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The supernova of the MAGIC gamma-ray burst GRB 190114C^{★,★★}

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ABSTRACT

We observed GRB 190114C (redshift $z = 0.4245$), the first gamma-ray burst (GRB) ever detected at TeV energies, at optical and near-infrared wavelengths with several ground-based telescopes and the *Hubble* Space Telescope, with the primary goal of studying its underlying supernova, SN 2019jrj. The monitoring spanned the time interval between 1.3 and 370 days after the burst, in the observer frame. We find that the afterglow emission can be modelled with a forward shock propagating in a uniform medium modified by time-variable extinction along the line of sight. A jet break could be present after 7 rest-frame days, and accordingly the maximum luminosity of the underlying supernova (SN) ranges between that of stripped-envelope core-collapse SNe of intermediate luminosity and that of the luminous GRB-associated SN 2013dx. The observed spectral absorption lines of SN 2019jrj are not as broad as in classical GRB SNe and are instead more similar to those of less-luminous core-collapse SNe. Taking the broad-lined stripped-envelope core-collapse SN 2004aw as an analogue, we tentatively derive the basic physical properties of SN 2019jrj. We discuss the possibility that a fraction of the TeV emission of this source might have had a hadronic origin and estimate the expected high-energy neutrino detection level with IceCube.

Key words. gamma-ray burst: individual: GRB 190114C – supernovae: individual: SN 2019jrj

1. Introduction

GRB 190114C was first identified as a long-duration gamma-ray burst (GRB) by the Burst Alert Telescope (BAT; Barthelmy et al. 2005) on board the *Neil Gehrels Swift* Observatory (*Swift*; Gehrels et al. 2004) and the Gamma-ray Burst Monitor (GBM; Meegan et al. 2009) of the *Fermi* satellite (Gropp et al. 2019; Hamburg et al. 2019). The trigger time was $T_0 = 20:57:03$ (UT dates are used throughout this paper). The time interval including 90% of the flux (T_{90}) is ~ 116 s as measured by *Fermi*/GBM (50–300 keV energy band) and ~ 362 s as measured by *Swift*/BAT (15–350 keV energy band). The fluence as measured by GBM in the 10–1000 keV energy band is $(4.433 \pm 0.005) \times 10^{-4}$ erg cm⁻² (Ajello et al. 2020).

GRB 190114C is the first reported GRB that was also detected in the TeV band by the Major Atmospheric Gamma Imaging Cherenkov (MAGIC) telescopes. High-energy gamma rays (0.2–1 TeV) were reported by the MAGIC Collaboration with high significance from the beginning of the observations and lasted for at least 20 min (MAGIC Collaboration 2019a); the emission was detected during both the prompt and after-

glow phases. The emission component of the early afterglow has a power comparable to that of the standard synchrotron component and has been interpreted as being due to the inverse-Compton mechanism (MAGIC Collaboration 2019b). However, since no firm conclusions about the production mechanisms of the GeV–TeV emission have been reached so far (Ravasio et al. 2019; Fraija et al. 2019b; Wang et al. 2019; Derishev & Piran 2019; Sahu & López Fortín 2020; Chand et al. 2020; Rueda et al. 2020), and since a pure leptonic scenario does not match the observed emission for GRB 190114C, we cannot exclude the hypothesis that part of this GeV–TeV emission may be caused by the presence of a hadronic component (Gagliardini et al., in prep.), as we discuss in Sect. 4.

The event was also detected by the Large Area Telescope (LAT; Atwood et al. 2009) of the *Fermi* satellite (Kocevski et al. 2019). Including the prompt and extended emission, the estimated fluence is $\sim 2.5 \times 10^{-5}$ erg cm⁻² (100 MeV–100 GeV energy band), which is nearly the highest fluence detected to date, second only to that of GRB 130427A (Ajello et al. 2020).

The afterglow emission from this GRB was detected at various wavebands from 0.65 GHz to 23 GeV (MAGIC Collaboration 2019a,b; Laskar et al. 2019; Misra et al. 2021; Jordana-Mitjans et al. 2020; Ajello et al. 2020). This allowed for the measurement of its redshift, $z \approx 0.4245$ (Selsing et al. 2019; Castro-Tirado et al. 2019), and a detailed study of its host-galaxy properties (de Ugarte Postigo et al. 2020). The uniqueness of GRB 190114C motivated our search for a possible associated supernova (SN) despite the adverse circumstances of a relatively large distance and a high local background (the bright host galaxy and the line-of-sight extinction). In this paper we

* Data are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/cat/J/A+A/659/A39>

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present the results of our observational campaign in which we detected and identified an SN component underlying the GRB (SN 2019jrr; Melandri et al. 2019; Melandri 2021) and characterised its behaviour.

Throughout the paper, distances are computed assuming a Λ cold dark matter Universe with $H_0 = 73 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.27$, and $\Omega_\Lambda = 0.73$ (Spergel et al. 2007; Riess et al. 2016). Magnitudes are in the AB system (Oke & Gunn 1983), and uncertainties are at a 1σ confidence level.

2. Observations and data reduction

2.1. Imaging

We observed the field of GRB 190114C between 1.34 and ~ 51.5 days (in the observer frame) after the burst event with several facilities: the 3.58 m New Technology Telescope (NTT), the 4.2 m *William Herschel* Telescope (WHT), the 3.58 m *Galileo* National Telescope (TNG), the 8.2 m Very Large Telescope (VLT), and the Large Binocular Telescope (LBT; two twin 8.4 m telescopes at Mt. Graham in Arizona, USA).

We also observed the location of GRB 190114C with the *Hubble* Space Telescope (HST) at five epochs 27–370 days after the burst with the Advanced Camera for Surveys Wide Field Channel (ACS/WFC) and three optical/near-infrared (NIR) filters (F606W, F775W, and F850LP). These frames were reduced via *astrodrizzle* to a final scale of $0.025'' \text{ pixel}^{-1}$. Some data obtained at late times with the NIR filters F110W and F160W were presented by de Ugarte Postigo et al. (2020).

