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Zero and Extremely Low-metallicity Rotating Massive Stars: Evolution, Explosion, and Nucleosynthesis Up to the Heaviest Nuclei

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Abstract

We present the evolution and the explosion of two massive stars, 15 and 25 M_{\odot} , spanning a wide range of initial rotation velocities (from 0 to 800 km s⁻¹) and three initial metallicities: $Z = 0$ ($[\text{Fe}/\text{H}] = -\infty$), 3.236×10^{-7} ($[\text{Fe}/\text{H}] = -5$), and 3.236×10^{-6} ($[\text{Fe}/\text{H}] = -4$). A very large nuclear network of 524 nuclear species extending up to Bi has been adopted. Our main findings may be summarized as follows: (a) rotating models above $Z = 0$ are able to produce nuclei up to the neutron closure shell $N = 50$, and in a few cases up to $N = 82$; (b) rotation drastically inhibits the penetration of the He convective shell in the H-rich mantle, a phenomenon often found in zero metallicity nonrotating massive stars; (c) vice versa, rotation favors the penetration of the O convective shell in the C-rich layers with the consequence of significantly altering the yields of the products of the C, Ne, and O burning; (d) none of the models that reach the critical velocity while in H burning lose more than 1 M_{\odot} in this phase; (e) conversely, almost all models able to reach their Hayashi track exceed the Eddington luminosity and dynamically lose almost all their H-rich mantle. These models suggest that rotating massive stars may have contributed significantly to the synthesis of the heavy nuclei in the first phase of enrichment of the interstellar medium, i.e., at early times.

Unified Astronomy Thesaurus concepts: S-process (1419); Stellar evolution (1599); Stellar rotation (1629); Massive stars (732); Core-collapse supernovae (304); Nucleosynthesis (1131)

Supporting material: machine-readable tables

1. Introduction

The most iron-poor low-mass stars ($M \sim 0.8 M_{\odot}$) are probably *second generation stars*, i.e., stars formed out of gas clouds enriched in metals by the ejecta of the first supernova explosions during the very early epochs of the evolution of the Universe. In recent years, large-scale surveys, often followed by high-resolution spectroscopy, allowed detailed measurements of the surface chemical composition of Fe-poor stars (Stellar Abundances for Galactic Archaeology Database, Suda et al. 2008, 2011; Yamada et al. 2013; Suda et al. 2017; Joint Institute for Nuclear Astrophysics Database, hereafter JINAbase; Yong et al. 2012; Roederer et al. 2014; Hansen et al. 2015; Abohalima & Frebel 2018; Starkenburg et al. 2018; Frebel et al. 2019). The scenario that emerges out of this large amount of data shows (among the other things) that (1) the Fe distribution function of Fe-poor stars peaks around $[\text{Fe}/\text{H}] \sim -2.7$; (2) the number of stars decreases sharply for $[\text{Fe}/\text{H}] < -3$; (3) there is a small number of objects with $[\text{Fe}/\text{H}] < -4$; (4) below $[\text{Fe}/\text{H}] = -2$ there is a progressive percentage increase of stars that show an *anomalous* high C abundance with respect to Fe that, in many cases, is also associated to large overabundances of N and O; (5) the vast

majority of the stars having $[\text{Fe}/\text{H}] < -4$ has $[\text{C}/\text{Fe}] \gg 0$; and (6) a number of very metal-poor stars show an enhancement of slow neutron capture nucleosynthesis (*s*-) process nuclei (identified by a $[\text{Ba}/\text{Eu}] > 1$), of rapid neutron capture nucleosynthesis (*r*-) process nuclei (i.e., $[\text{Ba}/\text{Eu}] < 0$) or both ($0 < [\text{Ba}/\text{Eu}] < 0.5$). In particular, Ba and Eu are widely used as representative proxies of the amount of matter synthesized by the *s*-process and the *r*-process nucleosynthesis, respectively, because their abundance can be measured relatively easily in the optical spectra of metal-poor stars. In the JINAbase sample, 10% of extremely metal poor (EMP) stars show the signature of neutron capture elements, the percentage increasing to 19% if one considers the whole catalog. It has been also possible to identify stars having $0 < [\text{La}/\text{Eu}] < 0.6$, which could represent the signature of an *intermediate* process (*i*-process) between the *s*- and the *r*-process (see, e.g., Cowan & Rose 1977; Hampel et al. 2016, and references therein).

While the main site where the bulk of the *r*-process nucleosynthesis occurs is still uncertain (although the *r*-process nucleosynthesis signature has been observed in the case of the kilonova associated to the detection of GW170817, see Pian et al. 2017), there is a general consensus that the *s*-process nucleosynthesis mainly takes place in intermediate mass stars ($1 \leq M_{\text{ZAMS}}(M_{\odot}) \leq 7$). The main reason is that the efficiency of the *s*-process nucleosynthesis (for each fixed initial Fe abundance) depends mainly on the neutron exposure (which is simply the total number of neutrons available) that is too low in



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massive stars to appreciably produce the bulk of the s -process nuclei. Massive stars may, in fact, contribute only to the synthesis of nuclei up to the first neutron closure shell. The canonical scenario proposed to explain the observed abundance of Ba in several EMP stars foresees a binary system formed by stars born out of gas enriched only by massive stars (Gallino et al. 1998; Suda et al. 2004; Cristallo et al. 2009; Straniero et al. 2014; Choplin et al. 2021). This binary system should be composed of a low mass and an intermediate mass star. The asymptotic giant branch (AGB) phase experienced by the intermediate mass star would be responsible for the s -process nucleosynthesis that would then be poured on the surface of the low mass companion through a wind or a common envelope phase. As a reminder, it is now widely accepted that the neutron flux responsible of the s -process nucleosynthesis in AGB stars has a primary origin as a consequence of the penetration of some protons below the base of the convective envelope at the end of the third dredge-up and the subsequent activation of the $^{12}\text{C}(\text{p},\gamma)$ first and of the $^{13}\text{C}(\alpha,\text{n})$ later (see Busso et al. 1999). Given the low abundance of the seed nuclei, the neutron-to-seed ratio is high enough in low-metallicity stars to push matter up to quite high atomic mass numbers (Goriely & Siess 2001; Travaglio et al. 2001; Cristallo et al. 2009, 2011).

In the last 20 yr, another scenario, not necessarily alternative to that of the AGB, has been proposed. In fact, a number of papers have shown that rotating massive stars can considerably boost the primary nucleosynthesis of several nuclei, namely ^{14}N , ^{19}F , and also elements beyond the Fe peak. Meynet et al. (2006), Hirschi (2007), and Ekström et al. (2008) were the first to show that the slow mixing of matter caused by rotation instabilities between the (central) He-burning and the H-burning shells (that we call entanglement between these two burning regions) in low-metallicity stars leads to an important production of ^{14}N , and they also suggested that such an entanglement could be responsible also for the synthesis of heavy nuclei. Pignatari et al. (2008) explored the possibility that a large amount of trans-Fe nuclei may be synthesized as a consequence of the entanglement between the He- and the H-burning zones, by means of a postprocessing that simulated the entanglement by injecting fresh ^{14}N in an He-burning environment up to a level of roughly 1% in mass fraction. This work showed that it is possible to produce a large amount of nuclei heavier than Zn in rotating stars but also that the very large neutron-to-seed ratio leads to the full destruction of the Fe seeds. Few years later, Frischknecht et al. (2012, 2016) presented a homogeneous set of stellar models in which for the first time it was studied the s -process nucleosynthesis by including a network with 737 nuclear species in the Geneva stellar evolution code. These computations extended up to the end of the central O burning and therefore missed the possible interplay between the O convective shell and the C-rich layers, the passage of the supernova shock wave, and the determination of the mass of the remnant, which is mass that determines which fraction of the mass of the star is ejected and which remains locked in the remnant. Note that, although it is certainly true that most of the s -process nucleosynthesis occurs in central He burning, the physical evolution of the CO core is crucial because the ashes of the central He burning are located within the CO core, i.e., behind the He convective shell, that therefore must be well traced.

In this paper, we present a preliminary set of evolutionary sequences that follow the hydrostatic evolution of the stars from the pre-MS up to the collapse of the core and then the formation and passage of the shock wave of the supernova explosion through the structure. The main goal is that of exploring the neutron capture nucleosynthesis as a function of both the initial Fe abundance and the initial equatorial rotational velocity. In particular, we aim to determine the minimum metallicity and the corresponding initial rotation velocity that allows a large production of the typical s -process elements observed in EMP stars. This work is organized as follows: Section 2 is dedicated to the description of the setup of the nuclear network to calculate the neutron capture nucleosynthesis in rotating massive stars; Sections 3 and 4 discuss the hydrostatic evolutionary properties of zero and very low-metallicity rotating massive stars and the explosion, respectively; the s -process nucleosynthesis yields as a function of the initial velocity and metallicity are presented in Sections 5 and 6; Section 7 shows a comparison between our theoretical predictions and a sample of representative observations of s -process elements; Section 8 shows a comparison with similar computations available in the literature; eventually, Section 9 summarizes our results.

2. FRANEC Code and Nuclear Network

The hydrostatic evolution of all the models discussed in this work has been computed by means of the version of the Frascati Raphson Newton Evolutionary Code (FRANEC) presented in detail in Chieffi & Limongi (2013; hereafter CL13), Limongi & Chieffi (2018; hereafter LC18). A summary of the main physical and numerical assumptions adopted in the code is presented in the Appendix A. The major effort in the present setup of the code was the choice of the nuclear network together with the database of nuclear cross sections. In this section, we discuss at some extent the main choices we made. Let us note that the update of the nuclear cross sections was frozen in 2019 October.

2.1. Strong Interactions

In general, we always preferred the experimental nuclear cross sections with respect to the theoretical ones. The nuclear cross section of each process was taken from KADoNiS v0.3 (Dillmann et al. 2006) for the neutron captures and from STARLIB (Sallaska et al. 2013) in all the other cases. If a nuclear cross section was not present in any of the two databases, it was searched for in the NACRE (Angulo et al. 1999) or NACRE II (Xu et al. 2013) compilations first and eventually in the Jina Reaclib (Cyburt et al. 2010) database. The only exceptions to this procedure were the nuclear cross sections of the reactions $^{17}\text{O}(\alpha, \gamma)^{21}\text{Ne}$ and $^{17}\text{O}(\alpha, \text{n})^{20}\text{Ne}$, taken from Best et al. (2011, 2013). Particular attention was paid to the computation of the nuclear cross sections of the reverse processes. As the temperature increases above roughly 2 GK, each process $a(i, j)b$ tends to be counterbalanced by the reverse process $b(j, i)a$ so that the net rate of each pair of processes as well as its contribution to the total nuclear energy generation rate depends on the very small difference between the forward and the reverse process. For this reason, we decided not to tabulate the nuclear cross sections of the reverse processes but to compute them at runtime for the exact value of the forward process. The advantage of this technique is that in

this way the nuclear cross section of the reverse process is exactly linked to the value of the forward process, providing a more stable and precise computation of the nuclear energy generation rate. We considered as the forward process of each pair the reaction having a positive Q -value.

2.2. Weak Interactions

The databases adopted for these processes include Fuller et al. (1982), Oda et al. (1994), Pruet & Fuller (2003), Langanke & Martínez-Pinedo (2000), Suzuki et al. (2016), and Li et al. (2016). In this case, the leading databases were those of Langanke & Martínez-Pinedo (2000) and Fuller et al. (1982) because they are the ones that cover the widest ranges both in temperature and density. If a process is not present in the first nor in the second database, the most recent value among Suzuki et al. (2016), Oda et al. (1994), and Pruet & Fuller (2003) is taken. If the reaction is not present in any of the abovementioned databases, its decay rate is assumed to be the terrestrial decay. The only exception to this procedure was the decay rate of ^{59}Fe into ^{59}Co because in this case we decided to adopt the decay rate provided by Li et al. (2016). We furthermore checked that all the decay rates progressively approach the terrestrial value at low temperature and low density.

2.3. Nuclear Network

The nuclear network is an extension of the one adopted in LC18. The main upgrades are (1) a wider extension toward larger atomic masses in order to properly manage higher neutron densities and (2) a larger number of elements (in particular, we added explicitly all elements between Tc and I).

The extension (in atomic mass) of the nuclear network is mainly dictated by the neutron density because it is this parameter (together with the temperature and density) that mainly controls how far matter can move out of the stability valley, because of the neutron captures, before decaying back toward its closest stable daughter. The parameter that controls the balance between beta decay and neutron capture may be written as the ratio B between decay rate and neutron capture rate:

$$B = \frac{\lambda_i(T, \rho)}{n_n \langle \sigma v \rangle_{\text{in}}(T)} \quad (1)$$

where n_n is the neutron density, λ_i is the probability of decay per time unit of the nucleus i , and $\langle \sigma v \rangle_{\text{in}}$ is the nuclear cross section of the neutron capture process on the nuclear specie i . This ratio mainly depends on the neutron density n_n and mildly on the temperature T and the density ρ . In massive stars, the s -process nucleosynthesis predominantly occurs in core and shell He burning and in shell C burning (see, e.g., LC18), and the typical physical conditions in these phases are $T \sim 2.5 \times 10^8 \text{ K}$ and $\rho \sim 10^3 \text{ g cm}^{-3}$ and $T \sim 10^9 \text{ K}$ and $\rho \sim 10^5 \text{ g cm}^{-3}$, respectively. The maximum neutron densities that are obtained in these conditions (in standard nonrotating models) are $n_n \sim 10^7 \text{ n cm}^{-3}$, in core and shell He burning, and $n_n \sim 10^{11} \text{ n cm}^{-3}$ in shell C burning. In order to take into account an even larger neutron production, in this work, we considered a limiting neutron density up to $n_n \sim 10^8 \text{ n cm}^{-3}$ for He burning and $n_n \sim 10^{14} \text{ n cm}^{-3}$ for C burning.

Table 1
The Nuclear Network

Element	Z	A_{\min}	A_{\max}	Element	Z	A_{\min}	A_{\max}
n	0	1	1	Br	35	79	85
H	1	1	3	Kr	36	78	89
He	2	3	4	Rb	37	84	89
Li	3	6	7	Sr	38	84	93
Be	4	7	10	Y	39	89	95
B	5	10	11	Zr	40	90	97
C	6	12	14	Nb	41	92	98
N	7	13	16	Mo	42	92	103
O	8	14	19	Tc	43	97	103
F	9	17	20	Ru	44	96	107
Ne	10	19	23	Rh	45	102	108
Na	11	21	24	Pd	46	102	114
Mg	12	23	27	Ag	47	107	114
Al	13	25	28	Cd	48	108	119
Si	14	27	32	In	49	112	119
P	15	29	34	Sn	50	112	128
S	16	31	37	Sb	51	121	131
Cl	17	33	38	Te	52	122	133
Ar	18	35	41	I	53	126	135
K	19	37	44	Xe	54	126	137
Ca	20	39	49	Cs	55	133	139
Sc	21	41	49	Ba	56	134	141
Ti	22	44	51	La	57	138	143
V	23	45	52	Ce	58	138	145
Cr	24	47	55	Pr	59	141	146
Mn	25	49	57	Nd	60	142	149
Fe	26	51	61	Pm	61	147	149
Co	27	53	62	Sm	62	147	155
Ni	28	55	65	Eu	63	151	155
Cu	29	57	66	Gd	64	152	159
Zn	30	60	71	Tb	65	159	159
Ga	31	62	72	Hg	80	202	205
Ge	32	64	77	Te	81	203	206
As	33	74	77	Pb	82	204	209
Se	34	74	83	Bi	83	208	209

Note. A_{\min} and A_{\max} are the minimum and maximum atomic weights of each element. Elements between Dy ($Z = 66$) to Au ($Z = 79$) are assumed to be at local equilibrium under neutron captures.

We therefore determined the maximum atomic mass of each element by requiring that $B \geq 100$, i.e., that the probability of decay were at least 100 times larger than the neutron capture:

$$\lambda_i(T, \rho) \geq n_n \langle \sigma v \rangle_{\text{in}}(T) \times 100. \quad (2)$$

We applied this procedure to all the elements with $31 \leq Z \leq 65$ and $80 \leq Z \leq 83$. The nuclear network that comes out from this procedure is reported in Table 1: it includes 524 isotopes and more than 3000 reactions fully coupled to the physical evolution of the star. It is important to note that, with respect to LC18, we have now only one cluster at local equilibrium corresponding to the elements with $65 < Z < 80$.

2.4. Initial Chemical Composition

The initial chemical composition, i.e., the composition of the gas cloud from which the star formed out, adopted in the case of zero metallicity models is not based on the theoretical computation of the Big Bang nucleosynthesis (BBN) but, on the contrary, on the abundances observed in an extremely metal-poor environment. In particular, we follow the work of Fields et al. (2020), in which they select the most reliable

Table 2

Initial Chemical Composition in Mass Fraction of Zero Metallicity Models

Element	Mass Fraction X
H	0.7550
² H	3.8507×10^{-5}
³ He	2.4916×10^{-5}
⁴ He	0.2449
⁷ Li	8.4564×10^{-10}

Note. See text.

environments in which the primordial abundances may still be visible. In particular, the abundance of ⁴He is derived from observations of extragalactic H II emission lines; the abundance of deuterium is estimated through the study of quasar absorption systems; the reference abundance of ⁷Li is taken from the analysis of stellar spectra of low-metallicity stars. For ³He, there are not enough reliable observations; therefore, for this isotope, we adopt the value provided by Coc et al. (2013), which is derived from the local observations of our Galaxy. The abundances of all the nuclear species having $Z \geq 4$ are put to zero. The initial abundances in mass fraction adopted in this work for the zero metallicity models are shown in Table 2.

For the higher-metallicity models, we adopt a scaled solar chemical composition with the exception of C, O, Mg, Si, S, Ar, Ca, and Ti, for which we adopt an enhancement with respect to the solar value derived from the observations of low-metallicity stars, i.e., $[\text{C}/\text{Fe}] = 0.18$, $[\text{O}/\text{Fe}] = 0.47$, $[\text{Mg}/\text{Fe}] = 0.27$, $[\text{Si}/\text{Fe}] = 0.37$, $[\text{S}/\text{Fe}] = 0.35$, $[\text{Ar}/\text{Fe}] = 0.35$, $[\text{Ca}/\text{Fe}] = 0.33$, $[\text{Ti}/\text{Fe}] = 0.23$ (see, e.g., Cayrel et al. 2004; Spite et al. 2005). The adopted solar chemical composition is the one provided by Asplund et al. (2009), which corresponds to a total metallicity equal to $Z = 1.345 \times 10^{-2}$. Therefore, as a result of the enhancements mentioned above, the metal fraction corresponding to $[\text{Fe}/\text{H}] = -N$ is $Z = 3.236 \times 10^{-(N+2)}$. We also assume that the initial abundance of ⁴He does not significantly vary from the adopted BBN value in the range of the explored metallicity, and therefore, it is kept constant. Table 3 summarizes the metallicity range explored in this work.

3. Stellar Models

We explored the evolution of two massive stars (15 and $25 M_{\odot}$) spanning a wide range of initial equatorial surface velocities, from 0 to 800 km s^{-1} , that correspond to a range in $\Omega/\Omega_{\text{crit}}$ that extends up to $\simeq 1$. Three extremely low metallicity were considered: $[\text{Fe}/\text{H}] = -\infty, -5, -4$.

A summary of the main properties of the computed models is reported in Table 5. We use the following convention to refer to the models: the first part of the name is the three-digit mass, the second one is a letter that marks the metallicity of the set, and the three last digits represent the initial rotation velocity in kilometers per second. The zero metallicity set is labeled as “Z,” while the letters “F” and “E” correspond respectively to $[\text{Fe}/\text{H}] = -5$ and -4 : 025z450, for example, indicates a zero metallicity $25 M_{\odot}$ star having an initial equatorial rotation velocity equal to 450 km s^{-1} . Each quantity is evaluated at the end of every burning phase. The label “MS” marks the beginning of the main-sequence (MS) phase. The various columns refer to the following: (1) the burning phase, (2) the duration of the phase in years, (3) the maximum size of the convective core during the burning phase in solar masses,

Table 3

The Metallicity Explored in This Work

Set Name	[Fe/H]	Z	⁴ He	Number of Models
Z	$-\infty$	0	0.2449	14
F	-5	3.236×10^{-7}	0.2449	11
E	-4	3.236×10^{-6}	0.2449	7

Note. Z represents the absolute metallicity, i.e., the sum of all the abundances in mass fraction of the elements heavier than He. The abundance of ⁴He is supposed to remain constant through the different metallicity.

(4) the logarithm of the effective temperature in kelvin, (5) the logarithm of the luminosity in solar units, (6) the total mass in solar masses, (7) the size of the He core in solar masses, (8) the size of the CO core in solar masses, (9) the surface equatorial rotation velocity in kilometers per second, (10) the surface angular velocity in s^{-1} , (11) the ratio of surface angular velocity to the critical one, (12) the total angular momentum J in units of $10^{53} \text{ g cm s}^{-1}$, and (13)–(15) the surface mass fractions of H, ⁴He, and ¹⁴N, respectively. We discuss the evolution of the nonrotating models (up to the onset of the core collapse) first, and then the role played by rotation.

3.1. The Nonrotating Models

3.1.1. The H Burning

The lack of nuclear species with $Z \geq 6$ seriously affects the evolution of a zero metallicity star both because the very low opacity forces these stars to spend their lives as compact blue objects, and also because the lack of the energy provided by an initial abundance of CNO nuclei forces these stars to contract and raise their central temperature much more than their more metal-rich counterparts. Figure 1 shows the Hertzsprung–Russell (H-R) diagram of all models presented in this paper. The plots on the left and those on the right refer to the $15 M_{\odot}$ and the $25 M_{\odot}$, respectively. The two zero metallicity models are represented as black lines in the two upper panels.

