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Title	Extremely deep 150 MHz source counts from the LoTSS Deep Fields
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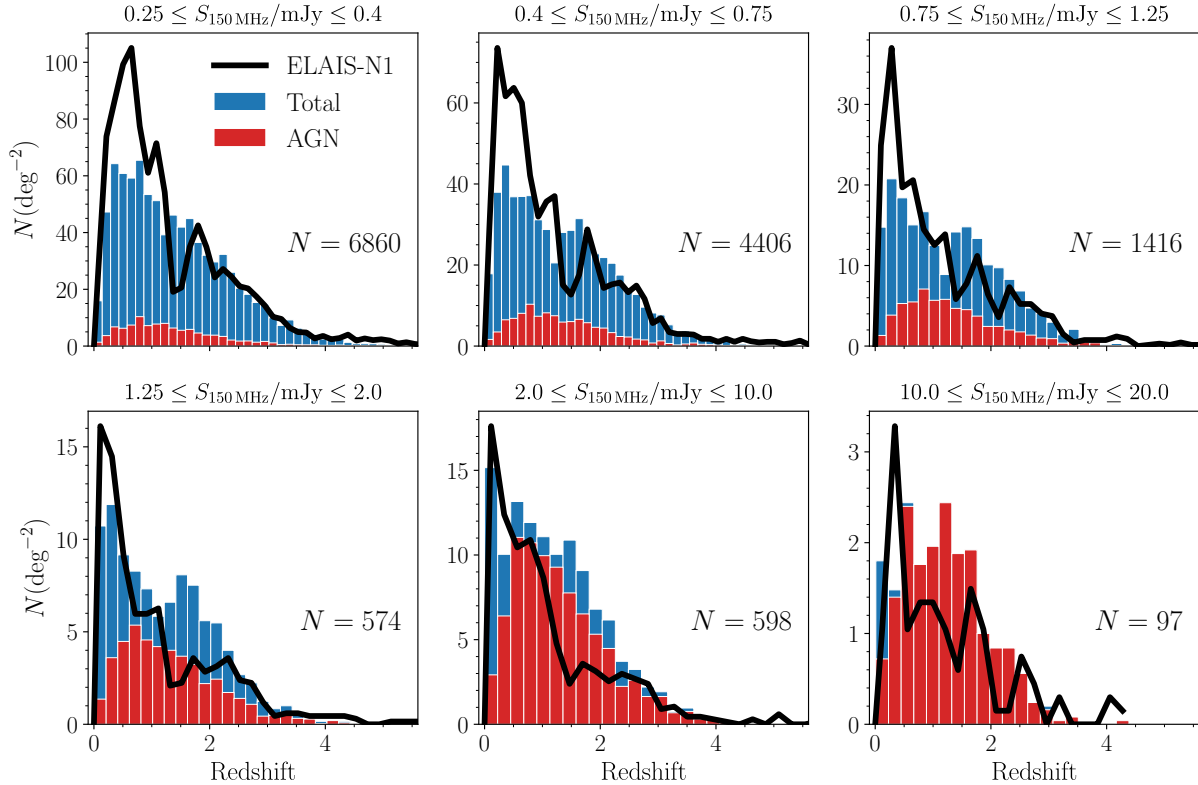


Fig. 11. Redshift distribution of the simulated sources in Bonaldi et al. (2019) catalog: the blue histogram corresponds to the total number of sources; the red histogram corresponds to the AGN component only. The solid black line shows the redshift distribution of the sources in the EN1 field. For a proper comparison the y -axis represents the source density in each catalog. Each panel corresponds to a different flux density bin, increasing from left to right and from top to bottom. Redshift bins range from $\Delta z = 0.14$ to $\Delta z = 0.22$ from the faintest to the brightest flux bin, i.e., they are larger than the estimated photometric redshift scatter by a factor 2–3 for AGN and by a factor ≥ 7 for galaxies. We caution that the EN1 redshift distributions are reliable only up to $z \sim 1.5$ for galaxies and up to $z \sim 4$ for AGN.

