



Publication Year	2017
Acceptance in OA @INAF	2021-04-13T07:39:47Z
Title	Evidence for the formation of comet 67P/Churyumov-Gerasimenko through gravitational collapse of a bound clump of pebbles
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DOI	10.1093/mnras/stx2741
Handle	http://hdl.handle.net/20.500.12386/30739
Journal	MONTHLY NOTICES OF THE ROYAL ASTRONOMICAL SOCIETY
Number	469

Evidence for the formation of comet 67P/Churyumov-Gerasimenko through gravitational collapse of a bound clump of pebbles

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Accepted 2017 October 18. Received 2017 October 17; in original form 2017 February 3

ABSTRACT

The processes that led to the formation of the planetary bodies in the Solar system are still not fully understood. Using the results obtained with the comprehensive suite of instruments onboard the European Space Agency’s *Rosetta* mission, we present evidence that comet 67P/Churyumov-Gerasimenko likely formed through the gentle gravitational collapse of a bound clump of mm-sized dust aggregates (‘pebbles’), intermixed with microscopic ice particles. This formation scenario leads to a cometary make-up that is simultaneously compatible with the global porosity, homogeneity, tensile strength, thermal inertia, vertical temperature profiles, sizes and porosities of emitted dust and the steep increase in water-vapour production rate with decreasing heliocentric distance, measured by the instruments onboard the *Rosetta* spacecraft and the *Philae* lander. Our findings suggest that the pebbles observed to be abundant in protoplanetary discs around young stars provide the building material for comets and other minor bodies.

Key words: comets: individual: 67P/Churyumov-Gerasimenko – planets and satellites: formation – protoplanetary discs.

1 INTRODUCTION

Comets are thought to be primitive, because, owing to their small size, the amount of lithostatic compression and thermal metamorphism they experienced before they entered the inner Solar system is smaller than for larger bodies. For most of their life since formation they orbited the Sun at such large distances that they have

remained almost unaffected by solar irradiation. Thus, comets are the perfect witnesses to the processes that led to the formation of the planetesimals, the building blocks of the planets.

Due to the extended period of investigation of comet 67P/Churyumov-Gerasimenko (hereafter 67P) by the *Rosetta* spacecraft, which encompassed heliocentric distances between 3.6 and 1.2 au pre- and post-perihelion, and its comprehensive suite of experiments, our knowledge of 67P, and generally about comets, has increased enormously. For brevity, we refer to the *Rosetta* orbiter and *Philae* lander simply as *Rosetta*. The set of data delivered by *Rosetta* allows us to decipher the formation processes from

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$\sim \mu\text{m}$ -sized dust and ice particles to bodies with sizes of a few kilometres across. Simultaneously, the formation model will be used to derive measurable properties of active comets. These observables encompass structural parameters, such as size, porosity and homogeneity of the comet nucleus, as well as properties related to the activity of 67P, like outgassing rate and dust activity. Davidsson et al. (2016) have recently derived a comprehensive model for the formation of the bodies in the Kuiper Belt, which is based on the calculations of Weidenschilling (1997) who predicted that comets grow smoothly from microscopic particles all the way to kilometre sizes through accretion of bodies that are typically a factor of a few smaller in size than themselves. Thus, in this model there is no single characteristic size scale between the monomer grains and the cometesimal itself. In the following, we will show that the specific properties of 67P imply that it formed by the gentle gravitational collapse of a bound clump of mm-sized dust aggregates ('pebbles'), which survived to the present day, in contrast to the growth model by Weidenschilling (1997).

2 PLANETESIMAL FORMATION MODEL

The current understanding of how planetesimals form in a protoplanetary disc (PPD) is that initially all collisions among the solid dust or ice particles lead to sticking. This is because the van der Waals force (Heim et al. 1999) is strong enough to bind the grains together when they initially collide at very low speeds ($\ll 1 \text{ m s}^{-1}$; Weidenschilling 1977b). This hit-and-stick process leads to the formation of fractal aggregates (Blum et al. 2000; Krause & Blum 2004; Fulle & Blum 2017). If the solid particles are either non-icy or larger than $0.1 \mu\text{m}$ in size (Kataoka et al. 2013; Lorek, Lacerda & Blum 2017), fractal growth comes to a halt, when the impact energy exceeds the restructuring limit (Dominik & Tielens 1997; Blum & Wurm 2000). However, mutual collisions still lead to the growth of the aggregates until the bouncing barrier is reached for aggregate sizes of $\sim 1 \text{ cm}$ (Zsom et al. 2010) in an assumed minimum-mass solar nebula (MMSN) model (Weidenschilling 1977a) at 1 au, and $\sim 1 \text{ mm}$ in the comet-formation regions, respectively (Lorek et al. 2017), and perhaps larger for somewhat 'stickier' organic materials if the temperatures are $\sim 250 \text{ K}$ (Kudo et al. 2002). The growth times to the bouncing barrier are consistently ~ 1000 orbital time-scales (Lorek et al. 2017). This is within the lifetime of the solar nebula of a few million years (Ribas, Bouy & Merín 2015). Continued bouncing then leads to the rounding and compaction of the aggregates whose filling factor increases from $\phi_{\text{pebble}} \approx 0.05$ to $\phi_{\text{pebble}} \approx 0.40$ (Weidling et al. 2009). The filling factor of the aggregates describes the fraction of the pebble volume actually occupied by matter. The collision processes described here have been extensively investigated in the laboratory and can be considered robust (Blum & Wurm 2008; Güttler et al. 2010). The behaviour described above is valid for refractory materials but may change significantly for water ice with its tenfold increased sticking threshold (Kataoka et al. 2013; Gundlach & Blum 2015b). However, observations imply that the composition of 67P is dominated by non-volatile materials (Capaccioni et al. 2015; Fulle et al. 2016a; Quirico et al. 2016).

The next step in planetesimal formation is more controversial. We argue that planetesimal formation proceeded through spatial concentration of the mm-sized dust pebbles by the streaming instability (Youdin & Goodman 2005) that ultimately led to the formation of a gravitationally bound cloud of pebbles, which gently ($\lesssim 1 \text{ m s}^{-1}$) collapsed to form a planetesimal (Johansen et al. 2007; see Fig. 1). The streaming instability is a collective effect of dust particles. An

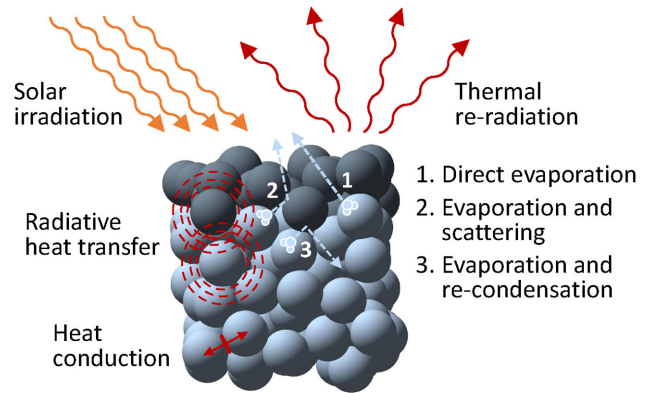


Figure 1. Schematic of the structure of comet nuclei. If comet nuclei formed by gentle gravitational collapse of a bound clump of dust aggregates, their packing morphology should be close to what is depicted in the figure. The dust pebbles are here shown as spheres and have a packing fraction of $\phi \approx 0.6$. At formation, the pebbles contain refractory materials and ices (light grey spheres). When approaching the Sun, pebbles close to the surface of the comet nucleus lose their icy constituents (dark grey spheres). Here, we assume that all pebbles whose centres are within two pebble radii above the ice line become desiccated. The evaporation of water molecules can either happen directly into vacuum (dashed arrow indexed 1), through a scattering process (2), or into the interior, where re-condensation occurs (3). The major energy flows are also indicated: absorption of solar radiation at the surface, re-radiation of heat from the surface, energy transport through the solid contacts between pebbles and thermal radiation in the interior of the comet nucleus, respectively.

individual dust particle with Stokes number $St \ll 1$ is suspended in the gas, which forces it to travel with sub-Keplerian velocity. This, in turn, leads to a rapid radial drift inwards (Weidenschilling 1977b). In contrast, a group of such grains is less affected and, thus, moves with a higher orbital velocity, which suppresses the radial drift. Here, the Stokes number is defined by $St = t_f \Omega_k$, with t_f being the particle stopping time in the gas and the Kepler frequency of the particle's orbit, respectively. If the concentration of the particles is sufficiently large, their feedback to the gas even strengthens the effect. Thus, such an instability region attracts all particles that cross its orbit, which leads to a rapid growth in mass concentration. If this concentration is high enough, the bound pebble cloud can gravitationally collapse to form a granular body (Johansen et al. 2007). It was shown that the dust-to-gas ratio¹ of the PPD plays an important role for the onset of the streaming instability. A slightly increased dust-to-gas ratio is required, while the streaming instability does not occur for solar metallicity (Carrera, Johansen & Davies 2015; Yang, Johansen & Carrera 2017). This means that planetesimal formation through the streaming instability must be delayed until part of the gaseous PPD has been dissipated. The disc lifetime is a few million years (Ribas et al. 2015) so that such a delayed planetesimal formation would also help to prevent the planetesimals from melting by short-lifetime radioactive decay (Davidsson et al. 2016).

The detection of extremely fluffy dust particles with filling factors $\lesssim 0.001$ (comprising ~ 1 per cent of the total mass, but consequently a much larger share of the volume of the comet nucleus) by the

¹ If we assume that in the comet-forming regions the temperatures were so low that basically all elements heavier than Helium were condensed, this value equals the 'metallicity'. In this context, 'dust' also encompasses the condensed volatiles, i.e. the ices, while 'gas' consists of H_2 and He, with only minor contributions of other species.

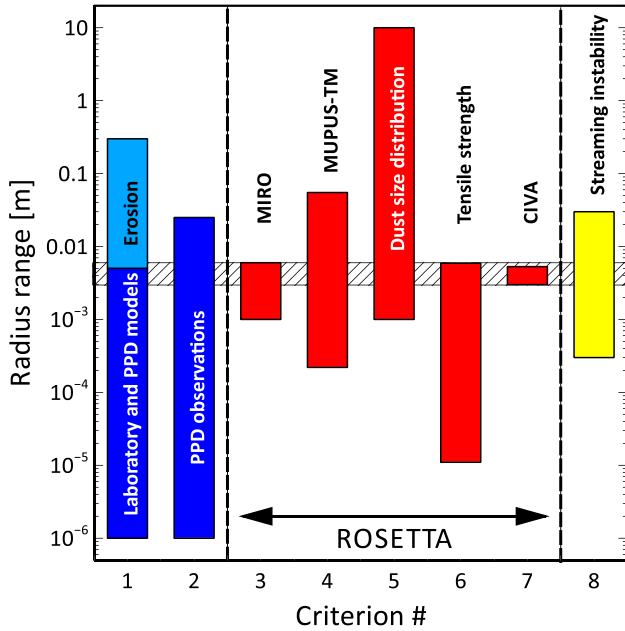


Figure 2. Size ranges of dust aggregates. From left to right: PPD models and observations (blue, criteria 1–2), *Rosetta* observations (red, criteria 3–7), and streaming instability criterion (yellow, criterion 8). The hatched region is the minimum width for pebble radii consistent with all *Rosetta* observations.

Rosetta/Grain Impact Analyser and Dust Accumulator (GIADA) instrument (Fulle et al. 2015) and the discovery of a fractal particle by the *Rosetta*/Micro-Imaging Dust Analysis System (MIDAS) instrument (Mannel et al. 2016) unambiguously show that the comet never experienced any global compression, because otherwise, the maximum yield strength of the fluffy aggregates would have been overcome and the aggregates compacted to filling factors $\phi_{\text{pebble}} \approx 0.4$. The maximum dynamic yield strength can be estimated following the numerical model by Dominik & Tielens (1997) and the experimental results by Blum & Wurm (2000) and is $Y = \rho v_{\text{mc}}^2/2 \approx 1$ Pa, with $v_{\text{mc}} \approx 1 \text{ m s}^{-1}$ and $\rho \approx 1 \text{ kg m}^{-3}$ being the impact velocity leading to maximum compaction (Dominik & Tielens 1997; Blum & Wurm 2000) and the mass density of the fractal aggregates, respectively.

A statistical analysis of the occurrence of showers of fluffy particles in the GIADA instrument shows that the fluffy parent aggregates must have had sizes on the order of a few mm (Fulle & Blum 2017). To fit these aggregates into the void spaces between the pebbles, the latter must have (average) radii of $a = 8.5 \text{ mm}$ (Fulle & Blum 2017). It should be mentioned that the porous dust aggregates detected by MIDAS and GIADA possess a fractal structure with consistent fractal dimensions, which establishes the co-existence of a fluffy/fractal and a pebble population (Fulle & Blum 2017). These fluffy aggregates must be intact remnants of the initial fractal dust agglomeration before impact compaction (Fulle & Blum 2017), as suggested by Mannel et al. (2016). Due to their slow relative velocities in the solar nebula, on the order of a few cm s^{-1} (Weidenschilling 1977b), collisions between the low-mass fluffy aggregates and the cm-sized pebbles result in sticking, without any significant compaction of the fluffy particles (Blum & Wurm 2008; Weidling et al. 2009; Güttler et al. 2010). The survival of fluffy dust aggregates until today is only possible if they were encased in the void space between the pebbles and if the pebbles survived the formation process of the

nucleus of 67P intact. The presence of fractal aggregates rules out all formation processes other than a gentle gravitational collapse of a bound clump of pebbles (Fulle & Blum 2017). In the alternative option, collisional coagulation, favoured by Davidsson et al. (2016), high-porosity or fractal dust aggregates would have experienced destructive high-speed (up to $\sim 50 \text{ m s}^{-1}$) collisions (Weidenschilling 1977b). In the following, we will show that the pebbles forming comet 67P have radii between ~ 3 and $\sim 6 \text{ mm}$, thus confirming that the presence of fractal dust in 67P requires a real change of paradigm regarding the collisional history of the outer Solar system (Farinella & Davis 1996; Morbidelli & Rickman 2015; Fulle & Blum 2017).