The proton–proton (PP) chain is able to produce enough energy to replace the one lost from the surface of the star just at the beginning of the central H-burning phase. Right after, the continuous increase of the mean molecular weight due to the conversion of protons in α particles leads necessarily to a progressive increase of the temperature. The low dependence of the energy generation rate of the PP chain on the temperature forces these stars to contract and heat more effectively than their more metal-rich counterparts, reaching very early a temperature high enough to partially activate the 3α nuclear reactions and therefore the synthesis of some ¹²C. The full CNO cycle activates immediately and progressively replaces the PP chain as the main energy producer: in both masses, the CNO cycle produces 50% of the nuclear energy when the central H burning is still 0.5 by mass fraction. At $H_c \sim 0.2$, the CNO cycle produces more than 80% of the energy required to sustain the $15 M_{\odot}$ and more than 90% in the $25 M_{\odot}$. As the central temperature increases, the amount of CNO nuclei produced by the 3α increases, so that toward the end of the central H-burning phase ($H_c \simeq 0.05$) it reaches a mass fraction of 4×10^{-10} ($15 M_{\odot}$) and 6×10^{-10} ($25 M_{\odot}$). During the very latest phases of the central H burning, the coupling $3\alpha + \text{CNO}$ cycle raises the abundance of ¹⁴N from a few times 10^{-10} to roughly 10^{-6} in both masses. Once the H is exhausted in the convective core, the H burning shifts in a shell where the 3α

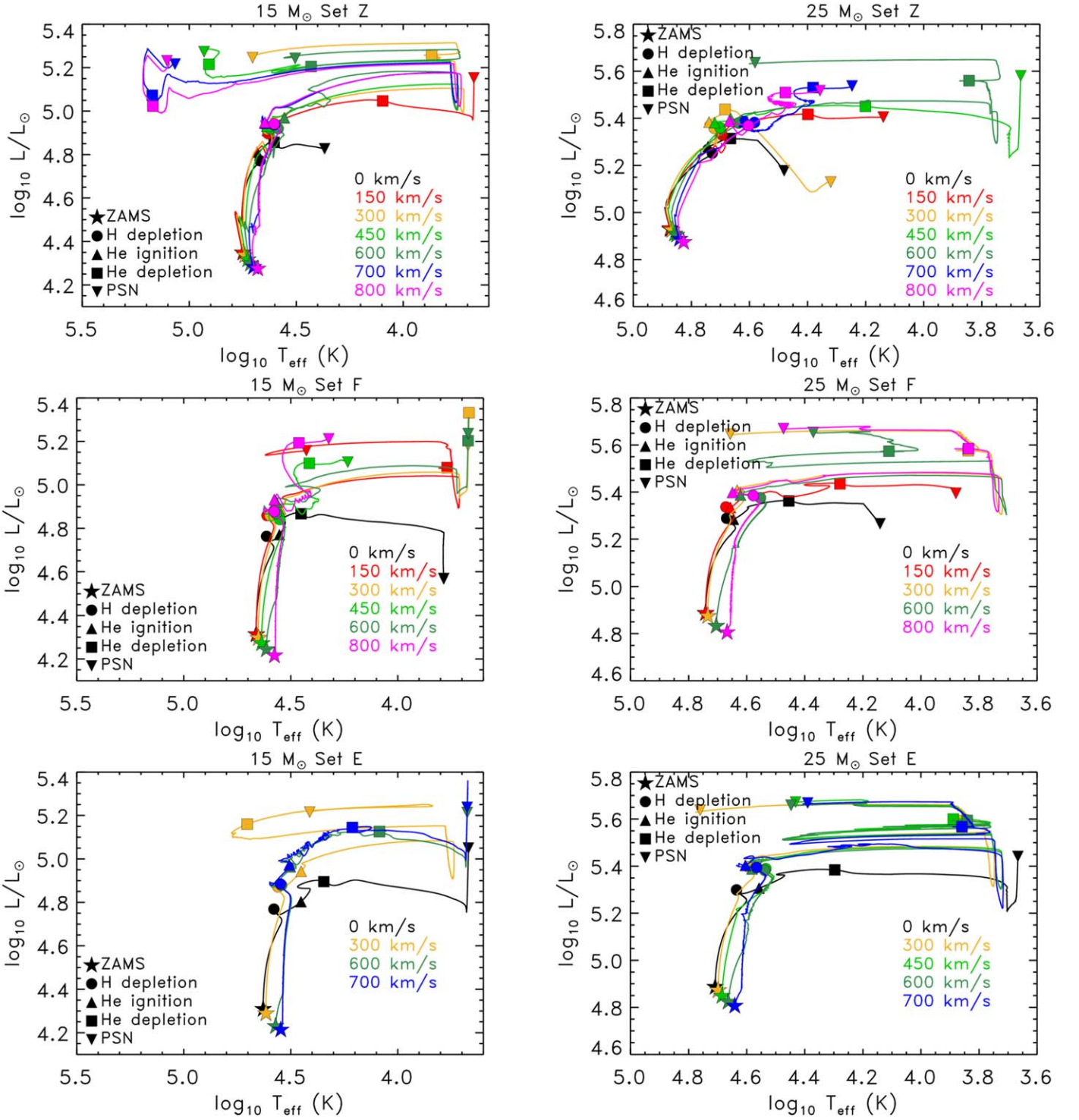


Figure 1. Evolution on the Hertzsprung–Russell (H-R) diagram of 15 (left panels) and 25 M_{\odot} (right panels) rotating massive stars. The different colors indicate the various initial equatorial velocity. The filled symbols mark different evolutionary stages.

and the CNO cycle still work together, so that the level of ^{14}N within the whole H exhausted core settles to a value of the order of 10^{-6} by mass fraction (again in both masses). Note that during the central H burning a convective shell forms well outside the convective core in the 25 M_{\odot} (the Kippenhahn diagrams of the zero metallicity stars are shown in the two upper panels of Figure 2 while those of the other two metallicities are shown in the second and third rows).

Turning from $Z = 0$ (or, equivalently, $[\text{Fe}/\text{H}] = -\infty$, Set Z) to $[\text{Fe}/\text{H}] = -5$ (Set F), the initial global abundance of the CNO nuclei ($X_{\text{CNO}} = 3.24 \times 10^{-7}$) is already high enough to fully sustain the star without the need of additional production of C in H burning. However, also at this metallicity, some C is produced toward the very end of the H burning so that once again the mass fraction of the ^{14}N within the whole H exhausted core reaches a value of the order of 10^{-6} by mass

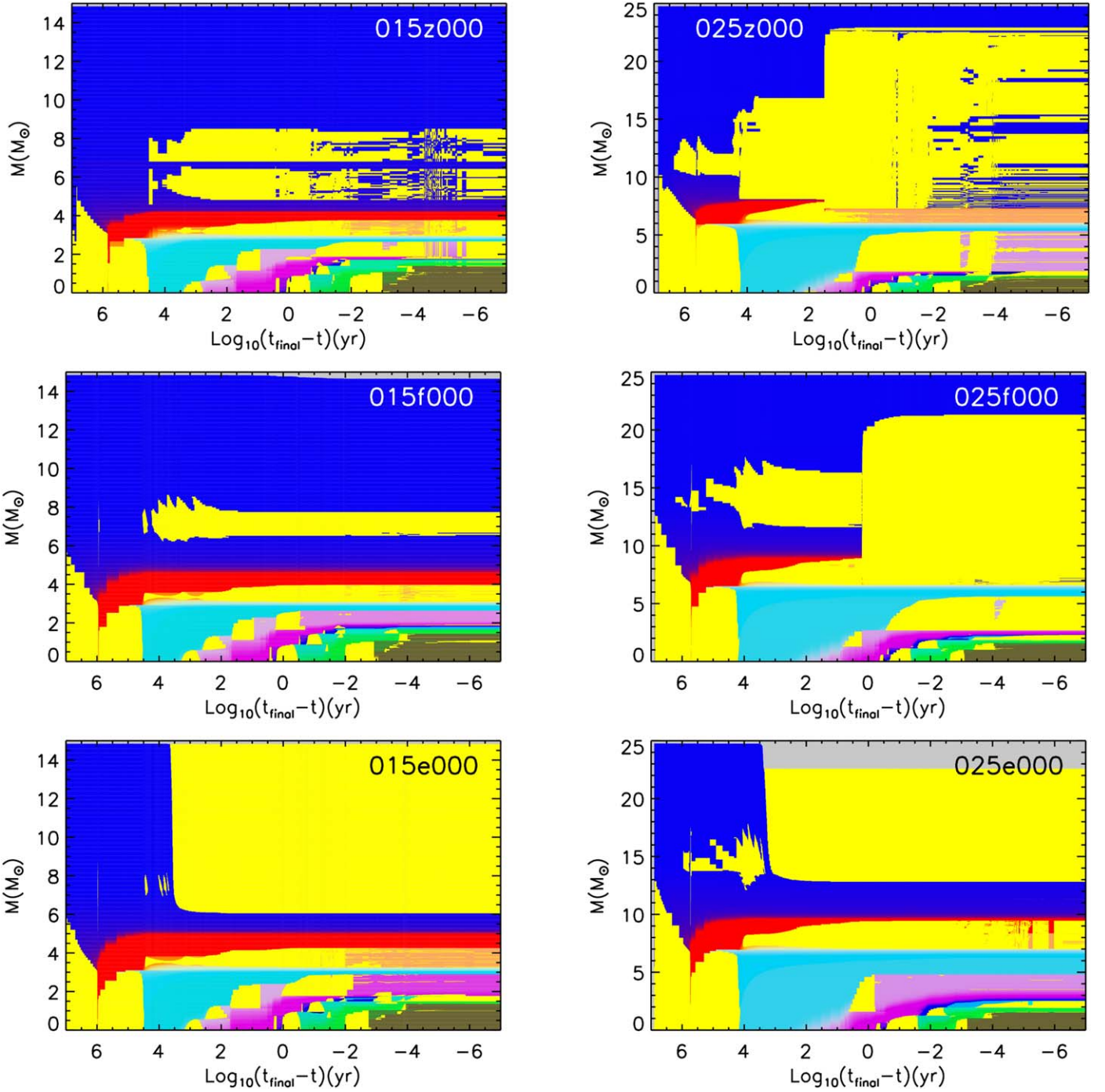


Figure 2. Kippenhahn diagrams of the nonrotating models. Top to bottom: Z, F, E. The x-axis represents the time prior the collapse of the Fe core, marked as t_{final} in the plot. The blue area marks the H-rich layers, the red one the pure He zone, the cyan the C/O region, the magenta the Ne/O region, the violet the O-rich layers, the green area the Si-rich zones while the brown zone the Fe core. The yellow area marks the convective zones.

fraction in both masses. The initial abundance of the CNO nuclei in Set E ($[\text{Fe}/\text{H}] = -4$) is higher than 10^{-6} so that the 3α processes at this metallicity do not even activate toward the end of the central H burning.

In general, the size of the convective core (that practically corresponds to the initial size of the He core) scales inversely with the initial metallicity because the lower the CNO abundance the larger the size of the convective core (the higher central temperature implies higher energy fluxes). But when the metallicity drops to zero, the PP chain overcomes the CNO

cycle, and the lower dependence of the energy flux on the temperature inverts the trend leading to convective cores (and hence He core masses) smaller than those proper of more metal-rich stars. This explains why the He core mass increases from $3.6 M_{\odot}$ (Set Z) to $3.9 M_{\odot}$ (both Sets F and E) in the $15 M_{\odot}$ and from $7.2 M_{\odot}$ (Set Z) to $8.1 M_{\odot}$ (both Sets F and E) in the $25 M_{\odot}$.

The last thing worth noting is that both stars practically evolve at a constant mass in central H burning because the mass loss (that scales directly with Z) is negligible at these extreme metallicities.

3.1.2. The He Burning

The natural consequence of the partial activation of the 3α already in MS, reinforced by the extremely low opacity of the H-rich mantle caused by the lack or extremely low abundance of metals, is that all models (Sets Z, F, and E) ignite and burn He on the blue side of the H-R diagram (black lines in the three rows of Figure 1). It is worth noting that the H convective shell that forms in H burning in the zero metallicity $25 M_{\odot}$ remains active also through the whole central He burning (upper right panel in Figure 2). A modest H convective shell that persists beyond the central He exhaustion (second and third rows in the right panel of Figure 2) develops also in the $25 M_{\odot}$ of Sets F and E.

At variance with the H-burning phase, the physical evolution of the He core in He burning (and beyond) does not depend any more directly on the metallicity because both the nuclear energy generation and the opacity are controlled only by the He abundance and the products of its nucleosynthesis (all primary elements). The initial metallicity influences the evolution of the He core only indirectly through the increase of the mass size of the He core caused by the advancing in mass of the H-burning shell and/or its decrease if the H-rich mantle is removed as a consequence of mass loss or binary interactions. In both masses, the increase of the He core mass in He burning scales monotonically with the metallicity. In the $15 M_{\odot}$ case, the increase amounts to $\sim 0.6 M_{\odot}$ in Set Z and to $\sim 0.9 M_{\odot}$ and $\sim 1.2 M_{\odot}$ in Sets F and E, respectively. In the $25 M_{\odot}$, the increase amounts to $\sim 0.7 M_{\odot}$ in Set Z and to $\sim 1.1 M_{\odot}$ and $\sim 1.6 M_{\odot}$ in Sets F and E.

The central He burning is powered essentially by the two well-known processes, 3α and $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$, and is characterized by a convective core that progressively advances in mass. The competition between these two processes contributes, together with the behavior of the convective core, to determine the abundance of ^{12}C left by the He burning. Such a value inversely scales with the final size of the He core and therefore inversely with the metallicity. In the present set of models, the values obtained in Set Z are $X_{\text{C}} = 0.36$ ($15 M_{\odot}$), and $X_{\text{C}} = 0.30$ ($25 M_{\odot}$) and reduce down to 0.32 ($15 M_{\odot}$) and 0.26 ($25 M_{\odot}$) at $[\text{Fe}/\text{H}] = -4$.

The ^{14}N left by the H burning is fully converted in ^{22}Ne , part of which is in turn converted in ^{25}Mg and ^{26}Mg toward the end of the He burning, through the two competing exit channels (n and γ) of the α capture. Neutrons produced by the n channel may activate (in principle) the s -process nucleosynthesis, but the extremely low abundances of ^{14}N and ^{13}C , coupled to the lack of seed nuclei, completely inhibit the possible formation of nuclei above Zn. In both models of Set Z, the heaviest element whose abundance reaches at least 10^{-4} by mass fraction at the end of the central He burning is ^{24}Mg . Beyond this nucleus, the abundances of all others nuclei drop quickly below 10^{-10} by mass fraction (see next section).

Once He is exhausted in the center, the He burning shifts in a shell where convection rapidly develops. In stars of lower metallicity ($[\text{Fe}/\text{H}] < -4$), the outer border of the He convective shell may penetrate the base of the H-rich mantle soon after the central C exhaustion bringing protons inside, at very high temperatures, where they ignite violently. The abrupt release of nuclear energy forces the outer border of the He convective shell farther, and it quickly moves outward in mass, eventually engulfing most of the H-rich envelope. In the present case, such a peculiar behavior of the He convective

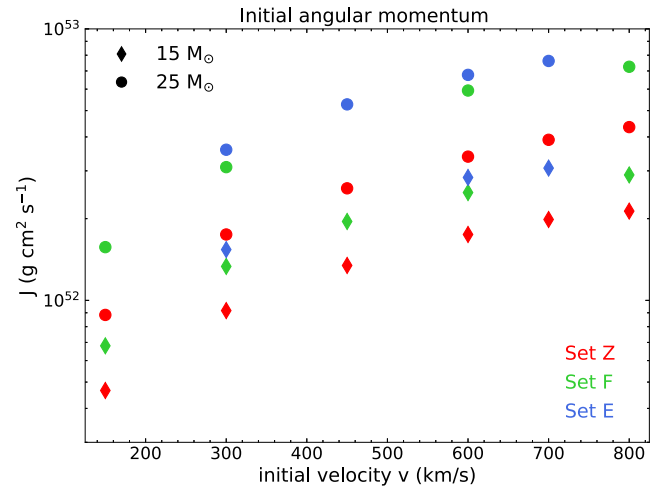


Figure 3. The total angular momentum J at the onset of the main-sequence phase in all the computed models. Diamonds represent $15 M_{\odot}$ models; dots represent $25 M_{\odot}$ models.

shell occurs in the $25 M_{\odot}$ of both Sets Z and F. Figure 2 shows clearly the penetration of the He convective shell in the H-rich mantle and the formation of a huge convective shell that covers most of the mantle. It goes without saying that the penetration of the He convective shell into the H-rich mantle produces a burst of production of ^{14}N (and related H-burning products) because it brings fresh protons in a C-rich region where the temperature is of the order of 200 MK or even more.

3.1.3. The Advanced Burning

As in the case of core He burning, also the physical evolution of the CO core of a massive star does not depend on the initial metallicity. Its further evolution depends on both the CO core mass size and the ^{12}C abundance left by the previous burning stage (Chieffi & Limongi 2020; Chieffi et al. 2021). The CO core mass plays the same role the initial mass has in H burning, while the abundance of ^{12}C determines the amount of fuel available to the C burning and therefore controls the presence/size of the C convective core as well as the number and extensions of the C convective shell. As far as the behavior of the H-rich mantle is concerned, the present set of models satisfy the general rule that the lower the initial metallicity the more difficult it is for the star to expand the H-rich envelope up to the Hayashi track. In fact, both zero metallicity stars remain at very high temperature all along the advanced burning phases, the models of Set F move somewhat toward the red without really reaching the red giant branch (RGB) while the initial metallicity of models of Set E is high enough to allow both models to reach the RGB soon after the central He exhaustion (see Figure 1, third row).

All three $15 M_{\odot}$ share a similar CO core mass ($\sim 3.1 M_{\odot}$) and abundance of ^{12}C (~ 0.34). Hence, the advanced evolutionary phases are quite similar: all of them form a C convective core of similar size, and three C convective shells (left column in Figure 2). In the case of the $25 M_{\odot}$, the two most metal-poor models share similar values of the two latter parameters ($M_{\text{CO}} \sim 6 M_{\odot}$ and $^{12}\text{C} \sim 0.28$) and hence show a similar evolution during the advanced burning stages: radiative central C burning and two similar C convective shells. The $25 M_{\odot}$ of Set E, on the contrary, forms a slightly larger CO core mass ($\sim 7 M_{\odot}$) and forms just one extended C convective shell. The

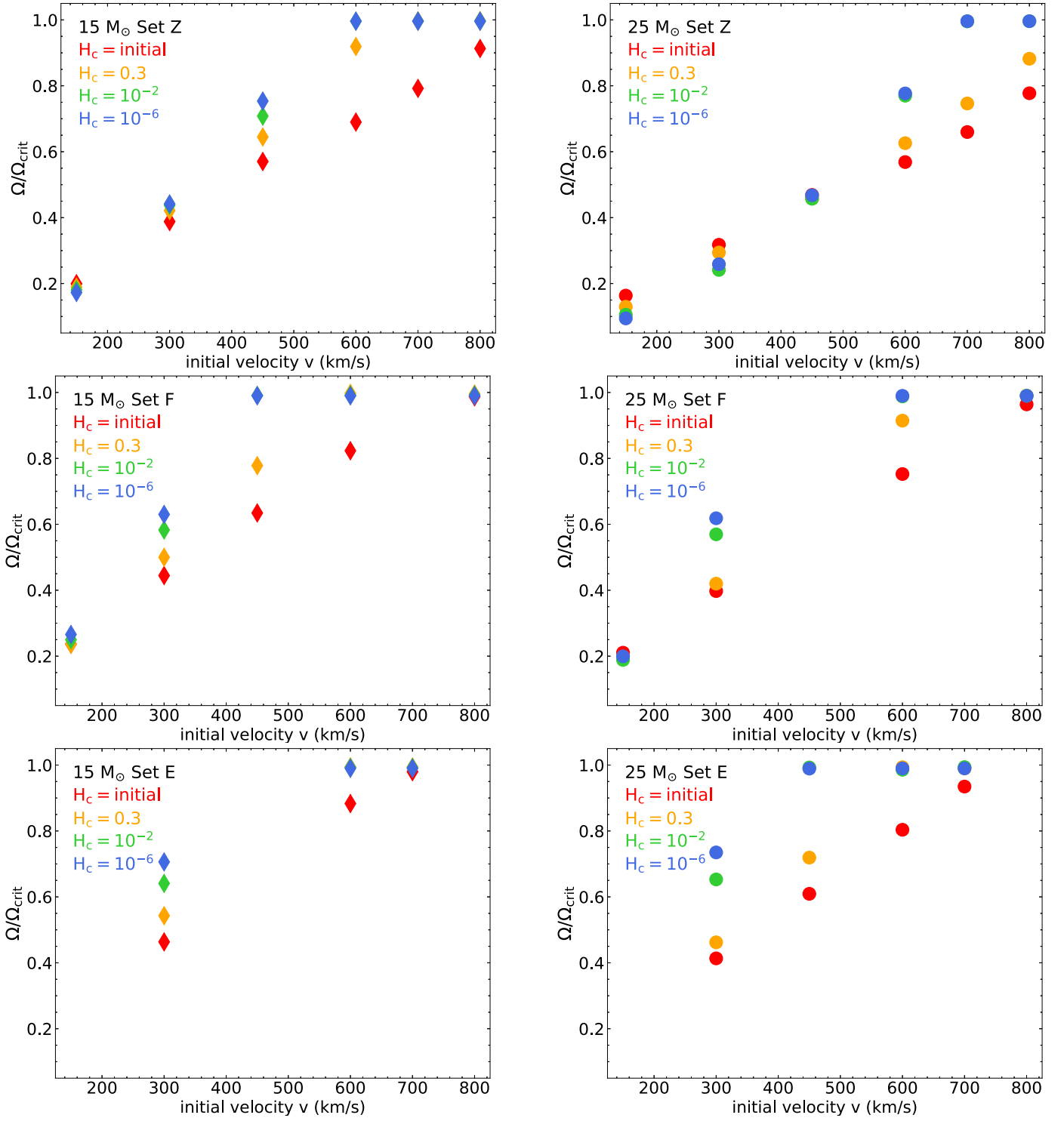


Figure 4. Ratio of surface angular velocity to critical velocity in the 15 M_{\odot} (left panels) and 25 M_{\odot} stars (right panels) in Set Z (first row), Set F (second row), and Set E (third row) for four characteristic central H abundances in mass fraction: initial (red), 0.3 (yellow), 10^{-2} (green), and 10^{-6} (blue).

way in which the C burning develops, in particular the number and extensions of the various C convective shells, influences the more advanced burning and plays a major role in sculpting the final density profile, or, equivalently, the mass–radius relation, at the core bounce: in other words, it largely controls the final run of the binding energy of the mantle of the star, i.e., all the zones above the Fe core, as a function of the mass coordinate (see, e.g., Chieffi & Limongi 2020; Chieffi et al. 2021;

Boccioli et al. 2023). This quantity obviously plays a crucial role in determining the *explodability* of a star because it is the main obstacle to the advancing of the shock wave in its way out. A larger or smaller binding energy of the mantle may lead to a failed or successful explosion. Instead of comparing the full M – R relation of different models, O’Connor & Ott (2011) proposed to use a single parameter to quantify the compactness of a star, the so-called ξ parameter, defined as

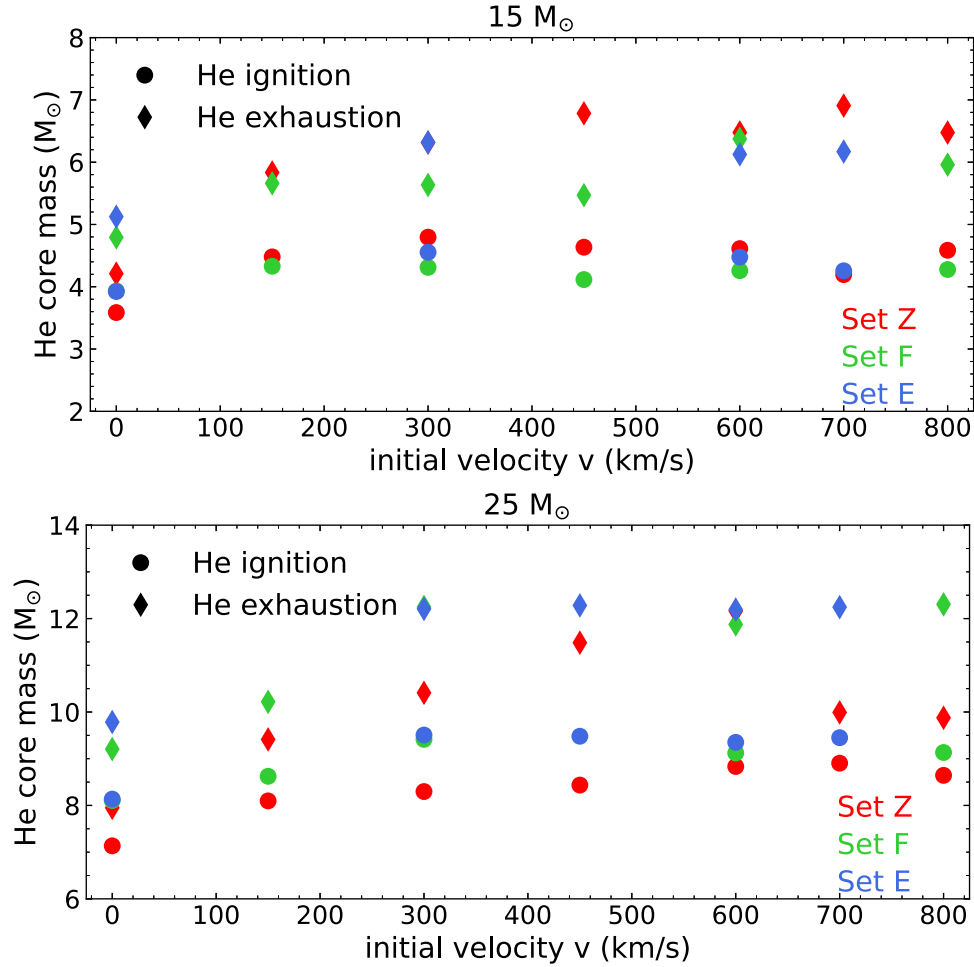


Figure 5. He core mass in the 15 (top panel) and 25 M_{\odot} models (bottom panel) at central He ignition (filled dots) and exhaustion (filled diamonds).

