

Limiting the shock acceleration of cosmic ray protons in the ICM

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ABSTRACT

Observations of large-scale radio emissions prove the existence of shock accelerated cosmic ray electrons in galaxy clusters, while the lack of detected γ -rays limits the acceleration of cosmic ray protons in galaxy clusters. This challenges our understanding of how diffusive shock acceleration works. In this work, we couple the most updated recipes for shock acceleration in the intracluster medium to state-of-the-art magnetohydrodynamical simulations of massive galaxy clusters. Furthermore, we use passive tracer particles to follow the evolution of accelerated cosmic rays. We show that when the interplay between magnetic field topology and the feedback from accelerated cosmic rays is taken into account, the latest developments of particle acceleration theory give results that are compatible with observational constraints.

Key words: acceleration of particles – MHD – shock waves – galaxies: clusters: intracluster medium – gamma-rays: galaxies: clusters.

1 INTRODUCTION

Some of the Universe’s largest particle accelerators are found in galaxy clusters. During the process of hierarchical structure formation, both shock waves and turbulence, which are observed by X-ray observations, form in the intracluster medium (ICM). Radio relics are large and elongated sources located at the clusters’ periphery (e.g. van Weeren et al. 2019). A likely explanation for relics is diffusive shock acceleration (DSA; e.g. Bykov et al. 2019, and references therein). Yet, several questions for the complete understanding of relics remain. If we were to assume that DSA operates similarly for both electrons and protons, then cosmic ray protons would be expected to fill the cluster-wide volume due to their long lifetime. However, to date the *Fermi* Large Area Telescope (hereafter *Fermi*) has not detected the γ -ray signal produced by inelastic collisions with the thermal protons, which limits the total energy of cosmic ray protons to be less than a few percent of the total gas energy within clusters (Ackermann et al. 2014, 2015, 2016).

Several works have investigated the missing γ -rays. Kang & Jones (2007) and Kang & Ryu (2013) used 1D diffusion–convection equations of shocks to derive the Mach number-dependent acceleration efficiencies. Yet, cosmological simulations showed that these efficiencies are too large and would produce a γ -ray signal still observable by *Fermi*, and that an overall efficiency of $\leq 10^{-3}$ is required to make clusters invisible in γ -rays (Vazza et al. 2016).

Recently, particle-in-cell (PIC) simulations have shown that the shock acceleration efficiencies depend not only on the shock strength but also on its obliquity, the angle between shock normal and the local magnetic fields (Caprioli & Spitkovsky 2014; Guo, Sironi & Narayan 2014a,b; Kang, Ryu & Ha 2019). These works showed that cosmic ray protons require a rather parallel alignment, while cosmic ray electrons prefer a more perpendicular orientation to be efficiently accelerated. In Wittor, Vazza & Brüggén (2016, 2017a), we found that the distribution of obliquities follows the distribution of random angles in a 3D space and therefore about two-thirds of all shocks are expected to be quasi-perpendicular and only one-third of all shocks tend to be quasi-parallel. While the radio emission stays unaffected by this, the γ -ray emission drops by a factor of about ~ 3 , which cannot explain the non-detection by *Fermi*.

More recent PIC simulations by Ha et al. (2018) showed that proton acceleration by low Mach number shocks in high- β plasmas [as the intracluster medium (ICM)] is quenched for shocks with Mach numbers below ~ 2.25 . In addition, Ryu, Kang & Ha (2019) included the dynamical feedback of cosmic ray pressure on the shock and derived new acceleration efficiencies for cluster shocks. Their model predicts that the acceleration efficiencies in the Mach number regime of 2.25–5.0 are in the range of 10^{-3} to 10^{-2} . Using grid simulations, Ha, Ryu & Kang (2019) found that these new findings produce γ -ray emission that is invisible to *Fermi*. However, they do not follow the evolution of cosmic ray protons throughout their simulation. Hence, in this contribution, we used methods already presented in Wittor et al. (2016, 2017a), but including the

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Table 1. Overview of the four simulations. ID: cluster name, M_{200} : cluster mass, r_{200} : cluster radius, M_{tracer} : tracer mass resolution, N_p : total number of tracers used, N_x^3 : number of resolution elements at the highest nested level of the ENZO simulation. All values are measured at redshift $z \approx 0$.

