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New insights into the use of Ultra Long Period Cepheids as cosmological standard candles

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ABSTRACT

Ultra Long Period Cepheids (ULPs) are pulsating variable stars with a period longer than 80 d and have been hypothesized to be the extension of the Classical Cepheids (CCs) at higher masses and luminosities. If confirmed as standard candles, their intrinsic luminosities, ~ 1 to ~ 3 mag brighter than typical CCs, would allow to reach the Hubble flow and, in turn, to determine the Hubble constant, H_0 , in one step, avoiding the uncertainties associated with the calibration of primary and secondary indicators. To investigate the accuracy of ULPs as cosmological standard candles, we first collect all the ULPs known in the literature. The resulting sample includes 63 objects with a very large metallicity spread with $12 + \log([O/H])$ ranging from 7.2 to 9.2 dex. The analysis of their properties in the VI period–Wesenheit plane and in the colour–magnitude diagram (CMD) supports the hypothesis that the ULPs are the extension of CCs at longer periods, higher masses and luminosities, even if, additional accurate and homogeneous data and a devoted theoretical scenario are needed to get firm conclusions. Finally, the three M31 ULPs, 8-0326, 8-1498, and H42, are investigated in more detail. For 8-1498 and H42, we cannot confirm their nature as ULPs, due to the inconsistency between their position in the CMD and the measured periods. For 8-0326, the light curve model fitting technique applied to the available time-series data allows us to constrain its intrinsic stellar parameters, distance, and reddening.

Key words: stars: distances – stars: variables: Cepheids – distance scale.

1 INTRODUCTION

The extragalactic distance scale is largely based on the period–luminosity (PL) relation of Classical Cepheids (CCs), a well-known class of Population I ($t < 400$ Myr) pulsating variable stars. Their pulsation period typically ranges from 1 to 100 d and their absolute visual magnitudes ($-8 < M_V < -2$ mag) are bright enough to make them easily detectable within the Local Group and (because of current space observations with the *Hubble Space Telescope*) in external galaxies up to ~ 30 Mpc (Riess et al. 2011). To reach cosmologically relevant distances, in the so-called Hubble flow, secondary distance indicators, such as the Tully–Fisher relation and Type Ia Supernovae (SNe Ia) have to be applied. These, in turn, need to be calibrated with primary distance indicators, including not only CCs but also Pop II standard candles, such as the Tip of the red giant branch or RR Lyrae stars. This procedure implies that any systematic error affecting primary and secondary distance indicators reflects on the Hubble constant evaluation based on the extragalactic distance scale (see e.g. Freedman et al. 2001; Altavilla et al. 2004; Di Criscienzo et al. 2006; De Somma et al. 2020a). The derivation of the Hubble constant H_0 from the Cepheid-based extragalactic distance scale has recently drawn a renewed attention in the context of a lively debate on the evidence of a tension between Hubble constant evaluations

based on the cosmic microwave background and local values based on the cosmic distance scale (see e.g. Riess et al. 2018, 2019, and references therein). However, notwithstanding theoretical and observational efforts (see e.g. Freedman et al. 2001; Riess et al. 2011; Fiorentino et al. 2013; Anderson & Riess 2018; De Somma et al. 2020a, and references therein) to reduce the uncertainties associated to primary distance indicators, the systematic errors still affecting secondary distance indicators (see e.g. Altavilla et al. 2004; Verde, Treu & Riess 2019, and references therein) also contributing to the final H_0 error budget.

In this context, the possibility to use primary indicators observable in the Hubble flow would be very important. Bird, Stanek & Prieto (2009) pointed out the presence of a small number of variables with long periods ($80 \lesssim P \lesssim 210$ d) in nearby forming galaxies (Magellanic Clouds, NGC 55, NGC 6822, NGC 300), hypothesized to be the counterparts at higher luminosity and mass of the CCs. Indeed, their light curves are very similar to the CC ones and Bird et al. (2009) show (see their figs 2, 4, and 5) that they appear to follow the extension at longer periods of the CC PL and period–Wesenheit (PW) relations. Because of their high luminosity, this class of variables could represent candidate primary distance indicators able to reach, in one step, distances of the order 100 Mpc and beyond, in particular with next-generation telescopes such as the European Extremely Large Telescope and the James Webb Space Telescope. Despite their promising role, the use of the ULPs as standard candles is largely debated in the literature due to the small

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sample of known ULPs and the particular observational strategy required to follow repeated pulsation cycles at these very long periods.

Fiorentino et al. (2012, 2013) analysed a sample of 37 Ultra Long Period Cepheids (ULPs) with known V and I magnitudes, identified in galaxies with a very large metallicity range $12 + \log(O/H)$ varying from ~ 7.2 to 9.2 dex. This sample includes the ULPs collected by Bird et al. (2009) in the galaxies LMC, SMC, NGC 55, NGC 300, NGC 6822 and IZw18, the two ULPs in M81 by Gerke et al. (2011) and those identified by Riess et al. (2011) in the framework of the SH0ES project,¹ in the galaxies NGC 1309, NGC 3021, NGC 3370, NGC 4536, NGC 5584, NGC 4038, and NGC 4258. Fiorentino et al. (2012, 2013) do not confirm the flat VI Wesenheit relation obtained by Bird et al. (2009) but find a relation similar to that obtained for the LMC Cepheids with no significant dependence on metallicity (as expected for the PW in these filters based on theoretical predictions; Fiorentino et al. 2007; Bono et al. 2008), but with an unexpected larger spread. This spread can be due to many different contributions such as, for example, poor statistics or light curve sampling for some ULPs, the use of non-homogeneous photometric data, but also the adoption of reddening and metallicity values from different sources.

Moreover, the two ULPs identified in the very metal-poor blue compact dwarf galaxy IZw18 have very long periods (about 125 and 130 d, respectively) and are very interesting because, at this very low metallicity range, evolution and pulsation models do not predict the existence of such ULPs (Fiorentino et al. 2010; Marconi et al. 2010).

Riess et al. (2011) CC samples were enlarged, updated, and recalibrated by Riess et al. (2016) and Hoffmann et al. (2016) finding a sample of 40 ULPs in 14 galaxies. These authors obtained a new calibration for all the observed samples and applied for all the galaxies a consistent procedure to identify variable stars and their properties. Among the 19 ULPs identified by Riess et al. (2011) in the three galaxies NGC 1309, NGC 3021, and NGC 3370 and adopted by Fiorentino et al. (2012), only 16 were confirmed as ULPs, but with a different period.