The question remains whether 67P was formed as we observe it today or through re-accretion of fragments from a catastrophic collision of an initially larger body (Morbidelli & Rickman 2015; Rickman et al. 2015). The fact that the pebbles stayed intact shows that the planetesimal that later became comet 67P had a radius of $< 50 \text{ km}$, because otherwise the collapse would have destroyed the pebbles (Bukhari Syed et al. 2017; Wahlberg Jansson et al. 2017). Recent numerical simulations indicate that a catastrophic collision between two pebble-pile objects can lead to the gravitational re-accretion of a km-sized body, preferentially from uncompressed and unheated material from the target body (Michel et al. 2016). Once the spatial resolution in such simulations is fine enough to follow the fate of individual pebbles, it may be decided whether or not such a secondary formation scenario of comet nuclei is in agreement with the presence of fractal dust aggregates.

3 THE SIZE OF THE PEBBLES FORMING COMET 67P

Below, we list arguments consistent with the pebble hypothesis of planetesimal formation. We will start with empirical, astronomical and theoretical aspects (criteria 1 and 2), followed by *Rosetta* observations of comet 67P (criteria 3–7), and finally will come back to the streaming instability criterion (criterion 8). In Fig. 2, we show ranges for the radii of the dust pebbles, either observed or theoretically predicted, for each of the eight items.

3.1 PPD models and observations

1. Pebble-size constraint from laboratory experiments and PPD models. From the standpoint of numerical disc simulations and laboratory data for the collisional behaviour of dust and ice aggregates, there are two obstacles that cannot be overcome. The first is the fragmentation barrier (dark blue in Fig. 2). When two dust aggregates collide above a certain impact velocity, disintegration of the dusty bodies is so strong that the largest surviving fragment has less mass than the original target (Bukhari Syed et al. 2017). In typical PPDs and outside dust-dominated sub-discs (where the velocities are not caused by dust-gas interactions and are, thus, very different), this means that collisions among bodies with size ratios ≤ 5 lead to the fragmentation of both bodies (Bukhari Syed et al. 2017) if they exceed $\sim 1 \text{ cm}$ in diameter for dust- and $\sim 10 \text{ cm}$ for ice-dominated materials, based upon velocities given by Weidenschilling (1997). The second obstacle is the erosion barrier (light blue in Fig. 2). Even if some ‘lucky survivors’ could escape catastrophic fragmentation, they cannot avoid being hit by small particles and agglomerates at relatively high velocities (exceptions are, again, dust-dominated sub-discs in turbulence-free dead zones). Experiments show that impacts by individual dust grains or small aggregates lead to mass loss of the target aggregate (Schräpler & Blum 2011; Krijt et al. 2015; Schräpler et al. 2017), which limits the radii to $\lesssim 30 \text{ cm}$ for dust

agglomerates in the region of 10–100 au. As the impact process liberates more fragments in the relevant size range than it consumes, erosion is inevitable.

Monte Carlo simulations using realistic collision physics show that the maximum aggregate size that can be achieved by direct coagulation depends on the heliocentric distance and monomer-grain size. Lorek et al. (2017) derived maximum aggregate masses between ~ 0.1 g at 5 au (only slightly dependent on monomer size) and $\sim 10^{-5}$ – 10^{-3} g at 50 au for 1–0.1 μm monomer size. With the fragmentation and erosion barriers (see above) in mind, we conclude that the maximum dust-aggregate diameter cannot exceed ~ 1 cm. Schr ppler et al. (2017) showed that the interplay between coagulation and erosion leads to a non-negligible mass fraction in very small grains and agglomerates so that we set the minimum dust size in Fig. 2 to 1 μm .

2. *Pebble-size constraint from observations of PPDs.* Over the past decades, observations of PPDs have been performed over a wide range of wavelengths (see e.g. the reviews by Williams & Cieza 2011; Testi et al. 2014). Visible and near-infrared observations of mostly scattered stellar light are sensitive to μm -sized dust and show the presence of these particles in PPDs of all ages (see e.g. the discussion in Dullemond & Dominik 2005). At longer wavelengths, thermal emission of large dust aggregates from close to the mid-plane dominates over scattering in the disc’s atmosphere. Very-long-wavelength observations show the presence of mm-sized and larger grains in PPDs (see e.g. van Boekel et al. 2004; D’Alessio et al. 2006; Natta et al. 2007; Birnstiel et al. 2010; Ricci et al. 2010; P rez et al. 2012).

At the current stage, it is unclear which aggregate sizes dominate the dust-mass spectrum of PPDs. However, there seems to be a size cut-off above which the abundance of larger grains considerably drops. Recently, spatially resolved observations of PPDs could determine this cut-off size for a range of distances to the central star. Testi et al. (2014) report that typically the size of the dust-emission region becomes smaller with increasing observation wavelength, which indicates that grain growth in the inner disc leads to larger grains than further out, in qualitative agreement with the model by Lorek et al. (2017). Testi et al. (2014) show two examples where mm-sized aggregates prevail at distances of 50–100 au, whereas around 20 au centimetre particles can be found. Recently, Tazzari et al. (2016) performed interferometric observations of three PPDs [including one source from the Testi et al. (2014) study] at wavelengths of 0.88–9.83 mm and derived the dust size cut-off of otherwise continuous size distributions at high spatial resolution. Similar to the two PPDs reported by Testi et al. (2014), Tazzari et al. (2016) found that the maximum dust-aggregate radii decrease with increasing distance to the central star: at 10 au, the pebble sizes are around 25 mm, whereas at 50 au, the maximum dust radii reach only 1–5 mm. Tazzari et al. (2016) analysed that the maximum size falls off with distance to the central star following a power law with exponent ~ -1.5 , whereas the Monte Carlo simulations by Lorek et al. (2017) find exponents $\gtrsim -1$. Dust properties at various distances to the central star have also been determined by Trotta et al. (2013), P rez et al. (2015) and Liu et al. (2017), which confirm grain growth with a maximum grain size decreasing with increasing distance.

These recent findings clearly prove the existence of pebble-sized dust aggregates at comet-formation distances. The maximum pebble size found by Tazzari et al. (2016) is shown in Fig. 2 as the maximum of the dust-size distribution and as a proxy for the many other measurements. Here, the full range of observed dust sizes in PPDs from micrometres to centimetres is displayed.

3.2 Observations of comet 67P by *Rosetta/Philae* instruments

3. *Pebble-size constraint from measurements of the sub-surface temperatures by MIRO.* The Microwave Instrument for the Rosetta Orbiter (MIRO) instrument was the only sensor onboard the *Rosetta* orbiter to measure the subsurface temperature of the cometary nucleus. MIRO is a microwave radiometer in two narrow sub-millimetre and millimetre wavelength bands at $\lambda_{\text{sub-mm}} = 0.533$ mm and $\lambda_{\text{mm}} = 1.594$ mm, respectively, with a relative bandwidth of $\Delta\lambda/\lambda = 2 \times 10^{-3}$ (Gulkis et al. 2015; Schloerb et al. 2015). Thus, MIRO measures the thermal fluxes emitted by the cometary material in the Rayleigh–Jeans wavelength regime. Typical penetration depths are up to a few centimetres, depending on the absorption efficiency of the cometary material at the two MIRO wavelengths. We applied a thermophysical model (see Appendix A) to a synthetic comet consisting of pebbles and determined the diurnal temperature evolution at depths of up to 50 cm for a wide range of pebble radii and absorption coefficients for a position of 25° northern latitude and a heliocentric distance of 3.27 au.

The basic ingredients of our thermophysical model are as follows:

(i) *Insolation.* Depending on the position of the comet on its orbit, the location of the point considered on the nucleus surface, the local time at this location and the Bond albedo, we determine the absorbed total solar flux (see the left-hand side of equation A1). This incoming heat is balanced by direct re-emission from the comet surface (the first term on the right-hand side of equation A1) and the amount of energy transported into the nucleus (the second term on the right-hand side of equation A1). As the depth to which the diurnal and orbital heat waves penetrate into the comet interior is much smaller than the horizontal resolution of the MIRO instrument, we consider the heat transport a one-dimensional (1D) problem.

(ii) *Heat transport mechanisms.* The physical processes that we consider as most important to the (vertical) heat transport are conduction through the matrix of dust grains in contact (the second term on the right-hand side of equation A2) and radiative heat exchange between the (assumed) dust pebbles (the first term on the right-hand side of equation A2), respectively. We neglect heat flow by mass transport of gas and dust. Both terms that contribute to the heat conductivity (equation A2) are heavily dependent on the dust-aggregate size, which we assume to be monodisperse. Fig. A1 shows this for three dust temperatures. For small aggregates, the heat conductivity decreases with increasing aggregate size, due to the decrease of the total inter-aggregate contact area per unit comet area (see the dashed line in Fig. A1). For large dust aggregates, radiative heat exchange dominates over conduction, because it linearly depends on the size of the void spaces between aggregates, which naturally scale with aggregate size. However, radiative heat transport is temperature dependent as shown by the three curves in Fig. A1. The minimum heat conductivity is on the order of $10^{-4} \text{ W m}^{-1} \text{ K}^{-1}$ and is reached for aggregate radii of 0.1 mm and a temperature of 100 K. If no pebbles were present and the comet consisted of a homogeneous dust matrix, the heat conductivity would be $\sim 2 \times 10^{-3} \text{ W m}^{-1} \text{ K}^{-1}$ (the horizontal solid line in Fig. A1). All material parameters that we used to derive these heat conductivities are shown in Table A1.

(iii) *Solving the heat-transport equation.* Knowing the energy input and the basic heat-transport mechanisms, the heat-transport equation (equation A8) is solved using the Crank–Nicolson method (see Appendix A for details). This results in a vertical temperature stratification as a function of time for each dust-aggregate size (see Fig. 3).

(iv) *Producing synthetic MIRO data.* To compare the derived temperature profiles with the data acquired by the MIRO instrument (Gulkis et al. 2015), the blackbody radiation emitted from

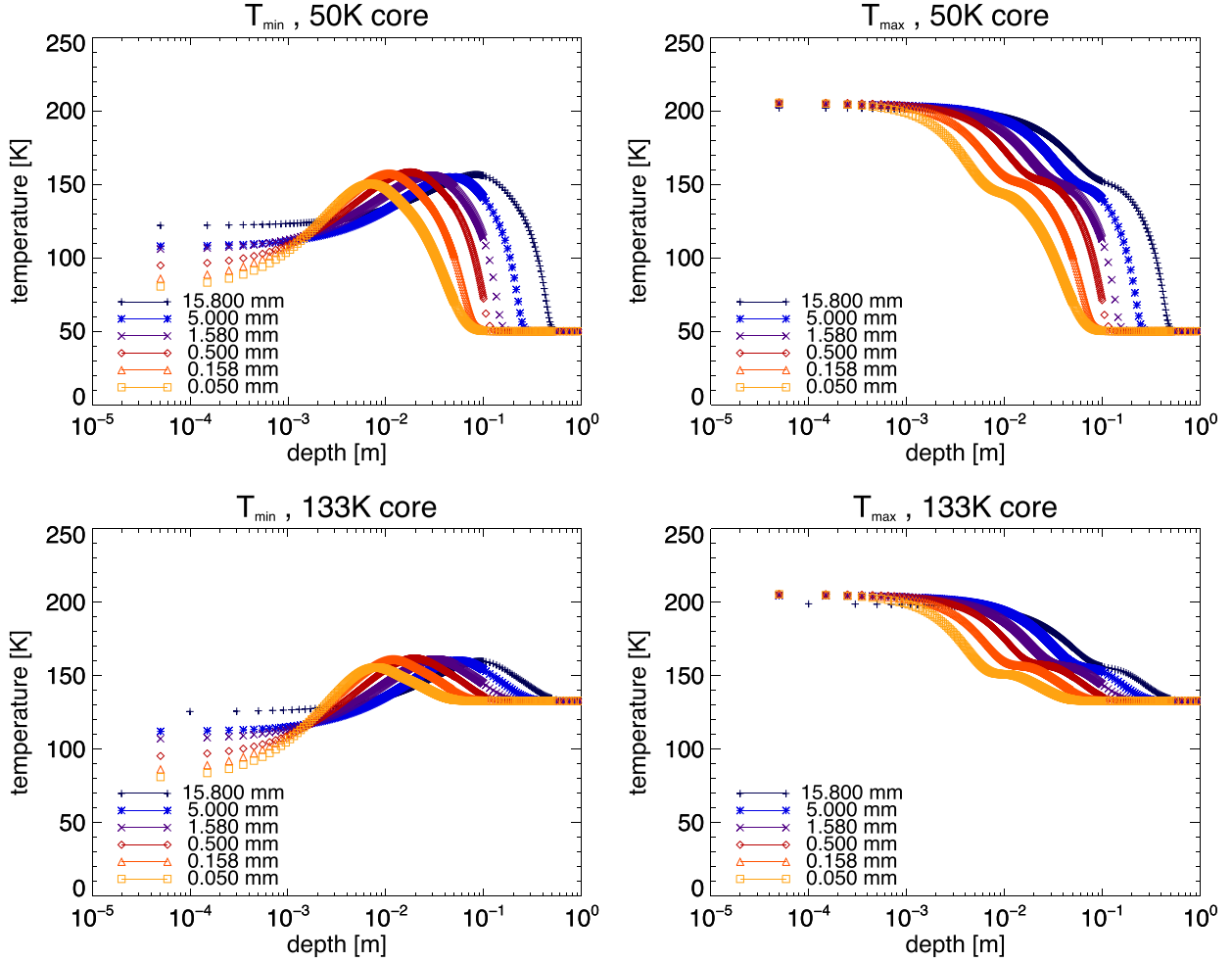


Figure 3. Snapshots of diurnal subsurface temperature profiles of a cometary nucleus that consists of dust aggregates of different sizes (marked by different colours, see legend) for minimum (left) and maximum (right) diurnal MIRO fluxes. The upper and lower plots show results for an initial temperature of 50 and 133 K, respectively.

different depths (and at different temperatures) inside the nucleus is integrated using the following emission-absorption algorithm,

$$F_{\lambda}(T) = \int_0^{\infty} \alpha_{\lambda} B_{\lambda}(T) e^{-\alpha_{\lambda} x} dx, \quad (1)$$

where x is the depth measured from the surface of the nucleus, α_{λ} is the length-absorption coefficient and $B_{\lambda}(T)$ is the Planck function for blackbody radiation. The integration is performed for the two different wavelengths used by the MIRO instrument, $\lambda_{\text{sub-mm}} = 0.533$ mm and $\lambda_{\text{mm}} = 1.594$ mm, respectively.