ID	M_{200} ($\times 10^{14} M_{\odot}$)	r_{200} (Mpc)	M_{tracer} ($\times 10^6 M_{\odot}$)	N_p ($\times 10^7$)	N_x^3
SP0m	5.41	1.72	3.25	1.70	256 ³
SP2m	8.29	1.99	5.58	2.28	320 ³
SP8m	7.40	1.92	3.28	1.82	384 ³
E5A	11.0	2.13	2.24	13.9	540 ³

new constrains on the minimum Mach number (Ha et al. 2018) and the acceleration efficiencies (Ryu et al. 2019) to study their effect on the γ -ray emission. Furthermore, we applied our modelling to a new set of high-resolution magnetohydrodynamical (MHD) simulations. This work is structured as follows: first, we introduce our simulations in Section 2. In Section 3, we present our results, and we conclude our work in Section 4.

2 SIMULATIONS

2.1 ENZO simulations

Here, we analysed clusters that were simulated with the MHD code ENZO (Bryan et al. 2014). We point to recent works (e.g. section 2.1 in Wittor et al. 2019) for the numerical details.

We took three clusters from the *San Pedro*-cluster catalogue, which targets the topological study of relics (Wittor et al., in preparation). The *San Pedro* simulations use nested grids to provide a uniform resolution at the highest refinement level. Each simulation covers a root grid of $(140 \text{ Mpc h}^{-1})^3$ and is sampled with 256^3 cells. Using MUSIC (Hahn & Abel 2011), an additional region of $\sim(4.4 \text{ Mpc h}^{-1})^3 - (6.6 \text{ Mpc h}^{-1})^3$ centred around each cluster is further refined using 5 levels, i.e. 2^5 refinements, of nested grids for a final resolution of $\sim 17.09 \text{ kpc h}^{-1}$. Each nested region is at least 3.5^3 times larger than the volume enclosed in r_{200}^3 . We initialized a uniform magnetic field with a value of 10^{-7} G in each direction.

We used cosmological parameters that are based on the latest results from *Planck* (i.e. Planck Collaboration VI 2018): $H_0 = 67.66 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_b = 0.0483$, $\Omega_m = 0.3111$, $\Omega_{\Lambda} = 0.6889$, $\sigma_8 = 0.8102$, and $n = 0.9665$.

In this work, we analyse three *San Pedro* clusters, called SP0m, SP2m, and SP8m, that cover a mass range of $M_{200} \approx (5.41-8.29) \times 10^{14} M_{\odot}$ (see Table 1). The dynamical state of the three systems is quite active: SP2m and SP8m are both undergoing major merger events close to redshift $z \approx 0$. On the other hand, SP0m hosts a major merger event at $z \approx 0.4$.

We increased our sample by adding one more massive, $M_{200}(z = 0) \approx 1.1 \times 10^{15} M_{\odot}$, cluster (E5A), obtained with earlier ENZO simulations and a similar numerical set-up (Vazza et al. 2018; Domínguez-Fernández et al. 2019). This cluster is an active major merger and it undergoes various merging episodes, including a major merger during its lifetime. For the further analysis, we use the reconstruction of the sixth adaptive mesh refinement level. This assures a uniform resolution of 15 kpc across a large enough volume of $\sim(8.5 \text{ Mpc})^3$ to follow both components of the major merger. For this work, we used the following cosmological parameters: $h = 0.72$, $\Omega_{\Lambda} = 0.742$, $\Omega_M = 0.258$, and $\Omega_b = 0.0441$.

2.2 CRATER simulations

We use our Lagrangian code CRATER to follow the evolution of the shock accelerated cosmic ray protons in the ENZO simulations. CRATER has been already used to study the cosmic rays and turbulence in galaxy clusters (e.g. Wittor et al. 2016, 2017a,b). For details of the implementation, we point to these references.

At redshift $z \approx 1$, we injected $\sim(5-28) \times 10^6$ particles, with a mass resolution of $\sim(2.24-8.58) \times 10^6 M_{\odot}$, into each ENZO simulation. The mass resolution gives a constant and high sampling of the final cluster mass, which is crucial to properly model the γ -emission. Following the mass inflow, we injected additional tracers from the boundaries at run-time. At redshift $z \approx 0$, each cluster is modelled by $\sim(1.7-13.9) \times 10^7$ particles.