In addition, Ngeow et al. (2015), using the R -band data of the Palomar Transient Factory (PTF), identified a sample of ULP candidates. For these variables, the authors performed a follow-up to obtain VI band time-series, and only two, namely 8-0326 and 8-1498, have been classified as ULPs with period of 74.427 ± 0.120 d and 83.181 ± 0.178 d, respectively (even if one of these stars has a period shorter than 80 d). Then, they used these variables to derive M31 distance and test their goodness as standard candles.

Very recently, Taneva et al. (2020) published BVR photometry for another candidate M31 ULP, identified using PTF data, namely H42 with a period of 177.32 d.

The resulting sample, including 63 objects, is also characterized by a large metallicity spread and is statistically more significant than those adopted by Bird et al. (2009) and Fiorentino et al. (2012, 2013), allowing us to improve the analysis of the properties of these variables and to get information on their use as standard candles for the cosmic distance ladder.

The ULP sample adopted in this paper is presented in Section 2. Their VI Wesenheit relation is discussed in Section 3 and the other ULP properties are analysed in Section 4. In Section 5, we discuss the comparison of the ULP sample with theoretical pulsational models, analysing, in particular, the properties of the M31 ULPs, for which time-series data are available (Ngeow et al. 2015; Taneva et al. 2020),

¹ ‘Supernovae and H0 for the Equation of State’ to observe Cepheid variables in galaxies hosting SNe Ia.

and the light curve model fitting technique can be applied (see also Marconi et al. 2013a, 2017; Ragosta et al. 2019, and references therein). The conclusions close the paper.

2 ULP SAMPLE

In Table 1, we list the ULP sample we collected in this work for which we have VI mean magnitudes. It includes the 18 ULPs compiled by Bird et al. (2009; hereinafter Bird sample), the 2 M81 ULPs by Gerke et al. (2011), the 2 M31 ULPs confirmed by Ngeow et al. (2015), and the 40 ULPs identified by Riess et al. (2016) and Hoffmann et al. (2016) (hereinafter SH0ES sample). We do not have new ULPs or new mean magnitude determinations for already known ULPs neither in the *Gaia* DR2 Cepheid sample reclassified by Ripepi et al. (2019) nor in the recent OGLE Collection of Variable Stars in the Milky Way and the Magellanic Clouds (Soszyński et al. 2015, 2017; Udalski et al. 2018; Soszyński et al. 2019).

In Table 1, the colour excesses are those of the host galaxies based on the Galactic dust reddening maps by Schlafly & Finkbeiner (2011). The references relative to V , $V - I$, distance modulus and $12 + \log(O/H)$ for the Bird sample and IZw18 are reported in Fiorentino et al. (2012) and for M81 in Gerke et al. (2011). For M31, V and $V - I$ are taken from Ngeow et al. (2015), the distance modulus from de Grijs & Bono (2014), the metal abundances of the two ULPs using their position (Lee et al. 2013) and the metallicity gradient measured in this galaxy by Gregersen et al. (2015)² instead of using M31 mean metallicity. For the SH0ES sample, V and $V - I$ are obtained applying photometric transformation by Sahu, Deustua & Sabbi (2014) to the UVIS-WFC3 F555W and F814W Hoffmann et al. (2016); the distance moduli and the individual metal abundances (obtained from the metallicity gradient of the host galaxy) are tabulated in Riess et al. (2016) and Hoffmann et al. (2016). For all the ULPs, we also report the corresponding Z metallicity.³

For the M31 ULP H42, we do not have any I band measurement, but we have the mean magnitudes in the B and V bands obtained by Taneva et al. (2020): $V = 18.16$ mag and $(B - V) = 1.32$ mag with a period of 177.32 d. As for the other M31 ULPs, we adopted $\mu = 24.46$ mag and $E(B - V) = 0.05$ mag for the distance modulus and reddening and determined the metallicity from its position and the metallicity gradient by Gregersen et al. (2015), obtaining $Z = 0.01$.

3 PERIOD–WESENHEIT RELATIONS FOR ULPs

In Fig. 1, the ULPs reported in Table 1 are compared with LMC OGLE (bottom panel, Soszyński et al. 2015) and NGC 4258 (upper panel, Hoffmann et al. 2016; Riess et al. 2016) CCs, respectively, in the PW_{VI} plane, with $W_{VI} = I - 1.55(V - I)$. The black line in the bottom panel and the dashed black line in the upper panel represent the W_{VI} by Soszyński et al. (2015; with a slope of -3.314 ± 0.008) and Riess et al. (2016; with a slope of -3.38 ± 0.02 mag for $P > 10$ d obtained with a global fit), respectively.

The dispersion of the ULPs, in this plot, is much larger than that of the LMC OGLE CCs, but very similar to that of the NGC 4258

²Gregersen et al. (2015), in the framework of the PHAT survey, analysed the metallicity distribution of 160 Cepheids in the Andromeda galaxy, finding a metallicity $12 + \log([O/H])$ varying between 8.82 and 9.12 dex (see their fig. 11) corresponding to a Z ranging between 0.01 and 0.03.

³ $[O/H] = \log(O/H) - \log(O/H)_{\odot}$ with $\log(O/H)_{\odot} = -3.10$. Assuming that $[O/H] = [Fe/H]$, we obtain $[O/H] = \log Z - \log Z_{\odot}$ and then $Z = 10^{[O/H] + \log Z_{\odot}}$, with $Z_{\odot} = 0.02$

Table 1. ULPs with V and I mean magnitudes.