$\xi_i = M_i(M_{\odot})/R_i(1000 \text{ km})$. According to these authors, the most reliable mass coordinate at which this parameter should be evaluated is $M = 2.5 M_{\odot}$. Over the years, it has become clear that this parameter, per se, is not very reliable in predicting the real final fate of a star, but it is anyway useful because it is a synthetic way to describe at least the final compactness of a star through a single number (see, e.g., Ertl et al. 2016; Burrows et al. 2019; Chieffi & Limongi 2020, and references therein). The main physical properties of the stars at the onset of the core collapse, including the $\xi_{2.5}$ parameter, are shown in Table 6 of Appendix B.

3.2. The Role of Rotation

As already extensively discussed in literature (see, e.g., Meynet et al. 2006; CL13; LC18, and references therein), the inclusion of some angular momentum changes many evolutionary properties of the stars; among the others, it activates instabilities that drive some mixing of the matter in layers that would otherwise be in radiative equilibrium, forces a star (through the centrifugal force) to inflate its mantle much more (and much faster) than its nonrotating counterpart at the end of the central H-burning phase, and triggers episodes of (dynamical) mass loss. The red (Set Z), green (Set F), and blue symbols (Set E) in Figure 3 show the relation between the total angular momentum injected in each model and the initial rotational velocity (at the beginning of the central H-burning phase). Note that the amount of angular momentum injected in

stars with the same rotational velocity scales directly with the metallicity because the higher the metallicity the more expanded the star in the MS. The diamonds refer to the 15 M_{\odot} while the dots refer to the 25 M_{\odot} . The corresponding initial values of $\Omega/\Omega_{\text{crit}}$ are shown in Figure 4. The same figure shows that this ratio increases in central H burning and that the fastest rotating models reach the break up velocity before the central H exhaustion. Note that the expansion of the surface that occurs in central H burning would lead, per se, to a decrease of $\Omega/\Omega_{\text{crit}}$ in the absence of transport of the angular momentum from the interior toward the surface. It is the outward transport of angular momentum that forces $\Omega/\Omega_{\text{crit}}$ to increase. In stars that are metal-rich enough to lose a substantial amount of mass in MS, $\Omega/\Omega_{\text{crit}}$ is kept well below 1 by the efficient angular momentum removal operated by mass loss, while the lack of an efficient mass loss at zero and extremely low metallicity leads to the pile up of angular momentum to the surface and hence to the continuous increase of $\Omega/\Omega_{\text{crit}}$. The most external layers in which such a ratio reaches the value of one become unbound, and they are lost in the interstellar medium. However, the total amount of mass lost by this phenomenon is quite modest because the models reach the break up velocity only toward the end of the central H-burning phase (Figure 4). In all explored cases, the amount of mass lost by the models due to such a phenomenon never exceeds 1 M_{\odot} . It is worth noting that none of our models approaches the condition of quasi homogeneous mixing (see, e.g.,

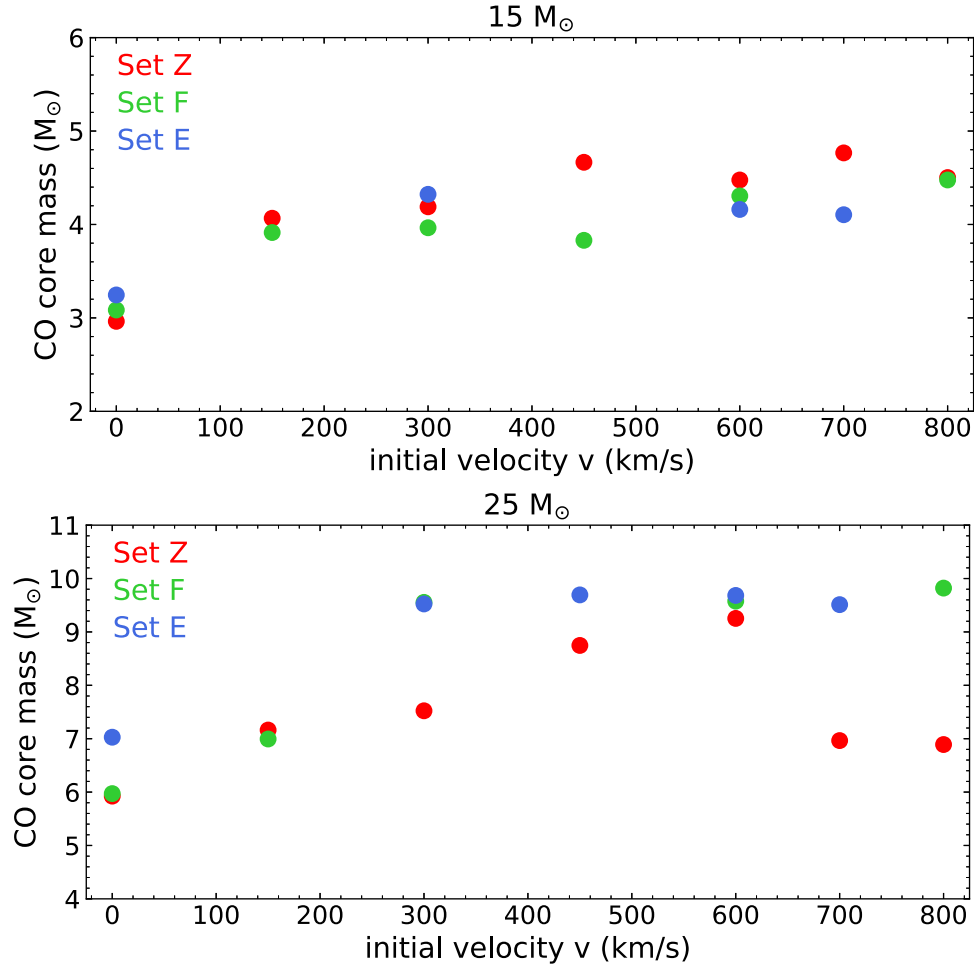


Figure 6. CO core mass at central He depletion in the $15 M_{\odot}$ (top panel) and $25 M_{\odot}$ models (bottom panel).

Yoon et al. 2012; Banerjee et al. 2019), although a few of them start their evolution with a rotation velocity very close to the break up one.

The continuous stirring of matter caused by the rotation induced instabilities leads to more extended H convective cores and also to the diffusion of the products of the central burning in the H-rich mantle. The trend of the He core mass versus the initial rotation velocity is shown in Figure 5. There is a general increase of the He core mass with the initial equatorial rotation velocity v_{ini} , even if with some exceptions due to the complex interplay among the various convective zones that develop during the evolution of the stars. The synthesis of fresh C by the 3α reaction in rotating stars during H burning is quite similar to that occurring in the nonrotating models: zero metallicity stars synthesize an abundance of C of the order of a few times 10^{-10} by mass fraction while no models of Sets F and E require the activation of the 3α during most of the central H burning. Similarly to what happens in the nonrotating case, toward the end of the central H burning, the models of both Sets Z and F synthesize enough C to increase the N abundance up to a value of the order of 10^{-6} by mass fraction in the whole He core, independently on the initial rotation velocity. Also, the rotating models of Set E behave like their nonrotating counterparts; therefore, the ^{14}N present in the He core of these models is simply the one that descends from the initial CNO abundance.

The very high temperature at which the H burning occurs in models of Sets Z and F leads to the He ignition and to the formation of a convective core immediately after the central H exhaustion when the models are still on the blue side of the H-R diagram. The rotation induced instabilities, which in H burning led to both an increase of the H convective core and to the diffusion of the products of the nuclear burning into the H-rich mantle, in He burning continuously stir matter between the He convective core and the H-burning shell. The first consequence of such a stirring is that, similarly to what happens in H burning, the final CO cores are more massive than in the nonrotating case (Figure 6). The second one is that the continuous ingestion of fresh He in the convective core leads to a lower final abundance of ^{12}C in the He exhausted core. Figure 7 shows the final ^{12}C abundance as a function of the initial rotation velocity for both masses. The third one is that, as already found by Meynet & Maeder (2002), Chieffi & Limongi (2013), a continuous slow exchange of matter between the He convective core and the H-burning shell leads to a large enhancement of the products of the CNO (chiefly ^{14}N and ^{13}C) in both the He convective core and the whole radiative zone that separates the border of the convective core from the H-burning shell. We call such a strong continuous reprocessing of matter between the He- and the H-burning entanglement. The consequences of this entanglement will be discussed in Section 3.3.

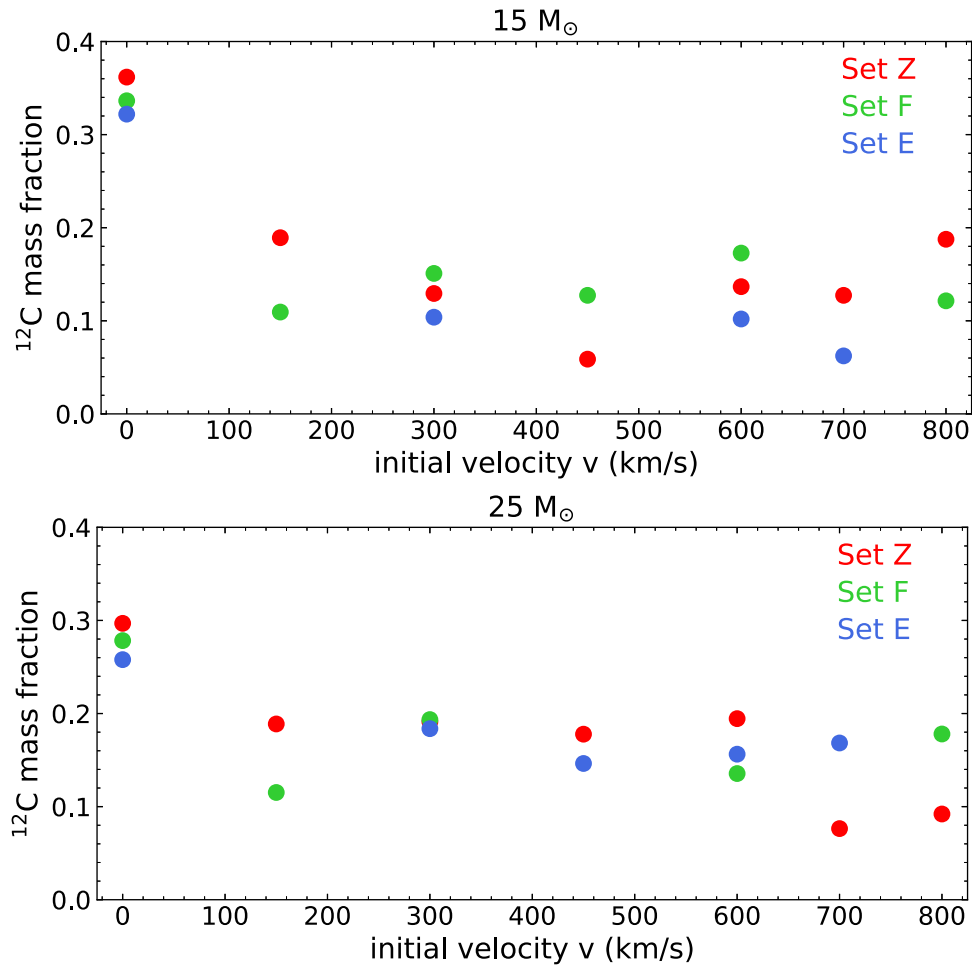


Figure 7. ^{12}C abundance in mass fraction at the central He depletion as a function of the initial equatorial rotation velocity in the 15 (top panel) and $25 M_{\odot}$ cases (bottom panel).

If the initial rotation is fast enough, a significant mixing of C might drive the formation of H convective shell, which grows progressively in mass producing a shape that in the Kippenhahn diagram looks like an eagle’s beak. Such a peculiar H convective shell forms in the 025z700, 025z000, 015f450, 015f800, 015e600, and 015e700 models. Although there is a clear general trend that shows that such a convective shell forms in the fastest rotating stars, one should not expect a strict correlation because rotation leads simultaneously to an expansion of the H mantle (lower densities and temperature imply lower H-burning rates), to the increase of the C abundance in the H-rich mantle (which implies higher H-burning rates), and to larger He core masses (that would speed up the evolution of the He core, reducing the time available for the secular instabilities to bring freshly synthesized C in the H-rich mantle). The Kippenhahn diagrams of all the rotating models are shown in Figures 8–13.

The path of all rotating models in the H-R diagram reflects the complex interplay occurring among the various convective zones that form during the evolution of these stars and is shown in the various panels of Figure 1. Also the rotating models ignite He as a blue supergiant (BSG), but, at variance with their nonrotating counterparts that spend all their central He-burning lifetime as BSG, they are able (in many cases) to almost reach their Hayashi track on a nuclear timescale. The rotating $15 M_{\odot}$ of Set Z, for example, reaches their Hayashi track toward the

end of the central He burning, consuming up to 20% of the He as a red supergiant (RSG). By the way, this means that extremely metal-poor stars may populate the Hertzsprung gap in central He burning. All models able to approach their Hayashi track, however, overcome their Eddington luminosity when their surface temperature drops below ~ 8000 K, lose most of their H-rich mantle on a dynamical timescale, and turn back to a BSG configuration on a thermal timescale. Note that the super-Eddington regime is always reached in the atmosphere of the star, within $10^{-4} M_{\odot}$ from the surface, well before the formation of an extended convective envelope, in layers where the superadiabatic gradient practically coincides with the radiative one. This is a quite new result since the extremely metal-poor stars (including the Population III) have never been expected to experience mass-loss events, but, on the contrary, they were believed to evolve at constant mass unless their rotational velocity reaches the break up velocity. The model with $v_{\text{ini}} = 150 \text{ km s}^{-1}$ is the only one whose luminosity never overcomes the Eddington one and hence remains an RSG up to the final collapse. The rotating $25 M_{\odot}$ of Set Z, on the contrary, remains to the blue side of the H-R diagram expanding only moderately during the central He burning. The reason is the presence of an H convective shell that slows down or even prevents the expansion of the models toward their Hayashi track. Only the models with an initial rotation velocity equal to 450 and 600 km s^{-1} reach their Hayashi track because of the

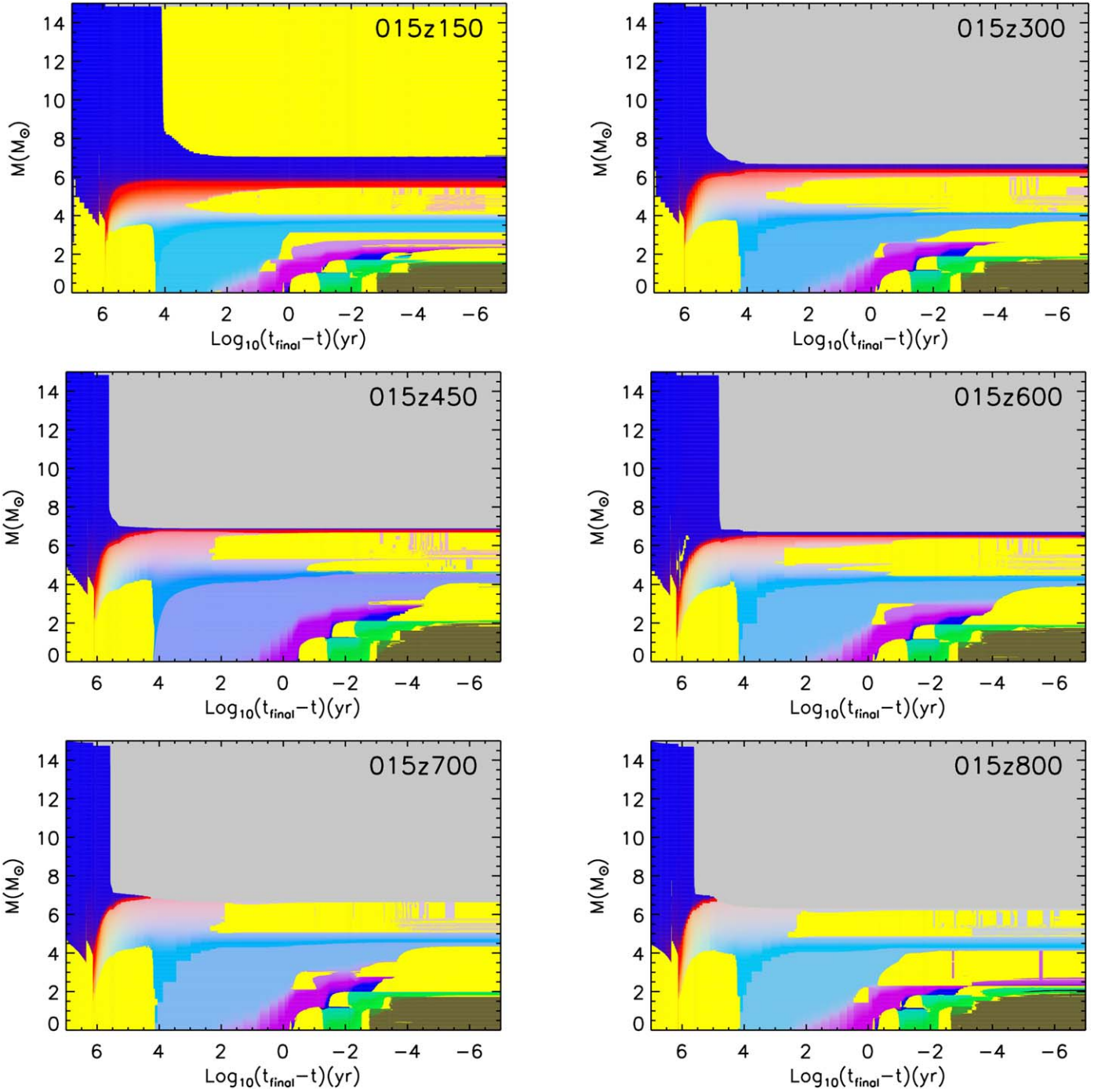


Figure 8. Kippenhahn diagrams of the rotating $15 M_{\odot}$ zero metallicity models. The color coding is the same as in Figure 2.

smaller mass size of the H convective shell, and only the one started with $v_{\text{ini}} = 600 \text{ km s}^{-1}$ exceeds its Eddington luminosity, and loses most of its envelope becoming again a BSG. The path in the H-R diagram of the rotating models of both Sets F and E is quite similar to that of the models of Set Z. All of them ignite He as BSG and move on a nuclear timescale toward their Hayashi track. Once again, only the models that do not form an extended H convective shell become RSG; the others remain BSG all along their central He-burning phase (see Figure 1). All rotating models that are able to reach their Hayashi track before the end of the central He burning overcome their Eddington luminosity when their surface temperature drops to

8000 K, and start losing dynamically a large fraction of their H-rich mantle becoming again BSG.

We have already discussed in Section 3.1.2 that the physical evolution of any model beyond the central He burning is basically independent on the initial mass and metallicity since the two main drivers of the evolution in the advanced burning phases are the CO core mass and the amount of ^{12}C left by the He burning. In addition to this, the advanced burning phases are almost independent also on the initial rotation velocity because (a) the CO core is so compact that the centrifugal force is not able to distort significantly the shape of the star with respect to a spherical configuration, and (b) the rotation

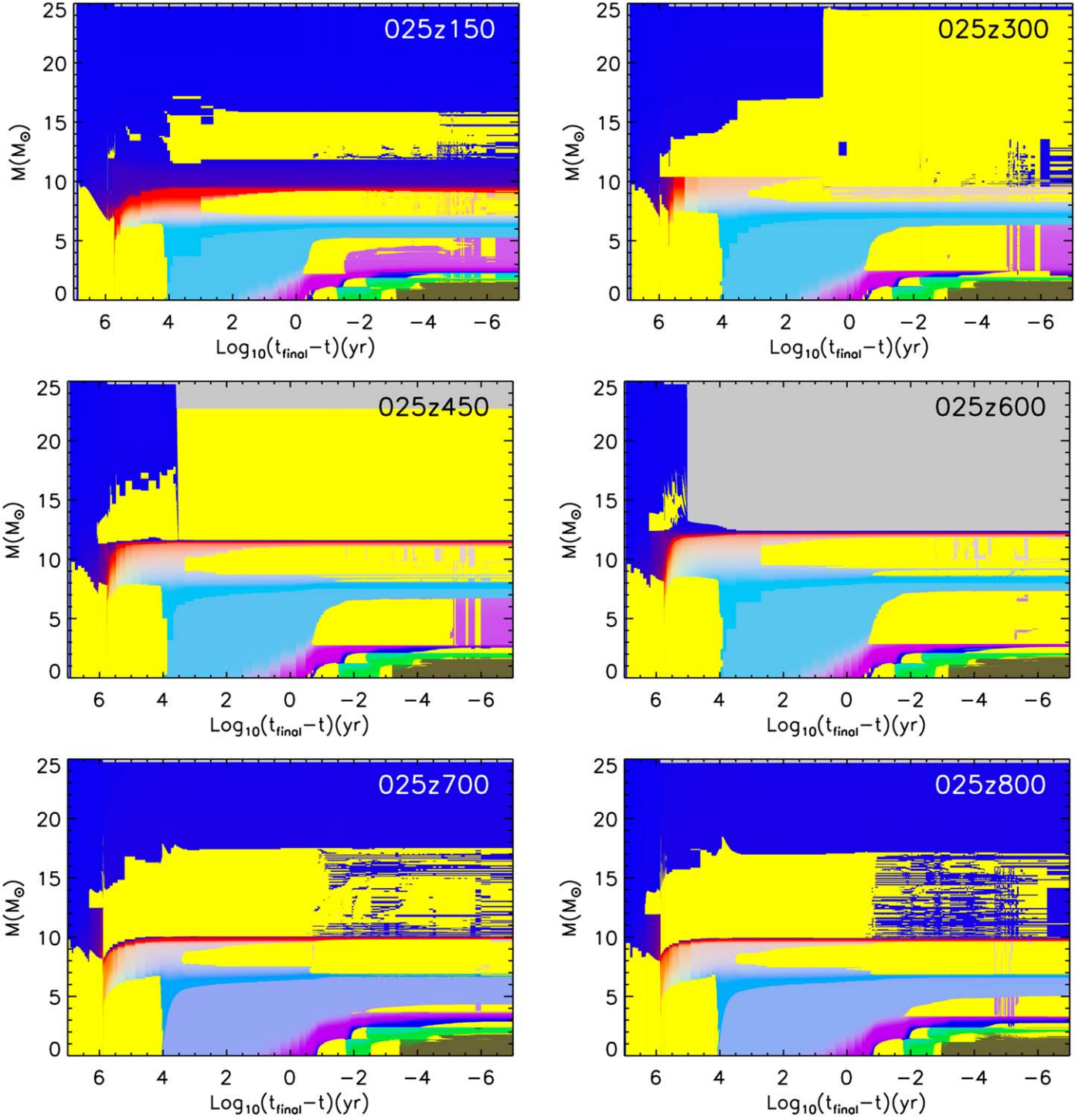


Figure 9. Kippenhahn diagrams of the rotating $25 M_{\odot}$ zero metallicity models. The color coding is the same as in Figure 2.

induced instabilities do not have time to grow so that neither the angular momentum nor the chemicals are transported any more by the rotation driven instabilities. The only exception is the transport of the angular momentum in the convective regions: since we assume instantaneous mixing of the angular momentum in all the convective regions, we force Ω to become flat in each convective region even in the advance burning (as discussed in CL13).