The tracers used a temperature jump-based shock finder to detect shocks in the ICM (section 2.2 in Wittor et al. 2017a). For each detected shock, they compute the Mach number

$$M = \sqrt{\frac{4}{5} \frac{T_{\text{new}}}{T_{\text{old}}} \frac{\rho_{\text{new}}}{\rho_{\text{old}}}} + 0.2. \quad (1)$$

We defined the corresponding obliquity as the angle between magnetic field and the shock propagation direction, which is calculated as the difference between the pre- and post-shock velocities measured by the tracers $\Delta \mathbf{v} = \mathbf{v}_{\text{post}} - \mathbf{v}_{\text{pre}}$:

$$\theta_{\text{pre/para}} = \arccos \left(\frac{\Delta \mathbf{v} \cdot \mathbf{B}_{\text{pre/para}}}{|\Delta \mathbf{v}| |\mathbf{B}_{\text{pre/para}}|} \right). \quad (2)$$

Using the shock velocity and the pre-shock density, we computed the kinetic energy flux across each shock as $F_{\psi} = 1/2 \cdot \rho_{\text{pre}} v_{\text{sh}}^3$. The associated thermal and cosmic ray energy fluxes are $F_{\text{th}} = \delta(M) F_{\psi}$ and $F_{\text{CR}} = \eta_i(M) F_{\psi}$. The gas thermalization efficiency, $\delta(M)$, was derived by Kang & Ryu (2013). For the cosmic ray acceleration efficiency, $\eta_i(M)$, we assumed a variety of models denoted by i . For comparison with Wittor et al. (2016, 2017a), we use the efficiencies from Kang & Ryu (2013), hereafter η_{13} . We further tested the new acceleration efficiencies given in Ryu et al. (2019) for $Q_i = 3.5$ and $p_{\text{min}} = 780 \text{ MeV}/c$, hereafter η_{19} , and we combined them with more restrictions on the shock type: Following Caprioli & Spitkovsky (2014), we included the case of only quasi-parallel shocks, i.e. $\theta < 45^\circ$, accelerating protons, hereafter θ_{45} . Based on Ha et al. (2018), we only let shocks with $M > 2.25$ accelerate cosmic ray protons, hereafter $M_{2.25}$. Following the definition by Ha et al. (2018), we will refer to shocks with Mach number above $M > 2.25$ as supercritical shocks. Finally, we only let quasi-parallel shocks with $M > 2.25$ accelerate cosmic ray protons, hereafter $\theta_{45}, M_{2.25}$. We stress that, unlike Wittor et al. (2017a), we do not compute effective acceleration efficiencies, but use the acceleration efficiencies from the thermal pool. For each different injection model, we computed the time integrated gas and cosmic ray energy at redshifts z_j as

$$E_{\text{gas/CR}}(z_j) = \sum_{z=1}^{z_j} \sum_{n=1}^{N_p} F_{i,n}(M, \theta) \Delta t(z). \quad (3)$$

Depending on the assumed acceleration model, the sum across the particles, i.e. the sum across n , is only taken for the shocks that fulfil the conditions summarized.