All of our images were reduced following standard procedures, including de-biasing and flat-fielding. The photometric calibration was carried out by using a set of field stars selected from the Pan-STARRS1 data archive¹.

In Fig. 1 we show three images obtained with HST, VLT, and LBT at similar epochs. GRB 190114C is located close to the nuclear region of a galaxy (‘A’) that interacts with a companion galaxy (‘B’) located $\sim 1''$ to its north-east (de Ugarte Postigo et al. 2020). The two galaxies are almost blended in the majority of our ground-based images, so their combined light must be subtracted in order to isolate the transient emission. Aperture photometry was used for all images, including those from HST, with a radius of ~ 2.5 to include both galaxies. From the measured magnitudes (reported in Table 1) we subtracted the combined flux of the two-galaxy system ($r = 21.66 \text{ mag}$, $i = 21.09 \text{ mag}$, and $z = 20.97 \text{ mag}$), as estimated from the latest HST observations. These galaxy-subtracted magnitudes are reported in Fig. 2. No K -correction was applied, owing to the lack of simultaneous spectra covering the IR wavelength range. We note that the r band light curve (Fig. 2a) levels off after day ~ 20 , suggesting some extra background contribution ($\sim 0.001 \text{ mJy}$) that was not accounted for in our subtraction (this may have occurred, for instance, if a compact clump due to a star forming region is located right under the location of the GRB). This extra contribution was subtracted from the r band points before computing the bolometric light curve.

2.2. Spectroscopy

We observed GRB 190114C in the optical/NIR band with the LBT using the Multi-Object Double Spectrographs MODS-1 and MODS-2 (Pogge et al. 2010) in dual-grating mode (grisms G400L and G670L) on 2019 January 29 (mid-observation time

of 13.25 days after the burst trigger). For both MODS spectra we used the same instrumental configuration, consisting of a slit width of $1.2''$ and dual-grating mode, covering the spectral range $3200\text{--}9500 \text{ \AA}$ and yielding spectral resolution $R = \lambda/\Delta\lambda \approx 1000$. Considering both MODS together, a total of 2.0 h of exposure time was obtained under moderately good seeing ($\sim 1.3''$), but at high airmass (~ 2) given the low declination of the target.

Data reduction was carried out at the Italian LBT Spectroscopic Reduction Center² by means of scripts optimised for LBT data, adopting the standard procedure for long-slit spectroscopy with bias subtraction, flat-fielding, bad-pixel correction, sky subtraction, and cosmic-ray decontamination. Wavelength calibration (in air) was obtained using spectra of Hg, Ar, Xe, and Kr lamps, providing an accuracy of $\sim 0.08 \text{ \AA}$ over the whole spectral range. Relative flux calibration was derived from the observations of a spectrophotometric standard star.

We also obtained spectra of GRB 190114C with the VLT/FORS2, using the low-resolution 300I-OG590 grism, at 19.17, 22.15, 27.19, and 51.2 observer days after the GRB detection. The complete journal of observations and the corresponding instrumental configurations are reported in Table 2 (see also Fig. A.1). The fourth-epoch spectrum was used as a template for the underlying host-galaxy system. In this spectrum, we see no flux excess at the wavelengths corresponding to the r -band filter (see Sect. 2.1). Therefore, we have not subtracted any extra flux from the spectra. If any such extra background were present, its subtraction would make the spectrum redder still (see Sect. 3.2). We reduced the FORS2 data using ESOREX recipes that permitted us to first correct the raw science frames for the bias and the flat-field and then to determine the spectral extraction mask used for the wavelength calibration of the science and standard-star spectra. Thereafter, we obtained the two-dimensional wavelength- and flux-calibrated GRB spectra, and finally used the IRAF-*apall* package for a more accurate background subtraction. The wavelength range covered in all of our observations is $6100\text{--}10,300 \text{ \AA}$, which corresponds to the rest-frame wavelength range $4280\text{--}7227 \text{ \AA}$.

We performed accurate flux calibration of our spectra using R_Iz photometry obtained with FORS2, using a polynomial interpolating function to first fit the observed photometry, then convert to flux densities, and finally determine the correction term for each spectrum. We also corrected for the fact that the R filter covers only $\sim 46\%$ of the observed spectral emission.

3. Results

3.1. X-ray and optical/NIR afterglow

In Fig. 2 our optical and NIR observations are shown together with data in the same bands taken from the literature (MAGIC Collaboration 2019b; Misra et al. 2021; Jordana-Mitjans et al. 2020; Kann et al. 2019; Im et al. 2019; D’Avanzo et al. 2019; Kim & Im 2019; Kumar et al. 2019a,b; Kim et al. 2019; Mazaeva et al. 2019; Watson et al. 2019; Bikmaev et al. 2019), and with the *Swift*/XRT light curve in the observed range $0.3\text{--}10 \text{ keV}$, as archived in the *Swift* repository³ (Evans et al. 2009).

Prior work on the very early afterglow phase of GRB 190114C (i.e. during the first hours after explosion) found it to be dominated by a reverse-shock component (Laskar et al. 2019; Jordana-Mitjans et al. 2020). Misra et al. (2021) determined the presence of intrinsic absorption along the line of sight