The integration of equation (1) is stopped at a finite depth when $F_{\lambda}(T)$ for the respective aggregate size saturates and, thus, no further flux contributions from deeper layers are expected.

We derived diurnal brightness temperatures by running the model until the diurnal heating and cooling cycle reached a steady state, with two initial temperatures of 50 and 133 K. As we could not realistically model the long-term evolution of the internal temperature of the comet, we chose these two extreme cases, which represent a cold (50 K) and warm (133 K) storage of the nucleus of 67P in recent history. In Fig. 3, we display two snapshots of the internal temperature distribution for each of the initial temperature conditions. The left two graphs show the time of minimum MIRO flux during a comet day at 3.27 au distance from the Sun, whereas the

right two plots characterize the temperature stratification for the diurnal maximum MIRO flux. The coloured curves represent internal temperatures for different dust-aggregate sizes, as indicated in the legend of Fig. 3.

It turned out that the results presented below are rather insensitive to the actual choice of the internal starting temperature. As can be seen in Fig. 3, the temperature variation with depth at night (left two graphs in Fig. 3) is entirely the same for both initial conditions down to depths where the maximum temperature is achieved, which depends on the aggregate size, due to the size-dependent radiative term in the heat-transport equation (see equations A2 and A3). Beneath the temperature maximum, the temperature drops quickly with increasing depth to the initial value. In full sunlight (right two graphs in Fig. 3), temperatures systematically decrease from the surface downwards until they reach a plateau, which indicates the depth of the previous-day heat wave. Also here, there is no difference in temperature stratification between the two initial cases upwards of this plateau. For deeper layers, the sudden drop to the initial temperature is similar to the night-time case. As most of the MIRO flux stems from the topmost few centimetres and increases with increasing temperature, the actual choice of the initial condition makes only a small difference in the synthetic MIRO data (see Fig. 5 below).

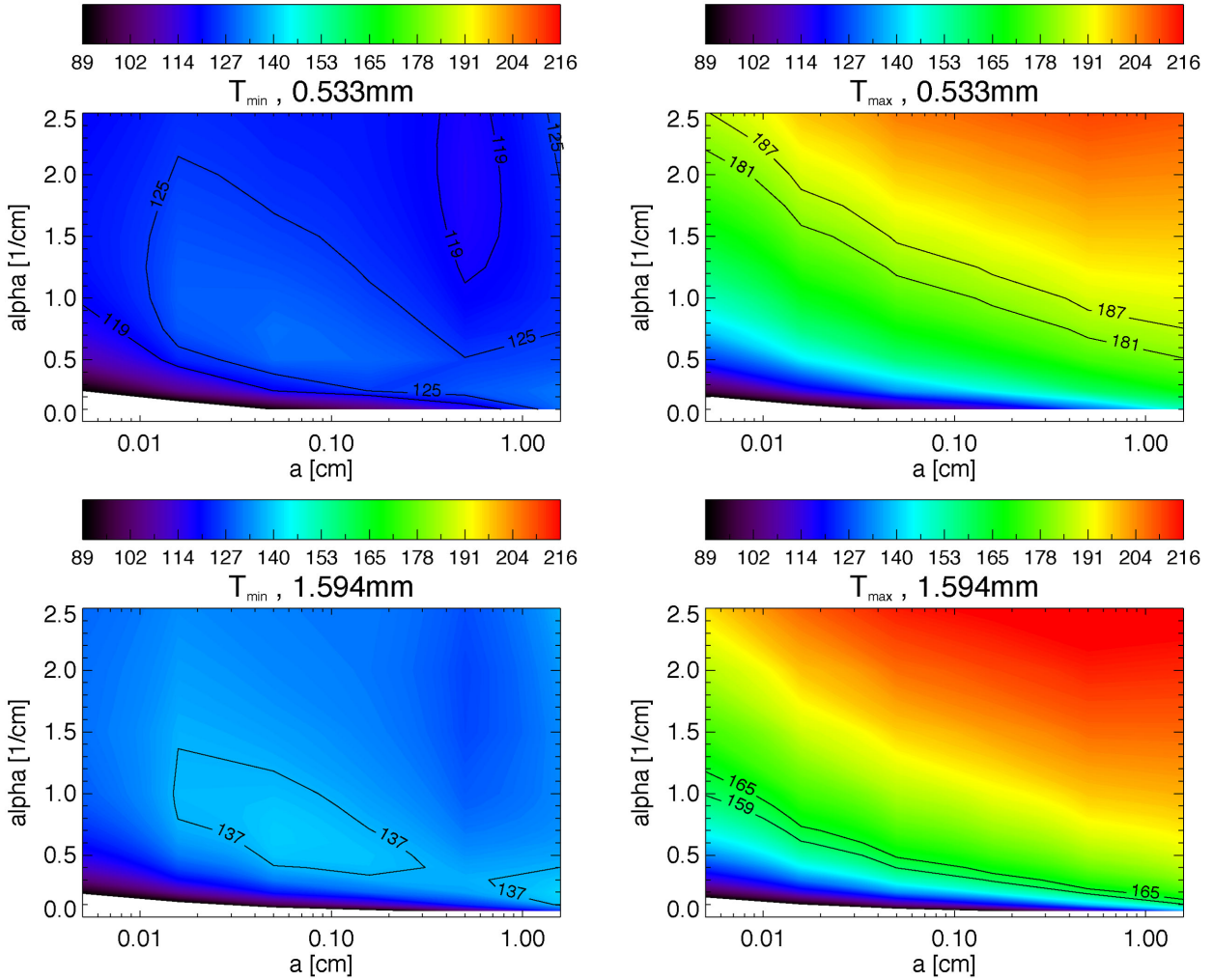


Figure 4. Simulation results for minimum and maximum diurnal MIRO temperatures for an initial temperature of 50 K. Minimum (two left-hand panels) and maximum diurnal temperatures (two right-hand panels) are indicated by colours (see colour bar) as a function of pebble radius (x -axis) and absorption coefficient (y -axis) for the sub-mm channel (upper two panels) and the mm-channel of MIRO (lower two panels). The contours mark the two extreme temperatures that are in agreement with the MIRO data, i.e. a good match between synthetic and measured data can be found between the contours.

We then compared for both initial temperatures the expected monochromatic emission temperature of the comet for the two MIRO wavelengths, calculated following equation (1), with the subsurface temperature measurements by MIRO (see Fig. 5 in Gulikis et al. 2015). We used a maximum illumination intensity of $\cos\vartheta = 0.96$ in equation (A1), representing the MIRO measurements (Gulikis et al. 2015) at northern latitude of 25° . As the criterion of match between the MIRO observations and model calculations, we chose the minimum and maximum diurnal temperatures measured by MIRO. These are for the sub-mm channel² $T_{\min} = (122 \pm 3)$ K and $T_{\max} = (184 \pm 3)$ K and for the mm-channel $T_{\min} = (140 \pm 3)$ K and $T_{\max} = (162 \pm 3)$ K, respectively. We systematically varied the absorption coefficient for the material in the range of $\alpha_{\text{sub-mm}} = 0.25\text{--}50\text{ cm}^{-1}$ (in steps of 0.25 cm^{-1}) for the sub-mm channel and $\alpha_{\text{mm}} = 0.10\text{--}50\text{ cm}^{-1}$ (in steps of 0.10 cm^{-1} for $\alpha_{\text{mm}} \leq 1.0\text{ cm}^{-1}$ and in steps of 1.0 cm^{-1} for $\alpha_{\text{mm}} > 1.0\text{ cm}^{-1}$)

² The temperature values in the sub-mm channel were increased by 6 per cent relative to Gulikis et al. (2015), due to a 94 per cent beam efficiency (see Schloerb et al. 2015).

in the mm channel. Pebble radii were varied between $a = 50\text{ }\mu\text{m}$ and $a = 1.58\text{ cm}$ in logarithmically equidistant steps of $\sqrt{10}$.

Fig. 4 shows a mosaic of derived minimum and maximum temperatures for the two MIRO wavelengths in the aggregate-size and absorption-coefficient range described above and for an initial temperature of 50 K. For both MIRO channels, an anticorrelation between the required absorption coefficient and the aggregate size can be discerned. This degeneracy is evident when Fig. 3 is examined. Due the dominance of radiative heat transport and the corresponding linear dependency of the heat conductivity on the pebble size (see Appendix A), the diurnal penetration depth of the heat wave scales with the square root of the pebble radius. To achieve the same synthetic MIRO temperature, the absorption coefficient therefore has to decrease with increasing dust-aggregate size. The two contours in each of the four panels of Fig. 4 denote the boundaries of the measured MIRO temperature ranges as defined above. A formal agreement between the synthetic and measured MIRO data can be achieved in both MIRO channels for dust-aggregate sizes of a few millimetres. However, while the range of maximum synthetic MIRO temperatures is quite large for the various aggregate sizes and absorption lengths, the minimum temperatures are relatively

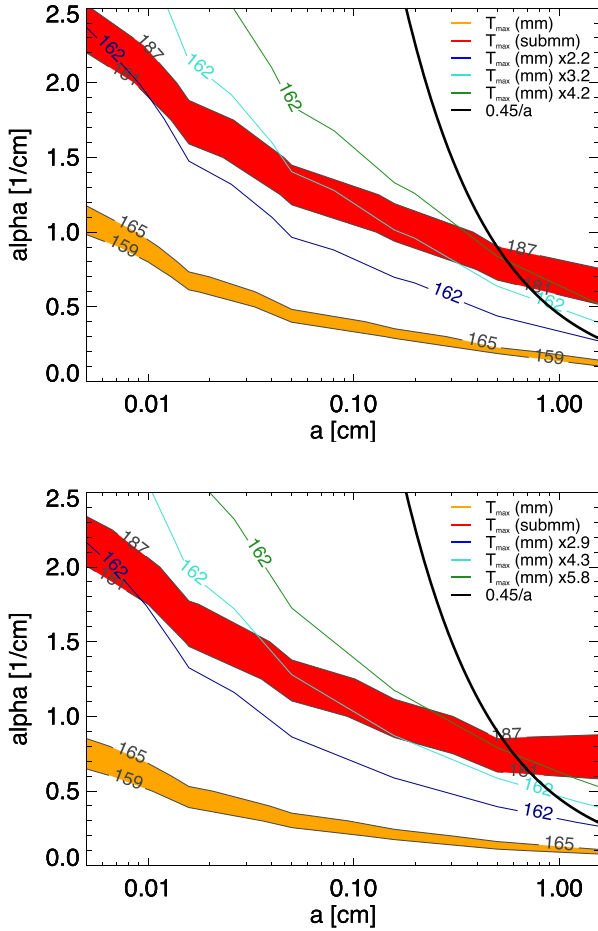


Figure 5. Comparison between measured and modelled maximum diurnal MIRO temperatures. As broad coloured bands, pebble radii (x -axis) and absorption coefficients (y -axis) are shown for which the synthetic and measured maximum temperatures overlap for the sub-mm channel (upper red band) and the mm-channel (lower orange band) of MIRO. The blue, turquoise and green curves denote $2.2\times$, $3.2\times$ and $4.2\times \alpha_{\text{mm}}$ (50 K initial temperature, upper plot) and $2.9\times$, $4.3\times$ and $5.8\times \alpha_{\text{mm}}$ (133 K initial temperature, lower plot) the mm-curve, respectively. The black curve denotes the maximum possible absorption length (see the text for details).

insensitive to changes in these parameters (see Fig. 4). Thus, the MIRO minimum-temperature measurements do not efficiently constrain the aggregate sizes so that we need additional aggregate-size restrictions, which will be discussed hereafter.

A comparison of the two MIRO channels for the maximum MIRO temperatures is shown in Fig. 5, where the red (sub-mm channel) and orange (mm channel) bands in the plot denote the aggregate-size and absorption-coefficient ranges for which an agreement between the MIRO measurements and the simulations could be achieved for both starting temperatures. As noted above, we cannot derive the aggregate sizes on comet 67P with this data alone, due to the degeneracy between aggregate size and absorption length. However, we can use additional information on the absorption coefficient to exclude very large and very small aggregate sizes, respectively. Assuming a dust-aggregate radius a and optically thick aggregates, the maximum absorption coefficient is given by geometrical optics and reads $\alpha_{\text{max}} = n \pi a^2$, with n being the number density of the aggregates. We assume a packing density of $\phi = 0.6$, which is close to the random close packing (RCP) limit (see Section 4.1), and get

$\alpha_{\text{max}} = \frac{3\phi}{4a} = \frac{0.45}{a}$. This relation between the absorption coefficient and aggregate size is shown as a solid black line in Fig. 5. It is evident that for aggregate sizes larger than $a \approx 6$ mm (independent of the initial temperature); the calculated absorption coefficient exceeds the geometrical value for perfectly absorbing particles so that we can exclude aggregates with these sizes. In the above analysis, we neglected surface reflection, which in principle can enlarge the distance travelled by the heat wave before it escapes the surface over the geometrical depth. However, this effect should be small for mm-sized aggregates and geometrical depths of ~ 10 cm, because of the rather low permittivity ϵ of the nucleus material. For $\epsilon = 1.27$, as measured by the Rosetta/Comet Nucleus Sounding Experiment by Radiowave Transmission (CONCERT) instrument (Kofman et al. 2015), and under the assumption that this value does not change too much from metre to millimetre wavelengths, we get a surface reflectivity of only 0.4 per cent, which leads to a total reflection loss over 10 cm depths of ~ 8 per cent for aggregates with $a = 5$ mm.

The ratio between the calculated values of the absorption coefficient for the two MIRO wavelengths, $\alpha_{\text{sub-mm}}/\alpha_{\text{mm}}$ can be estimated from Fig. 5. The blue, turquoise and green curves denote $2.2\times$, $3.2\times$ and $4.2\times \alpha_{\text{mm}}$ (50 K initial temperature, upper plot) and $2.9\times$, $4.3\times$ and $5.8\times \alpha_{\text{mm}}$ (133 K initial temperature, lower plot) the mm-curve, respectively. We can derive from Fig. 5 that $\alpha_{\text{sub-mm}}/\alpha_{\text{mm}} \approx 2.2 \dots 4.2$ ($T = 50$ K) and $\alpha_{\text{sub-mm}}/\alpha_{\text{mm}} \approx 2.9 \dots 5.8$ ($T = 133$ K), respectively. As the ratio of the MIRO frequencies ν is exactly 3, we get a spectral index of $\beta' = \frac{d \log \alpha}{d \log \nu} = 0.7 \dots 1.3$ ($T = 50$ K) and $\beta' = \frac{d \log \alpha}{d \log \nu} = 1.0 \dots 1.6$ ($T = 133$ K), with the lower β' values for the smaller dust aggregates.

