled lines are indeed relatively insensitive to microturbulence, even though the components have a relatively large summed equivalent width.

A further concern when working with spectral lines that yield anomalously high abundances, but also with lines in metal-rich and especially cool stars in general, is the contribution of unaccounted blends from molecular and atomic species. The accurate wavelength of molecular lines blending is a concern, but if the wavelengths are known precisely enough, these lines may be properly accounted for. The CN line list we use (Snedden et al. 2014) is very precise, so such blends can be accurately taken into account. Blended atomic lines might make an abundance analysis impossible; the existence of such blends might be known, but their atomic data are not accurately known, or there might be unknown blending lines that are not taken into account at all. However, in our spectra, all four Sc I lines are stronger than modeled by approximately the same amount. Therefore, it is very unlikely that all four lines would be blended at the same time. We therefore conclude that the Sc I lines are not significantly affected by blends.

Sc I lines are known to be temperature sensitive, and one concern would be that the anomalously strong Sc I lines are caused by a systematically incorrect temperature scale. To assess this possibility, we have determined the [Sc/Fe] abundances and the equivalent widths from a grid of stellar models. We have focused on the temperature range of M giants ( $3000 < T_{\text{eff}}/[\text{K}] < 4000$ ) since these are optimal objects to be observed in the NSC. A surface gravity is determined for a given ( $T_{\text{eff}}$ ,  $\log g$ ) combination from the Yale–Yonsei (YY) isochrones (Demarque et al. 2004). Figure 4 shows the derived Sc number density abundances from a line of a typical equivalent width of 300 mÅ. A decrease of 100 K in  $T_{\text{eff}}$  increases the derived Sc abundances by more than 0.1 dex. The scandium lines are indeed temperature sensitive, but this alone cannot explain the systematically stronger lines for our cooler stars. There is no reason to believe that the cooler solar neighborhood stars have  $T_{\text{eff}}$  systematically too high by up to 800 K.

We conclude that our derived abundances, based on an LTE abundance analysis, are precise and accurate to within at least 0.2 dex, with the temperature sensitivity being the largest source of uncertainty. However, we can also conclude that stars below approximately  $T_{\text{eff}} < 3800$  K should not be used for deriving stellar scandium abundances from these lines based on a traditional LTE analysis. We have demonstrated the strong temperature dependence but we cannot specify which model assumptions are invalidated, complicating any abundance analysis. However, with its low ionization potential, Sc I is a minority ionization stage throughout the photosphere, and any departures from LTE (and 3D effects) will affect Sc I lines more than ionized lines (Asplund 2005). Changes in the ionization rates, and therefore the ionization balance, change the relative population of the minority species more than that of the majority species.

No non-LTE investigations of scandium have been made for cool giants (to our knowledge), but Zhang et al. (2008) investigated the formation of *optical* scandium lines in the Sun and found large departures from LTE for Sc I lines and none for ionized lines. The Sc I lines in the Sun are weaker than expected from LTE, whereas we see the opposite for M giants. Whereas for metal-poor, cool stars, photoionization is a major process that can under-populate neutral atoms (Gehren et al. 2001), leading to weaker lines in non-LTE, for collision-dominated ions (Gehren et al. 2001), photon suction and over-recombination tend to strengthen the lines instead. An

over-recombination can be caused by the smaller mean-intensity-field compared to the Planck function, which is the case in the near-IR (Asplund 2005). These are processes that could cause stronger lines than expected from an LTE treatment.

The treatment of convection when using a full 3D hydrodynamical modeling instead of using a traditional 1D approach could also significantly affect the line formation. For neutral lines in the near-IR formed in red giants discussed in Kučinskas et al. (2013), Černiauskas et al. (2017), which are slightly warmer than ours, the abundance corrections are shown, however, to be small.

A strong suspicion is thus that Sc I lines formed in cool M giant atmospheres also are affected by non-LTE effects. In their non-LTE study of titanium lines, with a similarly low ionization potential as for scandium, Bergemann et al. (2012) show that the J-band lines in supergiants are indeed strengthened in non-LTE. The effect increases for increasing metallicities and decreasing temperatures, from a negligible effect at 4200 K to 0.4 dex at 3400 K, their lowest temperature point. Above 4200 K, the opposite effect is in play. If the same processes are important for scandium, these trends could explain also the strengthening of the scandium lines for cool, metal-rich stars. A detailed non-LTE study is, however, required to find the dominant process in play for the scandium lines in the K-band for M giants. However, in general, it is difficult to isolate the dominant process causing a departure of a Boltzmann–Saha level population for a transition in a complex atomic structure (Bergemann et al. 2012).