There are two additional distinctive features caused by rotation. The first one is that rotation inhibits the penetration of the He convective shell in the H-rich mantle (a feature that in

nonrotating models leads to the synthesis of a large amount of primary ^{14}N ; Heger & Woosley 2010; Limongi & Chieffi 2012, and reference therein). Basically, all authors who published over the years with models of zero or extremely low metallicity found that in some mass intervals the He convective shell penetrates the H-rich mantle whose main effect is to produce a large amount of primary ^{14}N . In the nonrotating models presented in this work, such a merging occurs in both the $25 M_{\odot}$ of Sets Z and F (see Figure 2). Vice versa, none of the corresponding rotating models shows such a merging (with one exception). The main reason is that the stirring of the matter

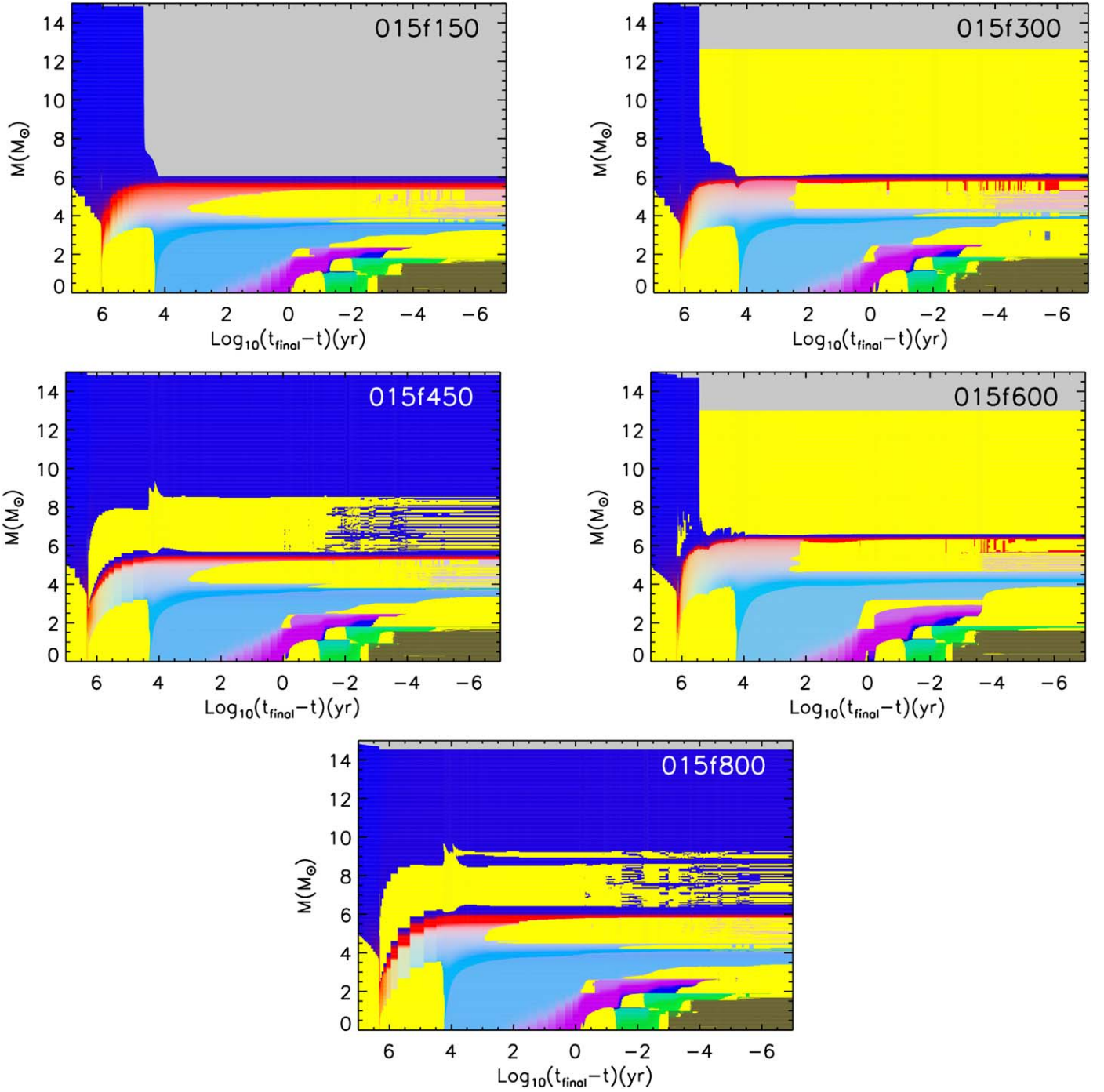


Figure 10. Kippenhahn diagrams of the rotating $15 M_{\odot}$ models of $[\text{Fe}/\text{H}] = -5$. The color coding is the same as in Figure 2.

driven by the rotation leaves a quite smooth He profile at the central He exhaustion (instead of the essentially vertical profile typical of the nonrotating models, see also CL13; and LC18). As a consequence, the He convective shell forms in a region of variable He; and therefore, its abundance is much lower than in the nonrotating case (where it is of the order of 1); such a lower abundance reduces significantly the energy produced by the 3α and therefore the capability of the outer border of the He convective shell to penetrate into the H-rich layers. It must also be considered that the distance, in mass, between the He core and the CO core masses increases with the initial rotation velocity, and therefore, the base of the H-rich mantle is farther

away from the outer border of the He convective shell than in the case of nonrotating models. The only exception to this general trend is the $25 M_{\odot}$ of Set Z, rotating at 300 km s^{-1} . The reason is easily understood by looking at the upper right panel in Figure 9. In this case, in fact, the H convective shell is particularly wide and extends down to the region of variable He since the beginning of the central He burning. This means that (1) the He convective shell forms much closer to the H-rich mantle, and (2) the H profile is so steep that any ingestion (even modest) of H immediately leads to a H-burning runaway event because of its high concentration (almost the initial one).

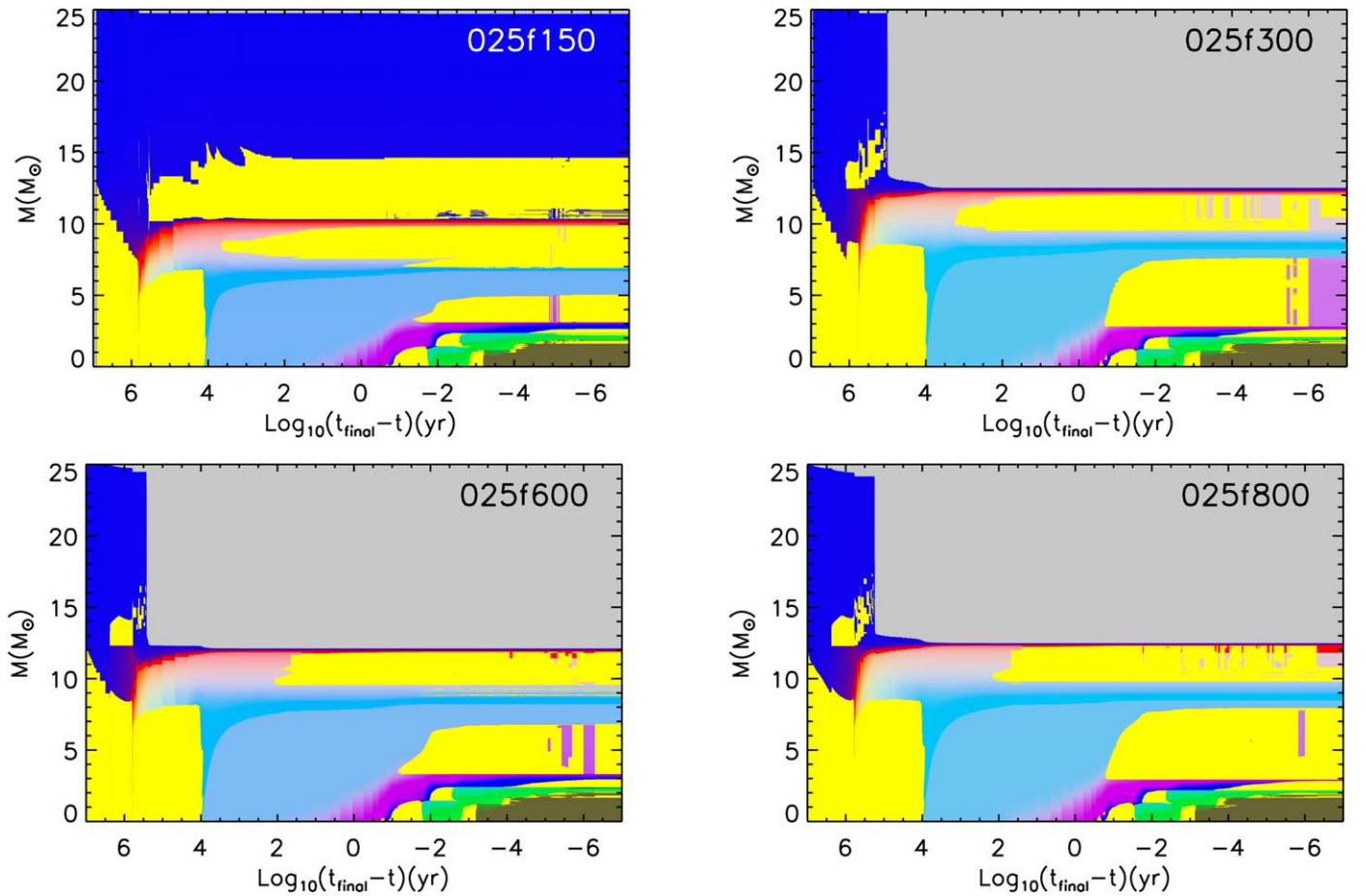


Figure 11. Kippenhahn diagrams of the rotating $25 M_{\odot}$ models of $[\text{Fe}/\text{H}] = -5$. The color coding is the same as in Figure 2.

The second distinctive feature of the rotating models is the penetration of the O convective shell well within the C-rich zone soon after the central Si exhaustion in many rotating models. In particular, this phenomenon occurs in all the rotating $15 M_{\odot}$ models of the three metallicities (except for the models 015z150 and 015z800), while it does not occur at all in the $15 M_{\odot}$ nonrotating models nor in any of the $25 M_{\odot}$, rotating or not. The Kippenhahn diagrams of the $15 M_{\odot}$ models (Figures 8, 10, and 12) show clearly such an occurrence. The reason that leads most of the $15 M_{\odot}$ rotating models to experience the penetration of the O convective shell within the Ne- and C-rich layers is quite difficult to determine robustly because the rotating ones end the central He burning with a much lower C abundance (and hence, in turn, Ne abundance) with respect to their nonrotating counterparts, and this occurrence affects all the advanced evolutionary phases. However, we note that both rotating and nonrotating models develop an O convective shell that closely approaches the Ne-rich layers; but while in the first case, the merging occurs; in the second one, it does not. A closer look at the models at the time of the merging (i.e., soon after the disappearance of the Si convective shell) shows that the models with a lower Ne abundance (the rotating ones) show a smaller entropy jump at the base of the Ne burning shell with respect to their respective nonrotating models. The role of the Ne abundance in determining the entropy jump may be understood by considering that such a jump would vanish as the Ne abundance would turn to zero because in this limiting case any difference, in the nuclear energy generation and in the chemical composition,

would disappear. Figure 11 shows, as a typical example, a comparison between the entropy profiles of the 015e000 (nonrotating, with no merging) and the 015e300 (mildly rotating, with an extended merging). The figure clearly shows the presence of a larger entropy barrier in the nonrotating model with respect to that present in the rotating one at the base of the ^{20}Ne -rich zone (at $\log P \sim 22.7$). To be absolutely clear, we are not saying that the smaller entropy barrier present in the rotating models determines, per se, the penetration of the O convective shell in the Ne-rich region but, simply, that a lower entropy barrier certainly favors (i.e., represents a smaller obstacle) the growth of the O convective shell. An additional point worth being stressed here is that also the criterion adopted to determine the outer (actually any) border of the O convective shell plays a pivotal role. The adoption of the Ledoux criterion instead of the Schwarzschild one, e.g., would obviously disfavor the penetration of the outer border of the convective shell across the chemical discontinuity. Note, however, that also in this respect a lower Ne abundance would in any case imply a lower gradient of molecular weight. The possible occurrence of a merging of the O convective shell in the C-rich zone is of great interest because it would reduce the yields of the products of the C burning and increase those of the O burning. The reason is that the merging spreads the products of the C burning down to the base of the O convective shell (where they are easily destroyed by the passage of the shock wave), and, vice versa, it spreads out the products of the O burning where they can survive to the passage of the shock wave (see Ritter et al. 2018; Roberti et al. 2023; and

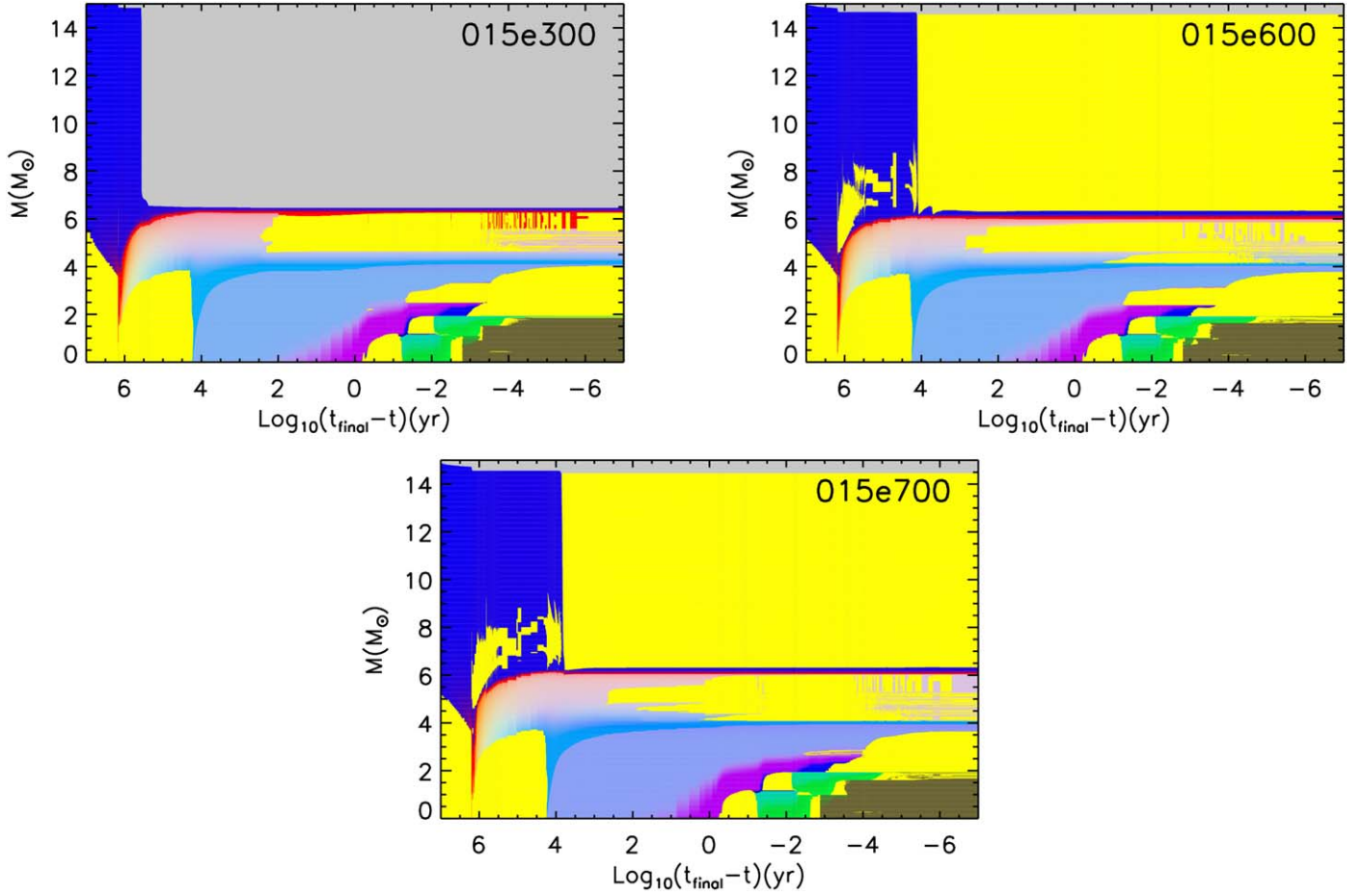


Figure 12. Kippenhahn diagrams of the rotating $15 M_{\odot}$ models of $[\text{Fe}/\text{H}] = -4$. The color coding is the same as in Figure 2.

Section 3.3). This problem certainly deserves a deeper analysis, and we plan to address this problem in the next future. The $25 M_{\odot}$ models do not show such a behavior of the O convective; because, in this case, even in the models with a low ^{12}C mass fraction (and therefore, in turn, a low ^{20}Ne mass fraction), the outer border of the O convective shell always remains quite far from the O/Ne discontinuity.

The main physical properties of the stars at the onset of the core collapse are shown in Table 6 of Appendix B. The final fate of a massive star, i.e., if a successful explosion will occur or not, depends on the interplay between the amount of energy stored in the shock wave (that would push matter outward) and the binding energy (that opposes to the ejection of the mantle). As already discussed in Section 3.1.2, the binding energy at the onset of the collapse is the result of the overlap of the various nuclear burning phases that followed each other in the hydrostatic evolution of the star. Since rotation modifies somewhat the various burning stages, it is interesting to see how rotation modifies the binding energy of a stellar model, which directly reflects, in turn, the final mass–radius relation. We already introduced the compactness $\xi_{2.5}$. Another interesting point in which it is interesting to evaluate the compactness is at the CO core, i.e., ξ_{CO} , since it reflects the behavior of the C convective shells in the advanced burning stages. Figure 15 shows the trend of the compactness, evaluated in these two points, as a function of the initial rotation velocity and of the metallicity. $\xi_{2.5}$ shows a modest increase with the initial rotation velocity, while ξ_{CO} shows a significantly larger

dependence on it. This suggests that, generally speaking, rotating models would *not* be more difficult to explode. However, since the compactness parameter can give at most a preliminary idea of the final fate of a star, we plan to address in the future such a problem with the aid of codes able to follow the collapse and rebound of the collapsing core (see, e.g., Boccioletti et al. 2023).

3.3. Nucleosynthesis

In this section, we discuss basically how rotation affects the yields of the various nuclear species at these extreme metallicities. The key differences induced by rotation on the chemical evolution of a star are essentially two: the first one is that rotation leads to larger CO core masses and lower C abundances at the end of the central He burning, and this implies that rotating stars tend to behave as stars of moderately larger mass, and the second one is the entanglement between the central He burning and the shell H burning. The consequence of this phenomenon is the formation of a robust concentration of ^{14}N (and ^{13}C) within the He core in all models. The ^{14}N engulfed in the He convective core is rapidly converted in ^{22}Ne while ^{13}C is fully destroyed by the (α, n) nuclear reaction becoming therefore a primary neutron source. The ^{14}N and the ^{13}C that instead remain locked between the border of the convective core and the base of the H shell are left substantially unaltered because of the relatively low temperature of this region. We call this region, rich in ^{14}N , ^{13}C , and in

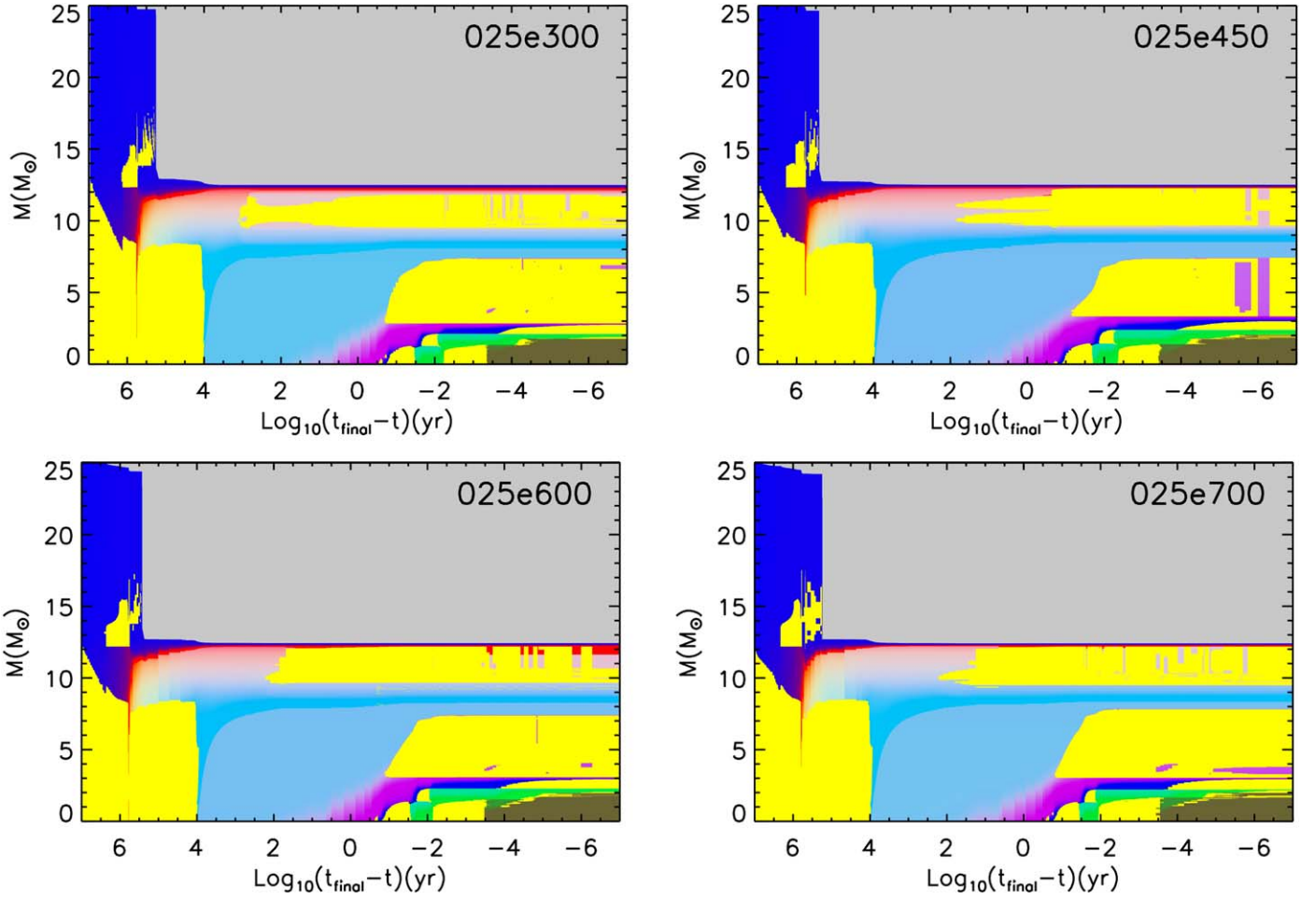


Figure 13. Kippenhahn diagrams of the rotating $25 M_{\odot}$ models of $[\text{Fe}/\text{H}] = -4$. The color coding is the same as in Figure 2.