Galaxy	Period (d)	V (mag)	$V - I$ (mag)	μ_0 (mag)	$E(B - V)^{(1)}$ (mag)	$12 + \log(O/H)$ (dex)	Z
Bird sample							
LMC	109.2	12.41	1.07	18.50	0.07	8.396	~ 0.008
LMC	98.6	11.92	1.11	18.50	0.07	8.396	~ 0.008
LMC	133.6	12.12	1.09	18.50	0.07	8.396	~ 0.008
SMC	210.4	12.28	0.83	18.93	0.03	7.982	~ 0.002
SMC	127.5	11.92	1.03	18.93	0.03	7.982	~ 0.002
SMC	84.4	11.97	0.91	18.93	0.03	7.982	~ 0.002
NGC 55	175.9	19.25	0.84	26.43	0.01	8.053	~ 0.003
NGC 55	152.1	19.56	0.95	26.43	0.01	8.053	~ 0.003
NGC 55	112.7	20.18	1.05	26.43	0.01	8.053	~ 0.003
NGC 55	97.7	20.54	1.25	26.43	0.01	8.053	~ 0.003
NGC 55	85.1	20.84	1.38	26.43	0.01	8.053	~ 0.003
NGC 300	115.8	20.13	0.97	26.37	0.01	8.255	~ 0.004
NGC 300	89.1	19.71	1.02	26.37	0.01	8.255	~ 0.004
NGC 300	83.0	19.26	0.77	26.37	0.01	8.255	~ 0.004
NGC 6822	123.9	17.86	1.40	23.31	0.21	8.114	~ 0.003
IZw18	130.3	23.96	0.96	31.30	0.03	7.211	~ 0.0004
IZw18	125.0	23.65	0.97	31.30	0.03	7.211	~ 0.0004
M81 ULPs							
M81	96.8	21.52	1.40	27.69	0.07	8.77	~ 0.013
M81	98.981	21.69	1.42	27.69	0.07	8.77	~ 0.013
M31 ULPs							
M31	74.427	18.684	1.428	24.46	0.05	9.03	~ 0.02
M31	83.181	18.856	1.073	24.46	0.05	9.03	~ 0.02
SHOES sample							
M101	81.521	22.70	1.04	29.14	0.008	9.15	0.028
NGC 1015	87.327	25.90	1.04	32.50	0.029	8.704	0.010
NGC 1015	97.489	26.09	1.15	32.50	0.029	9.033	0.022
NGC 1309	80.886	25.87	1.10	32.52	0.035	9.115	0.026
NGC 1309	84.543	26.89	1.03	32.52	0.035	8.885	0.015
NGC 1309	84.888	26.00	1.23	32.52	0.035	9.007	0.020
NGC 1309	90.592	26.54	1.27	32.52	0.035	8.781	0.012
NGC 1309	90.713	26.37	1.23	32.52	0.035	8.838	0.014
NGC 1309	90.911	26.51	1.02	32.52	0.035	9.061	0.023
NGC 1448	93.353	25.08	1.15	31.31	0.012	8.852	0.014
NGC 1448	97.203	25.32	1.37	31.31	0.012	8.849	0.014
NGC 2442	81.839	27.90	1.83	31.51	0.179	9.076	0.024
NGC 2442	91.57	26.64	1.56	31.51	0.179	8.878	0.015
NGC 3370	84.917	26.03	1.05	32.07	0.028	9.029	0.021
NGC 3370	88.165	25.51	0.93	32.07	0.028	8.756	0.011
NGC 3370	96.096	25.84	1.16	32.07	0.028	8.798	0.013
NGC 3972	85.622	25.06	1.00	31.59	0.013	8.878	0.015
NGC 3982	83.302	24.94	0.80	31.74	0.012	9.074	0.024
NGC 4038	80.257	24.03	1.08	31.29	0.041	9.046	0.022
NGC 4038	80.274	25.99	1.24	31.29	0.041	9.065	0.023
NGC 4038	83.753	24.42	0.88	31.29	0.041	9.105	0.025
NGC 4038	93.069	25.42	1.21	31.29	0.041	9.055	0.023
NGC 4038	93.35	24.53	0.90	31.29	0.041	9.01	0.020
NGC 4038	93.573	25.68	1.45	31.29	0.041	8.937	0.017
NGC 4038	94.396	25.38	0.99	31.29	0.041	9.026	0.021
NGC 4038	95.644	24.06	0.82	31.29	0.041	9.071	0.024
NGC 4038	97.11	24.35	0.70	31.29	0.041	9.094	0.025
NGC 4258	83.258	23.20	1.07	29.39	0.014	8.743	0.011
NGC 4258	84.618	23.60	1.42	29.39	0.014	8.77	0.012
NGC 4536	93.621	24.15	0.97	30.91	0.016	8.905	0.016
NGC 4536	98.775	24.29	1.24	30.91	0.016	8.887	0.015
NGC 4639	81.011	26.35	1.39	31.53	0.023	9.055	0.023
NGC 5584	81.2	25.73	1.15	31.79	0.035	8.95	0.018
NGC 5584	81.356	25.58	1.10	31.79	0.035	8.743	0.011
NGC 5584	85.106	25.18	0.98	31.79	0.035	8.836	0.014
NGC 5584	85.709	25.70	1.03	31.79	0.035	8.891	0.016
NGC 5584	88.513	25.95	1.19	31.79	0.035	8.804	0.013
NGC 5584	97.752	26.18	1.42	31.79	0.035	8.811	0.013
NGC 7250	83.098	25.96	1.29	31.50	0.136	8.605	0.008
UGC9391	82.992	27.20	1.26	32.92	0.009	8.946	0.018

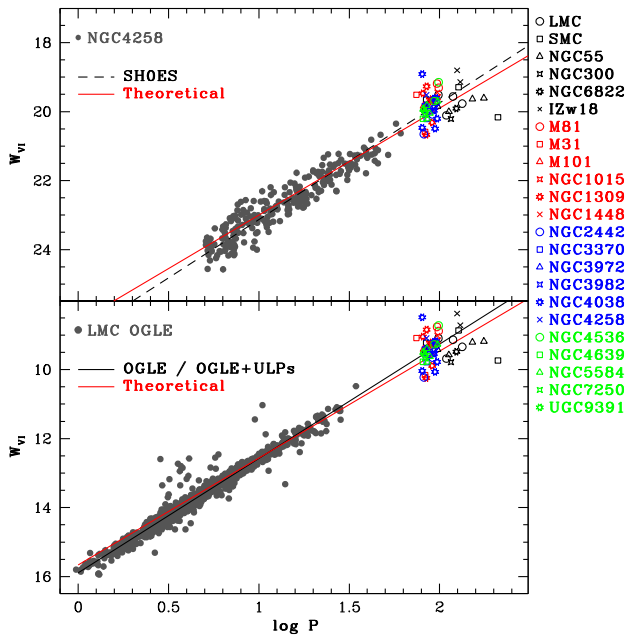


Figure 1. W_{VI} for the ULPs in Table 1 compared with LMC OGLE (the grey dots in the bottom panel; Soszyński et al. 2015) and NGC 4258 (the grey dots in the upper panel; Hoffmann et al. 2016 Riess et al. 2016) CC sample, respectively. The black line in the bottom panel represents the LMC VI Wesenheit obtained by Soszyński et al. (2015), whereas the dashed black line in the upper panel is the VI Wesenheit relation by Riess et al. (2016) in the framework of the SHOES project. The red line in both panels represents the theoretical metal dependent W_{VI}^T by Fiorentino et al. (2007) adopting $Z = 0.01$ (see Section 5 for details). The symbols adopted for the ULPs are labelled in figure.