#### 4.4. Vanadium and Yttrium Lines in the K-band

In the K-band, there are a number of very strong vanadium and yttrium lines, see, for example, the spectra plotted in Figure 1. Do et al. (2018) suggest these elements to be significantly enhanced at the Galactic center, also with a potentially very different chemical enrichment history there. Based on the similarity of the solar neighborhood stars we present here, one might suspect that the V I and Y I lines might suffer from the same line strengthening effects as the scandium lines do.

Yttrium is homologous to scandium, residing just below scandium in the periodic table. It has the same atomic structure but with principle quantum numbers one unit larger and thus 4d and 5s instead of 3d and 4s for Sc I, which makes Y I lines of the configurations  $4d^25s-4d5s5p$  appear at low excitation energies. The strength of the Y I line should therefore react in the same way to the line formation process, and is thus expected to be stronger in the same way as in the case of Sc I. In addition, lanthanum residing in the period below yttrium, would show a similar effect for the lines  $5d^26s-5d6s6p$ , had there been lines detected in the K-band. Only the relative abundance differs. Laboratory studies of Y I and La I are ongoing.

Vanadium is the next odd element after scandium, lying after titanium in the periodic table. Its structure more closely resembles that of the iron-group elements, such as Fe I with the majority of the strong transitions appearing at high excitation. There are exceptions, such as the transition at  $3d^5 a^6S-3d^5(^5D)4p z^6P$  at 22493 Å. A non-LTE strengthening of vanadium cannot be excluded. We infer that non-LTE strengthening is the best option to explain the odd behavior of vanadium, given the arguments advanced here for scandium.

## 5. Conclusions

Our question in this paper is whether the abundance of scandium in stars observed in the NSC is really unusual. An unusual abundance would have a profound effect on our understanding of the formation of the NSC and its stellar population. There are several physical reasons for a spectral line to be strong, and by going through all of these, we conclude that the strong Sc I lines in the NSC are most likely due to line formation effects and certainly not due to an anomalous high scandium abundance. These Sc I lines in the K-band are not good abundance diagnostics for the elements in cool M giants. Our conclusion is based on the fact that similar stars in the solar neighborhood, where the scandium abundances are known, show similarly strong Sc I lines, much stronger than can be modeled with traditional synthetic spectroscopy. We conclude that the Sc I lines in cool stars are strong everywhere in the Galaxy and this is an inherent property of the line formation process, and should not be used to derive the scandium abundance of the stars. Lines of ionized scandium should be used instead or studies should use warmer stars. Non-LTE calculations for scandium, and perhaps other physical phenomena needing theoretical modeling, are needed before we can use the Sc I lines at all.

Our findings emphasize the perils of attempting to infer composition from a small number of lines that are far too strong for any conventional application of abundance analysis. Although high resolution infrared spectroscopy makes it possible to study the composition of stars in highly obscured regions, the relative paucity of weak lines requires that work in the infrared is approached with great caution. In the case where anomalies are suspected, it is important to turn to general established trends derived from optical measurements in the disk and bulge, as an additional essential check before claiming to discover unusual composition. We also note that at high metallicities, it would be quite surprising to see large enhancements of any species, that would imply extreme productions of individual elements in a metal-rich environment.

The cool giants we have analyzed are almost certainly on the asymptotic giant branch (AGB) and, as such, they are likely to be the most luminous stars in their stellar population, contributing a substantial fraction of the K band integrated light. We know that the NSC is a complex stellar population with a wide range of age and we might expect many extragalactic NSCs to also have wide age ranges and possibly host very substantial populations of cool, luminous AGB stars. Individual supergiants can also contribute a substantial portion of the integrated light in the K band. There is a growing trend to attempt to infer detailed abundances (e.g., abundances of individual atomic species) from the integrated light of stellar populations. The temptation is strong for the extragalactic NSCs of low luminosity spirals, which have relatively low broadening due to the stellar velocity dispersion, making them very attractive targets for spectrum synthesis. We emphasize that if such a practice is carried out for the integrated light in the K band, it should be done using actual spectra of solar neighborhood giants and a full population synthesis code. The numbers of cool AGB stars are small, and their contribution to the stellar population is stochastic (Frogel et al. 1990). Even then, our understanding of line formation for cool giants is far from complete and therefore, we suggest that integrated light studies using only the K band be avoided.

High resolution spectroscopy in the near-infrared is a relatively new subject area. The advent of very high resolution spectrographs on the current generation of 8–10 m telescopes and future plans for ELTs give the subject great promise. It is important to support this endeavor with an equally serious investment in laboratory measurements, so that full advantage can be taken of the expected bounty of high quality data.

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*Facility:* Keck II (NIRSPEC).

*Software:* SME (Valenti & Piskunov 1996, 2012), BSYN & EQWIDTH (Gustafsson et al. 2008).

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