¹ <https://panstarrs.stsci.edu/>

² <http://www.iasf-milano.inaf.it/software>

³ https://www.swift.ac.uk/xrt_curves/00883832/

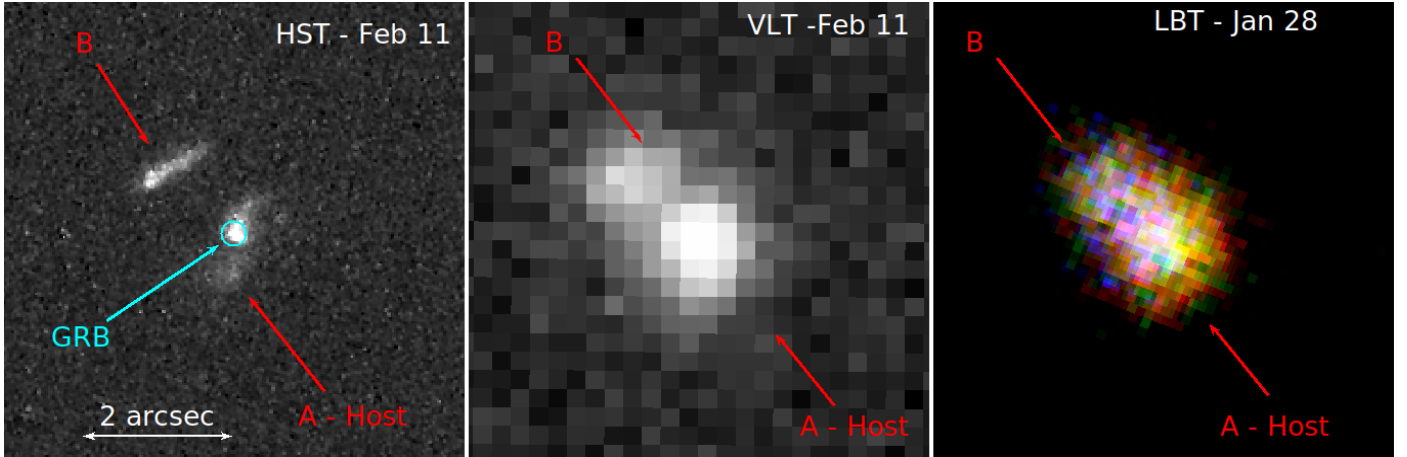


Fig. 1. GRB 190114C host galaxy (A) and its interacting galaxy (B), as observed with HST ($F606W$ filter), VLT (R filter), and LBT (gri image) at similar epochs. North is up, and east is to the left.

Table 1. Observed magnitudes (AB system) of the transient prior to subtraction of the two-galaxy system and not corrected for Galactic extinction.

Δt (d)	Magnitude (err)	Telescope	Δt (d)	Magnitude (err)	Telescope	Δt (d)	Magnitude (err)	Telescope
	<i>g</i>		227.13	21.66 (0.07)	HST		<i>z</i>	
12.97	22.33 (0.08)	TNG	370.57	21.66 (0.07)	HST	1.34	18.84 (0.07)	NTT
13.27	22.37 (0.07)	LBT		<i>i</i>		8.96	20.27 (0.10)	WHT
	<i>r</i>		1.34	19.24 (0.05)	NTT	10.17	20.34 (0.06)	VLT
1.34	19.94 (0.05)	NTT	8.96	20.65 (0.06)	WHT	12.23	20.50 (0.04)	VLT
8.96	21.33 (0.06)	WHT	10.17	20.69 (0.04)	VLT	12.23	20.55 (0.10)	NTT
10.17	21.35 (0.04)	VLT	12.22	20.87 (0.05)	VLT	12.97	20.53 (0.07)	TNG
12.22	21.40 (0.05)	VLT	12.23	20.92 (0.09)	NTT	14.18	20.64 (0.05)	VLT
12.23	21.40 (0.05)	NTT	12.97	20.96 (0.04)	TNG	15.97	20.66 (0.11)	TNG
12.97	21.42 (0.05)	TNG	13.27	20.92 (0.05)	LBT	19.00	20.65 (0.07)	TNG
13.27	21.45 (0.05)	LBT	14.17	20.91 (0.05)	VLT	19.20	20.60 (0.07)	VLT
14.17	21.43 (0.05)	VLT	15.97	20.90 (0.05)	TNG	22.15	20.64 (0.07)	VLT
15.97	21.45 (0.13)	TNG	19.00	20.93 (0.04)	TNG	24.22	20.74 (0.08)	NTT
19.00	21.45 (0.10)	TNG	22.15	21.02 (0.05)	VLT	27.19	20.78 (0.08)	VLT
19.17	21.47 (0.03)	VLT	24.22	21.04 (0.04)	NTT	34.98	20.86 (0.10)	TNG
22.15	21.44 (0.03)	VLT	27.19	21.05 (0.07)	VLT	51.20	20.95 (0.08)	VLT
24.22	21.46 (0.05)	NTT	34.98	21.13 (0.12)	TNG	51.44	20.94 (0.08)	VLT
27.19	21.46 (0.03)	VLT	51.20	21.20 (0.12)	VLT	325.37	20.97 (0.09)	NTT
34.98	21.48 (0.15)	TNG	325.36	21.17 (0.04)	NTT		<i>F850LP</i>	
51.20	21.48 (0.10)	VLT		<i>F775W</i>		27.27	20.82 (0.09)	HST
325.34	21.51 (0.09)	NTT	27.27	20.91 (0.08)	HST	56.37	20.90 (0.07)	HST
	<i>F606W</i>		165.03	21.05 (0.07)	HST	227.13	20.97 (0.08)	HST
27.27	21.54 (0.07)	HST	227.13	21.09 (0.08)	HST	370.57	20.97 (0.08)	HST
165.03	21.63 (0.06)	HST	370.57	21.09 (0.09)	HST			

Notes. Time since burst (Δt) is in the observer frame.

of $A_V = 1.9$ – 2.4 mag (for a Milky Way extinction curve). They also analysed the radio and X-ray afterglow data from early times to ~ 100 days, ignoring the optical data on account of the fact that they are affected by host-galaxy and SN components. Under the assumption that a spectral cooling break is located between the radio and X-ray wavelengths, they found no clear consistency of the data with the standard fireball scenario unless the shock microphysical parameters vary with time. The [MAGIC Collaboration \(2019b\)](#) analysis of the radio-to-X-ray afterglow in the first 3 days determined an intrinsic $A_V = 1.8$ mag, consistent with that found by [Misra et al. \(2021\)](#). In this paper, we focus on the SN component and aim at characterising it in the context

of other nearer GRB SNe and stripped-envelope core-collapse SNe. Our decomposition of the optical galaxy-subtracted data into afterglow and SN components takes the previous analyses into account but introduces the element of intrinsic absorption variation.