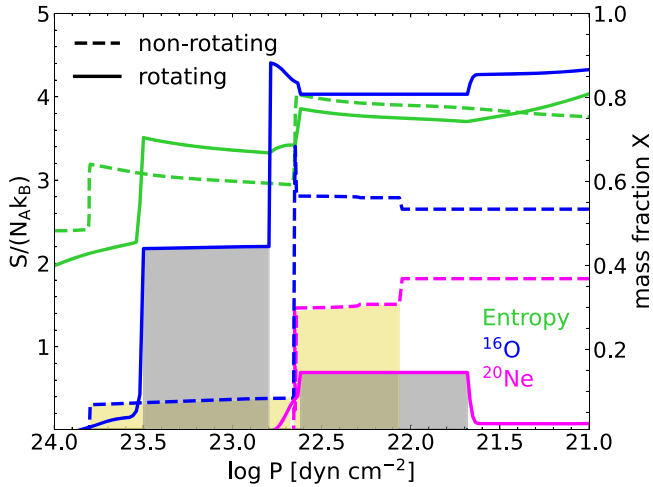


Figure 14. Comparison of the entropy profile (per nucleon in units of Boltzmann constant k_B , green lines) as a function of the internal pressure P between the nonrotating 015e000 model (dashed lines) and the rotating 015e300 one (solid lines). Blue and magenta lines show the abundances in mass fraction of ^{16}O and ^{20}Ne , respectively, in the two cases. The yellow and the gray zones show the O and Ne convective regions in the nonrotating and in the rotating models, respectively.

general products of the CNO cycle, *CNO pocket*. Toward the end of the central He burning, the $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$ nuclear reaction activates in the convective core, providing therefore a

quite robust primary neutron source. This primary neutron source depends of course on the efficiency of the entanglement between the He and H burning, which, in turn, is strictly connected to the initial rotation velocity. A useful tool able to quantify the efficiency of the chemical mixing between the H- and the He-burning regions in the rotating models is the χ parameter, defined in LC18 as follows:

$$\chi(\text{N}, \text{Mg}) = \frac{X(^{14}\text{N})}{14} + \frac{X(^{18}\text{F})}{18} + \frac{X(^{18}\text{O})}{18} + \frac{X(^{22}\text{Ne})}{22} + \frac{X(^{25}\text{Mg})}{25} + \frac{X(^{26}\text{Mg})}{26}, \quad (3)$$

and it is simply the sum by number fraction of all the nuclei between ^{14}N and ^{26}Mg involved in the conversion of N into Mg. This parameter remains constant if the He- and the H-burning regions do not interact; because, in this case, the ^{14}N burning may populate only nuclei of the chain that goes from the ^{14}N to the $^{25}\text{Mg}/^{26}\text{Mg}$. Conversely, in rotating stars, the amount of ^{14}N increases continuously because of the progressive conversion of freshly made ^{12}C into ^{14}N . Figure 16 shows the strong correlation between the variation of the χ parameter and the initial rotation velocity. Since χ is basically a proxy of the amount of ^{22}Ne present in the core, the neutron density in He burning increases as the initial rotation velocity increases, turning from the negligible values of $10^2\text{--}10^4 \text{ n cm}^{-3}$ (typical of the nonrotating models at

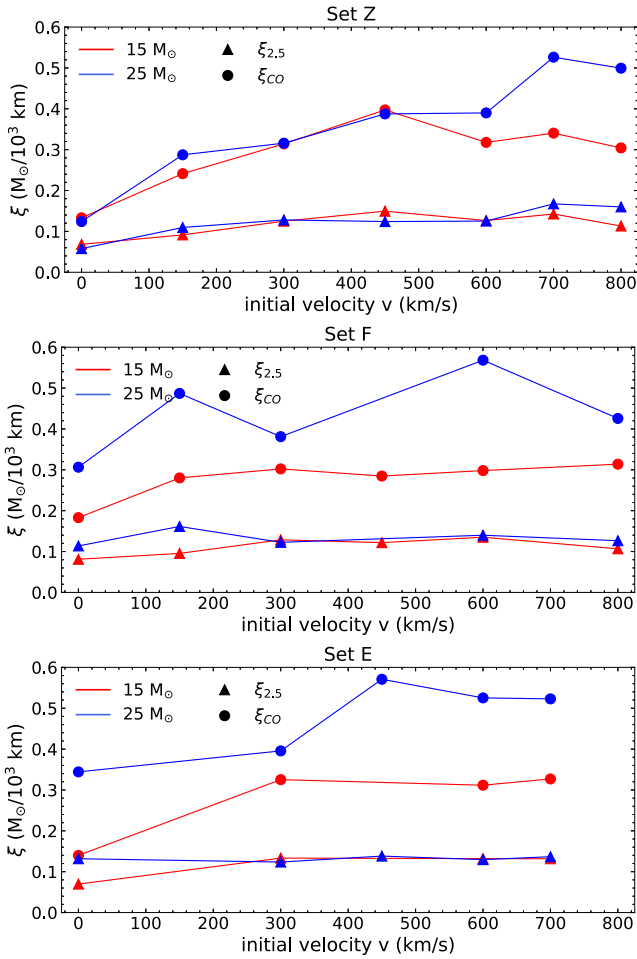


Figure 15. The compactness ξ of the star evaluated at $2.5 M_{\odot}$ (filled dots) and at the border of the CO core (filled triangles) at the presupernova stage in $15 M_{\odot}$ (red points) and $25 M_{\odot}$ (blue points) in Set Z (top panel), Set F (central panel), and Set E (bottom panel).

these metallicities) up to values of the order of $\sim 10^7 \text{ n cm}^{-3}$, i.e., very close to that of solar metallicity models.

At zero metallicity, this quite large neutron density does not allow in any case the synthesis of nuclei heavier than Zn, not even the s -process weak component because of the lack of seed nuclei. The high neutron density, in this case, leads to the synthesis of several neutron-rich nuclei like, e.g., $^{25-26}\text{Mg}$, ^{23}Na , and, in progressively faster rotating stars, of ^{27}Al , $^{28-29-30}\text{Si}$, ^{31}P , and $^{32-33-34}\text{S}$.

At higher metallicity (Sets F and E), the presence of seed nuclei, coupled to the high neutron-to-seed ratio, allows the synthesis of heavy nuclei up to, in some cases, the strong component (i.e., up to Pb).

In the following, for simplicity, we will mainly discuss Sr, Ba, and Pb to describe the climbing of the matter along the chart of the nuclides as a function of the initial metallicity and rotation velocity.

Figure 17 shows a snapshot of the internal structure of four representative models at the end of the central He burning for Sets F and E. All four models show a consistent production of the weak component (represented by ^{88}Sr), and the $15 M_{\odot}$ shows an increase of the elements of the main component (represented by ^{138}Ba). The nucleosynthesis extends up to ^{208}Pb in both $15 M_{\odot}$ models. Note that also ^{19}F shows a pronounced

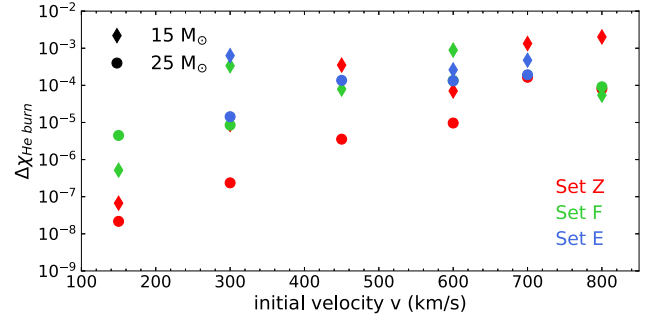


Figure 16. The variation of the parameter χ (Equation (3)) between central He ignition and exhaustion, as a function of the initial equatorial velocity for the $15 M_{\odot}$ (filled diamonds) and the $25 M_{\odot}$ (filled dots) in Set Z (red), Set F (green), and Set E (blue).

peak in both $15 M_{\odot}$, while the $25 M_{\odot}$ does not. It is worth noting that the core He-burning phase produces the bulk of the final amount of the s -process elements.

Once He is exhausted in the convective core, He burning shifts in shell where an extended convective shell soon develops. Although the neutron density reached at the base of the convective shell reaches values in the range $10^{8-10} \text{ n cm}^{-3}$, the overall contribution of the He convective shell to the synthesis of the heavy elements is quite modest. Figure 18 shows a snapshot of the four structures already shown in Figure 17 once the He convective shell is fully developed.

Although the He convective shell does not play an important role in the synthesis of the trans-Fe elements, it is actually the nursery of F. ^{19}F , in fact, is synthesized by the sequence of reactions first identified by Forestini et al. (1992): $^{14}\text{N}(\alpha, \gamma)^{18}\text{F}(\beta^+)^{18}\text{O}(\text{p}, \alpha)^{15}\text{N}(\alpha, \gamma)^{19}\text{F}$, where the protons necessary to feed the ^{18}O come from the $^{14}\text{N}(\text{n}, \text{p})^{14}\text{C}$, while the neutrons are produced by the $^{13}\text{C}(\alpha, \text{n})$. It is not easy to find an environment in which this chain of reactions may work because of the simultaneously need of both neutrons and ^{14}N . The He-burning shell in rotating massive stars perfectly embodies these requirements because of the large buffer of ^{14}N and ^{13}C present in the CNO pocket between the CO core and the He core. When the He convective shell develops and extends within the He core, it engulfs a large amount of ^{14}N and ^{13}C that are quickly brought to the He-burning temperature where the above quoted reactions may easily occur (see, e.g., CL13; LC18). ^{19}F may reach a concentration as high as 10^{-4} in mass fraction in the fastest rotating models.

The last neutron production site occurs in C burning, more specifically in the convective C shell burning where the ^{22}Ne survived the central He burning reacting with the α particles provided by the $^{12}\text{C}(^{12}\text{C}, \alpha)\gamma$ nuclear reaction, pours a substantial amount of neutrons. Although the contribution of the C burning to the synthesis of the elements heavier than Zn is modest, it is worth noting that, even if the C convective shell does not increase the yields of the heavy nuclei, it does not even destroy them significantly (Figure 19). Typical temperatures and densities at the base of the C convective shell are $T = 1.2\text{--}1.5 \text{ GK}$, and $\rho = 1\text{--}2 \times 10^5 \text{ g cm}^{-3}$, and the neutron densities span the range $10^{11}\text{--}10^{13} \text{ n cm}^{-3}$.

Beyond the C burning, no s -process nuclei production is possible because the temperature is high enough that they are progressively and completely photodisintegrated.

There is however another phenomenon that occurs in the $15 M_{\odot}$ rotating models. In fact, as discussed in Section 3.2,

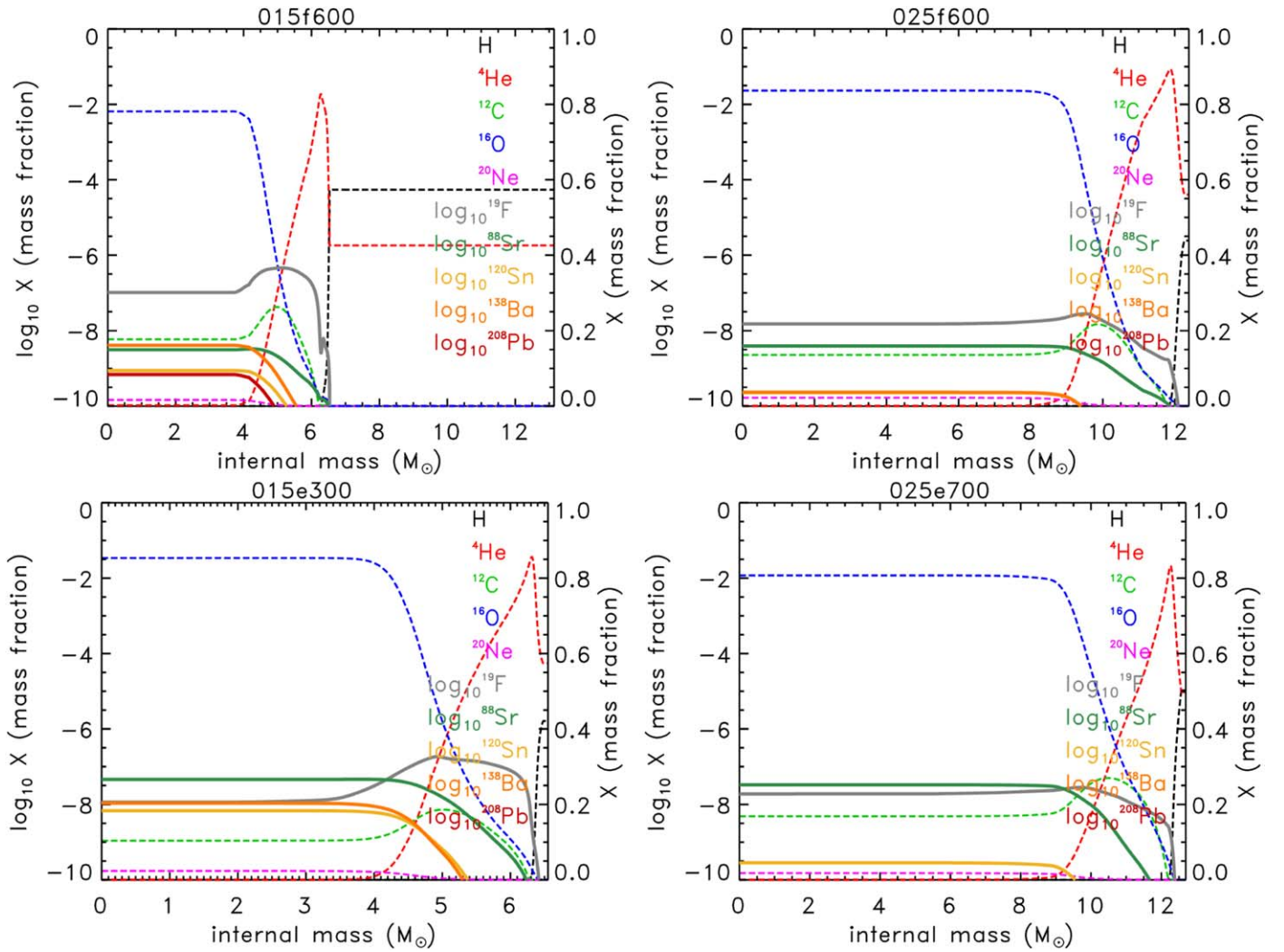


Figure 17. Internal structure at core He exhaustion of four representative models 015f600, 025f600, 015e300, and 025e700. The dashed lines (right y-axis) represent the main nuclear species (H, ^4He , ^{12}C , ^{16}O , and ^{20}Ne), while the solid lines (left y-axis) show the internal profile of selected s-process isotopes: ^{88}Sr (weak component), ^{138}Ba (main component), ^{208}Pb (heavy component), and one isotope between the neutron magic nuclei $N = 50$, and $N = 82$, ^{120}Sn . At last, the gray solid line represents the ^{19}F abundance.

during the very late stages of their evolution, the O convective shell merges with the C shell and ingests a sizable amount of fresh ^{12}C . The result of this phenomenon is the formation of a large O convective shell in which part of the products of the C shell burning is reprocessed. In particular, the most abundant nuclei that emerge from this interaction are the typical products of the O burning (see discussion in Section 6). This extended convective region preserves these intermediate and Fe-peak nuclei from being reprocessed by the explosive nucleosynthesis. In the case of the element above Fe, the effect of such an ingestion is the destruction of the heaviest isotopes and an increase of the abundances of the elements of the weak component in the extended convective shell. Figure 20 shows the result of such a mixing in two representative cases.

As discussed in the previous sections (Sections 3.1.2 and 3.2), in several cases, the He convective shell penetrates the H-rich region, and the extra energy produced by the proton ingestion in the He shell leads to the consequent formation of a large convective region that rapidly covers a large part of the H-rich envelope. This phenomenon has been associated to the

synthesis of primary ^{14}N at early times. In both nonrotating $25 M_{\odot}$ stars, the abundance of ^{14}N in the extended convective shell reaches a concentration of $\sim 3 \times 10^{-3}$ in mass fraction. But this merging leads also to the production of a strong neutron flux due to α captures on ^{13}C . Very high neutron densities may be obtained, typical of the so-called *intermediate* neutron capture process (*i-process*), i.e., $n_n \sim 10^{14} \text{ n cm}^{-3}$. In the 025z000 model, similarly to the He-burning phase in the rotating case, these neutrons are absorbed by lighter nuclei, populating the light and intermediate nuclei up to Ti. The most abundant isotopes in the newly formed H convective shell are ^{14}N , ^{13}C , ^{22}Ne , and ^{23}Na . In the 025f000 model, the most abundant nuclei are ^{89}Y , ^{105}Pd , ^{111}Cd , and ^{125}Sb ; therefore, the neutron capture nucleosynthesis favors in this case the synthesis of some nuclei belonging mostly to the weak component. Note that ^{125}Sb is an unstable nucleus; therefore, it will contribute to the abundance of ^{125}Te . Figure 21 shows the internal structure before (left panels) and after (right panels) the merging of the H and He convective shell in the nonrotating $25 M_{\odot}$ stars at $[\text{Fe}/\text{H}] = -\infty$ (upper panels) and -5 (lower panels).

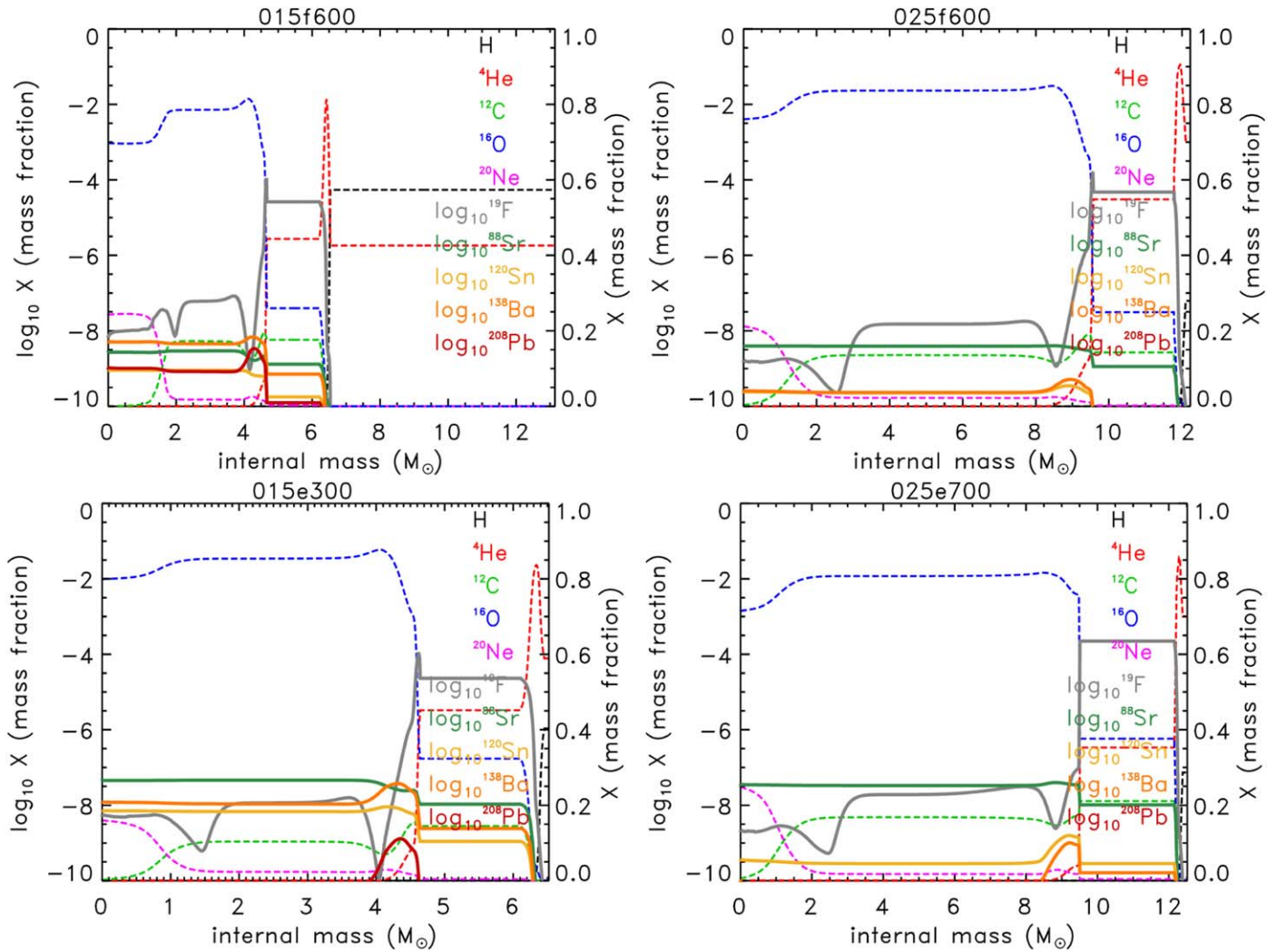


Figure 18. Same as Figure 17, but after the formation of the He convective shell.

4. The Explosion

In the previous section, we discussed in detail the evolution of models of 15 and 25 M_{\odot} having different metallicity and initial rotation velocities, starting from the pre-MS up to the onset of the iron core collapse and the associated nucleosynthesis. The last step necessary to obtain the chemical composition of the ejecta requires the simulation of the passage of the shock wave within the mantle together with the determination of the mass of the remnant. In this paper, the explosion has been computed by means of the HYdrodynamic Ppm Explosion with Radiation diffusION (HYPERION) code: this is a lagrangian hydrodynamic flux limited diffusion radiation code, designed to calculate the explosive nucleosynthesis, remnant mass, and light curve associated with the explosion of a massive star. This code is presented and extensively described in Limongi & Chieffi (2020). More specifically, the explosion is triggered by means of a thermal bomb, i.e., by depositing the minimum amount of thermal energy, at a mass coordinate of $0.8 M_{\odot}$ in the presupernova model (i.e., well inside the Fe core), that leads to the full ejection of the mantle above the Fe core. The remnant mass is fixed by requiring the ejection of $0.07 M_{\odot}$ of ^{56}Ni . No mixing nor fallback (see, e.g., Umeda & Nomoto 2002, 2005) are taken into account. We stop our hydrostatic calculation, and

hence define the presupernova model, when the central temperature is ~ 6 GK. At this stage, the first Si convective shell has already exhausted, and the final Fe core is formed.

A typical example of the influence of the explosive burning on the final yields is shown in Figure 22. The upper panel shows, in fact, the abundances of the most abundant nuclei, plus the two isotopes ^{88}Sr and ^{138}Ba (representative of the s -process elements), before (dashed lines) and after (solid lines) the passage of the shock wave. The zones exposed to the various explosive nuclear burning are marked by the gray areas (complete Si burning, $T > 5 \times 10^9$ K; incomplete Si burning, $T > 4 \times 10^9$ K; explosive O burning, $T > 3.3 \times 10^9$ K; explosive Ne burning, $T > 2.1 \times 10^9$ K; explosive C burning, $T > 1.9 \times 10^9$ K). This figure clearly shows that the chemical composition is deeply modified by the explosive nucleosynthesis up to a great fraction of the C convective shell. The two selected isotopes representative of the s -process elements are mainly produced by the core He burning so that their final yields are dominated by the hydrostatic component.