Cepheid sample. There are many possible causes for this large spread. As we know, ULPs, as well as CCs, are observed in very dense environments so that they are subject to high (and possibly spatially varying) reddening and blending effects. A possible variation of the reddening law can influence the spread of the Wesenheit due to a not complete correction of mean (or differential) reddening. However, the very narrow OGLE Cepheids PW relation seems to support the reliability of the adopted colour term. On the other hand, blending can have an important role in the dispersion of this relation. This effect has been analysed by several authors. In particular, Anderson & Riess (2018, and references therein) pointed out that the blending effect is the major error source in the distance scale calibration and increases with the distance of the observed galaxies. In our analysis, another possible contribution to the spread can be due to the adopted individual values of reddening and distance. However, a similar spread is observed in much farther galaxies such as NGC 4258, where these effects are not expected to contribute.

In Fig. 2, we compare the distribution in the PW_{VI} plane of the ULPs in Table 1 with the PW relations obtained by Soszyński et al. (2015) for the LMC OGLE sample (the black line), by Bird et al. (2009) for the ULPs (the black-dashed line), whereas the red-dashed line is the relation obtained in this work adopting all the compiled ULPs ($W_{VI} = -0.93 \log P - 7.28$ with $\sigma = 0.38$). The adoption of a sample collected by different authors can introduce systematic errors in our analysis. For this reason, we carried out a fit for the Wesenheit relation, based only on the SHOES ULP sample, obtaining $W_{VI} = -2.89 \log P - 3.42$ with an intrinsic dispersion $\sigma = 0.36$ (the blue line in Fig. 2). This result is significantly different from the

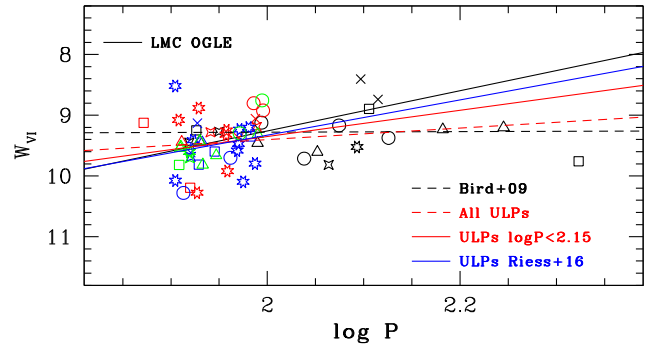


Figure 2. VI Wesenheit function only for the ULPs in Table 1 placed at the distance of the LMC. The black line is the LMC W_{VI} by OGLE (Soszyński et al. 2015), the black-dashed line is the W_{VI} by Bird et al. (2009), the red-dashed line, the red line, and the blue line are the W_{VI} obtained in this work using all the ULPs, those with $\log P < 2.15$ and only those compiled by Riess et al. (2016), respectively. The symbols for the ULPs are the same adopted in Fig. 1.

relation obtained adopting the full sample, but we have to note that the range $\log P > 2.15$ is very poorly sampled (due to the difficulty to identify and characterize very long period variables), probably creating a false trend for the Wesenheit relation. For this reason, we perform an additional fit excluding these longest periods stars, obtaining $W_{VI} = -2.15 \log P - 4.89$ with $\sigma = 0.38$ mag (the red solid line in figure). This relation is much steeper than the almost flat slope by Bird et al. (2009): $W_{VI} = -0.05 \log P - 9.12$ with $\sigma = 0.36$ mag and in better agreement with the result based on the SHOES sample. It is worth to note that, in the period range covered by the ULPs, this relation is in good agreement (with a difference in the inferred W magnitude smaller than ~ 0.05 mag) with the result by Soszyński et al. (2015) for LMC OGLE CCs. On this basis, we perform a global fit including the LMC OGLE CCs and our ULPs, obtaining a slope of -3.30 ± 0.01 and a $\sigma = 0.14$ mag in perfect agreement with that by Soszyński et al. (2015), -3.314 ± 0.008 , both using all the ULPs with $\log P \leq 2.15$ and involving only the SHOES ULPs. The very small error of 0.01 mag, obtained in the global fit, is due to the very large OGLE sample (2455 CCs) that dominates the dispersion term. In any case, this result represents an important hint to consider the ULPs as the counterparts of the CCs at higher mass and luminosity and seems to confirm the higher robustness of the fit obtained using only the SHOES sample. On the other hand, we have to underline that also this last fit shows a large sigma due to the dispersion of the ULPs around the Wesenheit relation, notwithstanding the accurate and homogeneous photometry. To investigate if a possible origin of this dispersion is the metallicity spread, in Fig. 3 we show the differences between the Wesenheit relation as defined for the LMC CCs, $W(LMC)$, and that in the host galaxy $W(gal)$ versus the individual metal abundances for all the ULPs with $\log P \leq 2.15$. No significant trend is noted in this plot. The observed spread can be intrinsic and/or due to different effects, such as photometric errors, crowding, blending, but no firm conclusion can be drawn on the basis of current data sets.

4 ULP PROPERTIES

Fig. 4 shows the position of the ULP sample in Table 1 (the symbols are the same adopted in Fig. 1) in the colour-magnitude diagram (CMD) V_0 versus $(V - I)_0$, compared with the LMC OGLE CCs (the grey dots, Soszyński et al. 2015). The ULPs seem to locate

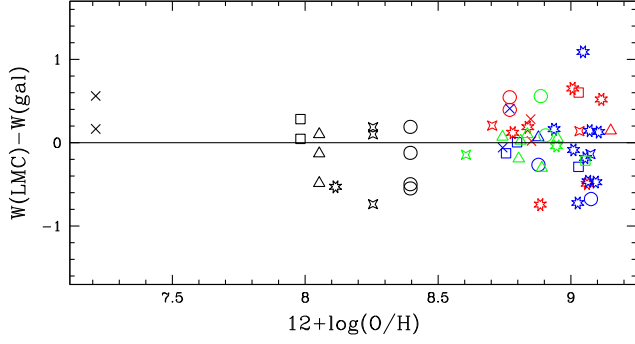


Figure 3. Differences between the Wesenheit relation as defined for the LMC CCs, $W(LMC)$, and that in the host galaxy $W(gal)$ for all the ULPs in Table 1 versus their metallicity. The symbols for the ULPs are the same adopted in Fig. 1.