photometric and 9% spectroscopic, see Paper IV). 3% of the sources do not have redshift estimates, and are not included in the analysis. We believe the effect of neglecting these sources does not alter the main results of our analysis. Photometric redshifts can be considered robust up to $z = 1.5$ for galaxies ($\sigma_{\text{NMAD}} = 1.48 \times \text{median}(|\Delta z|/(1 + z_{\text{spec}})) = 0.02$), and up to $z = 4$ for AGN ($\sigma_{\text{NMAD}} = 0.064$; we refer to Paper IV for more details).

In Fig. 11 we show the redshift distributions of the sources in the EN1 field (solid black lines) for various flux density bins. These distributions are compared with the simulated distributions based on Bonaldi et al. (2019) evolutionary models (blue histogram bars). In the flux density bins spanning from 0.25 to 0.75 mJy we see a clear deficiency of the simulated sources, in agreement with the observed excess in the counts. This deficiency is mainly associated with sources at $z < 1$. The fact that the source counts’ excess is observed in all of the LoTSS fields (see e.g., Fig. 8) seems to rule out the case this is due to cosmic variance. We cannot exclude however, that the clustering properties assumed in the simulation may play a role in producing the observed discrepancy¹¹. At larger flux densities ($S \gtrsim 1$ mJy), we see an opposite trend, i.e., there is an excess of simulated sources with respect to observations. This is again consistent with the deficiency observed in our counts in the range 2–20 mJy. This excess is associated with intermediate redshift ($1 < z < 2$) sources, and appears to be mostly due to an excess of

AGN in the simulated catalog, at least at flux densities larger than a few mJy. We note that both the source excess at sub-mJy fluxes and the AGN deficiency at the brightest fluxes are observed at redshifts where the involved populations (galaxies and AGN in the former, AGN only in the latter) have robust photometric redshift estimates.

7. Conclusions

In this paper, we have presented the source number counts derived from the LoTSS Deep Fields: the Lockman Hole (LH), the Boötes (Boo) and the Elais-N1 (EN1). With central rms noise levels of 22, 33, 17 $\mu\text{Jy beam}^{-1}$ the LH, Boo and EN1 fields are the deepest obtained so far at 150 MHz, allowing us to get unprecedented observational constraints to the shape of the source counts at 150 MHz sub-mJy flux densities. We compared the source counts derived from the LoTSS deep fields with other existing source-counts determinations from low- and high-frequency radio surveys, and state-of-the-art evolutionary models. Our counts are in broad agreement with those from the literature, and show the well known upturn at $\lesssim 1$ mJy, which indicates the emergence of the star forming galaxy population. More interestingly, our counts show for the first time a very pronounced drop around $S \sim 2$ mJy, which results in a prominent ‘bump’ at sub-mJy flux densities. Such a ‘drop and bump’ feature was not observed in previous counts’ determinations (neither at 150 MHz nor at higher frequency). While sample variance can play a role in explaining the observed discrepancies, we believe this is

¹¹ We note, however, that a similar discrepancy is observed when comparing EN1 to the wide tier of the Bonaldi et al. (2019) simulations, where clustering is not implemented.

mostly the result of a careful analysis aimed at deblending confused sources from the radio source catalogs (see Paper II). Our counts cannot be fully reproduced by any of the existing evolutionary models. From a qualitative comparison with Bonaldi et al. (2019) simulated catalogs, we find that the sub-mJy ‘bump’ appears to be associated with an excess of low-redshift ($z < 1$) galaxies and/or AGN, while the drop at mJy flux densities seems to be due to a deficiency of AGN at redshifts $1 < z < 2$. A more in-depth investigation of these preliminary results will be the subject of forthcoming papers, based on more comprehensive comparisons with models.

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Appendix A: LoTSS Deep Fields - Counts' tables

Table A.1. 150 MHz normalized differential radio-source counts as derived from the Lockman Hole final catalogs.