In order to have a global information on the effect of the explosion on the s -process element abundances, we show in the lower panel of Figure 22 a comparison between the elemental explosive (red line) and pre-explosive (black line) ejected masses (yields) obtained for the 025f600 model. The pre-

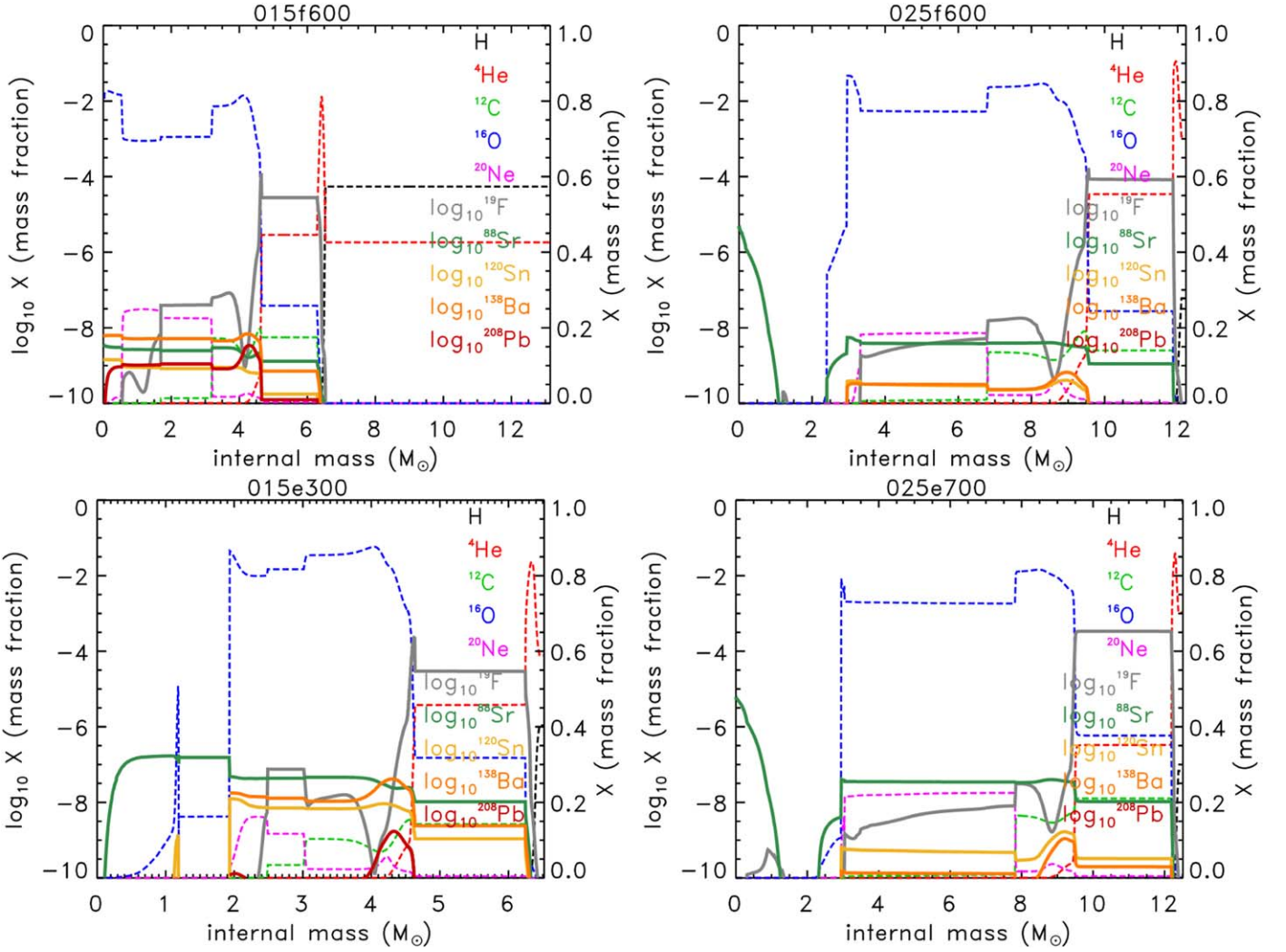


Figure 19. Same as Figure 17, but after the full development of the C convective shell.

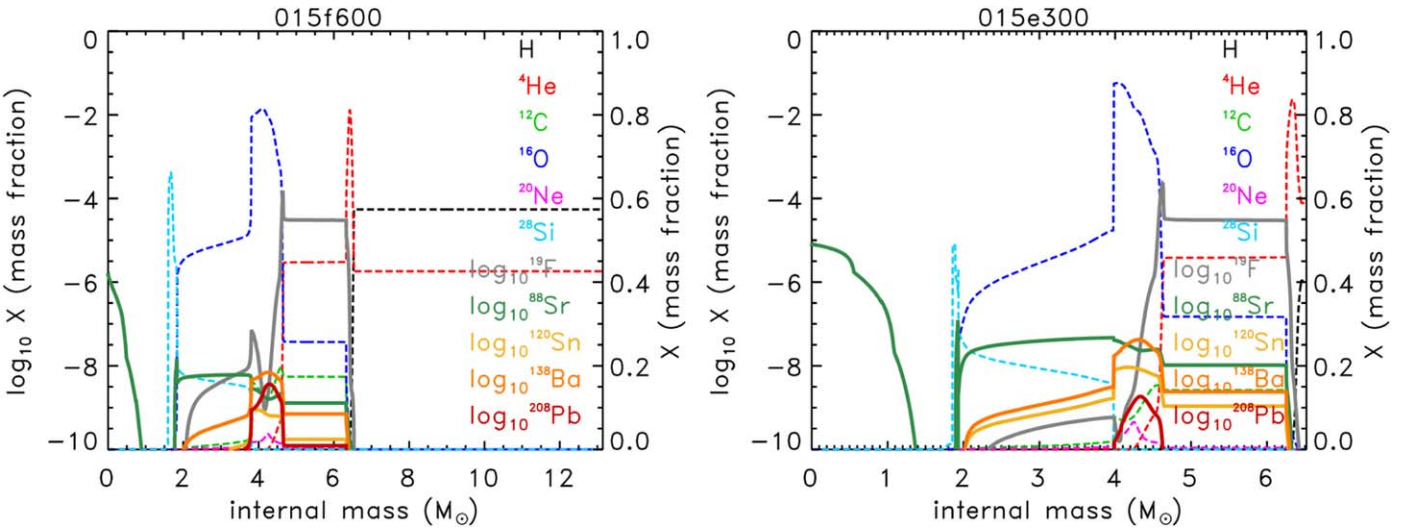


Figure 20. Internal structure after the C–O shell merger in two $15 M_{\odot}$ rotating stars, i.e., 015f600 (left panel) and 015e300 (right panel). The dashed lines (right y-axis) represent the main nuclear species (H, ^4He , ^{12}C , ^{16}O , ^{20}Ne , and ^{28}Si), while the solid lines (left y-axis) show the internal profile of selected s-process isotopes: ^{88}Sr (weak component), ^{138}Ba (main component), ^{208}Pb (heavy component), and one isotope between the neutron magic nuclei $N = 50$, and $N = 82$, ^{120}Sn . Finally, the gray solid line represents the ^{19}F abundance.

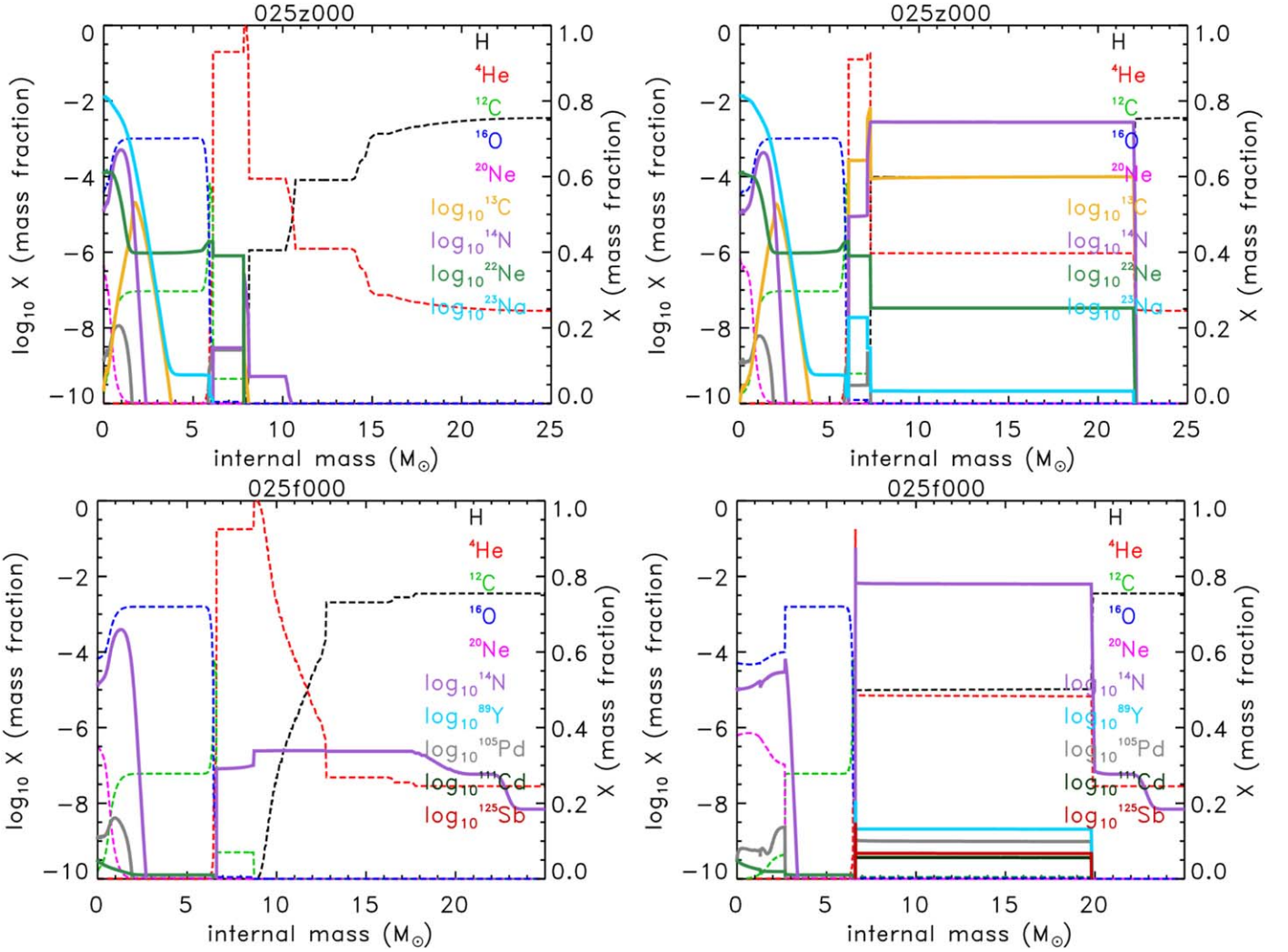


Figure 21. Internal structure of the nonrotating $25 M_{\odot}$ star of Set Z (top panels) and Set F (bottom panels) before (left panels) and after (right panels) the convective H–He shell merging. The black, red, green, magenta, and blue solid lines represent the abundance in mass fraction of the principal nuclear species (H, ^4He , ^{12}C , ^{20}Ne , and ^{16}O) as a function of the internal mass coordinate, and they refer to the secondary y-axis. The other solid lines show the internal distribution of the most produced nuclei during the merger between the H and the He convective shells (in particular, ^{14}N is the violet solid line), and they refer to the principal y-axis.

explosive yields have been computed by adopting the same mass cut obtained by the simulation of the explosion, i.e., $3.13 M_{\odot}$ in this specific case. As expected, the explosion produces iron peak elements as well as intermediate mass elements between Si and Ti. Vice versa, the other elements, i.e., those lighter than Al or heavier than Ni, are very mildly or not affected at all by the passage of the shock wave (see, e.g., CL13; LC18, and references therein).

5. The Yields

We have seen above that the elements more affected by rotation are N plus all the ones whose synthesis is widely dependent on the presence of a neutron source, i.e., the elements above the Fe group and F. As proxies of all the nuclei above the Fe group, we will discuss the yields of Sr, Ba, and Pb since they are the ones that mark the three neutron magic numbers with $N = 50, 82$, and 126 . A complete table of all the yields obtained in this work is presented in Appendix D.

5.1. Nitrogen

Nitrogen is synthesized by the CNO cycle in the hydrostatic H-burning stage, and it is therefore a typical secondary element in nonrotating stars. The only exception occurs at zero metallicity where the He convective shell engulfs part of the H-rich mantle in some models. The abrupt ingestion of protons at temperatures of the He burning in a C-rich environment leads to a burst of synthesis of nitrogen (primary). We obtain such an ingestion in the two nonrotating models 025z000 and 025f000. As already discussed in Sections 3.2 and 3.3, rotation plays a critical role in the production of N. Figure 23 shows the N yield as a function of the initial rotation velocity for all the computed models. Both masses and all three metallicities show a steep increase of the N yield up to $v_{\text{ini}} = 300 \text{ km s}^{-1}$ and a rough plateau for larger initial velocities. It is worth noting that rotation may lead to N yields as high as those provided by the nonrotating massive stars where the penetration of the He convective shell in the H-rich mantle occurs. Therefore, the rather high and somewhat unexpected N abundance plateau obtained from observations in low-metallicity halo stars of

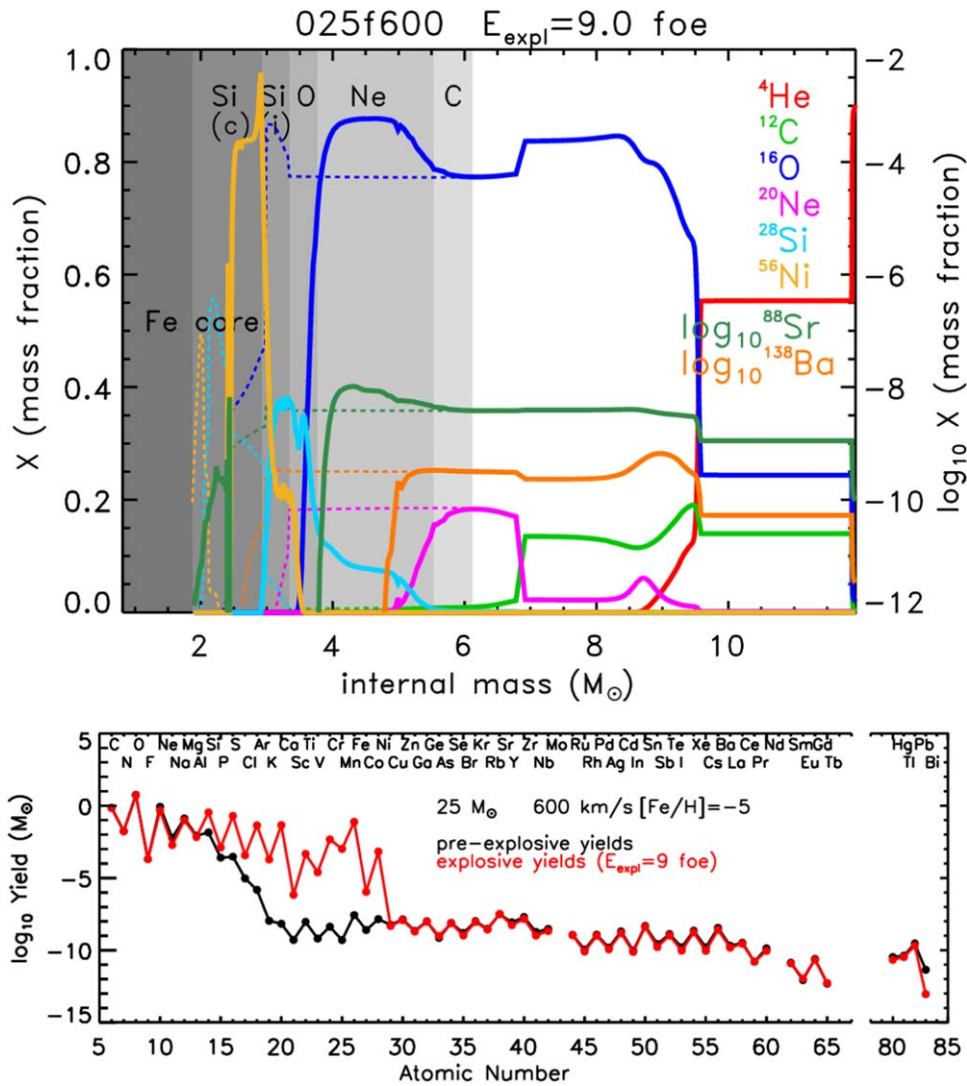


Figure 22. Top panel: presupernova (dashed lines) and postexplosive (solid lines) structure of a $25 M_{\odot}$ star at $[\text{Fe}/\text{H}] = -5$, rotating at 600 km s^{-1} . In this case, the abundances are presented as a function of the internal mass of the star, from the center up to the base of the H shell. The gray bands in the plot mark each explosive burning stage in the corresponding internal mass coordinate, as discussed in the text. The dashed lines represent the abundances of the isotopes at the presupernova stage, while the solid lines represent the isotopic abundances after the explosive nucleosynthesis. Bottom panel: pre-explosive (black dots) and explosive (red dots) yields of the model 025f600.

the Milky Way (Chiappini et al. 2005, 2006; Grisoni et al. 2021) could be explained in terms of the nucleosynthesis of these very low-metallicity massive stars (rotating and not). By the way, the temporal evolution of N in the context of the chemical evolution of the Milky Way and its connection with the average rotation velocity of the stellar generations of different metallicities has been addressed in detail by Prantzos et al. (2018) and later on by, e.g., Grisoni et al. (2020, 2021) and Franco et al. (2021). Of course, a conclusive analysis on this subject would require additional models as well as a quantitative estimate of the contribution of these stars and of the initial distribution of their rotation velocities to the enrichment of N in the early stages of evolution of the Galaxy and of the Universe in general.

5.2. Fluorine

The MS of processes that leads to the synthesis of fluorine is the one identified by Forestini et al. (1992) and described in Section 3.3. Prantzos et al. (2018) have shown that rapidly rotating massive stars can be responsible of the synthesis of

fluorine at low metallicity (see also Grisoni et al. 2020; Franco et al. 2021). Here we confirm such a result also at extremely low metallicities. Figure 24 shows the dependence of the ^{19}F yields on the initial rotation velocity for both masses and the three initial rotation velocities. The plot shows a good trend with the velocity, while it is almost independent of the initial metallicity, resembling that of N. In particular, it increases with the initial rotation velocity and then bends toward a rough plateau for $v_{\text{ini}} > 300 \text{ km s}^{-1}$, reaching values as high as 10^{-4} – $10^{-3} M_{\odot}$. Note, however, that the nonrotating models in which the H–He shell merging occurs do not contribute significantly to the synthesis of F.

5.3. The Heavy Elements

Let us consider first the sum of the yields of all the elements heavier than Zn. Figure 25 shows this quantity as a function of the initial rotation velocity for stars of Sets F and E. Note that zero metallicity stars do not synthesize any appreciable amount of elements beyond Zn (Chieffi & Limongi 2004) and hence do

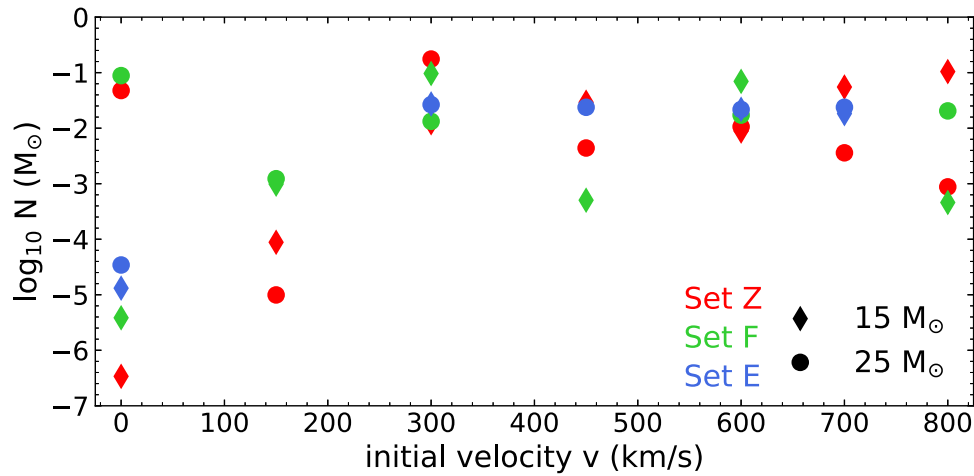


Figure 23. Nitrogen yields as a function of the initial rotation velocity.

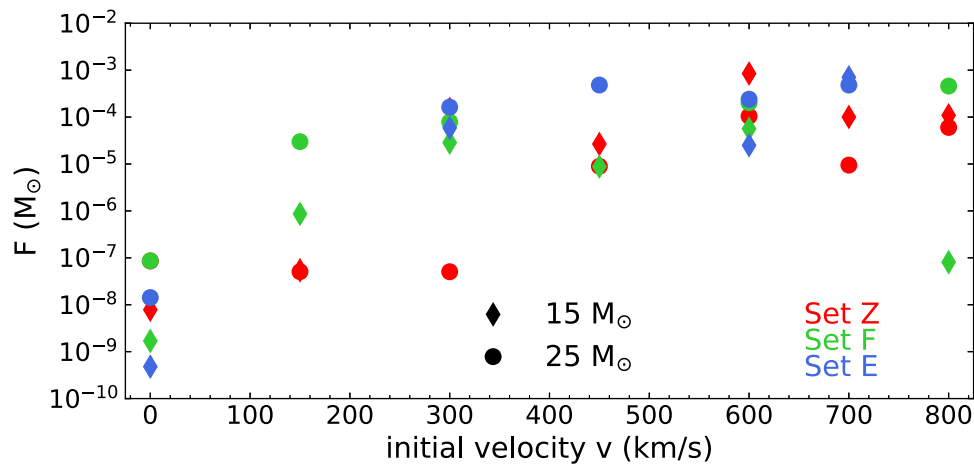


Figure 24. Fluorine yields as a function of the initial rotation velocity.

not appear in this plot. The quantity plotted in the figure is the net total yield, defined as the difference between the final and the initial sum of the yields, of all the elements with $Z > 30$ up to $Z = 83$ (hereinafter S3083). An overall look at the figure shows a definite increase of S3083 with the initial rotation velocity. A closer look shows a few other features worth being mentioned. First of all, while three out of the four nonrotating models (015f000, 015f000, and 025f000) barely reach a global abundance of the order of 10^{-10} – $10^{-9} M_{\odot}$, the model 025f000 shows a much larger increase of S3083 (of the order of $10^{-7} M_{\odot}$, green dot). Such a high abundance is the consequence of the merging of the He convective shell with the H-rich mantle. The abrupt ingestion of protons down to the He-burning layers triggers a short burst of neutrons due to the activation of the $^{13}\text{C}(\alpha, n)^{16}\text{O}$ nuclear reaction rate that leads to a nonnegligible neutron capture nucleosynthesis. The second thing worth noting is that, for each mass, S3083 increases up to a rotation velocity of the order of 300 km s^{-1} and then bends considerably for large initial rotation velocities. In the $15 M_{\odot}$ of Set F, the rotation increases S3083 up to a factor of the order of 50 times the initial value while the increase may become 10 times larger (i.e., 500 times) in the $15 M_{\odot}$ of Set E. In the $25 M_{\odot}$, S3083 may increase up to a factor 1000 with respect to the nonrotating model while it remains roughly flat in the $25 M_{\odot}$ of Set E and close to the value obtained in the nonrotating case.

The global picture shown by Figure 25 does not say anything about the distribution of the elements between Ga and Bi but only how much matter flows above Zn as a function of the mass and initial rotation velocity. In order to understand how matter populates different parts of the chart of the nuclides, we will take advantage of the existence of the three magic neutron numbers 50, 82, and 126. Nuclei having these numbers of neutrons have in fact a minimum of the neutron capture nuclear cross section and therefore constitute the main barriers to the flux of the matter toward heavier nuclei. Depending on the neutron-to-seed ratio and the neutron exposure, matter may stop at the first, second, or third neutron closure shell.

As proxies of the nuclei that have a magic neutron number, we consider the following three key nuclei: $^{88}\text{Sr}(N=50)$, $^{138}\text{Ba}(N=82)$, and $^{208}\text{Pb}(N=126)$. Figure 26 shows in the left column the dependence of the yields of these three nuclei on the initial rotation velocity for both Sets F and E, while the trend with respect to the $\Delta\chi$ (which basically quantify the amount of primary ^{14}N produced by the entanglement between the He and H burning; see Section 3.3) is shown in the right column. The yields of all three nuclei scale directly with the initial rotation velocity (and $\Delta\chi$), a clear indication of the increase of the neutron flux with the initial rotation velocity. The main increase in the yield of ^{88}Sr occurs for initial rotation velocities in the range 150 – 300 km s^{-1} ; the dependence

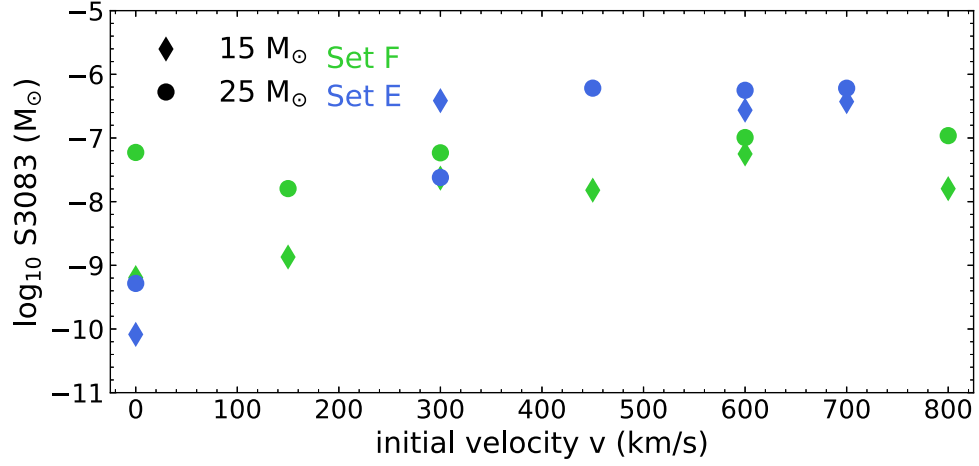


Figure 25. Total net yield of elements from Ga up to Bi (S3083; see text) as a function of the initial velocity for all the explored metallicity.