Draine (2006), Natta et al. (2007) and Testi et al. (2014) showed that a value of $\beta' \approx 1$ for wavelengths around 1 mm is characteristic for MRN-type size distributions with size cut-off of $a_{\text{max}} \gtrsim 1$ mm. For size distributions with smaller maximum sizes, β' typically reaches values of $\beta' \approx 2$ for mm wavelengths. Menu et al. (2014) showed that the resulting dust opacities (see below) are in agreement with models of mixtures of amorphous silicates and carbonaceous material if the contributions from sub-mm-sized dust aggregates are negligible. From this analysis, we conclude that the most likely aggregate sizes to explain the MIRO measurements fall into the range $a \approx 1$ mm to $a \approx 6$ mm. We should like to point out that in the above analysis, we ignored electromagnetic interference between neighbouring dust aggregates. Although this might be a crude approximation, near-field effects are probably of small importance for materials with small index of refraction, as suggested by the low opacities at mm wavelength and low permittivity of $\epsilon = 1.27$ measured by CONCERT at 3.3 m wavelength (Kofman et al. 2015).

It should also be mentioned that for this analysis, we ignored the heat sink due to ice sublimation because of the low outgassing rate at 3.27 au. Details about the influence of outgassing rate on the internal temperatures can be found in Appendix A. However, future investigations will have to take the latent heat of water ice and the ice-dust boundary as a free parameter into account.

With a mass density of comet 67P of 0.53 g cm^{-3} (Jorda et al. 2016), we convert the derived absorption coefficients $\alpha_{\text{sub-mm}} \approx 0.8\text{--}1.2 \text{ cm}^{-1}$ and $\alpha_{\text{mm}} \approx 0.2\text{--}0.4 \text{ cm}^{-1}$ for a dust-aggregate size range of $a = 1\text{--}6$ mm (see Fig. 5) into mass-absorption coefficients (opacities) of $\kappa_{\text{sub-mm}} \approx 1.5\text{--}2.3 \text{ cm}^2 \text{ g}^{-1}$ and $\kappa_{\text{mm}} = 0.4\text{--}0.8 \text{ cm}^2 \text{ g}^{-1}$, respectively. These values are slightly higher than those calculated by Draine (2006) for astrosilicate, but seem to be typical for carbonaceous material, and provide for the first time

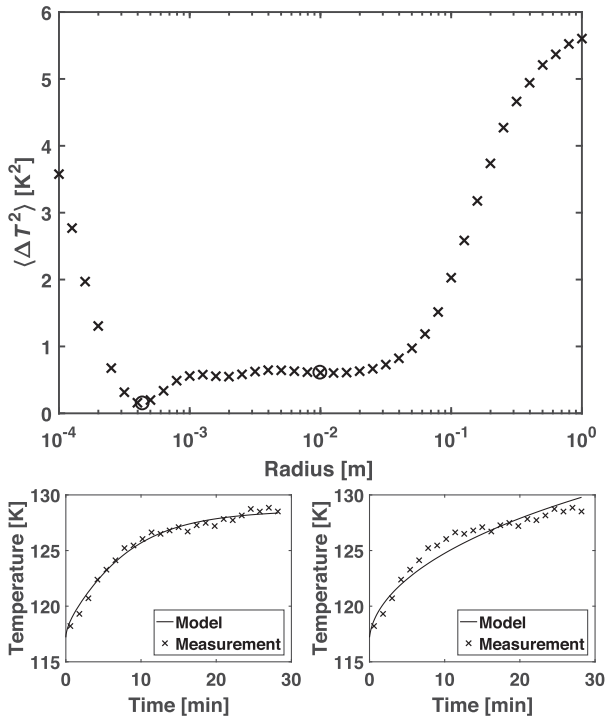


Figure 6. Comparison between MUPUS-TM data and the model. Top: Mean squared temperature deviation between the measurements and the FEM model of the comet surface for different pebble radii. Bottom: Surface temperature of comet 67P measured by MUPUS-TM (crosses; Spohn et al. 2015) and best-fitting model (solid curves) with a pebble radius of $a = 0.44$ mm (bottom left) and $a = 10$ mm (bottom right).

direct estimates of these important properties (albeit for a complex hierarchical arrangement of aggregates), which will be helpful in future modelling of dust processes in protoplanetary and debris discs. As mentioned above, the opacities derived by Menu et al. (2014) for a mixture of silicates and carbonaceous material are in broad agreement with our estimates when the aggregates are typically millimetre sized.

4. Pebble-size constraint from the surface heating curve measured by Philae. The infrared radiometer Multi Purpose Sensors for Surface and Subsurface Science - Thermal Mapper (MUPUS-TM) recorded the surface temperature of the landing site of *Philae* (Spohn et al. 2015) over a total period of 40 h. Although the observed surface was most of the time in shadow, for short (~ 40 min) periods of insolation, the temperature rose from ~ 117 to ~ 129 K and then dropped off again. As MUPUS-TM recorded thermal-infrared radiation, we modelled by the finite element method (FEM) the temperature of a surface layer of equal-sized spherical pebbles when the insolation is momentarily switched on (see Appendix B).

Fig. 6 shows the values of the mean squared temperature deviation between the measurement and the FEM model as a function of pebble radius for the case of full illumination of the area observed by MUPUS-TM ($f_s = 1$ in equation B6). The best-fitting value of $a = 0.44$ mm is clearly the global minimum within four decades of realistic radii. However, a wide range of pebble radii from $a = 0.22$ to 55 mm solve the equations with $\langle \Delta T^2 \rangle \lesssim 1$ K², which is about the noise level in the MUPUS-TM data. Outside this radius range, the mean squared temperature deviation increases drastically (see Fig. 6). Smaller dust aggregates heat too fast to fit the measurements, whereas for larger pebbles the heat wave does not penetrate deep enough, which also leads to a mismatch between the measured and modelled temperatures.

The goodness of fit can also be seen in Fig. 6, where the MUPUS-TM data from Spohn et al. (2015) are shown as crosses together with the results of the FEM model (solid curves) for the best-fitting radius of $a = 0.44$ mm and an illumination factor of $f_{I\odot} = 0.16$ (see Appendix B) as well as for a pebble with a radius of $a = 10$ mm and an illumination factor of $f_{I\odot} = 0.24$. The same values were achieved for both limiting cases of the ambient temperature used for the heat exchange of the bottom sphere surface discussed in item (iii) of the model assumptions (see Appendix B). Deviations from the illumination of the whole observation area of the MUPUS-TM sensor, as described by equation (B6), with either a constant or a time-dependent fractional illuminated area do not influence the result for the size distribution of pebbles.

If we assume that the comet-nucleus surface does not consist of spherical pebbles, but is made of a layer of μ m-sized dust particles with a filling factor of $\phi = 0.4$, we can use the model shown in Appendix B and derive the optimal thickness of this dust layer to match the temperatures observed by MUPUS-TM. We get a reasonable fit (with a $\langle \Delta T^2 \rangle$ very similar to that shown in Fig. 6) when the half-thickness of the dust layer is between 100 μ m and 10 cm. For a thickness outside this range, $\langle \Delta T^2 \rangle$ increases similarly rapidly as in the case with pebbles. Thus, the measurements by MUPUS-TM indicate a characteristic size as shown in Fig. 2.

5. Pebble-size constraint from the size distribution of dust observed by Rosetta. The various dust-sensitive instruments onboard *Rosetta* and *Philae* (COSIMA, GIADA, OSIRIS, ROLIS) have detected individual size-frequency distributions of the dust over many orders of magnitude in diameter (see Appendix C). Taking these individual data sets and fitting piecewise power laws of the form $n(a)da \propto a^\beta da$, with $n(a)da$ being the number of detected dust particles in the radius range between a and $a + da$, shows that the exponent of the size-frequency distribution, β , systematically varies with the dust size (see discussion in Appendix C). A power-law size-frequency distribution translates into a total mass per logarithmic size bin of $M(a) \propto n(a)a^4 \propto a^{4+\beta}$. For $\beta < -4$, the logarithmic mass distribution function is dominated by the small-mass end, whereas for $\beta > -4$, the large particles dominate. The mass-dominating grains with $\beta \approx -4$ are present in the size range between millimetres and a few metres (see Fig. 7). Although one has to be careful with the assumption of a single continuous mass-distribution function throughout the observable size range, it is clear that pebble-sized dust aggregates are very abundant in comet 67P.

6. Pebble-size constraint from measurements of the tensile strength of comet 67P. For small bodies, it is not only gravity that keeps the objects in shape, but the internal cohesion plays an important role (Gundlach & Blum 2015a), which is caused by the mutual van der Waals attraction between dust grains in contact. A measure of the cohesion is the tensile strength of the material, i.e. the detachment force per effective particle cross-section. The various *Rosetta* instruments derived tensile strengths of 3–15 Pa and 10–20 Pa for the 67P surface material on a scale of 10s of metres (Groussin et al. 2015; Thomas et al. 2015) and 10–200 Pa for the bulk comet (Hirabayashi et al. 2016).

In general, the tensile strength of a particulate material is determined by the number of grain–grain contacts per unit cross-section. For a homogeneous material with no pebbles, only the packing density of the grains can alter the bulk cohesion. As the typical cohesion force between μ m-sized silica grains is on the order of 10^{-7} N (Heim et al. 1999), a network of these grains with a filling factor of $\phi = 0.20$ –0.54 possesses a tensile strength of 1000–3700 Pa (Blum & Schr ppler 2004). This was also recently confirmed to be the case for the sub-mm-sized dust aggregates entering the COSIMA instrument of *Rosetta* (Hornung et al. 2016). Organic material may

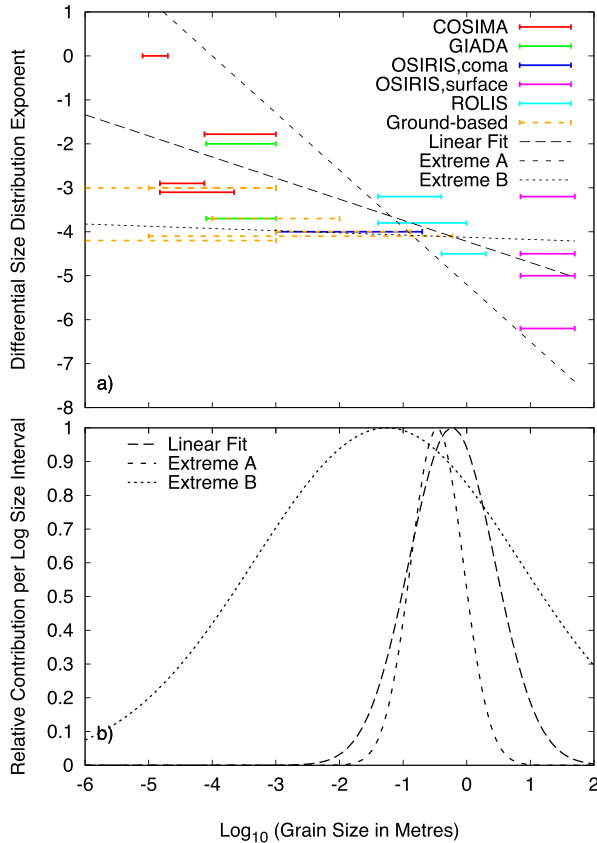


Figure 7. Particle size distribution for comet 67P. (a) Exponent of the size-frequency distribution function, β , of the dust emitted from the nucleus of comet 67P. Data (horizontal lines) stem from measurements by various instruments onboard *Rosetta* and from Earth-based observations. The three lines represent a linear fit to the data and two extreme approximations, one very steep and one very shallow. (b) Derived normalized mass-frequency distributions per logarithmic size interval for the three linear approximations shown in panel (a). For a flat line at $\beta = 4$ in panel (a), all size bins would contribute equally to the mass.

slightly lower these values, whereas for water ice in hexagonal form and for temperatures $\lesssim 200$ K, relevant for the sub-surface activity regions of comet 67P, tensile strengths will be a factor of ~ 10 higher (Gundlach et al. 2011b; Gundlach & Blum 2015b). Monomer-grain sizes smaller than $\sim 1 \mu\text{m}$ will also increase the tensile strength.

However, if the comet nucleus consists of a hierarchical arrangement of pebble-sized dust aggregates, it is the cohesion between these aggregates that determines the overall tensile strength of the comet, although the pebbles themselves possess much higher internal strengths (Blum et al. 2014, 2015). For low compression (as is the case for cometary nuclei, see Section 4.2), the contact area between two touching aggregates is much smaller than their cross-section so that the bulk tensile strength is reduced in comparison to a homogeneous dusty body. For spherical dust aggregates of radius a consisting of μm -sized silica particles, the bulk tensile strength of a cluster of pebbles with $\phi_{\text{pebble}} = 0.4$ and packed with $\phi = 0.6$ is

$$\Sigma = 0.21 \text{ Pa} \times \left(\frac{a}{1 \text{ cm}} \right)^{-2/3} \quad (2)$$

(Skorov & Blum 2012; Blum et al. 2014).

Thus, the derived tensile-strength values for comet 67P (see above) cannot be reconciled with a homogeneous dusty compo-

sition of the nucleus. This rules out any collisional-growth-only models for planetesimals (see e.g. Windmark et al. 2012), which rely on mass accretion in high-velocity impacts, because they compress the material to its densest state of $\phi \approx 0.4$ (Güttler et al. 2010) and lead to too high tensile strengths and bulk porosities much lower than the measured values for comet 67P (Kofman et al. 2015; Fulle et al. 2016b; Pätzold et al. 2016).

Taking into account that the derived bulk value for the tensile strength of comet 67P (see Hirabayashi et al. 2016) is also influenced by gravity – the central lithostatic compression of the large lobe of comet 67P is ~ 86 Pa (see below) – and that on scales of 10s of metres or larger water ice is present, which may increase the tensile strength by a factor of 10, we argue that the desiccated (water-ice-free) dust should have a tensile strength between $\Sigma = 0.3$ Pa (water ice dominates the tensile strength in the measurements) and $\Sigma = 20$ Pa (water ice is unimportant for the measured tensile strength). Thus, we get with equation (2) a range of pebble radii between $a_{\text{min}} = 0.0011$ cm and $a_{\text{max}} = 0.59$ cm.