In order to decompose the SN 2019jrz light from the galaxy-subtracted optical/NIR photometry, we constructed a model for the multi-wavelength afterglow. Following previous authors ([MAGIC Collaboration 2019b](#); [Fraija et al. 2019a](#); [Misra et al. 2021](#)), we assumed that a forward shock propagating in an external medium of uniform density is responsible for the X-ray and optical/NIR emission starting a few hours after explosion.

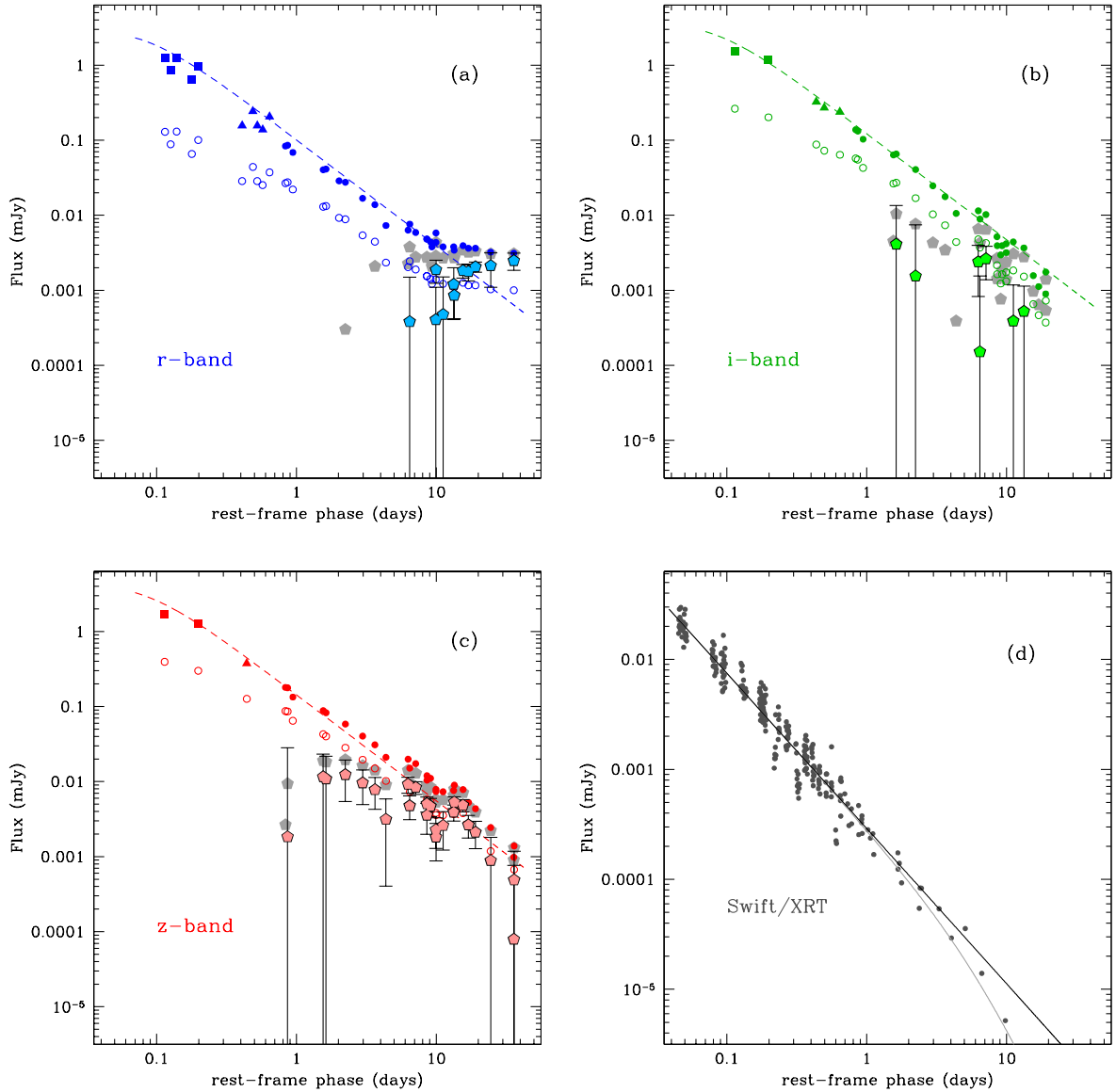


Fig. 2. Optical, NIR and X-rays light curves of GRB 190114C. (a) Light curves of the GRB 190114C counterpart in the optical r band (open blue circles). All fluxes were corrected for host-galaxy contribution, Galactic extinction, and redshift (but not K -corrected). A correction for dust absorption along the GRB line of sight in its host galaxy was also applied ($E(B-V) = 0.6$ mag, phase < 0.3 day, filled squares; $E(B-V) = 0.45$ mag, $0.3 < \text{phase} < 0.7$ day, filled triangles; $E(B-V) = 0.3$ mag, phase > 0.7 day, filled circles). The synchrotron model with no jet break ($t^{-1.4}$) is shown as a dashed blue curve at optical wavelengths, and the corresponding SN component is represented by light blue pentagons. If a jet break occurs at 7 days, the SN component is shown as grey pentagons. (b) Same as (a) for the NIR i band. Galaxy-subtracted points are in dark green and the SN points in light green. (c) Same as (a) for the NIR z band. Galaxy-subtracted points are in red and the SN points in pink. (d) Light curves of the GRB 190114C counterpart in X-rays (0.3–10 keV *Swift*/XRT data, dark grey filled circles). The synchrotron model with no jet break ($t^{-1.4}$) is shown as a solid black curve. If a jet break occurs at 7 days, the X-ray synchrotron model is shown as a solid grey curve. For clarity, uncertainties on data points were omitted.

We adopted the classical fireball formalism (Zhang & Mészáros 2004; Kumar & Zhang 2015); in particular, the electron energy power law has the form $dE/d\gamma \propto \gamma^{-p}$; ν_m and ν_c indicate the characteristic synchrotron frequencies related to the minimum electron energy and to the cooling energy, respectively. The synchrotron flux depends on time and frequency as $f(t) \propto \nu^{-\beta} t^{-\alpha}$.