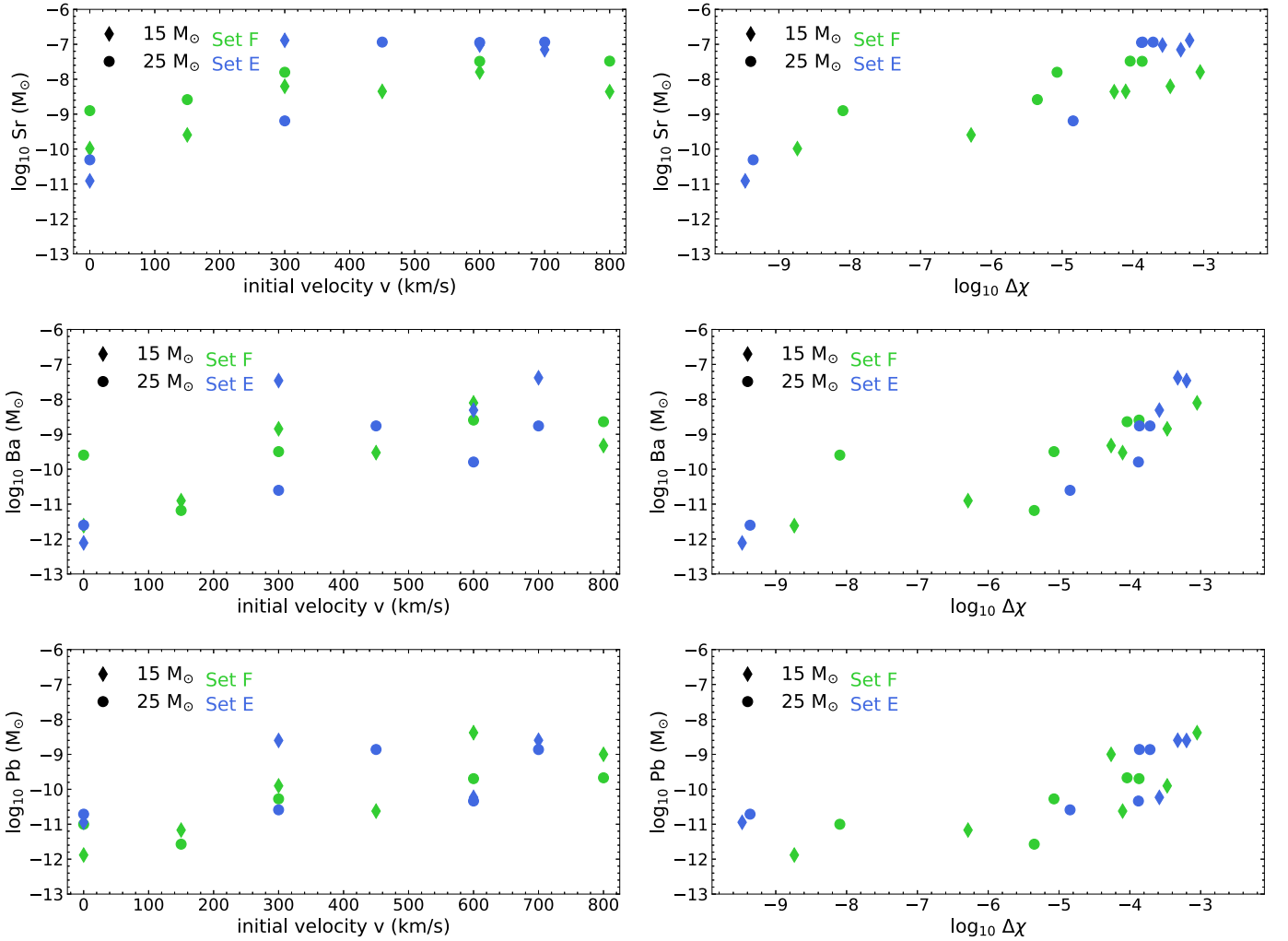


Figure 26. Trend of the yields of Sr, Ba, and Pb as a function of the initial rotation velocity (left panels) and of the $\Delta\chi$ parameter (right panels; see text): $15 M_{\odot}$ (green diamonds), $25 M_{\odot}$ (green dots) Set F, $15 M_{\odot}$ (blue diamonds), and $25 M_{\odot}$ (blue dots) Set E.

becomes much weaker above 300 km s^{-1} . This behavior may be easily understood by looking at Figure 16 that shows that the largest increase in the $\Delta\chi$ occurs between 150 and 300 km s^{-1} . Set E, in particular, shows a saturation of the Sr yield for both masses. The left panels in Figure 26 that refer to

Ba and Pb also show an increase of the yields with the initial rotation velocity even if with some scatter while the corresponding right panels show a much tighter scaling. The reason is obviously that the yields directly depend on the $\Delta\chi$ (because it is directly responsible of the neutron flux) and only

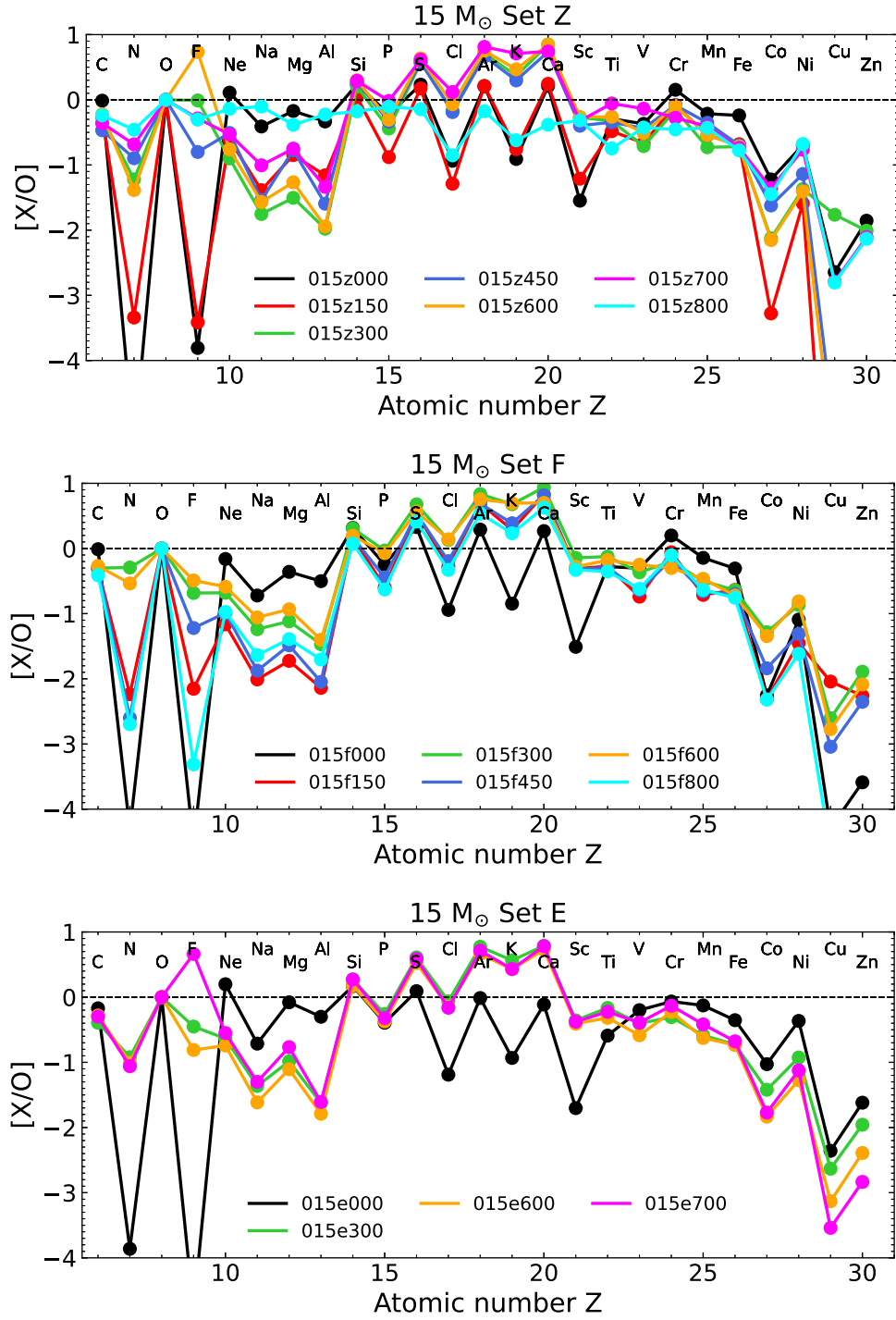


Figure 27. Logarithm of the production factors of the $15 M_{\odot}$ stars of Set Z (top panels), Set F (central panels), and Set E (bottom panels) as a function of the atomic number A . The color scale on the right marks the different initial equatorial velocity of the star, from nonrotating (dark blue) up to 800 km s^{-1} (yellow).

indirectly on the initial rotation velocity (because it determines the synthesis of primary ^{14}N in central He burning).

6. The $[X/O]$

In the previous section (Section 5), we have shown how the yields of a few key elements depend on the initial rotation velocity for the three metallicity under exam. In this section, we want to show all the elements C to Bi and discuss which nuclei are produced enough to have an impact on the chemical evolution of the matter and which do not. For sake of clearness,

let us discuss first the block of nuclei between C and Zn. An efficient way to make this analysis is to look at the $[X/O]$, which is simply the logarithm of the ratio between the yield of each element and that of the oxygen, minus the logarithm of the same ratio in the Sun, i.e., $[X/O] = \log_{10}(Y^i/Y^O) - \log_{10}(X_i^i/X_i^O)$, where Y is the yield in solar masses, and X_i is the relative solar abundances in mass fraction. Oxygen is by far the best candidate to be the reference element because (1) it is the most abundant nucleus synthesized in stars, (2) it is produced almost exclusively by massive stars, and (3) it is almost not affected by the explosive burning. A $[X/O]$ greater than, equal to, or smaller

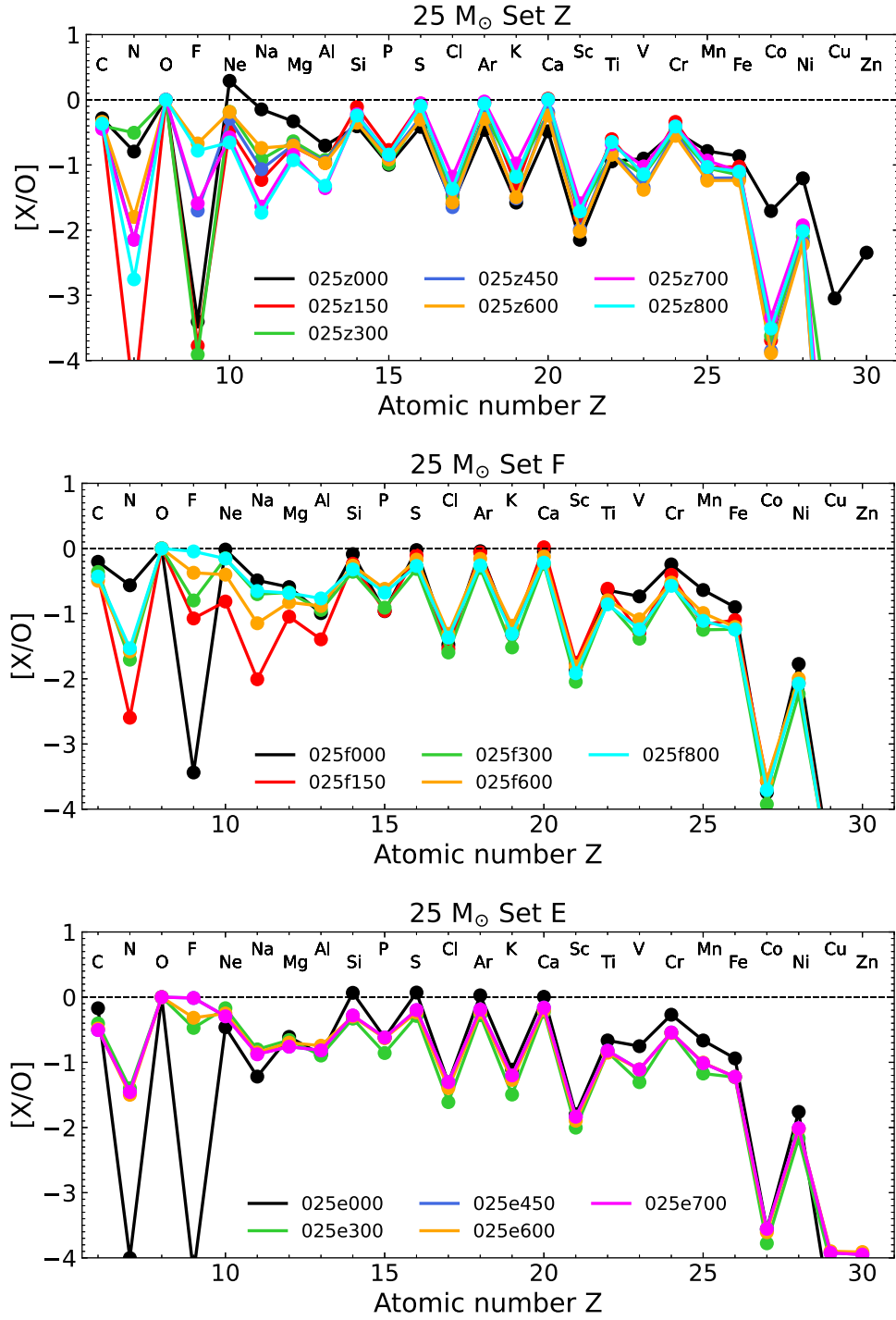


Figure 28. Same as Figure 27, but for the $25 M_{\odot}$ models.

than that of O immediately tells us if this element is produced relative to O as it is observed in the Sun or not. Figures 27 and 28 show the $[X/O]$ of the elements in the range C to Zn for all the models computed in the present work: they refer to the $15 M_{\odot}$ and $25 M_{\odot}$, respectively, while the three rows of each figure refer to Sets Z (upper panels), F (middle panels), and E (lower panels). The various colors refer to the different initial rotation velocities. The $[X/O]$ of all the nonrotating models (black dots and lines) show the well-known odd–even effect typical of the very metal-poor stars, i.e., the even nuclei (Mg to Ca) are produced approximately in right amounts with respect to O while the odd nuclei are more or less underproduced (N to K). Let us look at

the $25 M_{\odot}$ first. The three panels in Figure 28 show that only N and F are largely affected by rotation for all three metallicity and that there are rotation velocities for which both $[N/O]$ and $[F/O]$ get quite close to zero, i.e., are basically coproduced with O. The nuclei synthesized by C burning, i.e., Ne, Na, Mg, and Al, show a sizable dependence on rotation in both Sets Z and F, although not as large as N and F, (because the amount of C left by the He burning depends on the velocity) while models of Set E do not. All other nuclei show only a marginal dependence on the initial rotation velocity. If we turn to the $15 M_{\odot}$, the situation is somewhat different. In addition to the odd–even effect that is always present, these models show that in many of the rotating

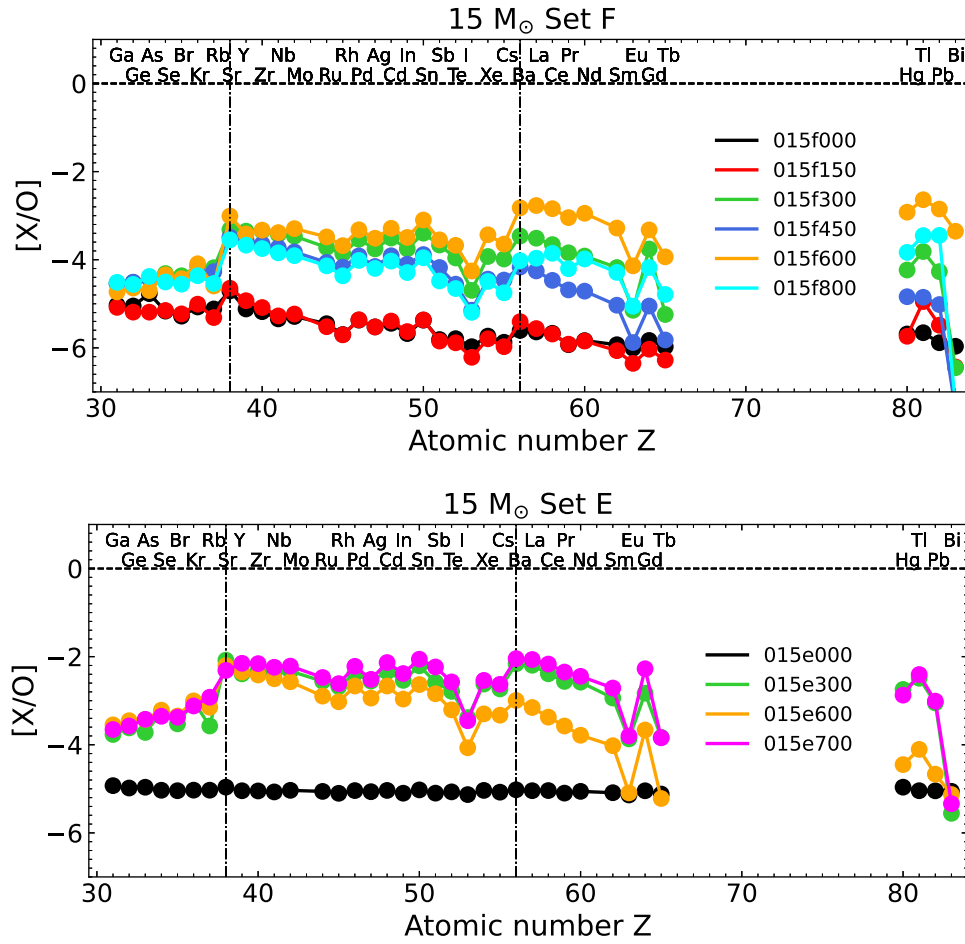


Figure 29. $[X/O]$ distribution for the $15 M_{\odot}$ stellar models for Set F (top panel) and Set E (bottom panel) as a function of the atomic number Z . The two vertical dashed-dotted lines correspond to the atomic number of Sr ($Z = 38$) and Ba ($Z = 56$).

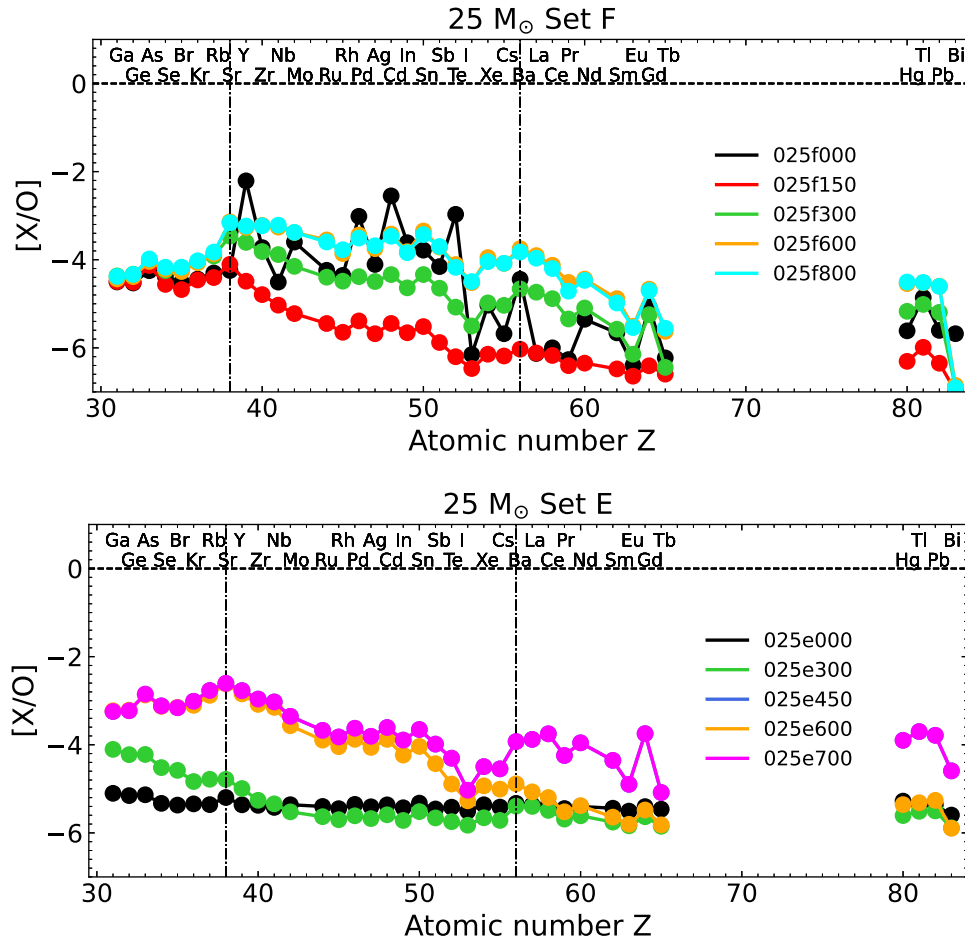
models there is an overproduction of the elements between Si and Ca and an underproduction of the elements Ne to Al, while none of the nonrotating models shows such a feature. Such an apparently strange behavior is the simple consequence of the penetration of the O convective shell in the region where the ashes of the C burning are present (see Section 5) that occurs when a star is in shell O burning. When such a mixing occurs, part of the products of the O burning are brought upward in layers external enough to not be seriously affected by the passage of the shock wave, and, vice versa, products of the C burning are brought internally enough to be destroyed by the passage of the shock wave. The consequence is therefore that the yields of the products of the C burning are reduced while those of the O burning are increased. It is worth noting that such a mixing occurs (in the present set of models) only in the rotating models. The reason is that, how we already discussed above, the rotation leads to smaller amount of C at the end of the He burning and hence a lower amount of Ne in the C exhausted core; a less efficient Ne burning shell does not represent a strong barrier to the advancing of the outer border of the O convective shell so that the O convective shell overcomes the Ne shell and penetrates in the C convective shell.

The $[X/O]$ of the elements Ga to Bi is shown in Figures 29 and 30. Once again, the two figures refer to the 15 and $25 M_{\odot}$, respectively, while the two rows refer to Sets F (top panel) and E (bottom panel). The various colors refer to the different initial rotation velocities. Both $15 M_{\odot}$ models show that rotation

increases significantly the weak, main, and strong component of the neutron capture nucleosynthesis. Let us remind that the elements between Ga and the first neutron closure shell are usually referred to as the weak component; those between the first and the second neutron closure shells are usually named the main component while the nuclei around the third peak are named the strong component. If we consider Sr, Ba, and Pb as the proxies for the three components, we find that $[Sr/O]$ reaches values as high as -3 and -2 in Sets F and E, respectively, as well as Ba and Pb. Of course, while the weak component is easily populated even at the slowest rotation velocities, the main and even more the strong component require much higher rotation velocities. In the case of the $25 M_{\odot}$, we must consider that the nonrotating model experiences the He–H merger, and the large neutron flux determined by the abrupt ingestion of protons within the He-burning region produces a burst of production of heavy nuclei with major peaks at Y, Pd, Cd, and Te. Apart from this specific model, all the others show that once again the first peak around Sr is quite well populated while the second one at Ba remains roughly 1 order of magnitude below that of Sr. It is however remarkable that a nonnegligible amount of mass is able to overcome the neutron magic number $N = 50$ anyway. Only the fastest rotating models are able to raise somewhat the third peak.