S_{\min}	S_{\max}	ΔS	x	N_S	$N_{-\sigma}^{+\sigma}$	Sys ⁻	Sys ⁺	c_1	c_2
0.25	0.35	0.10	0.30	6673	42.35 ^{0.52} _{0.52}	4.56	2.82	1.12	1.34
0.35	0.50	0.15	0.42	5314	48.08 ^{0.67} _{0.66}	1.38	2.73	1.01	1.10
0.50	0.71	0.21	0.59	3545	51.21 ^{0.87} _{0.86}	0.24	2.48	1.00	1.06
0.71	1.00	0.29	0.84	2077	49.18 ^{1.10} _{1.08}	0.02	2.09	1.00	1.04
1.00	1.41	0.41	1.19	1119	43.55 ^{1.34} _{1.30}	0.04	1.54	1.01	1.03
1.41	2.00	0.59	1.68	683	44.29 ^{1.76} _{1.70}	0.00	1.89	1.01	1.02
2.00	2.83	0.83	2.38	390	42.01 ^{2.24} _{2.13}	0.00	1.94	1.01	1.01
2.83	4.00	1.17	3.36	272	49.19 ^{3.16} _{2.98}	0.00	2.77	1.01	1.01
4.00	5.66	1.66	4.76	184	55.86 ^{4.42} _{4.12}	0.00	3.60	1.01	1.01
5.66	8.00	2.34	6.73	148	75.45 ^{6.71} _{6.20}	0.00	4.09	1.01	1.01
8.00	11.3	3.30	9.51	132	113.1 ^{10.7} _{9.9}	0.0	4.0	1.01	1.01
11.3	22.6	11.3	16.0	172	158.4 ^{13.0} _{12.1}	0.0	2.3	1.01	1.01
22.6	45.3	22.7	32.0	128	333.2 ^{32.1} _{29.5}	0.0	1.3	1.01	1.01
45.3	90.5	45.2	64.0	74	543.7 ^{70.6} _{63.2}	0.2	2.2	1.01	1.01
90.5	181	90.5	128	45	935.1 ^{160.2} _{139.4}	2.5	4.2	1.01	1.01
181	724	543	362	46	2144 ³⁶³ ₃₁₆	3	15	1.01	1.01
724	2896	2172	1448	17	6335 ¹⁹⁰⁹ ₁₅₃₇	18	86	1.00	1.00

Notes. Columns are as follows: S_{\min} and S_{\max} are the minimum and maximum flux densities (expressed in mJy), respectively; Δ denotes the flux density intervals; x is the geometric mean of S_{\min} and S_{\max} ; N_S is the number of sources in respective bins; N is the normalized source counts and σ is the Poissonian errors on the normalized counts; Sys⁺ and Sys⁻ are the systematic errors, accounting for different modeling of resolution and Eddington bias corrections (see Sects. 4 and 5 for more details); the correction factor c_1 represents the weighting applied to the counts to account for resolution and Eddington biases; the correction factor c_2 also includes the weighting due to the visibility function.

Table A.2. 150 MHz normalized differential radio-source counts as derived from the Boötes final catalogs.