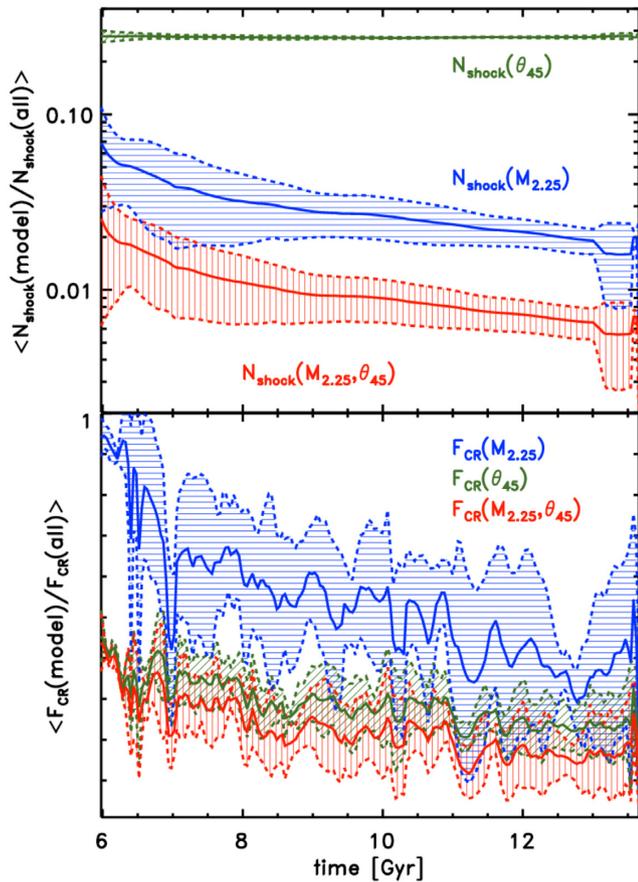


Figure 1. Temporal evolution of the shock fraction (top) and cosmic ray energy flux ratios (bottom). In both panels, the solid lines show the average of the four simulations and the dashed lines give the standard deviation.

3 RESULTS

3.1 Shocks and cosmic ray energy flux

First, we estimated the number of different types of shocks (e.g. $\theta < 45^\circ$, $M > 2.25$, etc.) in our simulations. Therefore, we define the shock fraction as the ratio between the number of a specific type of shock and the total number of shocks. In the top panel of Fig. 1, we plot the shock fraction averaged over the four simulations in time. The fraction of quasi-parallel shocks, the green line, stays constant in time, ~ 28 per cent, and also the standard deviation across the different simulations is small. This agrees with Wittor et al. (2017a), where we reported that the distribution of shock obliquity follows the distribution of angles between random vectors in a 3D space and, hence, about one-third of all shocks are expected to be quasi-parallel. In contrast, the fraction of supercritical shocks decreases in time by a factor of ~ 4.3 . The fraction of supercritical quasi-parallel shocks follows a similar trend, but it drops from ~ 2.3 to ~ 0.5 per cent. Hence, less than ~ 3 per cent of all shocks are expected to accelerate cosmic ray protons.

To investigate the amount of the energy processed by shocks in our different models, we define the cosmic ray energy flux ratio as $F_{\text{CR}}(\text{model})/F_{\text{CR}}(\eta_{19})$. Here, ‘model’ is replaced by the three models that cut on obliquity, Mach number, and both. In the bottom panel of Fig. 1, we show the evolution of the flux ratio averaged over the four simulations.

At early times, most, $\sim (94 \pm 5)$ per cent, of the cosmic ray energy flux is processed by supercritical shock. This seems obvious, as the cosmic ray energy flux scales with the shock acceleration efficiency, which increases significantly for supercritical shocks (see fig. 4 in Ryu et al. 2019). Throughout the cluster evolution, the relative contribution of supercritical shocks shows a large variation with an average value of ~ 53 per cent. Overall, it decreases to $\sim (20 \pm 16)$ per cent reflecting the occurrence of fewer supercritical shocks at later times. The reduction of supercritical shocks is also shown in the cosmic ray energy flux processed by quasi-parallel shocks, which is initially $\sim (45 \pm 6)$ per cent and decreases to $\sim (12 \pm 7)$ per cent. This drop is less than that for the supercritical shocks, as high Mach number shocks tend to cluster around structures (Wittor et al. 2016); therefore, there can be an excess in supercritical quasi-parallel shocks. On average, the quasi-parallel shocks process ~ 29 per cent of the cosmic ray energy flux. This is in agreement with the fact that on average ~ 27 per cent of the shocks are quasi-parallel.

The cosmic ray energy flux processed by supercritical quasi-parallel shocks, i.e. shocks that are expected to accelerate cosmic ray protons, is $\sim (44 \pm 7)$ per cent at $t \approx 6$ Gyr. The flux ratio follows roughly the same evolution as for the quasi-parallel shocks, though it is on average a factor of ~ 1.3 smaller, and it drops to $\sim (10 \pm 7)$ per cent at the end of the simulations. The amount of flux processed by supercritical quasi-parallel shocks is larger than what one would expect from the average number of these kinds of shocks. Again, this reflects the clustering of supercritical shocks around structures.

3.2 γ -ray emission

We computed the γ -ray emission for each cosmic ray population as described in section C1 in Wittor et al. (2017a) and references therein (Huber et al. 2013; Vazza et al. 2015; Donnert et al. 2016). Given the large cooling time-scales of cosmic ray protons, we did not include any energy losses and our results impose upper limits on the γ -ray flux. We based our energy range, 100 MeV to 10 GeV using 16 energy bins, similar to *Fermi* (Ackermann et al. 2016). In Fig. 2, we give maps of the γ -ray emission for the most restricted cosmic ray model, i.e. η_{19} , θ_{45} , and $M_{2.25}$. In addition, we show the baryonic densities contours and the region of r_{200} . In all cases, γ -ray emission is mostly confined within r_{200} . Moreover, the peak of γ -ray emission always overlaps with the densest regions. In E5A, the γ -ray emission is more prominent in the right sub-cluster.