The MAGIC Collaboration analysis of the multi-wavelength afterglow at early epochs (< 3 observer days; MAGIC Collaboration 2019b, see their extended data in Fig. 6) shows that the frequency ν_m crosses the optical band < 2 rest-frame hours after the explosion. On the other hand, the cooling frequency ν_c is still above the X-ray frequencies at ~ 2 rest-frame days. Since ν_c scales as $t^{-1/2}$, it does not cross the

X-ray band in the time interval covered by our optical monitoring. Therefore, from the X-ray spectral index $\beta_X = 0.94$ reported in the *Swift*/XRT repository⁴ (Evans et al. 2009), we derive an electron energy power-law index $p = 2\beta_X + 1 = 2.88$. The decay of the X-ray light curve is then given by $\alpha = (3/4)(p-1) = 1.41$, consistent with the value of $\alpha_X = 1.344 \pm 0.003$ fitted by Misra et al. (2021). This is shown with a solid line in Fig. 2d.

Since there is no cooling break between the optical and X-ray bands, the optical spectral slope and time decay past the ν_m passage must be the same as in X-rays. However, the thin synchrotron spectrum that fits the X-ray emission over-predicts

⁴ https://www.swift.ac.uk/xrt_spectra/00883832/

Table 2. Summary of spectroscopic observations.

Day (2019)	Phase ^(a) (Day)	Slit ($''$)	T_{exp} (s)	Seeing ($''$)	Tel./Instr.
Jan 28	9.30	1.0	8×900	1.30	LBT/MODS
Feb 3	13.45	0.7	3×900	1.26	VLT/FORS2
Feb 6	15.55	1.0	3×900	0.70	VLT/FORS2
Feb 11	19.09	1.0	3×900	0.90	VLT/FORS2
May 6	35.94	1.00	3×900	0.65	VLT/FORS2

Notes. ^(a)Phases with respect to the time of burst (T_0) are in the rest frame.

the optical galaxy-subtracted flux (dashed curves in Fig. 2a–c). This was interpreted by the MAGIC Collaboration as evidence of dust extinction along the line of sight to the GRB on top of the Galactic one. Their estimate for this intrinsic extinction is $A_V = 1.83 \pm 0.15$ mag, broadly in agreement with other independent analyses of the early-time afterglow spectral energy distribution (Laskar et al. 2019; Misra et al. 2021). However, this value exceeds the amount of extinction that is necessary to correct our data after 0.7 rest-frame days (indeed, their optical flux distributions at ~ 0.7 and ~ 2 rest-frame days also seem overcorrected). For a reddening of $E(B-V) \approx 0.3$ mag, assuming it takes place entirely at the redshift of the GRB (likely dust extinction in the host galaxy), our optical data after 0.7 day match the synchrotron prediction (see Figs. 2a–c). Prior to that, the optical data are still below the synchrotron time curve and present a flattening towards the earlier epochs that cannot be accounted for by only the passage of ν_m . A higher intrinsic reddening, gradually decreasing from $E(B-V) = 0.6$ mag to $E(B-V) = 0.3$ mag, is necessary to correct the data between 0.1 and 0.7 rest-frame days, consistent with the MAGIC Collaboration finding. This suggests that the intrinsic dust extinction has possibly varied with time. It should be noted that the Galactic extinction curve used by us (Cardelli et al. 1989) and the Large Magellanic Cloud extinction curve used by the MAGIC Collaboration to evaluate the intrinsic extinction coincide at the rest-frame wavelengths of our observations (Pei 1992).

As also noted by Misra et al. (2021), the X-ray light curve may decay at a quicker rate after 1 rest-frame week, probably owing to the presence of a jet break, which should be achromatic. Because of the likely emergence of an SN component in the same time interval, it is difficult to directly establish whether the optical light curve presents a similar jet break. However, if the optical synchrotron light curve steepened simultaneously with the X-rays, the residuals of its subtraction from the galaxy-subtracted points, representing the SN component, would depend critically on this break time. We thus modelled the steepening light curve assuming a post-break decay index of $\alpha_2 = p = 2.88$ and a range of time breaks. The X-ray light curve is consistent with any time break larger than ~ 7 rest-frame days. In Fig. 2d we show the X-ray light-curve fit for the two extreme cases of a break at ~ 7 days and at ~ 100 rest-frame days, the latter virtually coinciding with no break during the X-ray monitoring.

3.2. Supernova component

Although the decomposed SN 2019jrz curves cover a limited wavelength range (~ 4000 – 7000 Å in the rest frame), we attempted to construct a pseudo-bolometric light curve in this interval by integrating the SN 2019jrz signal in the *riz* bands and adding flux bluewards and redwards of this range by extrapolat-

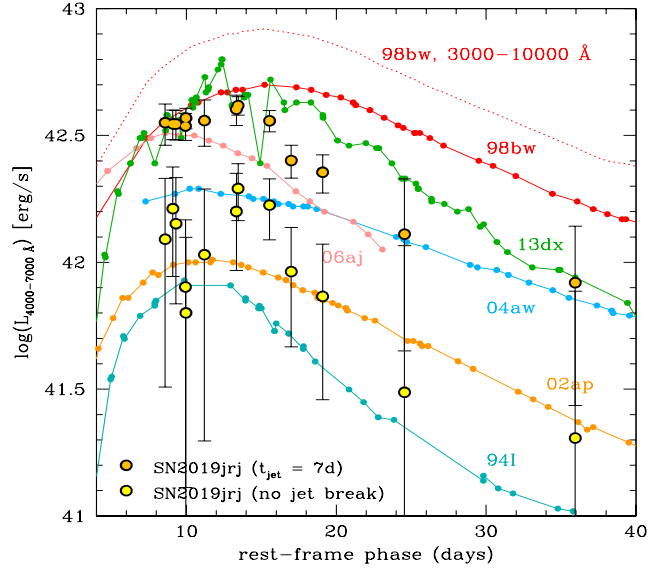


Fig. 3. Light curves of SN 2019jrz computed in the 4000–7000 Å range under the assumptions that a jet break occurs at 7 rest-frame days or does not occur until at least several months after the GRB. The light curves of other core-collapse SNe computed in the same wavelength range from available photometry (Galama et al. 1998; McKenzie & Schaefer 1999; Patat et al. 2001; D’Elia et al. 2015; Toy et al. 2016; Mazzali et al. 2021; Pian et al. 2006; Ferrero et al. 2006; Taubenberger et al. 2006; Foley et al. 2003; Tomita et al. 2006) are shown, as is the light curve of SN 1998bw in the 3000–10000 Å range (dotted red curve). For clarity, uncertainties are shown only for SN 2019jrz.