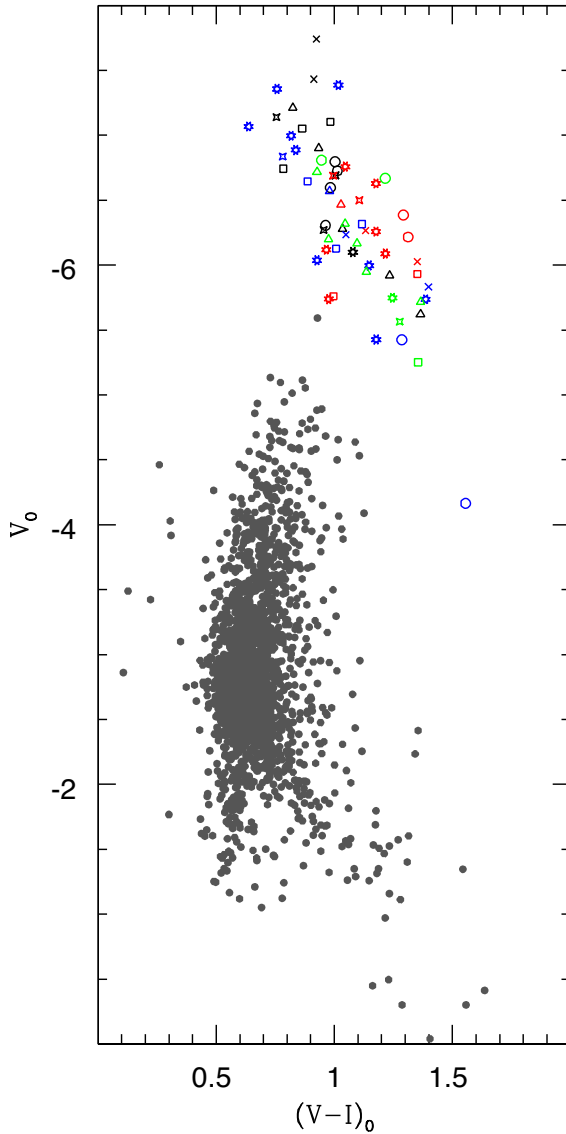


Figure 4. CMD V_0 versus $(V - I)_0$ for LMC OGLE Cepheids (the grey dots) and ULPs in Table 1. The symbols for the ULPs are the same adopted in Fig. 1.

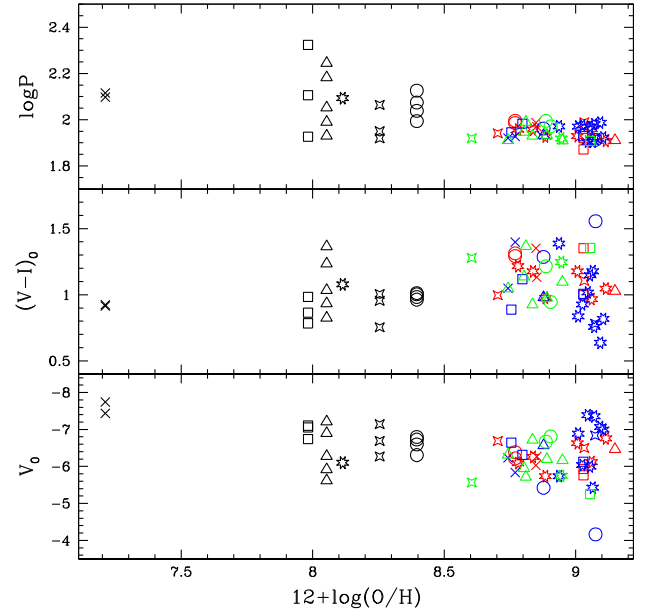


Figure 5. We plot the period (upper panel), and the absolute colour (middle panel) and magnitude (bottom panel) of ULPs in Table 1 versus their metallicity. The symbols for the ULPs are the same adopted in Fig. 1.

in a region that corresponds to the extrapolation of CC Instability Strip towards higher masses and luminosities, thus confirming the result already found in the PW plane, even if a number of objects appear to be more luminous and bluer than expected. To investigate the causes of this behaviour, we analyse in Fig. 5 the dependence of ULP periods, colours, and absolute visual magnitudes on the metal abundance. We notice that more metal-poor ULPs appear to have longer periods and to be slightly brighter and bluer than the other pulsators. This occurrence could partially justify the position in the CMD of the ULPs belonging to SMC, NGC 55, NGC 300, and IZw18. On the other hand, the SHOES metal-rich ULPs do not appear systematically redder and fainter, being distributed on a wide range of colours and magnitudes. This holds in particular for the NGC 4038 ones, for which the stellar metallicity has been recently confirmed to be solar by Lardo et al. (2015). At this stage, we cannot conclude if this behaviour is an intrinsic property of the ULPs or due to a not sufficient photometric accuracy, crowding and/or blending effects. Probably, a more statistically significant sample of photometrically homogeneous and accurate data, covering larger period and metallicity ranges, is needed to clarify the observed trend.

In Fig. 6 we show the $V_0 - (V - I)_0$ CMD only for the ULPs in Table 1 and the evolutionary tracks by Bressan et al. (2012),⁴ for 14 (the solid lines) and 20 M_{\odot} (the dashed lines), including the mass range covered by the ULP luminosities (Bird et al. 2009; Fiorentino et al. 2012), and for metallicities ranging from $Z = 0.0005$ to $Z = 0.03$ (see labels in Fig. 6), representative of the observed range covered by our sample. Due to the higher masses and in turn, shorter evolutionary times expected for the ULPs,⁵ the probability to observe this class

⁴Transformed to the Johnson bands using the Chen et al. (2019) web tool <http://stev.oapd.inaf.it/YBC/index.html>.

⁵Taking into account the very recent theoretical instability strip computed by De Somma et al. (2020a), we have that the crossing time for a 20 M_{\odot} are about 1.2 Myr and for a 14 M_{\odot} , about 2 Myr in comparison with that of 10^5 and 10^4 yr for a 6 and a 11 M_{\odot} (De Somma et al. 2020b), respectively.