In Fig. 3, we plot the evolution of the γ -ray emission for each cosmic ray model measured in the whole simulation box, as well as the upper limit on the COMA cluster given in Ackermann et al. (2016). For all clusters except SP0m, which is much lighter than COMA, the η_{13} model produces γ -ray emission that is above the COMA limit. In all clusters, the γ -ray emission associated with the η_{19} model is about a factor of ~ 4.5 smaller than in the η_{13} model and, hence, it drops in always below the *Fermi* limit of COMA. Additional cuts in Mach number and/or obliquity reduce the γ -ray emission further by factors of ~ 6.5 – 23.4 compared to the η_{13} model.

This suggests that already the η_{19} model might explain the non-detection of γ -rays. In order to examine whether the simulated clusters could be observed by *Fermi*, we compared our sample with Ackermann et al. (2014) who set upper limits on the γ -ray flux in the energy range 500 MeV to 200 GeV, measured in r_{200} , for a larger sample of clusters. In Fig. 4, we plot the cluster mass

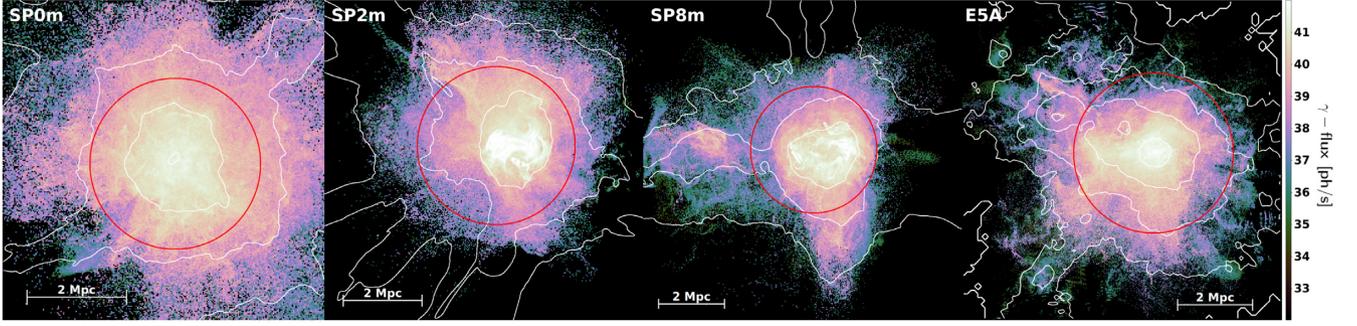


Figure 2. Map of the integrated γ -ray flux for the η_{19} , θ_{45} , and $M_{2.25}$ models. The white contours are the baryonic density at $10^{-27.25}$, 10^{-28} , $10^{-28.75}$, and $10^{-29.5}$ g/cm^3 . The red circles mark the r_{200} .

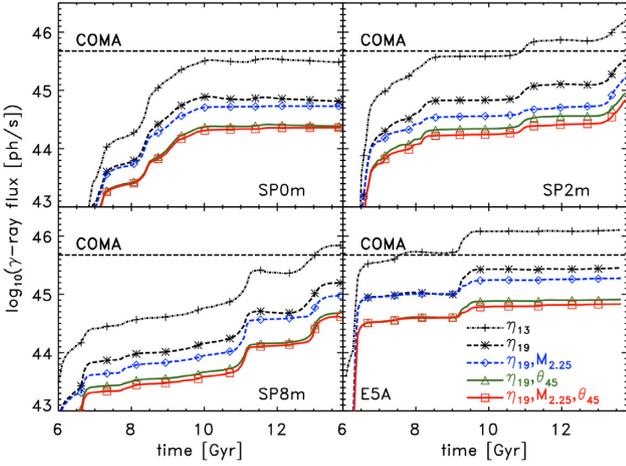


Figure 3. Time evolution of the γ -ray flux for the different cosmic ray models and the COMA upper limit (dashed line; Ackermann et al. 2016).