If the gas pressure at the bottom of the ice-free dust layer close to the surface of a comet nucleus exceeds the tensile strength, the whole layer is locally torn off and accelerated away from the comet. As long as the incoming solar heat flux is sufficiently large, the process of build-up and destruction of an ice-free pebble crust is repetitive and defines the dust activity of the comet. As the model cannot predict the lateral extent of the emitted dust layer, we can only speculate that the observation of free-flying dust with sizes of a few decimetres (see point 5 in this section) is due to the ‘folding’ of initially flat clusters of pebbles. The folding process is physically plausible, because the pattern of the gas flow around the cluster causes stresses within the cluster that can easily overcome the rolling resistance so that the cluster collapses to a spheroidal shape. Tensile-strength values of ~ 1 Pa at the surface of 67P are not in contradiction to measured bulk values of 10–200 Pa (Hirabayashi et al. 2016), because the increased lithostatic pressure towards the centre leads to an enduring increased tensile strength (Blum et al. 2014, 2015; Gundlach & Blum 2016). Given the size of the lobes of 67P and the increased stickiness of water ice (Gundlach & Blum 2015b) over the desiccated surface material, a range of 10–100 Pa is expected. On top of that, the gravitational strength towards the centre of 67P should be on the order of 100 Pa (Gundlach & Blum 2016).

Finally, it should be noted that the tensile-strength values measured on the surface of comet 67P (3–15 Pa; Groussin et al. 2015) are possibly an upper limit, because cliffs with lower tensile strengths would have collapsed at smaller sizes and to smaller fragments and, thus, may have escaped observations by *Rosetta*/Optical, Spectroscopic, and Infrared Remote Imaging System (OSIRIS).

7. Pebble-size constraint from direct observations by the CIVA camera on Philae. Direct observation of resolved positive relief features with sub-cm spatial resolution was possible with the Comet Infrared and Visible Analyser (CIVA) instrument on *Philae*. The 695 pebbles found on CIVA images #3 and #4 possess diameters between 3.7 and 16.25 mm (Poulet et al. 2016). Their cumulative size distribution cannot be fitted with a single power law and is very steep at the large end and very flat at the small end. The size range within one standard deviation from the median of the 412 pebbles of the CIVA image #4 is 6.0–10.6 mm. Thus, the pebble radii are between $a = 3.0$ and 5.3 mm.

3.3 Streaming instability criterion

8. Pebble-size constraint from the streaming instability. The streaming instability is capable of concentrating dust particles with Stokes

numbers around $St \approx 0.1$ (Carrera et al. 2015; Yang et al. 2017). Larger particles possess larger stopping times so that the Stokes number is also a measure for the dust size. However, not all particle sizes are equally well concentrated. While concentration of pebbles with $St \approx 0.1$ is feasible for dust-to-gas ratios of $Z = \Sigma_s/\Sigma_g \approx 0.015$ (where Σ_s and Σ_g are the surface densities of the solid and gaseous components of the PPD), smaller and larger pebbles require higher metallicities, e.g. $Z \approx 0.02$ for $St \approx 0.006$ and $St \approx 0.6$ (Yang et al. 2017). Assuming a MMSN model Weidenschilling (1977a), the mid-plane gas density of the solar PPD at 30 au was $3 \times 10^{-13} \text{ g cm}^{-3}$, the mid-plane temperature was 50 K, and the metallicity was $Z \approx 0.01$. Using published gas-drag equations (Weidenschilling 1977b) and scaling the required higher dust-to-gas ratios of $Z = 0.02$ by respective lower gas densities, caused, e.g., by partial dissipation of the solar nebula, we get pebble radii between $a_{\min} = 3 \times 10^{-4} \text{ m}$ and $a_{\max} = 0.03 \text{ m}$ for which the streaming instability should work.

3.4 How large are the pebbles forming comet 67P?

It must be emphasized that different observations are sensitive to different pebble ‘size’ definitions. While the temperature-sensitive devices (MUPUS-TM, MIRO) mostly react on the volume-to-surface ratio of the pebbles, i.e. linearly with pebble size, the tensile strength scales with pebble radius to the power of $-2/3$, the detection of dust by imaging is sensitive to the cross-section of the particles, i.e. scales with radius squared, and the dust size distributions shown in Fig. 7 use a variety of analyses and can mostly not distinguish between homogeneous dust aggregates and clusters thereof. We do not necessarily expect a straightforward agreement of all derived pebble radii if the true pebble sizes are non-monodisperse. No single observation should be overemphasized (and over-interpreted) to constrain the formation process of comet 67P. However, a comparison between the different criteria (see Fig. 2) shows that a reasonable consensus can be reached among all measurements shown above for pebble radii in the range from $a \approx 3$ to $\approx 6 \text{ mm}$, denoted by the hatched area in Fig. 2. It is interesting to note that this size range falls right into the minimum of the metallicity-Stokes number curve derived by Yang et al. (2017) for the transition between non-SI and SI regimes of the PPD, assuming gas densities as in the MMSN model. Thus, a metallicity of $Z \gtrsim 0.015$, only slightly raised above the solar value, is required.

4 DISCUSSION

Using the above result that comet 67P likely formed by a gentle gravitational collapse of a bound clump of mm-sized dust pebbles, we will now make predictions about its properties and will show that these are in agreement with observations.

4.1 Porosity

If we consider the structure of a planetesimal formed by the gentle gravitational collapse of a bound clump of pebbles, we can derive its volume filling factor (Skorov & Blum 2012) and compare it to that of the nucleus of comet 67P. It must be noted that for a total mass of collapsing pebbles corresponding to a final planetesimal radius of 50 km or smaller, the mutual collisions of the pebble-sized dust aggregates are so gentle that they neither get further compacted nor fragmented (Wahlberg Jansson & Johansen 2014; Wahlberg Jansson et al. 2017). Thus, the volume filling factor of the pebble-sized dust aggregates is determined by the bouncing phase before transport to the outer solar nebula, which yields ϕ_{pebble}

≈ 0.4 (Weidling et al. 2009; Zsom et al. 2010). In addition, the pebbles will be randomly packed throughout the volume of the planetesimal. There is insufficient gravitational stress to considerably deform or break individual aggregates inside the planetesimal (Groussin et al. 2015, but see also below). Hence, the volume filling factor of the pebbles has to fall between random loose packing (RLP) and RCP values (Onoda & Liniger 1990). RLP is the loosest possible configuration under which low-cohesion spheres can pack and has a volume filling factor for low-gravity objects of $\phi_{\text{RLP}} = 0.56$ (Onoda & Liniger 1990). As the gravitational stress inside comet 67P is on the order of $\sim 100 \text{ Pa}$ and, thus, higher than cohesive and shear strengths, the pebbles will always arrange in the densest possible configuration. Any external perturbations, such as vibrations or lithostatic stresses, will cause a further densification up to the RCP limit, which has been determined for equal-size spheres to be $\phi_{\text{RCP}} = 0.64$ (Onoda & Liniger 1990). For polydisperse spheres, the RCP can reach somewhat higher limits, e.g. $\phi_{\text{RCP}} = 0.68$ for a log-normal size distribution with a standard deviation of 0.3 (Baranau & Tallarek 2014). Thus, we expect a total volume filling factor for the planetesimal between $\phi_{\text{tot}} = \phi_{\text{pebble}} \times \phi_{\text{RLP}} = 0.22$ and $\phi_{\text{tot}} = \phi_{\text{pebble}} \times \phi_{\text{RCP}} = 0.26 \dots 0.27$ (or slightly higher for higher degrees of polydispersity among the pebbles). If the volume filling factor of the pebbles is $\phi_{\text{pebble}} = 0.46$, as recently inferred from *Rosetta*/GIADA measurements (Fulle et al. 2016b), we get $\phi_{\text{tot}} = \phi_{\text{pebble}} \times \phi_{\text{RLP}} = 0.26$ and $\phi_{\text{tot}} = \phi_{\text{pebble}} \times \phi_{\text{RCP}} = 0.29 \dots 0.31$, respectively. Due to the high porosity contrast between pebbles and fractal aggregates, we here disregard that the void spaces among the pebbles are not empty but filled with fluffy dust clusters (Fulle & Blum 2017).

The derivation of the total volume filling factor for comet 67P naturally depends on the assumed dust-to-ice ratio and material parameters (mass density, gas permittivity). In the literature, the inferred values are $\phi_{\text{tot}} = 0.25 \dots 0.30$ (derived through gravity field measured by the Rosetta Radio Science Investigation (RSI); Pätzold et al. 2016), $\phi_{\text{tot}} = 0.21 \dots 0.37$ (derived through direct density measurements of the pebbles by GIADA; Fulle et al. 2016b), and $\phi_{\text{tot}} = 0.15 \dots 0.25$ (derived through the permittivity measured by CONSERT; Kofman et al. 2015), respectively. Taking into account the individual uncertainties and underlying assumptions, we can state that the most likely values for the volume filling factor are in the range $\phi_{\text{tot}} = 0.25 \dots 0.31$. This is in excellent agreement with our prediction.

Thus, we can already conclude at this point that the bulk of the pebbles have never seen impacts with speeds greater than $\sim 10 \text{ m s}^{-1}$, because pebbles are being compacted to $\phi_{\text{pebble}} \approx 0.55$ to ≈ 0.90 (and structurally destroyed) for impact velocities of 50 and 1000 m s^{-1} , respectively (Beitz et al. 2016). Even for the loosest possible pebble packing, RLP, this would result in $\phi_{\text{tot}} = 0.31 \dots 0.50$, which exceeds the published values.

4.2 Homogeneity

A gentle gravitational collapse of a bound clump of mm-sized pebbles leads to a homogeneous body on all size scales down to the pebble size. This is consistent with findings by CONSERT (Kofman et al. 2015) and RSI (Pätzold et al. 2016), whose resolution limits are, however, much larger than the pebble size. The absence of scattering in the CONSERT data indicates the absence of large contrast in the dielectric constant within the investigated depth, suggesting that cavities or density enhancements larger or comparable to the wavelength (3.3 m) do not exist within the volume examined. However, measurements by CONSERT and RSI cannot exclude voids in

the ~ 10 – 100 m size range in the bulk of the comet nucleus, due to a lack of observational volume (CONCERT) and sensitivity (RSI). CONCERT data are compatible with a slow variation of the dielectric constant over the top ~ 100 m from the surface of 67P (Ciarletti et al. 2015), which cannot be explained by our formation model and could well be an evolutionary process. At the current stage, the gravitational collapse of a bound cloud of pebbles can also not account for the observed layering of the two lobes of comet 67P (Massironi et al. 2015), which speaks for an individual formation (or evolution) of the two lobes.

Measurements based on observations by the OSIRIS instrument indicate a difference in mass density between the two lobes of 5–15 per cent, with the large lobe being denser (Jorda et al. 2016). This could be the result of lithostatic compression inside the larger lobe of 67P. The lithostatic pressure inside a homogeneous object with radius r and a mean mass density ρ due to its own gravity at a depth x is given by $p(x, r) = \frac{2}{3}\pi\rho^2 G [r^2 - (r - x)^2]$, where G is the gravitational constant. The volume-averaged pressure is $\bar{p}(r) = \frac{4}{15}\pi\rho^2 Gr^2$; the peak pressure at the centre of the body is $p_c(r) = \frac{2}{3}\pi\rho^2 Gr^2$. For the radii of the two lobes of comet 67P, $r_1 = 1.43$ km and $r_2 = 0.89$ km, and densities $\rho_1 \approx 550$ kg m $^{-3}$ and $\rho_2 \approx 500$ kg m $^{-3}$ (Jorda et al. 2016), we get $\bar{p}_1 = 35$ Pa, $\bar{p}_2 = 11$ Pa, $p_{c,1} = 86$ Pa and $p_{c,2} = 28$ Pa, respectively. Taking into account that the two lobes are in contact and that the centre of mass is inside the larger of the two lobes, the compressive stress inside the larger lobe is further increased. Its volume-averaged upper limit can be calculated by assuming that the whole body is spherical with a radius of $r = 1.65$ km and a mass density of $\rho = 530$ kg m $^{-3}$ and yields $p \lesssim 100$ Pa.

Low-velocity impact experiments of glass spheres of 5 mm radius and 1.37 g mass (and, thus, a density of $\rho = 2600$ kg m $^{-3}$), dropped from $h = 2$ mm above the flat surface, consisting of ~ 20 layers of dust aggregates with ~ 1 mm diameter, yielded intrusions of 1–2 mm (Isensee 2016). As the impact pressure $p_{\text{imp}} = \rho gh \approx 25$ – 50 Pa is constant at the scale of the impactor radius and then decays inversely proportional to the distance squared (Beitz et al. 2016), the resulting density increase was ~ 10 – 30 per cent. As the lithostatic pressure contrast between the two lobes is on the same order as the impact pressure in the impact experiments, we expect a similar density contrast between the two lobes, which matches the findings by Jorda et al. (2016). Although impacts are dynamical processes, in this example the impact velocity of 0.14 – 0.20 m s $^{-1}$ is much smaller than the sound speed so that the impacts were quasi-static.

The compressive strength of overhangs on the 10 m scale on the surface of comet 67P were estimated to be 30–150 Pa (Groussin et al. 2015). These strength values are reached within the large lobe, but not in the small lobe of comet 67P. Thus, we expect material failure only in the inside of the large lobe that leads to a densification, which is in qualitative agreement with the observation of the density contrast between the two lobes.

4.3 Thermal inertia

Our planetesimal-formation model can be readily used to derive the thermal inertia of the near-surface material of the nucleus of comet 67P. The thermal inertia is a measure of the ability of the material to resist changes in temperature due to energy fluxes and is defined by $I = \sqrt{k\rho c_p}$, with k , ρ and c_p being the heat conductivity, the mass density and the heat capacity, respectively. Using similar values as those in Schloerb et al. (2015), $\rho = 500$ kg m $^{-3}$ and $c_p = 500$ J kg $^{-1}$ K $^{-1}$, and the model of the heat conductivity by Gundlach & Blum (2012) (see also Appendix A and Fig. A1) for $a = 5$ mm, i.e. $k = 10^{-2}$ W m $^{-1}$ K $^{-1}$ for $T = 200$ K

and $k = 10^{-3}$ W m $^{-1}$ K $^{-1}$ for $T = 100$ K, we get thermal inertia between $I = 16$ J K $^{-1}$ m $^{-2}$ s $^{-1/2}$ ($T = 100$ K) and $I = 50$ J K $^{-1}$ m $^{-2}$ s $^{-1/2}$ ($T = 200$ K). This agrees very well with MIRO results of $I = 10$ – 30 J K $^{-1}$ m $^{-2}$ s $^{-1/2}$ and $I = 10$ – 50 J K $^{-1}$ m $^{-2}$ s $^{-1/2}$ (Gulkis et al. 2015; Schloerb et al. 2015).