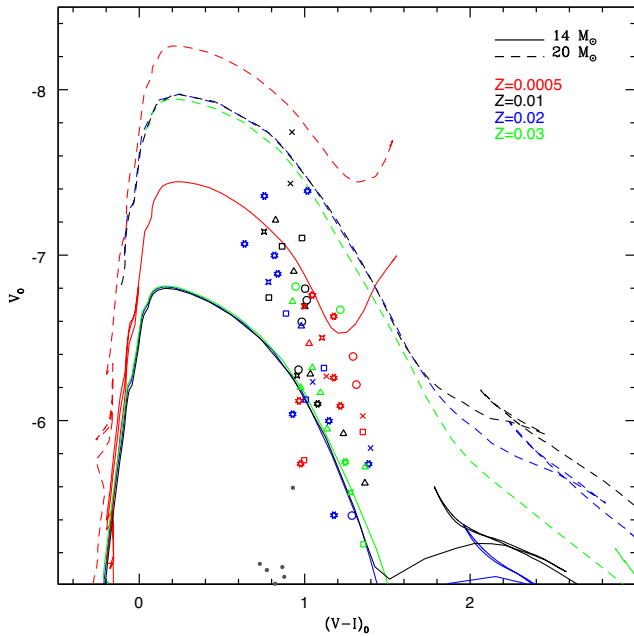


Figure 6. CMD V_0 versus $(V - I)_0$ for our ULP sample (the symbols for the ULPs are the same adopted in Fig. 1). The stellar tracks for 14 (the solid line) and 20 (the dashed line) M_\odot and for different metallicities ranging between $Z = 0.0005$ to 0.03 (see labels in figure).

of pulsators in an external galaxy is lower than for CCs. Indeed, the evolutionary tracks for these masses do not show the blue loop crossing the instability strip as in the lower mass range.

5 COMPARISON WITH PULSATIONAL THEORETICAL MODELS

In this section, we compare the observed pulsation properties of the investigated ULPs with the predictions of non-linear convective pulsation models (see e.g. Caputo, Marconi & Musella 2000; Marconi, Musella & Fiorentino 2005; Fiorentino et al. 2007; Marconi et al. 2010, and references therein). In both panels of Fig. 1, we also plot the theoretical metal-dependent Wesenheit relation obtained by Fiorentino et al. (2007), $W_{VI}^T = -2.67 - 3.1 \log P + 0.08 \log(Z)$ with a $\sigma = 0.11$ mag, shifted for the distance modulus of LMC and NGC 4258, respectively. The metallicity adopted to plot this theoretical relation is $Z = 0.01$, close to the LMC metallicity, but, as shown in Caputo et al. (2000) and Fiorentino et al. (2007), the theoretical Wesenheit function built using V and I bands has a negligible dependence on the chemical composition varying by 0.04 mag in the range from $Z = 0.01$ to $Z = 0.03$. This relation has been obtained in the framework of a theoretical scenario based on non-linear, non-local time-dependent convective pulsation models relying on physical and numerical assumptions discussed in our previous papers (see e.g. Bono, Marconi & Stellingwerf 1999; Marconi et al. 2005, and references therein) and assuming a large range of masses (from 3 to 13 M_\odot) and chemical compositions ($0.0004 < Z < 0.04$, $0.25 < Y < 0.33$, Fiorentino et al. 2002; Marconi et al. 2005, 2010, and references therein). These models allow us to predict all the relevant pulsation observables, including the period, amplitude and morphology of light and radial velocity curves as a function of the input parameters (see e.g. Natale, Marconi & Bono 2008; Marconi et al. 2017, and references therein).

As the theoretical and observational PW relations show a good agreement, within the respective σ , we can confirm the conclusions reached above, adopting the relation by Soszyński et al. (2015). On the other hand, we deduce that to better understand the ULP behaviour both in the Wesenheit plane and in the CMD, we need to extend our theoretical scenario to the larger masses typical of the ULPs.

An alternative route to constrain the individual distances, allowing us to simultaneously constrain the intrinsic stellar properties, of pulsating stars is the model fitting of observed light curves (see e.g. Natale et al. 2008; Marconi et al. 2013a; Ragosta et al. 2019, and references therein).

Among the ULPs of our sample, for the three M31 ones, we also have time-series data by Ngeow et al. (2015) and Taneva et al. (2020) and the investigation of their light variations could offer a unique opportunity to obtain fundamental information both on the reliability of the adopted pulsation models and on the use of the ULPs as standard candles.

The distance moduli, obtained by applying the theoretical VI Wesenheit relation to the two M31 ULPs found by Ngeow et al. (2015; the two open squares in the CMD), are 24.07 ± 0.11 mag for 8-0326 and 25.29 ± 0.11 mag for 8-1498 (the errors are determined by the intrinsic dispersion of the theoretical relation). The obtained average distance modulus is 24.70 ± 0.16 mag, with a large error due to the significant difference between the two individual values, but still consistent with some of the most recent reliable estimates of M31 distance in the literature. In particular, de Grijs & Bono (2014) found 24.46 ± 0.10 mag performing an accurate weighted mean of different results obtained by stellar distance indicators, such as Cepheids, RR Lyrae, and the tip of the red giant branch, whereas Wagner-Kaiser et al. (2015), using a Cepheid PL relation, found a distance modulus of 24.32 ± 0.09 mag in the optical bands and 24.51 ± 0.08 mag in the near-infrared ones.

Based on the results in Section 3, we derive the distance moduli also applying the ULP Wesenheit relation obtained using only the SHOES sample. The resulting distance moduli are 24.38 ± 0.36 mag and 25.51 ± 0.36 mag (the errors are determined by the σ of the relation) for 8-0326 and 8-1498, respectively. In this case, the mean distance is 24.94 ± 0.51 mag, consistent within the errors with the other quoted M31 distance evaluations, but with a much larger error.

Both adopting the theoretical relation and the empirical one based on SHOES ULPs, we find a large deviation of the distance modulus of 8-1498. The peculiar properties of this star are discussed in the following.

5.1 Model fitting of the M31 ULPs

In the left-hand panel of Fig. 7, we plot the V_0 , $(V - I)_0$ CMD with the two M31 ULPs found by Ngeow et al. (2015), 8-0326 and 8-1498 (the red open squares), overimposed to the evolutionary tracks for metallicity $Z = 0.02$ and stellar masses ranging from 12 to 20 M_\odot . In the right-hand panel of the same figure, we plot the position of the M31 ULP by Taneva et al. (2020), H42 (the black-filled circle), in the $V, B - V$ CMD overimposed to the evolutionary tracks for metallicity $Z = 0.01$, and masses equal to 10, 18, 20, and 24 M_\odot . We notice that the ULP 8-0326 is located on the $M = 16 M_\odot$ evolutionary track, with M , $\log L$, and T_e of about 15.7 M_\odot , 4.57 dex and 4300 K, respectively. From these values, we can infer the predicted pulsation period by relying on the PL-colour-mass (PLCM) relation by De Somma et al. (2020a) and find a period of about 91 d that is longer than the observed value (74.427 d, Ngeow et al. 2015). To reproduce the observed period, we need to increase T_e up to about 4500 K or decrease