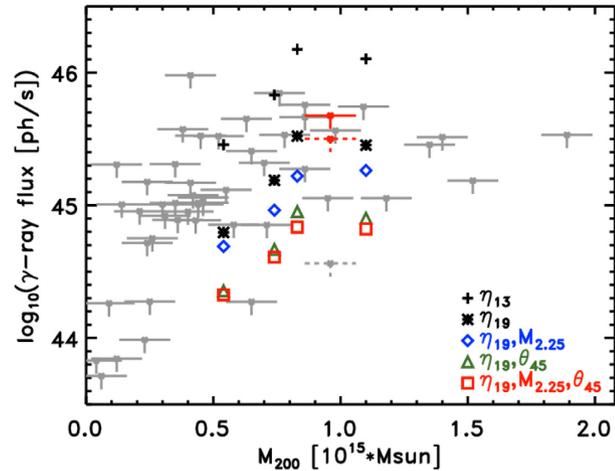


Figure 4. The total γ -ray flux within r_{200} versus the cluster mass M_{200} . The grey crosses give the upper limits in the energy range 500 MeV to 200 GeV (Ackermann et al. 2014). Specifically, the grey dashed cross is the upper limit for the COMA. The red solid cross gives the deeper limits for COMA (Ackermann et al. 2016) and the red dashed cross is an estimate for the improvement on the upper limit after 10 more years of *Fermi* observations. The symbols give the γ -ray flux of the different models in the simulations.

against the upper limit.¹ In addition, we plot the upper limit for the COMA cluster as given in Ackermann et al. (2016)² and an estimate for the COMA upper limit after 10 yr of *Fermi* observations.³ We note that the deeper upper limit for COMA is larger than the limit in Ackermann et al. (2014), as Ackermann et al. (2016) probed lower energies that have more low-energy particles for a power-law distribution. For a proper comparison with the limits given in Ackermann et al. (2014), we additionally computed the γ -ray flux in the same energy range. Yet, the γ -ray fluxes do not change significantly, as the effective cross-section equation 79 in Kelner, Aharonian & Bugayov (2006) peaks at 1.22 GeV and rapidly decreases for lower energies. This has been also observed in other works (e.g. Brunetti, Zimmer & Zandanel 2017). Hence, in Fig. 4, we plot the, somewhat larger, γ -ray fluxes in the energy range of 100 MeV to 10 GeV measured inside r_{200} , i.e. only inside the red circle in Fig. 2.

If our simulated clusters are compared to the available mass- γ -flux relation derived from *Fermi* observations, all of them should be detected by *Fermi* for the η_{19} model (black asterisks). If only supercritical shocks accelerate protons (blue diamonds), the γ -ray flux is reduced by a factor of ~ 2 at the most and all clusters remain detectable. The additional cut in obliquity (red squares) lowers the γ -ray flux significantly and, without exceptions, the simulated clusters drop below the *Fermi* limits. Only SP0m remains at the edge of what could be observable, as its γ -ray flux is above the upper limit of Abell 2877. However, we found fairly little information about Abell 2877 in the literature. Hence, it is not clear whether Abell 2877 and SP0m are in a similar dynamical state and whether their evolution is comparable. Hence, one should not take this data point too strictly. If only quasi-parallel shocks of all strengths accelerate protons (green triangles), the γ -ray flux is slightly above the γ -ray flux of the η_{19} , $M_{2.25}$, and θ_{45} models. Hence, the γ -ray emission is mostly reduced by the cut in obliquity, which is already enough to explain the non-detection of γ -rays.

As an alternative approach, the stacking of γ -ray count maps has also been explored to produce statistical upper limits for the average cluster population (Huber et al. 2012, 2013). We performed a qualitative assessment of stacking on our clusters, by computing

¹We used the M_{200} values from table 1 and $F_{\gamma, 500 \text{ MeV}}^{UL}$ values of an extended source from table 6, both given in Ackermann et al. (2014).

²We refer to the value given in table 1 for a cored profile with $\Gamma = 2.3$, which is similar to that in our simulation.

³We rescaled the upper limit from Ackermann et al. (2016) given the estimates in figs 2.1 and 5.1 in de Angelis et al. (2018).

the arithmetic mean of the γ -ray emission in a region of size $\sim(2.13 \text{ Mpc})^2$ centred around our simulated clusters. We find a mean flux is $\sim 4.16 \times 10^{44} \text{ ph s}^{-1}$, which is still below the deep COMA limit of Ackermann et al. (2016). The stacked signal of the simulations is also below the upper limit of Huber et al. (2013), when rescaled to the same energy range by assuming a spectral index of 2.3.