ing the spectral flux to 4000 Å and 7000 Å, respectively, using a constant. In Fig. 3 we report two pseudo-bolometric curves computed in this way under the two extreme assumptions that a jet break occurs at 7 rest-frame days or does not occur until at least several months after the GRB. These two curves provide the most probable range of the pseudo-bolometric luminosity of SN 2019jrz. For comparison, we show the bolometric light curves of other core-collapse SNe computed in the same wavelength interval. A break at 7 rest-frame days causes the SN component to have a peak luminosity similar to that of SN 2013dx, while absence of a jet break (i.e. a jet break occurring at times later than a few months) causes the SN component to have a peak luminosity comparable to less-luminous core-collapse SNe, in particular SN 2004aw (Fig. 3).

Among our spectra (see Table 2), we concentrate our analysis on the one taken 13.45 rest-frame days after the explosion (approximately corresponding to the maximum brightness of SN 2019jrz), which has the highest signal-to-noise ratio. Even so, individual features cannot be unambiguously detected and atomic species cannot be identified. Therefore, our considerations below are based only on the general spectral shape and appearance. After correcting this spectrum for Galactic extinction ($E(B-V)_{\text{Gal}} \approx 0.013$ mag; Schlafly & Finkbeiner 2011) and intrinsic extinction (with $E(B-V) = 0.3$ mag) in the rest frame and subtracting the afterglow component, the residuals are inconsistent with the spectrum at maximum light of the most luminous GRB SNe, 1998bw and 2013dx (panel a in Fig. 4).

Comparison with maximum-light spectra of less-luminous core-collapse SNe is more satisfactory (panels b and c of Fig. 4). Since both SN luminosity and spectral shape depend on temperature, we conclude that SN 1998bw must be regarded only as an extreme analogue of SN 2019jrz, while its best proxies are in fact less-luminous core-collapse SNe with narrower lines

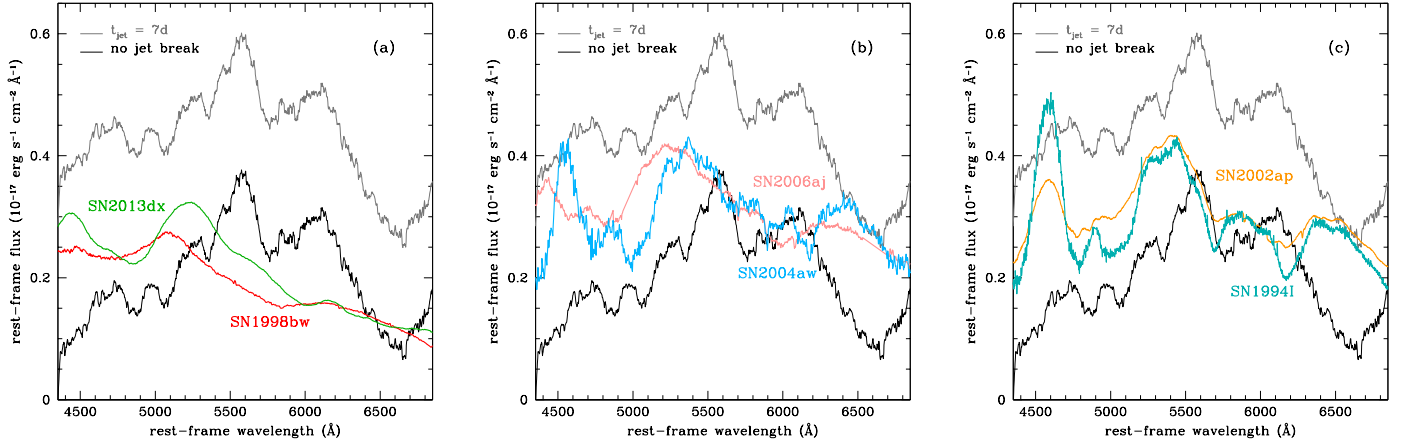


Fig. 4. Comparison between SN 2019jrj spectra and other GRB SNe. (a) Spectra of SN 2019jrj at maximum light obtained under the assumptions of a jet break at 7 rest-frame days (grey upper curve) or no break (black lower curve) and corrected for Galactic reddening ($E(B - V)_{\text{Gal}} \approx 0.013$ mag; Schlafly & Finkbeiner 2011) and line-of-sight reddening at the source ($E(B - V) = 0.3$ mag). For comparison, maximum-light spectra of the GRB SNe 1998bw (Patat et al. 2001) and 2013dx (D’Elia et al. 2015; Mazzali et al. 2021) are shown. These are de-reddened for Galactic extinction, reduced to the rest frame, and scaled in flux to match the SN 2019jrj flux level. (b) Same as in panel a, but compared with maximum-light spectra of the core-collapse Type Ic SNe 2004aw (Taubenberger et al. 2006) and 2006aj (associated with an X-ray flash; Pian et al. 2006; Mazzali et al. 2006). (c) Same as in panel a, but compared with maximum-light spectra of the core-collapse Type Ic SNe 1994I (Filippenko et al. 1995; Foley et al. 2003) and 2002ap (Mazzali et al. 2002; Foley et al. 2003).