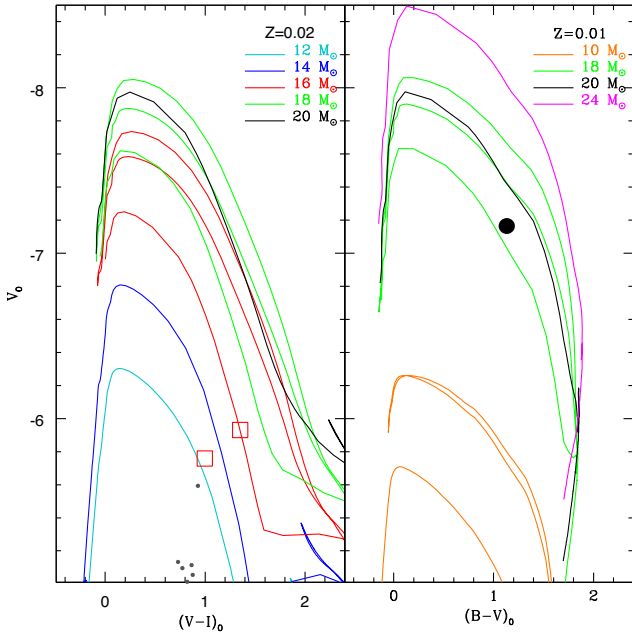


Figure 7. Left-hand panel: V_0 versus $(V - I)_0$ CMD for the M31 ULPs (the red open squares) by Ngeow et al. (2015), 8-0326 and 8-1498, with stellar tracks for $Z = 0.02$ and mass between 12 and $20 M_{\odot}$ (see colours and labels in figure). Right-hand panel: V_0 versus $(B - V)_0$ CMD for the M31 ULP (the black-filled circle) by Taneva et al. (2020) with stellar tracks for $Z = 0.01$ and mass between 10 and $24 M_{\odot}$ (see colours and labels in figure).

the luminosities down to about 4.43 dex. To preserve the mass–luminosity relation, also considering the non-negligible uncertainty related to colour–temperature transformation (with differences of about 150 K due to variations in the adopted model atmospheres, see also Marconi et al. 2015, and references therein), in the following we adopt $T_e = 4500$ K for ULP 8-0326 as starting point for our light curve model fitting procedure.

As for ULP 8-1498, its position in the CMD lies between the evolutionary tracks at 12 and $14 M_{\odot}$. By interpolating between these mass values we expect that the mass, the luminosity level and the effective temperature are around $12.5 M_{\odot}$, 4.3 dex, and 5000 K, respectively. These values, when used as input parameters in the theoretical PLCM mentioned above, correspond to a period of about 38 d, very different from the observed period of 83.181 d obtained by Ngeow et al. (2015).⁶

Concerning H42 ULP, Taneva et al. (2020) suggest a mass of $20 M_{\odot}$. Indeed, from its position in the V_0 , $(B - V)_0$ CMD, we infer a stellar mass ranging from 18 to $20 M_{\odot}$. By assuming a mass in this range and the corresponding luminosity and effective temperature, as derived from the evolutionary tracks, we applied the PLCM relation by De Somma et al. (2020a). As a result, we derived a period around 100 d. To obtain a period of 177 d, we need to decrease the mass to about $10 M_{\odot}$, but the corresponding magnitude and colour are not consistent with the evolutionary track for this mass value (orange line in the right-hand panel of Fig. 7).

Due to these inconsistencies between period mass and luminosity, we could not apply the light curve model fitting procedure to the variables 8-1498 and H42. Additional data are needed in order to

⁶We used Ngeow et al. (2015) data to re-determine the period of this ULP, obtaining the same result within the errors. On the contrary, adopting 38 d as period, the light curve is not phased.

understand if these results are affected by a poor period determination and to confirm the ULP nature of these variables.

To perform an accurate fit of 8-0326 light curves in V and I bands, we constructed a set of pulsation models with the period equal to the observed one (within ~ 2 per cent), a metal abundance $Z = 0.02$ (see Table 1) and varying the physical parameters around the values obtained above from the comparison with the evolutionary tracks in the CMD. In particular, as a first step, we fixed the mass and built iso-periodic $Z = 0.02$ model sequences varying the luminosity and in turn the effective temperature. Possible variations in the efficiency of superadiabatic convection were also taken into account by varying the mixing-length parameter α used to close the non-linear system of equations in the hydrodynamical code (see Fiorentino et al. 2007; De Somma et al. 2020a, for details).

The obtained theoretical light curves are transformed in the Johnson V and I bands, by adopting the atmospheric models by Castelli, Gratton & Kurucz (1997a,b).

To constrain the quality of the fit on a quantitative basis, we adopted a χ^2 analysis (for details, see e.g. Marconi et al. 2013b, 2017; Ragosta et al. 2019).

Once obtained the best combination of luminosity and effective temperature for which the predicted curves matches the observed ones, we fixed the effective temperature to the obtained value and built additional iso-periodic sequences varying the mass and, in turn, the luminosity. The best-fitting procedure was then repeated obtaining a final best-fitting model. This procedure provides us with the intrinsic stellar parameters mass, luminosity, effective temperature together with the apparent distance modulus in all considered bands. Using the apparent distance moduli obtained from our procedure, and fitting the Cardelli law for absorption (Cardelli, Clayton & Mathis 1989), it is possible to derive the absolute distance modulus together with the absorption in the V band. To estimate the uncertainties on the fitted parameters, we performed a set of 1000 bootstrap simulations consisting of resampling the photometric light curves and replicating the fit for every simulation (a detailed description of the fitting method is described in Molinaro et al., in preparation).