4.4 Outgassing of water vapour as a function of heliocentric distance and water-ice abundance on comet 67P

Using the thermophysical model described in detail in Appendix A, we calculated the expected outgassing rates for water vapour as a function of heliocentric distance and compared it to values inferred from Rosetta Orbiter Spectrometer for Ion and Neutral Analysis (ROSINA) measurements (Fougere et al. 2016). The free model parameters are the pebble radius, the thickness of the desiccated dust layer and the sub-surface areal coverage by water ice. For not too small dust pebbles (see Fig. A1), however, the heat conductivity per pebble radius is constant for a given temperature so that the former two parameters degenerate to a single parameter, i.e. the depth of the desiccated dust layer in units of the pebble radius.

We determined vertical steady-state temperature profiles (as proxies for the diurnal and seasonal sub-surface profiles) for insulations ranging from the sub-solar point at perihelion to 10^{-4} that value (in 10 000 steps) along the orbit of 67P and set the ice-dust boundary as a free parameter, ranging from the surface to 30 pebble radii deep. For each temperature profile, the temperature of the water ice at the ice-dust boundary and the corresponding sublimation rate were calculated [see table 1 by Gundlach, Skorov & Blum (2011a) for details]. Due to the gas permeability of the covering dust-aggregate layers, only a fraction of the sublimating molecules can escape into space. The number of escaping molecules as a function of the thickness of the desiccated dust-aggregate layer is calculated using the experimental results obtained by Gundlach et al. (2011a) (see equations A9–A12 and Table A1 for details) for a volume filling factor of the pebble packing of $\phi_{\text{packing}} = 0.59 \approx \phi_{\text{RCP}}$.

The outgassing rate of each surface segment is calculated by either choosing a thickness of two pebble radii, i.e. $x = 2a$ in equations (A9)–(A12) (nominal model), or such a thickness x that the pressure build-up at the ice–dust interface is maximal, i.e. $Z(T(x))$ in equation (A10) is maximal, which then leads to a corresponding outgassing rate (i.e. the amount of molecules able to penetrate through the covering material and able to escape into space). It turned out that both assumptions agree relatively well (the difference between the two methods in the outgassing rate per segment is less than 20 per cent, but the overall behaviour of the outgassing rate versus heliocentric distance follows the exact same trend) so that we here only follow the nominal model. To arrive at the total outgassing rate, the respective values of the individual surface segments are summed, taking the area of each surface segment and its time-dependent insolation into account. We assume pebbles with radii $a = 5$ mm (see Fig. 2) and, hence, a thickness of the desiccated dust-pebble layer of 1 cm.

We approximated the shape and orientation of 67P by a digital terrain model with 5000 facets (Jorda et al. 2016) and its real obliquity (Acton 1996) as well as by a 1000-facet sphere with an effective radius of 1.65 km and a rotation axis perpendicular to the orbital plane. Fig. 8 shows the resulting outgassing rates at different heliocentric distances derived for comet 67P. For comparison, the outgassing rates deduced from ROSINA data are shown by the blue triangles (Fougere et al. 2016). The black curves present the results of the two models under the assumption that the entire surface is active and the ice–dust interface is completely covered in water ice.

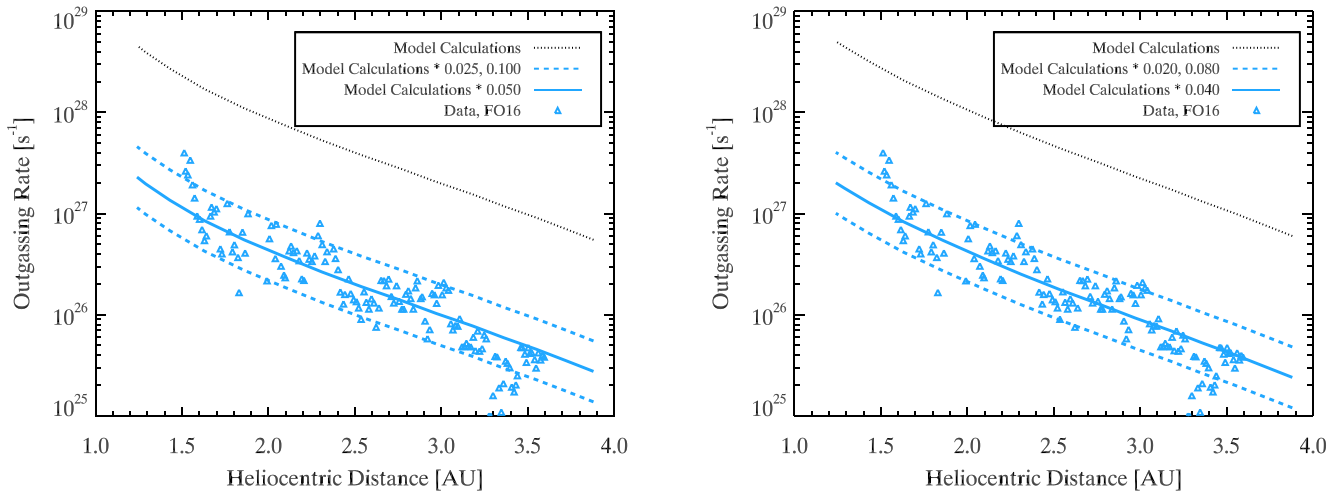


Figure 8. Water-vapour outgassing rates for comet 67P. Predictions of our thermophysical model (calculated for pebble radii of 5 mm) and an assumed dust–ice interface at 2 pebble radii (i.e. 1 cm) depth for the 67P outgassing rates of water ice (black dotted curves) and the measurements by *Rosetta*/ROSINA (Fougere et al. 2016) (triangles) are shown as a function of heliocentric distance. The solid and dashed blue curves denote models with different areal water–ice coverages at the dust–ice interface. Left: for a shape model of 67P consisting of 5000 facets and the obliquity of 67P and water–ice coverages of (from bottom to top) 2.5 per cent, 5 per cent and 10 per cent. Right: for a spherical comet consisting of 1000 facets with no obliquity and water–ice coverages of (from bottom to top) 2 per cent, 4 per cent and 8 per cent.

A comparison with the measured outgassing rates provides the possibility to estimate the fraction of active surface area or the areal coverage by water ice. We find that both models (a comet with the shape and obliquity of 67P and a spherical comet, respectively) provide excellent fits to the measured data if we assume that 5 per cent of the dust–ice interface area is covered in water ice (4 per cent for the spherical comet; see blue curves in Fig. 8). Thus, a homogeneous cometary sub-surface can explain the observed outgassing rate of comet 67P (see Fig. 8) and large areas of inactivity or hotspots of activity on the sunlit hemisphere are not required. This is in agreement with direct findings from *Rosetta* (Fulle et al. 2016a; Kramer & Noack 2016). From Fig. 8, it can be assumed that an even better match to the ROSINA data, particularly at the highest and lowest heliocentric distances, can be achieved if the water–ice coverage at large heliocentric distances is slightly smaller than average, whereas for small heliocentric distances a somewhat larger areal water–ice coverage could be present. This dichotomy seems plausible, because regions active during the northern summer (at large heliocentric distances) are covered in fall-back material from the southern summer. The southern latitudes are active at small heliocentric distances and produce more material than they receive during the southern winter. As the fall-back material deposited in northern latitudes has been exposed to direct sunlight, we expect it to contain a somewhat smaller abundance of water ice (see Fulle et al. 2017).

Some caution is required in interpreting the derived 5 per cent areal water–ice coverage or fraction of surface mass that is evaporating water ice. Assuming a thicker (thinner) desiccated dust cover leads to a diminished (increased) vertical heat transport that can formally be compensated by higher (lower) water–ice abundance. Thus, our model does not allow the prediction of the sub-surface water–ice coverage. However, if the water–ice abundance is known, we can use the model to estimate the thickness of the ice-free upper dust layer in units of the pebble radius.

With the assumption of an average dust-to-ice mass ratio of $\delta = 8.5$ (Fulle et al. 2016b), we get a global water–ice mass fraction of $Y = \frac{1}{\delta+1} = 0.105$ for the pristine comet nucleus. On the

southern hemisphere, part of the water ice evaporates before the dust is ejected, leaving behind emitted dust with a water–ice mass fraction Z and a mass fraction X of the water vapour. Thus, we get $Y = X + Z$ for the southern hemisphere. For the northern hemisphere, we assume that 20 per cent of its surface is primitive (Keller et al. 2015), with a water–ice content of Y , and 80 per cent of the surface is covered in deposit from the south, with a remaining water–ice abundance of Z . Therefore, we get for the northern hemisphere $0.2Y + 0.8Z = X$, because the sublimating water content is about the same in the north and the south (Fulle et al. 2016a; Fougere et al. 2016). Solving the two equations with $Y = 0.105$, we get $X = 0.05$, in agreement with the needed mass surface fraction fitting ROSINA Comet Pressure Sensor (COPS) data, and $Z = 0.05$, in agreement with the ice mass content in dust derived by Fulle et al. (2016a). This consensus with the observations means that our assumption of a thickness of the desiccated dust layer of two pebble radii is consistent. These values are in accord with the ice abundances of other Kuiper-belt objects (Fulle 2017).

It should also be mentioned that our outgassing model is not unique and that other models also predict a similar increase in water-production rate with decreasing heliocentric distance (Keller et al. 2015). Thus, the evaporation rate of water ice is neither diagnostic for the pebble radii nor for the build-up of the desiccated dust crust. However, a correct prediction of the outgassing rate of water is a necessary condition for a comet-formation model.

4.5 Size range for active comets

Laboratory data indicate that the tensile strength of the interior of a body formed by pebble collapse increases towards the centre (Gundlach & Blum 2016). This is due to a memory effect of lithostatic pressure experienced at any time since formation. As the lithostatic pressure increases with increasing size of the body, large active comets should be scarce, because dust activity can only be present if the gas pressure exceeds the tensile strength. A comparison between (active) Jupiter-family comets (JFCs) and (inactive) asteroids in cometary orbits shows that the latter are on average

larger than the former, although their perihelia distances are even smaller than those of the JFCs (Gundlach & Blum 2016). The size limit for activity was predicted to be between 2.7 and 4.5 km initial radius (Gundlach & Blum 2016). Both of the lobes of comet 67P are well below this limit so that they can sustain their activity until they vanish.

5 CONCLUSION

In conclusion, the analysis presented in this paper favours the formation of comet 67P through gravitational collapse of a bound clump of mm-sized dust pebbles and excludes any significant rearrangement (e.g. by catastrophic collisions) of the bulk of the pebbles since the gravitational accretion, which would have destroyed a significant fraction of the pristine fractals among the voids, rendering the observed rate of the GIADA showers of mm-sized fractal parent particles impossible (Fulle & Blum 2017). However, even sub-catastrophic collisions as suggested by Jutzi et al. (2017) and Jutzi & Benz (2017) cannot have acted on comet 67P. For an impact velocity of $v = 20 \text{ m s}^{-1}$ and near-equal-sized collision partners (as, e.g. in the case of the two lobes of comet 67P), we get a *global* compression of $\sim \rho v^2/2 = 10^5 \text{ Pa}$, with $\rho = 500 \text{ kg m}^{-3}$. This by far exceeds the tensile strength of the dust pebbles ($\sim 1\text{--}10 \text{ kPa}$) as well as the compressive strength of the fractals, which get maximally compressed when colliding at $v = 0.7 \text{ m s}^{-1}$ (Blum & Wurm 2000). Thus, any collision above $\sim 1 \text{ m s}^{-1}$ can be excluded for both lobes of comet 67P, which may have accreted from two cometesimals at collision speeds $< 1 \text{ m s}^{-1}$ (Jutzi & Asphaug 2015).

The fact that each of the two lobes of comet 67P is a pebble pile correctly predicts the comet's porosity, homogeneity and thermal inertia. With some additional assumptions of the water-ice abundance and the sub-surface depth of the dust-ice interface, the outgassing rate of 67P can also be reconstructed. On top of that, the dominance of the comet's total mass by dust pebbles predicts tensile strengths with which the dust activity can also be explained (Skorov & Blum 2012; Blum et al. 2014). The presence of a distinct size scale on comet 67P, as shown in Fig. 2, together with the fragility of the cometary material, excludes a formation of 67P by mutual collisions among larger and larger building blocks in the solar nebula, as proposed by Weidenschilling (1997) and Davidsson et al. (2016).

ACKNOWLEDGEMENTS

We thank Helena Schmidt for producing the RCP data for Fig. 1, Björn Davidsson and Paul Weissman for critical reviews of the first draft of the manuscript, Sam Gulkis for providing original MIRO data, Mark Hofstadter and F. Peter Schloerb for discussion about the MIRO data, Harald Mutschke for data and discussions on dust opacities, Wlodek Kofman and the CONSERT team for insight into the CONSERT data, Ekkehard Kürt for extensive discussions of the second version of the manuscript, Jörg Knollenberg for providing MUPUS-TM data and Philipp Heinisch for providing the *Philae* housekeeping data.

JB acknowledges support by the Deutsche Forschungsgemeinschaft (DFG) project BL298/24-1 as part of the Research Unit FOR 2285. MK thanks the DFG (SFB963) for support. IvB thanks the Deutsches Zentrum für Luft- und Raumfahrt for support under grant 50WM1536. RS thanks the Austrian Research Promotion Agency (FFG) for financial support. TM and MSB acknowledge funding by the Austrian Science Fund FWF P 28100-N36. TM acknowledges the Steiermärkische Sparkasse and the Karl-Franzens Universität Graz for their financial support. SFG and CS acknowledge the financial support of the United Kingdom Science and Technology

Facilities Council (grant ST/L000776/1; ERF). *Rosetta* is an ESA mission with contributions from its member states and NASA.