(i.e. lower photospheric velocities) and without a detected GRB (SN 2002ap, SN 2004aw). This in turn suggests that while a jet break that occurred as early as 7 days after GRB explosion is formally acceptable, it probably took place later. Along the same line of reasoning, if the break observed in the X-ray light curve at 7 days is wavelength-dependent, it is unlikely to have occurred much earlier in the optical, as in this case the resulting SN would be significantly more luminous than SN 1998bw; this would only worsen the incompatibility with the spectral shape of SN 2019jrj at maximum brightness.

We note that if the optical light were absorbed by a constant intrinsic absorption of $A_V \approx 2$ mag (MAGIC Collaboration 2019b; Misra et al. 2021), the SN peak luminosity under the assumption of a jet break at 7 d would be around 10^{43} erg s $^{-1}$. Such a luminosity is more typical for super-luminous SNe for which a long-lived blue spectrum is commonly observed (e.g., Gal-Yam 2019). This is inconsistent with the relatively red spectral shape observed for SN 2019jrj.

The best analogue of SN 2019jrj in luminosity level, light-curve shape, and spectral line width appears to be SN 2004aw, suggesting that these two SNe may have similar physical properties – a synthesised ^{56}Ni mass of $M_{\text{Ni}} \approx 0.2 M_{\odot}$, an ejecta mass of $M_{\text{ej}} \approx 3\text{--}5 M_{\odot}$, a kinetic energy of $E_{\text{kin}} \approx (3\text{--}6) \times 10^{51}$ erg, and a progenitor mass of $\sim 25 M_{\odot}$ (Mazzali et al. 2017). We stress, however, that these quantities should be regarded as rather uncertain, considering the relatively low quality of the light curve and spectra of SN 2019jrj and our poor ability to constrain the time of the jet break.

We also performed an analysis of the pseudo-bolometric light curve using the analytical model developed by Arnett (1982) for Type Ia SNe. This model can be applied to core-collapse Type Ic SNe with some caveats: first, the model assumes spherical symmetry for the SN ejecta and a constant opacity, κ (fixed to $0.07 \text{ cm}^2 \text{ g}^{-1}$), throughout the entire ejecta; second, it assumes that the total amount of nickel is concentrated at the centre of the ejecta, an assumption that for highly rotating progenitor stars is not entirely true (Izzo et al. 2019; Ashall et al. 2019). The model provides an estimate of the total kinetic energy of the SN ejecta, given the expansion velocity measured from

P Cygni absorption of spectral features around the peak brightness of the SN 5 , as well as an estimate of the total amount of ^{56}Ni synthesised in the explosion. The application of the Arnett formalism to our pseudo-bolometric light curves, assuming an average photospheric velocity of $15\,000 \text{ km s}^{-1}$, yields consistent results with those obtained above by following the analogy with SN 2004aw.

4. Discussion

Our analysis of GRB 190114C/SN 2019jrj, focusing both on the multi-wavelength afterglow and on the SN emission, led to the following main conclusions.

GRB 190114C was very energetic ($E_{\text{iso}} \approx 3 \times 10^{53}$ erg; MAGIC Collaboration 2019b), and it was one of the most energetic GRBs with an associated SN. With a minimum jet break time of 7 days, estimated from analysis of the X-ray light curve, GRB 190114C had an opening angle of at least 13° . This corresponds, for a uniform medium density of $\sim 1 \text{ cm}^{-3}$, to a corrected energy output of $\sim 2 \times 10^{51}$ erg. If the jet break occurred later, this translates into a larger energy.

Accordingly, the luminosity of SN 2019jrj may be as large as that of luminous GRB SNe (particularly SN 2013dx) or as low as that of the stripped-envelope core-collapse SNe 2004aw and 2002ap (not accompanied by a detected high-energy event; Taubenberger et al. 2006; Tomita et al. 2006). This underlines the need for late-time, accurate observations of low-redshift GRBs at all wavelengths to establish the presence of a possible jet break, which is in turn crucial for accurately determining the GRB intrinsic energy and the luminosity of the accompanying SN.

Interestingly, SN 2019jrj does not spectroscopically resemble the most energetic GRB SNe (i.e. GRB SNe with the

⁵ Measuring the total kinetic energy using the spectra at maximum light is highly uncertain. As shown by Mazzali et al. (2017), a change in kinetic energy of 50% is only visible in the spectra one week after the explosion, and not at maximum light. Therefore, we take 50% of the estimated value as the lower limit of the uncertainty in our measurement.

broadest absorption lines), like the prototypical SN 1998bw. Its maximum-light spectrum is instead more similar to that of core-collapse SNe that have less broad lines and no detected accompanying GRB, such as SNe 2004aw and 2002ap. This suggests that less-luminous and less-energetic SNe may also be viable GRB progenitors and may still produce high-energy events of substantial energy.

Decreasing absorption by dust at the source redshift at epochs earlier than 1 observer day, as derived from our combined analysis of the optical and X-ray afterglow light curves, is consistent with the drop in intrinsic neutral hydrogen absorption by a factor of 2 around the same time, as deduced from analysis of the X-ray spectra (Campana et al. 2021). The coherent behaviour derived from these independent analyses of different datasets reinforces the case for a time-variable absorber composed of both dust and gas, although its origin is not known. The seeming contradiction of assuming a uniform medium density in our model in the presence of variable intrinsic absorption is mitigated by the fact that this variation is mild and by our ignorance of the absorber nature and geometry.