In summary, although our sample is still fairly limited to fully compare with the *Fermi* sample, the observed trends are regular enough to derive some fiducial conclusions on the tested DSA models. We find that the acceleration efficiencies presented in Ryu et al. (2019) can explain the non-detection of γ -rays, if only quasi-parallel shocks with Mach numbers above $M > 2.25$ are able to accelerate cosmic ray protons. Furthermore, *Fermi* would not be able to detect any of our simulated clusters, if it observes for 10 more years (red dashed cross).

4 CONCLUSION

In this work, we have re-investigated the puzzle of the missing hadronic γ -ray emission in galaxy clusters (e.g. Ackermann et al. 2016). We have simulated evolution of cosmic ray protons accelerated according to different possible recipes of DSA in four galaxy clusters, using ENZO and our Lagrangian tracer code CRATER. We followed each cluster simulation using about 10^7 – 10^8 tracer particles that recorded shocks and computed the associated cosmic ray energy injected by the shock. We then computed the corresponding γ -ray flux for the different models for the shock acceleration efficiencies and compared this to the upper limits set by *Fermi*. Our findings are summarized as follows:

(i) The γ -ray flux within r_{200} produced with the new acceleration efficiencies, which account for the dynamical feedback of cosmic ray pressure on the shock, is reduced a factor of ~ 4.5 smaller on average; such reduction is, however, not enough to make all our simulated clusters invisible to *Fermi*.

(ii) As most of the cosmic ray energy flux is processed by shocks with $M > 2.25$, the γ -ray emission is not reduced significantly and the clusters remain detectable in γ -rays, if only shocks with $M < 2.25$ are excluded from cosmic ray proton acceleration.

(iii) While allowing cosmic ray proton acceleration only at quasi-parallel shocks produces γ -ray emission close to but above the *Fermi* limits, the predicted γ -flux drops below the *Fermi* limits if acceleration is additionally restricted to supercritical shocks only.

In conclusion, we have found that the new acceleration efficiencies given in Ryu et al. (2019) might explain the non-detection of γ -rays in galaxy clusters, but only if supercritical quasi-parallel shocks, i.e. $M > 2.25$ and $\theta < 45^\circ$, are able to accelerate cosmic ray protons. Besides the new acceleration efficiencies, the main contributor for reducing the γ -rays flux is the cut in obliquity, as most of the energy is being processed by shocks with $M > 2.25$. However, only the detection of a γ -ray signal can verify the exact acceleration scenario of cosmic ray protons. Our estimates show that even 10 more years of observations with *Fermi* are most likely not enough to make any significant detection and one would require more sensitive telescopes. As the Cherenkov Telescope Array will be most likely less sensitive than *Fermi* in the desired energy range (Cherenkov Telescope Array Consortium 2019), future hopes to detect γ -rays in galaxy clusters are restricted to the proposed mission All-sky Medium Energy Gamma-ray Observatory (McEnery et al. 2019).

As final caveats, we note that we did not include γ -ray emission associated with the turbulent (re-)acceleration of cosmic ray protons (e.g. Brunetti et al. 2017), which could increase the observed signal. Furthermore, we did not include possible re-acceleration of cosmic ray protons at shocks, either. Assuming that it operates only at supercritical quasi-parallel shocks, Ha et al. (2019) estimated that re-acceleration would increase the cosmic ray energy by $\sim (40 - 80)$ per cent. In general, it is argued that, at quasi-perpendicular shocks, protons go about one gyromotion in the shock foot and then advect downstream. Yet at subcritical shocks, overshoot/undershoot oscillations do not develop in the shock transition and the specular reflection of protons is negligible. Hence, upstream waves are not generated there. However, it remains unknown if pre-existing cosmic ray protons can be reflected efficiently at either quasi-perpendicular or subcritical shocks, leading to the self-excitation of upstream waves. Hence, the re-acceleration by turbulence and at shocks needs further investigations. Finally, we comment that the numerical resolution appears sufficient for the presented analysis as the average cosmic ray dynamic is likely to be converged, and that increasing the resolution would only affect the cluster cores, based on previous studies (e.g. Vazza, Gheller & Brügggen 2014).

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