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APPENDIX A: THERMOPHYSICAL MODEL OF THE COMETARY NUCLEUS

Owing to the low albedo of comet 67P/Churyumov-Gerasimenko, incoming solar irradiation is absorbed almost perfectly. Based upon OSIRIS images, a Bond albedo of only 1.2 per cent at 480 nm wavelength was derived (see table 3 in Fornasier et al. 2015) so that 98.8 per cent of the energy delivered by the Sun is being converted into heat in the upper few micrometres of the surface. From here, heat is transported to the deeper layers by conduction through the network of dust particles and by (infrared) radiation from pebble to pebble (Gundlach & Blum 2012). Once the heat wave reaches the deeper ice-bearing layers, we assume that the heat flux is partially used to evaporate the ice. Details about the energy-transport mechanisms follow below. The emerging water molecules can either directly escape into the vacuum of space or hit one or more dust aggregates on their way out (see Fig. 1). Inter-molecular collisions are relatively unimportant and are here neglected, as is the heat transport by water vapour. Gas-dust collisions lead to an outward-directed momentum transfer from the gas molecules to the dust aggregates. We treat this exchange of momentum by calculating the steady-state gas pressure at the ice–dust interface. The gas permeability of the dust layer is a function of its thickness (Gundlach & Blum 2012) and leads to the build-up of relatively higher pressures at the dust–ice interface for a higher number of dust-aggregate layers.

In order to derive the outgassing rate of comet 67P, we developed a 1D thermophysical model, which solves the heat transfer equation at different positions below the surface of 67P (see Table A1 for an overview of the model parameters). For the surface material, we assume that the gravitational collapse of the bound pebble cloud has gently formed a surface layer composed of aggregates (see Fig. 1) consisting of water ice and dust (Blum et al. 2014). The water ice has retreated from the first surface layers due to the solar heat and is located below the ice–dust boundary (i.e. at these depths, the dust aggregates may also contain water ice, or aggregates composed of water-ice particles, are found in between the dust aggregates). Energy absorption occurs at the first pebble layer (surface layer) of the nucleus and is derived by the steady-state energy balance equation,

$$I_{\odot} \left(\frac{r_H}{1 \text{ au}} \right)^{-2} (1 - A) \cos \vartheta = \varepsilon \sigma T_s^4 + \lambda(T) \left. \frac{\partial T}{\partial x} \right|_{\text{Surface}}. \quad (\text{A1})$$

Here, I_{\odot} is the solar constant, r_H is the heliocentric distance, A is the bond albedo, ϑ is the angle between the surface normal and the incident solar radiation, ε is the emissivity, σ is the Stefan–Boltzmann constant, T_s is the surface temperature, $\lambda(T)$ is the temperature dependent heat conductivity of the porous surface material and x is the depth beneath the surface (Gundlach et al. 2011a).

The heat conductivity is given by (Gundlach & Blum 2012)

$$\lambda(T) = \frac{16}{3} \sigma T^3 l(a) + H(a) \lambda_{\text{pebble}}(T, a). \quad (\text{A2})$$

The first term on the right-hand side of equation (A2) describes the heat conductivity through radiation inside the pores of the granular material with $l(a)$ being the mean free path of the photons in the void

space, which is a function of the pebble radius a through (Skorov et al. 2011)

$$l(a) = e_{\text{mfp}} \frac{1 - \phi_{\text{RCP}}}{\phi_{\text{RCP}}} a, \quad (\text{A3})$$

with ϕ_{RCP} and e_{mfp} being the volume filling factor of the pebble packing and a scaling factor, respectively. The second term on the right-hand side of equation (A2) is the heat conductivity through the network of aggregates, with $H(a)$ being the Hertzian dilution factor for a granular material, which can be expressed by

$$H(a) = \left[\frac{9\pi}{4} \frac{1 - \mu_{\text{pebble}}^2}{Y_{\text{pebble}}} \frac{\gamma_{\text{pebble}}}{a} \right]^{1/3} f_1 e^{f_2 \phi_{\text{RCP}}}, \quad (\text{A4})$$

where μ_{pebble} and Y_{pebble} are the Poisson ratio and Young's modulus of the pebbles, f_1 and f_2 are coefficients required to derive the influence of the packing structure on the heat conductivity and γ_{pebble} is the specific surface energy of the pebbles that can be formulated as

$$\gamma = \phi_{\text{pebble}} \gamma_{\text{grain}}^{5/3} \left[\frac{9\pi(1 - \mu_{\text{pebble}}^2)}{r_0 Y_{\text{grain}}} \right]^{2/3}, \quad (\text{A5})$$

with γ_{grain} , r_0 and Y_{grain} being the specific surface energy, the radius and Young's modulus of the monomer particles (Gundlach & Blum 2012).

Finally, $\lambda_{\text{pebble}}(T, r)$ is the internal heat conductivity of the pebbles, given by

$$\lambda_{\text{pebble}}(T, r) = \lambda_{\text{solid}}(T) \left[\frac{9\pi}{4} \frac{1 - \mu_{\text{grain}}^2}{Y_{\text{grain}}} \frac{\gamma_{\text{grain}}}{r_0} \right]^{1/3} f_1 e^{f_2 \phi_{\text{pebble}}}, \quad (\text{A6})$$

with μ_{grain} and ϕ_{pebble} being Poisson's ratio and the internal packing structure of the monomers inside the pebbles (Gundlach & Blum 2012). For the heat conductivity of the solid refractory grains, we used

$$\lambda_{\text{solid}} = 0.5 \text{ W m}^{-1} \text{ K}^{-1} \quad (\text{A7})$$

to account for the high abundance of organic material.

In Fig. A1, we compare the resulting heat conductivity according to equation (A2) for dust-aggregate radii between $a = 0.01$ and 100 mm . It turns out that radiative heat transport is the dominant effect for pebble radii above $\sim 0.1 \text{ mm}$. Thus, specific material properties, such as λ_{solid} , are relatively unimportant for the heat transport through a network of pebbles and only the pebble radius determines the heat conductivity. It is interesting to note that the resulting heat conductivity for pebble radii of $\sim 1\text{--}10 \text{ mm}$ and homogeneous dust layers consisting of μm -sized monomer grains (horizontal black line in Fig. A1) is very similar. Thus, the heat conductivity (or thermal inertia) alone is not diagnostic for the absence or presence of pebbles.

At the start of each simulation, the initial temperature is set for all simulated depths x to either $T = 50$ or 133 K , the latter being the orbital equilibrium temperature. The increase of the temperature below the surface due to the absorption of the solar radiation at the surface (equation A1) is derived by using the heat-transfer equation for porous materials,

$$\rho c \frac{\partial T}{\partial t} = \frac{\partial}{\partial x} \left[\lambda(T) \frac{\partial T}{\partial x} \right] + S(T), \quad (\text{A8})$$

where ρ is the density of the porous material, c is its heat capacity, T is the temperature and $S(T)$ is an additional term, which takes the

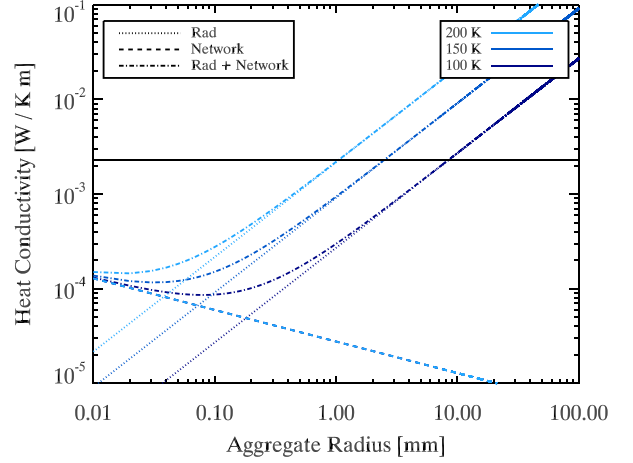


Figure A1. Heat conductivity as a function of dust-aggregate size. Shown is the heat conductivity of a network of spherical dust aggregates according to equation (A2) for temperatures of $T = 100, 150$ and 200 K , respectively. Due to the low solid-state heat conductivity through the pebble–pebble contacts (the second term on the right-hand side of equation A2) of $10^{-5}\text{--}10^{-4} \text{ W m}^{-1} \text{ K}^{-1}$, radiative heat transfer (the first term on the right-hand side of equation A2) dominates for aggregate radii above $\sim 0.1 \text{ mm}$ and all relevant temperatures. The horizontal black line at $2.2 \times 10^{-3} \text{ W m}^{-1} \text{ K}^{-1}$ denotes the heat conductivity through a homogeneous network of μm -sized dust grains with individual heat conductivities of $\lambda_{\text{solid}} = 0.5 \text{ W m}^{-1} \text{ K}^{-1}$.

energy loss due to the sublimation process into account (Davidsson & Skorov 2002), and is given by

$$S(T) = q Z(T) \Lambda \zeta(x). \quad (\text{A9})$$

Here, q and Λ are the surface-to-volume ratio and the latent heat of sublimation of water ice. $Z(T)$ is the sublimation rate, described by the Hertz–Knudsen equation

$$Z(T) = a_1 e^{-a_2/T} \sqrt{\frac{m}{2\pi k_B T}} - Z_0, \quad (\text{A10})$$

where a_1 and a_2 are empirical constants describing the sublimation pressure of water ice, m is the mass of a water molecule and k_B is Boltzmann's constant. Z_0 describes the backflow of molecules on to the ice surface leading to recondensation. Normally, this term is known by $Z_0 = p_{\text{gas}} \sqrt{\frac{m}{2\pi k_B T_{\text{gas}}}}$, where p_{gas} and T_{gas} are the pressure and temperature of the gas phase above the ice surface. However, under cometary-like conditions, where molecules escape into space, p_{gas} is practically zero so that this classical description of the backflow of molecules is not important for the energy budget of the system. However, the covering dust layer leads to backscattering of molecules on to the ice surface. The efficiency of this backscattering has been measured in laboratory experiments (Gundlach et al. 2011a). Thus, we can formulate a new Z_0 describing this backscattering of water molecules by the covering dust layer on to the ice surface, which reads

$$Z_0 = Z(T)(1 - \zeta(x)). \quad (\text{A11})$$

Here, $\zeta(x)$ is the fraction of escaping molecules as a function of the dust layer thickness x and is given by

$$\zeta(x) = (1 + x/b)^{-1}, \quad (\text{A12})$$

with b being an empirical permeability parameter that depends on porosity (see Table A1). With no dust cover ($x = 0$), all molecules

Table A1. Physical properties used in the thermophysical model.

Properties	Symbol	Value	
<i>Monomer dust grains</i>			
Radius	r_0	1.0×10^{-6} m	–
Young's modulus	Y_{grain}	5.5×10^{10} Pa	Chan & Tien (1973)
Poisson ratio	μ_{grain}	0.17	Chan & Tien (1973)
Heat capacity	C	1.0×10^3 J kg $^{-1}$ K $^{-1}$	–
Specific surface energy	γ_{grain}	0.01 J m $^{-2}$	Heim et al. (1999)
<i>Dust aggregates ('pebbles')</i>			
Radius	a	1.58×10^{-4} m 5.00×10^{-4} m 1.58×10^{-3} m 5.00×10^{-3} m 1.58×10^{-2} m	–
Volume filling factor	ϕ_{pebble}	0.4	Weidling et al. (2009); Güttler et al. (2010); Zsom et al. (2010)
Young's modulus	Y_{pebble}	8.1×10^3 Pa	Weidling, Güttler & Blum (2012)
Poisson ratio	μ_{pebble}	0.17	Weidling et al. (2012)
<i>Water–ice properties</i>			
Latent heat of sublimation	Λ	2.86×10^6 J kg $^{-1}$	Orosei et al. (1995)
Sublimation pressure (equation A10)	a_1 a_2	3.23×10^{12} Pa 6134.6 K	Gundlach et al. (2011a)
<i>Global properties</i>			
Thermal emissivity	ε	1.0	(Assumed)
Bond Albedo	A	0.012	Fornasier et al. (2015)
Volume filling factor of the dust-aggregate packing	ϕ_{RCP}	0.6	–
Scaling parameter for mean free path (equation A3)	e_{mfp}	1.34	Skorov et al. (2011)
Structure Parameter (equation A6)	f_1 f_2	5.18×10^{-2} 5.26	Gundlach & Blum (2012)
Heat conductivity of refractory grains (equation A7)	λ_{solid}	0.5 W m $^{-1}$ K $^{-1}$	(Assumed)
Permeability parameter (equation A12)	b	$13.85 \times a$	Gundlach et al. (2011a)
Surface-to-volume ratio (equation A9)	q	1.2×10^6 m $^{-1}$	–

can freely escape into space and $\zeta(x=0) = 1$, i.e. $Z_0(x=0) = 0$. For a pebble layer with a thickness $x \gg b$, all molecules are effectively prevented from escaping from the comet nucleus and $Z_0(x \rightarrow \infty) \rightarrow Z(T)$.

The heat transport of the porous dust-aggregate layers strongly depends on the temperature of the material (see Fig. A1), because radiation inside the void space between the pebbles plays the dominant role in the energy transfer process (Gundlach & Blum 2012) (see equation A2 for details). We assume that the aggregates are primarily composed of dust (Fulle et al. 2016b; Lorek et al. 2016). This means that the dust determines the physical properties of the surface material (e.g. the network heat conductivity and the heat capacity). Water ice is incorporated into the model by allowing the material to sublimate at the ice-dust boundary (taken into account by the additional term $S(T)$ in the heat transfer equation A8). The position of the water-ice boundary beneath the surface is treated as a free parameter and is varied between 1 and 30 pebble radii to

investigate how the positions of the ice–dust interface influence the resulting temperature profile.

Equation (A8) is solved via the Crank–Nicolson method, where $S(T)$ on the right-hand side is treated as a superficial source term, if applicable (Hu et al. 2017). The subsurface of the nucleus is discretized in depth into a number of numerical layers. The thickness of the layer, Δx , is always smaller than the pebble size in our simulation in order to resolve the fine variations of temperatures, especially near and at the surface. The upper boundary condition expresses the energy balance at the surface as given by equation (A1). The isothermal condition is adopted for the lower boundary, such as

$$\left. \frac{\partial T}{\partial x} \right|_{x=\mathcal{X}} = 0, \quad (\text{A13})$$

with \mathcal{X} being the isothermal depth.