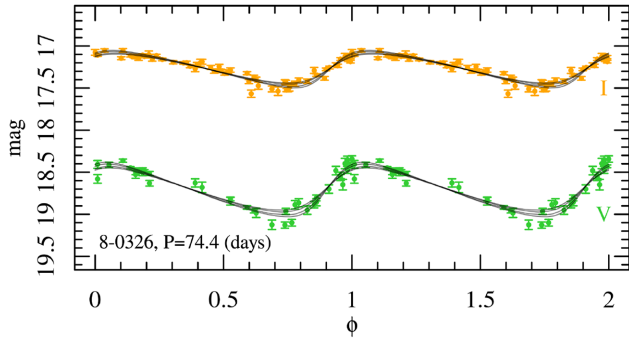
In our analysis, for each pulsator, we provide the best-fitting model obtained as a function of the adopted α parameter, and for each selection, additional three models that have a χ^2 in agreement, within the errors, with the best-fitting model. These results are reported in Table 2 that, for each model, lists its α value, period P_{mod} , mass M , effective temperature T_e and luminosity $\log(L/L_{\odot})$, together with the associated χ^2 , the obtained distance modulus in the V and I bands, μ_V and μ_I , the absorption in the V band A_V and the resulting absolute distance modulus μ_0 . Note that the uncertainties on the mass, effective temperature, and luminosity are fixed equal to the parameter steps used to generate the grid of models. The observed ULP light curves with the corresponding best-fitting model curves are shown in Fig. 8. Our best estimates of the distance modulus and of the absorption are obtained as the weighted mean of the tabulated values: $\mu_0 = 24.124 \pm 0.012$ mag and $A_V = 0.842 \pm 0.018$ mag. The inferred distance modulus is in agreement with the value obtained using the theoretical VI Wesenheit for this ULP, but smaller than the M31 distance modulus by de Grijs & Bono (2014) and Wagner-Kaiser et al. (2015). The absorption coefficient is in agreement within the errors with that obtained by Schlafly & Finkbeiner (2011) $A_V = 0.95 \pm 0.15$ mag.

6 CONCLUSIONS

With the final aim of characterizing ULPs as standard candles able to reach in one step the Hubble flow, in this paper, we updated and

Table 2. Direct fit results for LPV8-0326 (P obs = 74.4 d).

α (dex)	P_{mod} (d)	M (M_{\odot})	T (K)	$\log(L/L_{\odot})$ (dex)	χ^2	μ_V (mag)	μ_I (mag)	A_V (mag)	μ_0 (mag)
1.59	76.46	15.9 ± 0.2	4630 ± 25	4.57 ± 0.02	0.841 ± 0.113	24.958 ± 0.010	24.640 ± 0.005	0.828 ± 0.027	24.130 ± 0.019
1.60	76.46	15.9 ± 0.2	4630 ± 25	4.57 ± 0.02	0.856 ± 0.127	24.957 ± 0.010	24.641 ± 0.005	0.822 ± 0.033	24.135 ± 0.024
1.58	75.46	15.7 ± 0.2	4630 ± 25	4.57 ± 0.02	0.958 ± 0.122	24.954 ± 0.009	24.629 ± 0.006	0.847 ± 0.026	24.107 ± 0.017
1.56	76.08	15.7 ± 0.2	4680 ± 25	4.58 ± 0.02	0.965 ± 0.167	25.006 ± 0.011	24.671 ± 0.005	0.871 ± 0.032	24.135 ± 0.022


Figure 8. The ULPs light curves in V and I bands (the green and yellow dots, respectively) with the best fitting models (the dark lines) in Table 2.

enlarged the sample of 37 ULPs used by Fiorentino et al. (2012, 2013). This new sample includes 62 objects, for which we have V and I mean magnitudes, and is composed by the 18 ULPs collected by Bird et al. (2009), 2 ULPs in M81 (Gerke et al. 2011), 2 ULPs in M31 (Ngeow et al. 2015), and 40 ULPs identified in 14 galaxies by Riess et al. (2016) and Hoffmann et al. (2016), who enlarged, updated and re-calibrated the CC samples observed in the framework of the SH0ES project (Riess et al. 2011). To this sample, we also add a M31 ULP found by Taneva et al. (2020) for which we have B and V mean magnitudes. The covered metallicity $12 + \log(O/H)$ ranges from ~ 7.2 to 9.2 dex. The properties of these pulsating stars in the PW plane and in the CMD have been compared with different CC samples in the LMC (OGLE, Soszyński et al. 2015) and NGC 4258 (Riess et al. 2016) and with the theoretical metal dependent Wesenheit function by Fiorentino et al. (2007). The results do not confirm the almost flat slope suggested by Bird et al. (2009), as including all the ULPs with $\log P \leq 2.15$ we find $W_{VI} = -2.15 \log P - 4.89$ with $\sigma = 0.38$. To investigate how this result can be influenced by the adoption of a sample collected by different sources, we also derived the Wesenheit relation using only the SH0ES ULPs that represent a photometrically homogeneous sample obtaining a more robust result for the PW relation, namely $W_{VI} = -2.89 \log P - 3.42$ con $\sigma = 0.36$. The difference between this last relation and that obtained by Soszyński et al. (2015) for the LMC CCs, in the ULP period range is less than ~ 0.05 mag. On this basis, we perform a fit adding the ULPs to the LMC CC sample, obtaining $W_{VI} = -3.30 \log P - 2.62$ with $\sigma = 0.15$, both using all the ULPs with $\log P < 2.15$ that including only the SH0ES sample, in perfect agreement with that obtained using only the LMC OGLE CC by Soszyński et al. (2015). This result, together with the location of the ULPs in the CMD, seems to support the hypothesis that these variable are the extension at higher mass and luminosity of CCs, even if with a larger spread. This effect could be intrinsic, but also due to photometric limitations, crowding and blending. To get firm conclusions we need additional accurate data providing us with a photometrically homogeneous ULP sample, covering a larger range in period and metallicity. Moreover, we need

to extend the CC pulsational models up to $20 M_{\odot}$ to get theoretical information on the instability strip.

For the two M31 ULPs by Ngeow et al. (2015), 8-0326 and 8-1498, and for the one by Taneva et al. (2020), H42, we have time-series data published, so that we can analyse in detail their properties. Among these three ULPs, 8-1498 and H42 present inconsistency between their position in the CMD and the measured periods, thus suggesting that further observations are needed to confirm their nature as ULP. As for 8-0326, we apply the theoretical light curve model fitting method, using new ad hoc pulsation models based on a non-linear, non-local, time-dependent convective code (Natale et al. 2008; Marconi et al. 2013a; Ragosta et al. 2019). Through a χ^2 analysis of an extended set of models with the period fixed to the observed value and a wide range of input parameters, we were able to constrain the intrinsic stellar properties and constrain both the individual distance modulus and absorption. The obtained distance modulus is found to agree with that obtained using the VI Wesenheit for this ULP, but smaller than recent estimates of M31 distance by de Grijs & Bono (2014) and Wagner-Kaiser et al. (2015), whereas the absorption coefficient is in agreement within the error with the value obtained by Schlafly & Finkbeiner (2011).

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DATA AVAILABILITY STATEMENTS

The data underlying this article are available in the article.

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