It has been suggested that the afterglow of GRB 190114C could originate not only from synchrotron radiation but also from hadronic processes involving photomeson interaction, which may play an important role in the formation of the gamma-ray spectrum up to TeV energies (MAGIC Collaboration 2019a,b; Derishev & Piran 2019; Fraija et al. 2019b; Sahu & López Fortín 2020). If this is the case, the dissipation mechanism responsible for the acceleration of electrons up to high energy may also be responsible for the acceleration of protons to high energy and produce detectable high-energy neutrinos. In fact, the high-energy protons interact with photons, producing charged and neutral pions (Guetta 2015). The pion decay products include leptons and photons:

$$\pi^+ \rightarrow \mu^+ + \nu_\mu \rightarrow e^+ + \nu_e + \bar{\nu}_\mu + \nu_\mu, \quad (1)$$

$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu \rightarrow e^- + \bar{\nu}_e + \nu_\mu + \bar{\nu}_\mu, \quad (2)$$

$$\pi^0 \rightarrow \gamma + \gamma. \quad (3)$$

The TeV fluence of GRB 190114C has been estimated to be $f_{\text{TeV}} \approx 0.1 f_\gamma \approx 4.43 \times 10^{-5} \text{ erg cm}^{-2}$ and the TeV power-law spectrum index to be ~ -2 (MAGIC Collaboration 2019b). The particle spectra at the source may be obtained through a Monte Carlo simulation, as shown in Fig. 1 of Fasano et al. (2021), where the energy spectrum of the interacting protons, as well as the secondary particles emerging from the neutral pion decay of the interaction, is presented. The ordinate axis is in arbitrary units, as these spectra are not normalised. In order to determine a normalisation factor, we can assume that all of the TeV emission of GRB 190114C is due to a hadronic mechanism (Yacobi et al. 2014). In this case (Gagliardini et al., in prep.), the expected neutrino flux from this source is $f_\nu \approx 0.5 f_{\text{TeV}} \approx 2 \times 10^{-5} \text{ erg cm}^{-2}$. Considering the effective area of IceCube corresponding to the declination of the source ($\delta \approx -26^\circ$), the expected average number of upward muon detections for GRB 190114C is 0.04. Therefore, the non-detection of neutrinos from IceCube is not surprising. However, sources that have a declination similar to that of GRB 190114C are very good targets for the KM3Net neutrino telescope (because its effective area is maximal for sources with negative declination) that will be built in the Mediterranean Sea.

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Appendix A: Spectral sequence

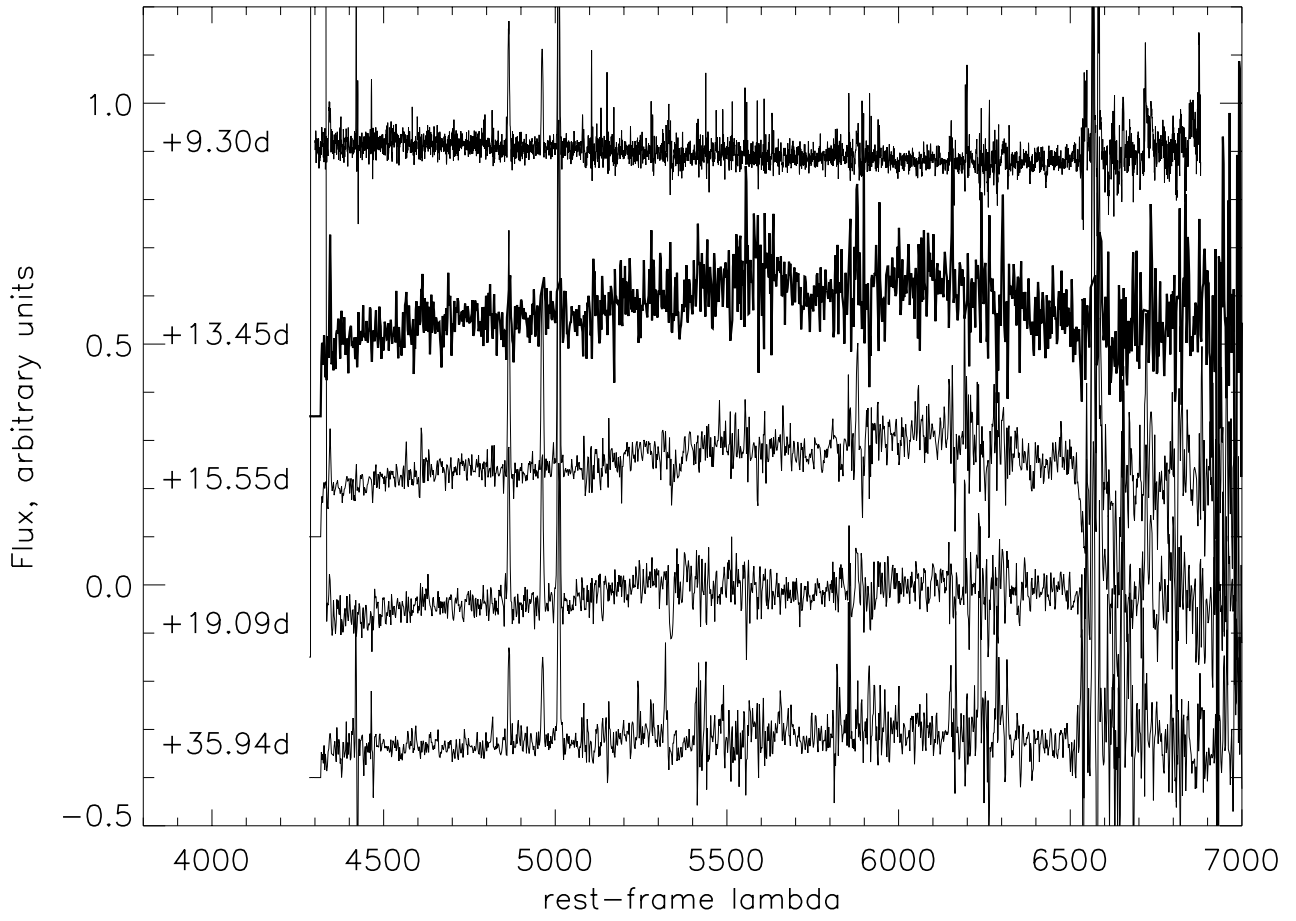


Fig. A.1. SN 2019jrj spectral sequence obtained with LBT and VLT between 9.3 and ~ 36 rest-frame days (see Table 2 and Sect. 2.2 in the main text for more details).