Because the energy input on the left-hand side of equation (A1) is periodic, it is mandatory to solve equation (A8) for the periodic variations of temperatures. At the starting epoch (which can be arbitrarily chosen for a certain heliocentric distance), say t_0 , the solution is initialized, assuming that the nucleus subsurface is isothermal with a constant profile (either $T = 50$ or 133 K throughout). The temperature profile is propagated in response to the varying energy input at each time step separated by Δt . To ensure numerical stability, the following criterion must be fulfilled

$$\Delta t \leq \frac{c\rho}{\lambda} \frac{\Delta x^2}{2}. \quad (\text{A14})$$

We perform the solution over precisely one comet rotation, for $t_0 \leq t \leq t_0 + t_p$, where t_p denotes the rotation period of 67P. The solution is iterated until the temperature profiles one rotation apart coincide, that is, $T(t_0) \approx T(t_0 + t_p)$, which indicates convergence of the solution.

We note that the surface temperature is not provided directly by the Crank–Nicolson scheme. Instead, it can be solved from equation (A8) for the energy balance via the Newton–Raphson method at each time step.

APPENDIX B: MODELLING THE MUPUS-TM DATA

The above heat-conductivity model was additionally used to reconstruct the measured temperature data recorded by the thermal mapper MUPUS-TM onboard the *Rosetta* lander *Philae* during its stay on the landing site Abydos of comet 67P (Spohn et al. 2015). From the housekeeping data of the solar cells on *Philae*, it can be seen that the solar cells received direct sunlight for about 40 min soon after the final touch-down. This duration is consistent with that of a temperature increase, recorded by MUPUS-TM, followed by a temperature decrease. We modelled the ~ 28 min temperature rise under the assumption that it was caused by insolation of the field of view of the thermal mapper. The modelling is based on the FEM algorithms served by the Partial Differential Equation Toolbox™ of MATLAB (Release 2016). For comparison of the measured temperature data with the results achieved by the numerical model, we used temperature values provided to us by the MUPUS team.

For the FEM modelling, the following simplifications were applied. The scenario to be modelled is a planar section of the comet surface heated from top by the Sun. As the pebble structure is assumed to be symmetric in the direction parallel to the comet surface, isothermal conditions hold and, thus, no heat exchange is present in this direction. The heat transfer by conduction from one pebble to another in the vertical direction is neglected in the model, because the contact regions are very small and few in comparison to the dominating amount of heat exchange by radiation between the pebble surfaces.

Owing to these assumptions, the heat transport problem can be reduced to a single sphere representing a dust aggregate on the cometary surface, which is being irradiated at its top half by the Sun (see Fig. B1). Due to the rotational symmetry of the heat transfer inside the spherical pebble, the calculations could be reduced to a 2D model of a semicircle with the symmetry axis at the centre line implemented in cylindrical coordinates. In the corresponding FEM model, following heat transport equation is solved

$$\rho\phi_{\text{pebble}}c \frac{\partial T}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} \left[\lambda(T)r \frac{\partial T}{\partial r} \right] + \frac{\partial}{\partial z} \left[\lambda(T) \frac{\partial T}{\partial z} \right], \quad (\text{B1})$$

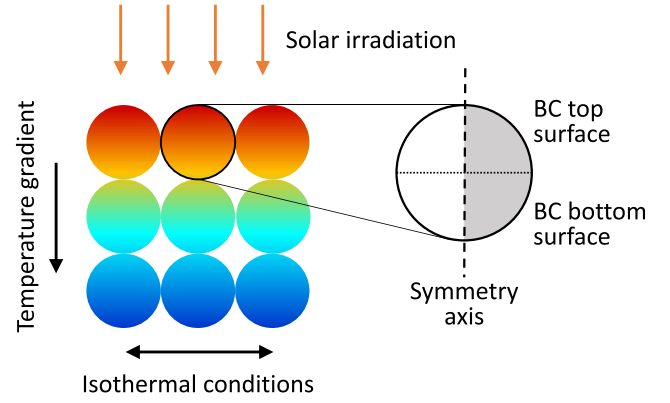


Figure B1. Sketch of the model set-up for reproducing the MUPUS-TM temperature data. Left: section of the comet surface consisting of spherical pebbles irradiated from top by sunlight. Right: reduction of the heat transfer problem to a single surface pebble due to the constant temperature gradient in vertical direction and isothermal conditions in horizontal direction. The FEM model of the single pebble is calculated in cylindrical coordinates for a two-dimensional (2D) semicircle with the vertical centre line of the pebble as symmetry axis and appropriate boundary conditions (BC) for the top and bottom surface.

with the density $\rho\phi_{\text{pebble}}$ of the porous pebble and its heat capacity c . The radial distance and height in the cylindrical coordinate system are given by r and z , respectively. The effective heat conductivity is defined by

$$\lambda(T) = \frac{16}{3} \sigma T^3 l(r) + \lambda_{\text{solid}} \left[\frac{9\pi}{4} \frac{1 - \mu_{\text{grain}}^2}{Y_{\text{grain}}} \frac{\gamma_{\text{grain}}}{r} \right]^{1/3} f_1 e^{f_2 \phi_{\text{pebble}}}, \quad (\text{B2})$$

as the sum of heat radiation through the void spaces between the monomers (first summand) and heat conduction by the contact areas of the monomers (second summand). The radiative part of the effective thermal conductivity follows from equation (A2) adapted to a single pebble and the conductive part equals equation (A6). For the chosen values in equation (B2), refer to Table A1. The initial condition T_0 for solving equation (B1) was extracted from the temperature data provided by the MUPUS team.

The heat exchange of the pebble with the surroundings, i.e. the irradiation of sunlight, heat re-radiation and radiational heat exchange with neighbouring pebbles, is implemented as specific boundary conditions at the top and bottom surface of the model sphere. The heat exchange by radiation with underlying pebbles at the bottom half of the sphere is incorporated in the model as a radiation boundary with an ambient temperature representing the surrounding pebbles. To consider the local temperature evolution during the heating period at the bottom surface of the pebble, influenced by the temperature evolution of the interior of the comet, two limiting cases were calculated: (1) The ambient temperature at the bottom half of the sphere remains constant and equal to the initial temperature $T_{\text{ambient}} = T_0$. (2) The ambient temperature at the bottom half of the sphere evolves like the temperature at the comet surface measured with MUPUS-TM. Both approaches correspond to the two extreme cases in which (1) no heat reaches the bottom of the pebble during the time of illumination, which is more likely for large pebbles, and (2) the heat is transferred from the top to the bottom of the pebble so efficiently that an isothermal condition is reached during the time-scale of the insolation, which is the case for small pebbles.

At the centre axis of the model sphere, a zero Neumann boundary condition was applied. The boundary condition at the surface of the top hemisphere is defined according to equation (A1) by the

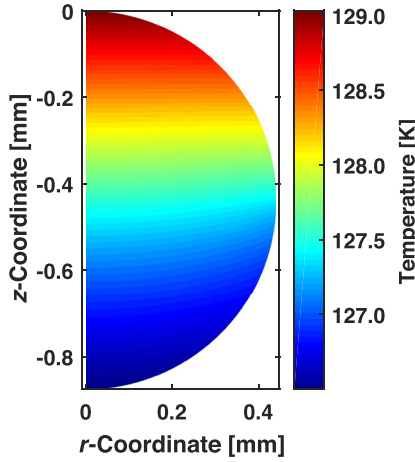


Figure B2. Temperature distribution inside the pebble sphere after ~ 28 min solar illumination as a result of the FEM model. The corresponding parameters for optimally fitting the measurements are $a = 0.44$ mm for the pebble radius and $f_{I\odot} = 0.16$ for the illumination factor.

balance of the absorption of energy from the Sun, the heat transport in the pebble interior and the re-radiation of heat from the surface. To account for a lateral distribution of pebbles with isothermal properties in the horizontal direction, the heat exchange by radiation with the environment (assumed at an ambient temperature of $T_{\text{ambient}} = 0$ K) was restricted to the vertical direction by the factor $\cos \vartheta$, i.e.

$$\lambda(T) \nabla T|_{\text{top surface}} = \left[\varepsilon \sigma (T_{\text{ambient}}^4 - T^4) + I_{\odot} \left(\frac{r_H}{1 \text{ au}} \right)^{-2} (1 - A) \right] \cos \vartheta, \quad (\text{B3})$$

with ϑ being the angle between the local normal to the surface and the vertical direction. The heliocentric distance r_H was chosen to be 2.99 au, corresponding to the distance between the Sun and comet 67P during the landing of *Philae*.

For the bottom half-sphere, the boundary condition at the sphere surface is determined by the energy balance between the heat conduction of the pebble interior and the heat exchange by radiation at the surface with the ambient temperature representing the surrounding pebbles, i.e.

$$\lambda(T) \nabla T|_{\text{bottom surface}} = \varepsilon \sigma (T_{\text{ambient}}^4 - T^4). \quad (\text{B4})$$

As the illumination angle is unknown, the solar constant I_{\odot} is multiplied in the model by a factor $f_{I\odot}$ between 0 and 1, which is treated together with the radius of the pebble, a , as a free parameter. For comparison of the measured temperature at a given time of illumination with a single temperature value of the modelled sphere surface (see Fig. B2), the (radiative) average temperature of the sphere surface was calculated by

$$T_{\text{sphere surface}} = \left(\frac{\sum d_i^2 T_i^4}{\sum d_i^2} \right)^{1/4}. \quad (\text{B5})$$

With this equation, the temperatures at the sphere surface at distances d_i from the centre axis of the 2D model are weighted by their squared distance to account for their corresponding surface ratio in 3D and are averaged by the fourth power to adopt the temperature measuring technique of the MUPUS-TM.

Finally, we also allow for partial direct illumination of the area observed by MUPUS-TM by applying the following mixing rule to the temperature:

$$T_{\text{model}} = \left(f_s T_{\text{sphere surface}}^4 + (1 - f_s) T_0^4 \right)^{1/4}. \quad (\text{B6})$$

The fraction of surface under direct illumination f_s was implemented in the model on the one hand as a constant free parameter and on the other hand as a time-dependent linear function $f_s = f_{s,0} + f_{s,1} t$.

With the `fminsearch` function in MATLAB (Release 2016), a function to find the minimum of a scalar function of several variables by the Nelder–Mead simplex search method, the optimal set of the pebble radius and the illumination factor can be found. The value to be minimized in this case is the mean squared difference of the MUPUS-TM temperature curve and the appropriate FEM model result

$$\langle \Delta T^2 \rangle = \frac{\sum_{i=1}^N (T_{\text{model},i} - T_{\text{measurement},i})^2}{N} \quad (\text{B7})$$

for the N data points available in the heating curve from Spohn et al. (2015).

APPENDIX C: DUST SIZE DISTRIBUTIONS MEASURED WITH *ROSETTA* AND FROM THE GROUND

An overview of the exponents β of the size distributions (see Section 3.2) measured by various *Rosetta* instruments is given in Fig. 7(a). COSIMA (Cometary Secondary Ion Mass Analyser) measured the size distribution from the material observed with the COSISCOPE camera on the collecting targets. The major unknown in this method is the degree of fragmentation the particles experience when hitting the target. The measurement near $\beta = -3$ is derived from pre-landing data and counts each particle individually (Hilchenbach et al. 2016), while the remaining COSIMA results shown are based on measurements obtained up to April 2015 and take into account a medium degree of fragmentation (Merouane et al. 2016). The COSIMA data shown here were averaged over several months. Grain Impact Analyser and Dust Accumulator (GIADA) data are derived from combined measurements by the GDS+IS sensors during time spans of typically a few days. The value of $\beta = -2$ was measured at heliocentric distances beyond 2 au, while $\beta = -3.7$ stems from perihelion (Rotundi et al. 2015; Fulle et al. 2016c). The OSIRIS coma data were derived from images of individual grains near the limb on four selected dates between 2014 August and 2015 August (Rotundi et al. 2015; Fulle et al. 2016c). OSIRIS surface data refer to boulder statistics in different terrains on the surface (Pajola et al. 2015). The Rosetta Lander Imaging System (ROLIS) data were obtained during *Philae*'s approach to the Agilkia landing site and refer to ‘rough’ (broken power law) and ‘smooth’ (single power-law) terrains, respectively (Mottola et al. 2015). No indication that the size distribution measured in the centimetre to metre range continues down to millimetre and sub-millimetre sizes was found, as this would lead to a saturation of the surface with unresolved small particles, which is inconsistent with the observed granular texture. Therefore, the material must be depleted in small grains, consistent with a more shallow power-law at sub-centimetre sizes. Ground-based measurements of the size distribution were obtained from numerical simulations of the morphology and brightness of dust tail and trail (Agarwal et al. 2010; Fulle et al. 2010).

The diagonal long dashed line in Fig. 7(a) is a fit to the data of the form $\beta = -0.48 \log_{10} a - 4.22$, with a being the particle

radius in metres, while the two other functions represent possible other, albeit extreme, linear approximations of the data to convey an impression of the uncertainty of the curves shown in Fig. 7(b). Here, the normalized mass-frequency distributions per logarithmic size interval for the three linear approximations shown in Fig. 7(a) are shown. We can see that most of the mass is emitted in the form of decimetre particles. The strong decline in the mass-frequency distributions for sizes below \sim cm (or \sim mm for the curve labelled ‘Extreme B’ in Fig. 7b) may indicate that this is the size of the primary building blocks (the ‘pebbles’) of the comet nucleus. We interpret dust particles smaller than \sim 1 mm as pebble fragments due to the ejection process, and larger dust ‘boulders’ (\gg 1 cm) as clusters of pebble-sized aggregates.

It must be mentioned that the data presented in Fig. 7(a) does not distinguish between ‘compact’ aggregates (which we interpret as pebbles or fragments/clusters thereof) and ‘fluffy’ ones [which could be surviving solar-nebula aggregates, as suggested by Manne et al. (2016), that formed contemporary to the formation of the

planetesimals through gravitational collapse of a bound clump of pebbles; see Fulle & Blum (2017)]. Only GIADA is capable of deriving the mass density of the grains (Fulle et al. 2016c) by measuring cross-section, momentum and velocity of individual particles simultaneously. If we want to derive a joint size distribution function for all *compact* aggregates, one has to be careful not to mix in data for the *fluffy* particles. This is not a problem for the aggregates \gtrsim 1 cm in size, because too large fluffy or fractal aggregates cannot survive between the (smaller) pebbles. However, those fluffy/fractal particles that fit into the void space between the \sim 1-cm-sized pebbles, must not be mixed with the pebbles themselves or fragments thereof. Thus, data from COSIMA has to be treated with caution, because they may contain contributions of both aggregate types.

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