S_{\min}	S_{\max}	ΔS	x	N_S	$N_{-\sigma}^{+\sigma}$	Sys ⁻	Sys ⁺	c_1	c_2
0.35	0.50	0.15	0.42	3992	46.96 ^{0.76} _{0.74}	1.91	3.38	1.04	1.19
0.50	0.70	0.20	0.59	3066	53.73 ^{0.99} _{0.97}	0.23	3.39	1.02	1.08
0.70	1.00	0.30	0.84	1812	51.33 ^{1.23} _{1.21}	0.00	2.76	1.02	1.06
1.00	1.41	0.41	1.19	949	44.17 ^{1.48} _{1.43}	0.00	2.01	1.02	1.03
1.41	1.99	0.58	1.68	580	44.64 ^{1.93} _{1.85}	0.00	2.55	1.02	1.02
1.99	2.82	0.83	2.37	345	44.35 ^{2.52} _{2.39}	0.00	2.94	1.02	1.02
2.82	3.99	1.17	3.35	234	50.83 ^{3.54} _{3.32}	0.00	3.98	1.01	1.02
3.99	5.64	1.65	4.74	155	56.20 ^{4.88} _{4.51}	0.00	4.99	1.01	1.02
5.64	7.97	2.33	6.70	146	88.87 ^{7.96} _{7.36}	0.00	6.99	1.01	1.01
7.97	11.3	3.33	9.48	117	119.8 ^{12.1} _{11.1}	0.0	5.9	1.01	1.01
11.3	22.6	11.3	15.9	125	137.4 ^{13.4} _{12.3}	0.0	2.8	1.01	1.01
22.6	45.1	22.5	31.9	96	298.1 ^{33.5} _{30.4}	0.0	1.4	1.01	1.01
45.1	90.2	45.1	63.8	75	657.5 ^{84.7} _{75.9}	0.8	3.2	1.01	1.01
90.2	180	89.8	128	41	1018 ¹⁸⁴ ₁₅₉	6	6	1.01	1.01
180	722	542	361	27	1502 ³⁴⁵ ₂₈₉	3	12	1.01	1.01
722	2886	2164	1443	11	4861 ¹⁹⁰⁸ ₁₄₆₆	9	48	1.00	1.00

Notes. Parameters as in Table A.1.

Table A.3. 150 MHz normalized differential radio-source counts as derived from the ELAIS-N1 final catalogs.

S_{\min}	S_{\max}	ΔS	x	N_S	$N_{-\sigma}^{+\sigma}$	Sys^-	Sys^+	c_1	c_2
0.18	0.26	0.08	0.22	7187	$38.85_{0.46}^{0.46}$	6.69	2.52	1.16	1.29
0.26	0.36	0.10	0.31	5340	$43.54_{0.60}^{0.60}$	2.11	2.33	1.02	1.08
0.36	0.51	0.15	0.43	3397	$44.84_{0.77}^{0.78}$	0.63	1.97	1.00	1.03
0.51	0.73	0.22	0.61	2081	$45.40_{1.00}^{1.02}$	0.02	1.72	1.00	1.01
0.73	1.03	0.30	0.86	1165	$42.58_{1.25}^{1.28}$	0.00	1.32	1.00	1.01
1.03	1.45	0.42	1.22	676	$41.18_{1.58}^{1.65}$	0.00	1.07	1.01	1.01
1.45	2.06	0.61	1.73	368	$37.59_{1.96}^{2.06}$	0.00	1.01	1.01	1.01
2.06	2.91	0.85	2.45	232	$39.83_{2.62}^{2.79}$	0.00	1.35	1.01	1.01
2.91	4.11	1.20	3.46	163	$47.00_{3.68}^{3.97}$	0.00	2.05	1.01	1.01
4.11	5.82	1.71	4.89	100	$48.44_{4.84}^{5.33}$	0.00	2.41	1.01	1.01
5.82	8.23	2.41	6.92	86	$69.90_{7.54}^{8.35}$	0.00	2.46	1.00	1.00
8.23	11.6	3.37	9.79	66	$90.85_{11.18}^{12.56}$	0.00	2.35	1.01	1.01
11.6	23.3	11.7	16.5	89	$130.7_{13.9}^{15.3}$	0.0	1.0	1.00	1.00
23.3	46.6	23.3	32.9	93	$385.9_{40.0}^{44.2}$	0.0	1.2	1.00	1.00
46.6	93.1	46.5	65.8	54	$634.4_{86.3}^{98.1}$	0.4	2.1	1.00	1.00
93.1	186	92.9	132	37	1230_{202}^{235}	3	5	1.00	1.00
186	745	559	372	17	1271_{308}^{383}	2	8	1.01	1.01
745	2979	2234	1489	5	2980_{1333}^{1929}	7	34	1.00	1.00

Notes. Parameters as in Table A.1.