7. Comparison with Observations

The plots shown in the previous section are based on the strong argument that O is by far the most reliable reference

Figure 30. Same as Figure 28 but for the $25 M_{\odot}$ models.

element to use as a comparison to evaluate the production of all the others. Unfortunately, O is very difficult to observe at very low metallicity, and therefore, the sample of stars for which the abundance of this element is available is quite scarce. If we want to compare our models with robust observed samples of stars, we are forced to choose another element. We arbitrarily chose Mg, an element for which a large number of observational data is available. Figures 31 and 32 show the $[X/Mg]$ of the elements Ga to Bi for both Sets F and E; because, here, we want to show if and which rotating models of extremely low metallicity can produce enough heavy elements in the range of values observed in a sample of extremely metal-poor stars. We selected observations of EMP stars with $[Fe/H] \leq -3.5$ from JINAbase (Abohalima & Frebel 2018), by obviously requiring that measures of Mg, Sr, and Ba are simultaneously available. These constraints allowed us to select 53 stars (Table 4). Unfortunately, the lack of Pb observations in metal-poor stars did not allow us to analyze also the strong component at such low metallicity.

The upper panel of Figure 33 shows a comparison between the $[Sr/Mg]$ observed in the sample of stars extracted from the database mentioned above and our theoretical predictions. Most of rotating models of both metallicities fit the range of values observed in these stars; hence, even a modest initial rotation velocity is able to raise the weak component up to the observed values. The analogous comparison for $[Ba/Mg]$ (lower panel of Figure 33) shows, on the contrary, that only the

fastest rotating models may fit the range of values observed at a metallicity lower than -4 or so.

If we consider only the models that have both $[Sr/Mg]$ and $[Ba/Mg] > -3$, i.e., above the minimum observed values, we can compare the $[Sr/Ba]$ observed in this sample of stars with the present models. This is an interesting ratio to look at since it is considered a good tracer of the origin of the abundances of these two elements. This ratio in fact changes significantly between the AGB and the massive stars scenarios. A low $[Sr/Ba]$ ratio ($[Sr/Ba] < 0$) is usually associated to the AGB stars because these are the stars in which the main component is predominantly produced, while a high $[Sr/Ba]$ ratio is generally interpreted as a signature of a massive star production because these stars produce primarily the weak component. Figure 34 shows that models having both $[Sr/Mg]$ and $[Ba/Mg] > -3$ also have $[Sr/Ba]$ in the range observed. Most of these models refer to the $15 M_{\odot}$ of both metallicity, while only a couple of fast rotating models of the $25 M_{\odot}$ of Set F meet these requirements. Instead, no $25 M_{\odot}$ of Set E simultaneously shows a $[Sr/Mg]$ and a $[Ba/Mg]$ above -3 . A couple of models are even able to give a $[Sr/Ba] < 0$, i.e., a value usually attributed to the operation of AGB stars.

8. Comparison with Literature Data

As far as we know, there are two papers that address the evolution of rotating massive stars with a network extended enough to follow the neutron capture nucleosynthesis, i.e.,

Table 4
Observations of EMP and UMP Stars with $[\text{Fe}/\text{H}] \leq -3.5$ from JINAbase (Abolima & Frebel 2018)

Number	Star Name	[C/Fe]	[Mg/H]	[Fe/H]	[Sr/H]	[Ba/H]
1	HE0013-0257	0.22	0.68	-3.82	-0.46	-1.16
2	CS22942-002	0.35	0.56	-3.61	-1.73	-1.24
3	CS22183-031	0.37	0.77	-3.57	-0.14	0.20
4	LAMOSTJ0126+0135	-0.51	0.42	-3.57	-1.61	-1.14
5	CS22189-009	0.30	0.44	-3.92	-0.89	-1.52
6	CS22963-004	0.51	0.58	-4.09	-0.95	-0.61
7	CS22172-002	0.09	0.18	-3.86	-1.21	-1.22
8	HE1012-1540	2.40	1.81	-4.17	-0.39	-0.28
9	HE1310-0536	2.36	0.42	-4.15	-1.08	-0.50
10	Boo-1137	0.26	0.45	-3.71	-1.32	-0.55
11	CS22878-101	-0.37	0.60	-3.53	-0.12	-0.37
12	CS22891-200	0.53	0.82	-4.06	-1.18	-0.75
13	CS22885-096	0.60	0.84	-4.41	-1.75	-1.64
14	CS22950-046	0.61	0.58	-4.12	0.10	-1.01
15	CS22897-008	0.60	0.60	-3.83	0.67	-1.17
16	CS29498-043	2.75	1.78	-3.87	0.10	-0.49
17	CS22956-050	0.26	0.67	-3.67	-0.44	-0.90
18	CS22960-053	1.40	0.77	-3.64	-0.01	1.03
19	CS22960-048	0.47	0.72	-3.91	-2.00	-1.59
20	CS22949-048	0.17	0.40	-3.55	-1.20	-1.45
21	CS22949-037	1.16	1.56	-4.38	0.49	-0.60
22	CS22952-015	-0.65	0.30	-3.87	-0.65	-1.50
23	BD+44493	1.20	0.89	-4.28	-0.55	-0.88
24	CS22881-032	<0.77	0.50	-3.55	0.23	-0.30
25	CS22898-047	0.40	0.55	-3.51	-0.14	-0.80
26	CS30339-073	0.20	0.45	-3.93	-1.11	-1.55
27	HE0056-3022	0.25	0.38	-3.77	-0.91	-1.46
28	CD-38245	<-0.19	0.66	-4.59	-0.63	-1.00
29	HE0048-6408	-0.28	0.40	-3.75	-0.82	-1.48
30	HE0057-5959	0.86	0.51	-4.08	-1.06	-0.46
31	HE0302-3417a	0.48	0.55	-3.70	-1.35	-2.10
32	HE1320-2952	<0.52	0.40	-3.69	-0.37	-0.96
33	HE1506-0113	1.47	0.89	-3.54	-0.84	-0.80
34	CS22948-066	-0.43	0.46	-3.50	-0.35	-0.83
35	HE2233-4724	-0.48	0.49	-3.65	-0.77	-1.13
36	HE2302-2154a	0.38	0.28	-3.88	-0.60	-1.50
37	HE2318-1621	0.54	0.20	-3.67	-1.00	-1.61
38	HE2331-7155	1.34	1.20	-3.68	-0.85	-0.90
39	SDSSJ090733.28+024608.1	...	0.36	-3.52	0.04	0.25
40	SDSSJ1322+0123	0.49	0.25	-3.64	-1.24	-1.30
41	SMSS_J004037.56-515025.2	-0.09	0.59	-3.83	-0.99	-1.01
42	SMSS_J005953.98-594329.9	1.20	0.61	-3.93	-1.11	-0.65
43	SMSS_J010651.91-524410.5	0.13	0.56	-3.79	-0.79	-1.64
44	SMSS_J024858.41-684306.4	0.66	0.57	-3.71	-0.15	0.59
45	SMSS_J085924.06-120104.9	-0.20	0.61	-3.63	-1.01	-1.23
46	SMSS_J173823.36-145701.0	0.60	0.44	-3.58	0.02	-0.25
47	SMSS_J184226.25-272602.7	<-0.29	0.62	-3.89	-1.77	-1.27
48	SMSS_J184825.29-305929.7	0.25	0.50	-3.65	-1.52	-1.58
49	HE1116-0634	0.08	0.82	-3.73	-2.26	-1.81
50	HE0218-2738	...	0.04	-3.52	-0.33	-0.05
51	HE0132-2429	0.83	0.39	-3.60	0.13	-0.85
52	HE0926-0546	<0.62	0.32	-3.73	-1.22	-0.83
53	G64-12	<1.10	0.50	-3.58	0.10	-0.27

(This table is available in machine-readable form.)

Frischknecht et al. (2012, 2016). They constitute a homogeneous set of models, computed with the same code and nuclear network: among their models, the only ones that can be reasonably compared to our models are those computed for $[\text{Fe}/\text{H}] = -3.8$, i.e., a $25 M_{\odot}$ computed with the two initial rotation velocity $v_{\text{ini}} = 333$ and 428 km s^{-1} , a $20 M_{\odot}$ with $v_{\text{ini}} = 305 \text{ km s}^{-1}$, and a $15 M_{\odot}$ with $v_{\text{ini}} = 277 \text{ km s}^{-1}$. For

sake of simplicity, these models will be globally referred to as F+16 in the comparison with our models.

Figure 35 compares in the upper panel the sum of the yields (in solar masses) of all the nuclei above the Fe peak irrespective of the heaviest nucleus appreciably synthesized. The two models that can be compared more directly show a quite contradictory result: our $15 M_{\odot}$ produces a much larger amount

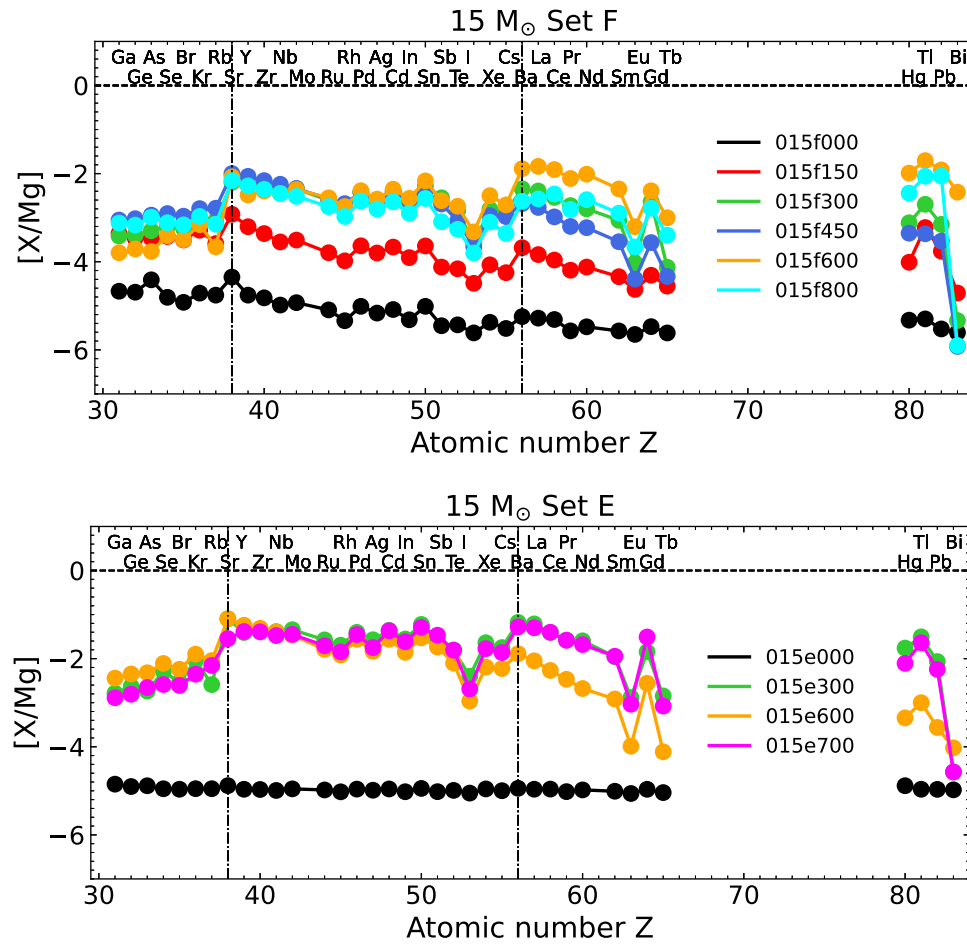
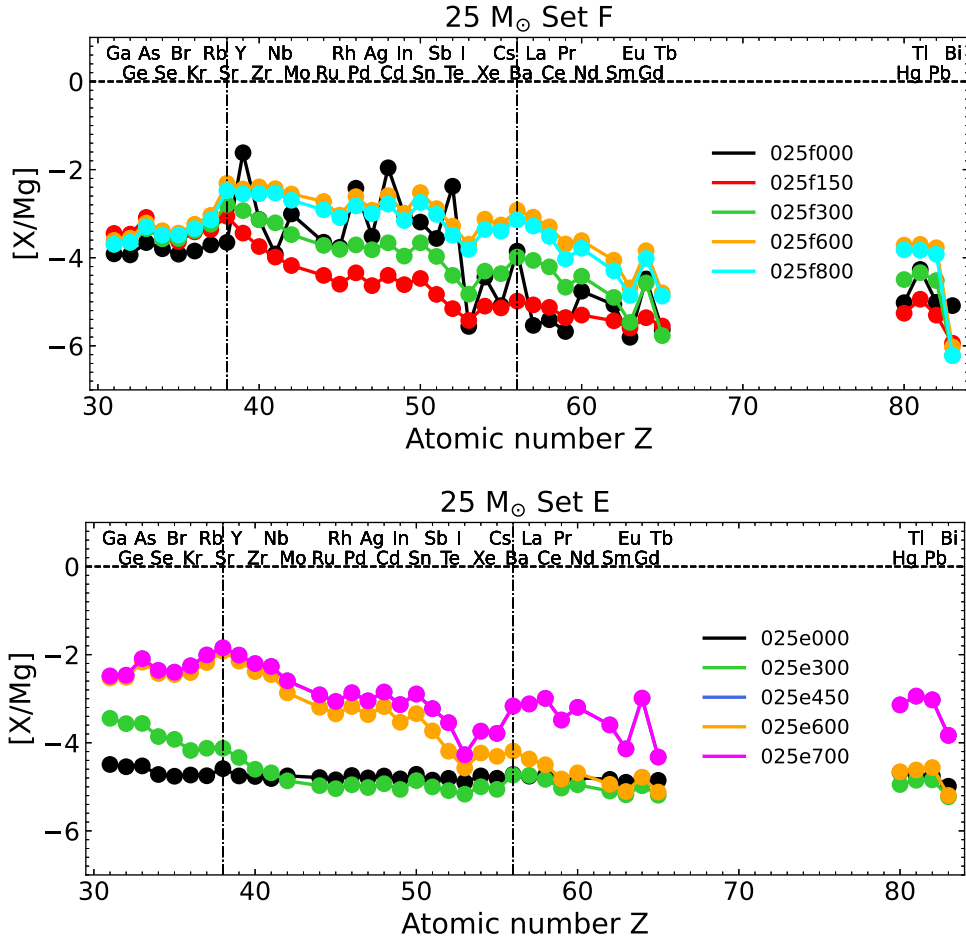


Figure 31. $[X/Mg]$ distribution for the $15 M_{\odot}$ stellar models for Set F (top panel) and Set E (bottom panel) as a function of the atomic number Z . The two vertical dashed-dotted lines correspond to the atomic number of Sr ($Z = 38$) and Ba ($Z = 56$).

of heavy nuclei than the F+16 model, while the two $25 M_{\odot}$ show that the one rotating faster provides yields quite similar to those from ours and that the dependence of the yields on the initial rotation velocity is quite similar. There is not a direct comparison for the $20 M_{\odot}$, but it seems to behave not much different from the $25 M_{\odot}$. On the other hand, its mass is only 20% lower than that of the $25 M_{\odot}$. In order to understand how far the matter flows toward the more massive nuclei, the middle and the lower panels in Figure 35 show a similar comparison but for Sr and Ba. Both figures show a pattern quite similar to that of the upper panel even if our models seem to produce more Ba than the F+16 ones. Figure 36 eventually shows again the same comparison but now for the $[Sr/Ba]$. This figure shows more clearly that we produce more Ba than that from F+16. We will not attempt to interpret the observed discrepancies because there are so many different choices in the computation of the evolution of a star (especially when rotation is taken into account) that our intention is simply that of showing how the results, in this case the yields, differ from one author to another.

There is another point we think to be of interest for the reader. F+16 point out that the main limitation for the synthesis of the elements beyond the Fe peak is that at these low metallicity and high neutron densities (i.e., very high neutron-to-seed ratio) all the Fe seeds are fully destroyed and that the passage from the first neutron shell toward the second one and beyond is the result of the conversion of Sr (that acts as the

main seed) in Ba. We find that it is not the case in our set, even if in many models ^{56}Fe is almost completely destroyed. The reason is that the destruction of ^{56}Fe does not imply necessarily the exhaustion of the seeds because part of the ^{56}Fe nuclei are still locked in nuclei within the Fe peak. To clarify the situation, we show in Figure 37 a small part of the chart of the nuclides that includes the Fe-peak nuclei. The number at the bottom of each nucleus is the (n, γ) nuclear cross section at 300 MK normalized to that of the $^{56}\text{Fe}(n, \gamma)$. The neutron density shown within the symbol of the unstable nuclei is the neutron flux necessary to favor (by a large factor) the neutron capture with respect to the decay. The nuclear cross section on the upper right part of the figure is the neutron capture nuclear cross section on ^{88}Sr . The stellar matter, within the Fe peak, is largely concentrated in ^{56}Fe . The ^{56}Fe destroyed by the neutron capture finds two main obstacles on its path toward Ga (where the neutron capture nuclear cross sections increases by an order of magnitude or more with respect to that on ^{56}Fe). The first one is ^{58}Fe that has a neutron capture nuclear cross section only slightly larger than that on ^{56}Fe , and in the second one, the major one, ^{64}Ni has a neutron capture in the nuclear cross section that is 60% smaller than that on ^{56}Fe . A large fraction of the initial ^{56}Fe populates ^{64}Ni before feeding the neutron capture nucleosynthesis because the branching at ^{63}Ni pushes directly matter either toward ^{64}Ni if the neutron density is higher than $\sim 10^5 \text{ n cm}^{-3}$ or toward ^{63}Cu first and the unstable ^{64}Cu that decays in ^{64}Ni in 60% of the cases and the remaining

Figure 32. Same as Figure 30 but for the $25 M_{\odot}$ models.

40% in ^{64}Zn . In other words, the exhaustion of the ^{56}Fe nuclei does not necessarily imply the exhaustion of the Fe-peak seeds available for the neutron capture nucleosynthesis because there may still be a consistent fraction of matter locked in ^{64}Ni available for the build up of heavy elements.

9. Summary and Conclusions

In this work, we computed 34 full evolutionary models of 15 and $25 M_{\odot}$ stars with the initial equatorial rotation velocity in the range between 0 and 800 km s^{-1} ($0.17 \leq \Omega/\Omega_{\text{crit}} \leq 1$), exploring three different metallicities ($[\text{Fe}/\text{H}] = -\infty, -5, -4$). The aim of this work was to study the physical properties and the nucleosynthesis of zero and very low-metallicity massive stars as a function of the initial rotation velocity, finding, if possible, the minimum metallicity, which allows a significant production of the elements heavier than the Fe-peak elements. The main new results of this work may be summarized as follows:

- (1) Core H burning leaves an abundance of ^{14}N of the order of 10^{-6} by mass fraction in all models of Sets Z and F, irrespective of their initial rotation velocity. This is not the abundance required to sustain the star in H burning (that amounts to a few times 10^{-10} by mass fraction) but corresponds to the amount of ^{12}C synthesized by the 3α in the very late phases of the H burning.
- (2) We find the penetration of the He convective shell in the H-rich mantle in the nonrotating $25 M_{\odot}$ of both Sets Z

and F, a phenomenon that leads to a large production of primary ^{14}N .

- (3) None of the models that reaches the surface critical velocity loses more than $1 M_{\odot}$ in central H burning because of the short timescale in which such a velocity is reached.
- (4) The entanglement between the He and the H burning not only reduces significantly the amount of ^{12}C left by the He burning but also leaves a very large amount of the products of the H and He burning in the radiative region between the CO and the He core masses.
- (5) In several models, the amount of C brought in the H-burning shell is large enough to trigger a convective shell whose temporal shape looks like an eagle's beak in the Kippenhahn diagram. The formation of this convective shell has important consequences on the evolution of the star: among the others, it inhibits its expansion toward a red giant configuration and hence the overcome of the Eddington luminosity.
- (6) All rotating models that sooner or later become red giants while in central He burning, exceed their Eddington luminosity, lose dynamically almost completely their H mantle, and turn therefore again toward a blue compact configuration.
- (7) Rotation reduces drastically the possibility of merging of the He convective shell in the H-rich layers, with the consequence that the ^{14}N production channel connected to this merging is drastically reduced in presence of rotation.
- (8) Rotation, vice versa, favors the C–O shell mergers just before the core collapse (but only in the $15 M_{\odot}$ models). The

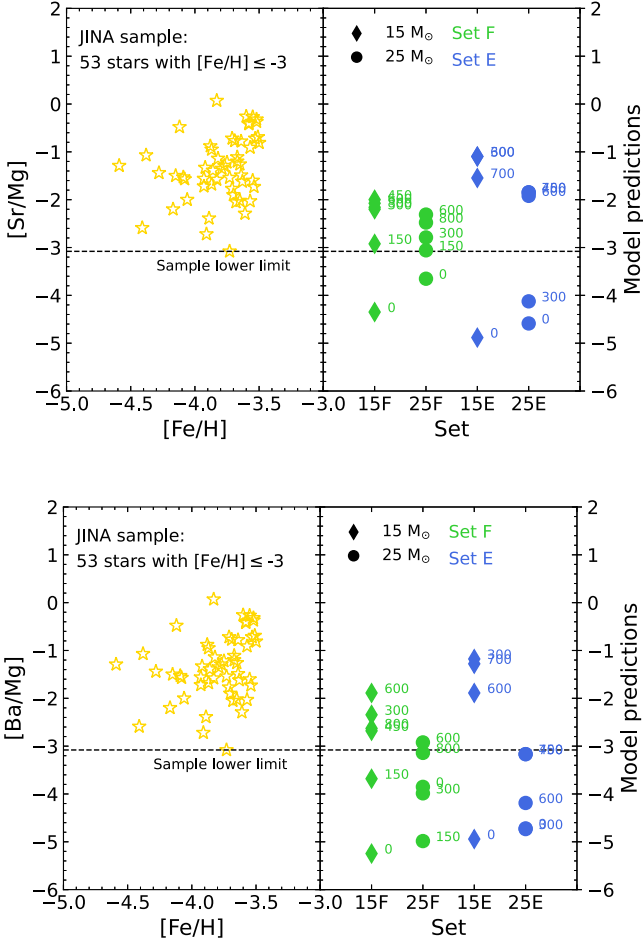


Figure 33. Upper panel: on the left side, the [Sr/Mg] ratio of sample of observations of stars with $[\text{Fe}/\text{H}] \leq -3.5$ taken from JINABase, and on the right side, our theoretical predictions. The horizontal dashed line shows the lowest observed [Sr/Mg] value of the sample. Lower panel: the same but for [Ba/Mg].

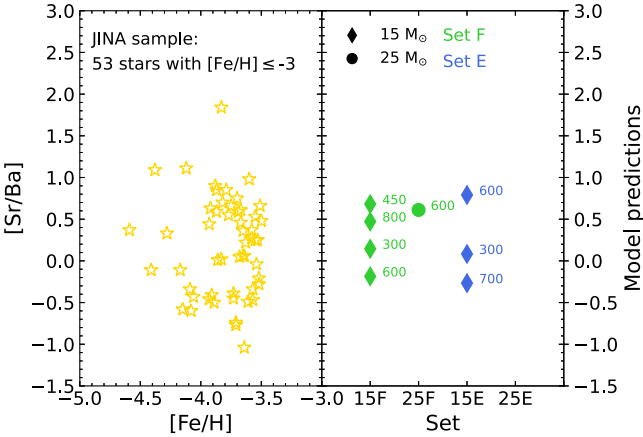


Figure 34. Left: [Sr/Ba] ratios in a sample of observations of stars with $[\text{Fe}/\text{H}] \leq -3.5$ taken from JINABase. Right: our theoretical predictions.

main consequence of such a merging is the increase of the final yields of the products of the O burning, the reduction of the yields of the elements produced by the C burning, as well as an increased photodisintegration of the heavy nuclei produced by the previous n capture nucleosynthesis.

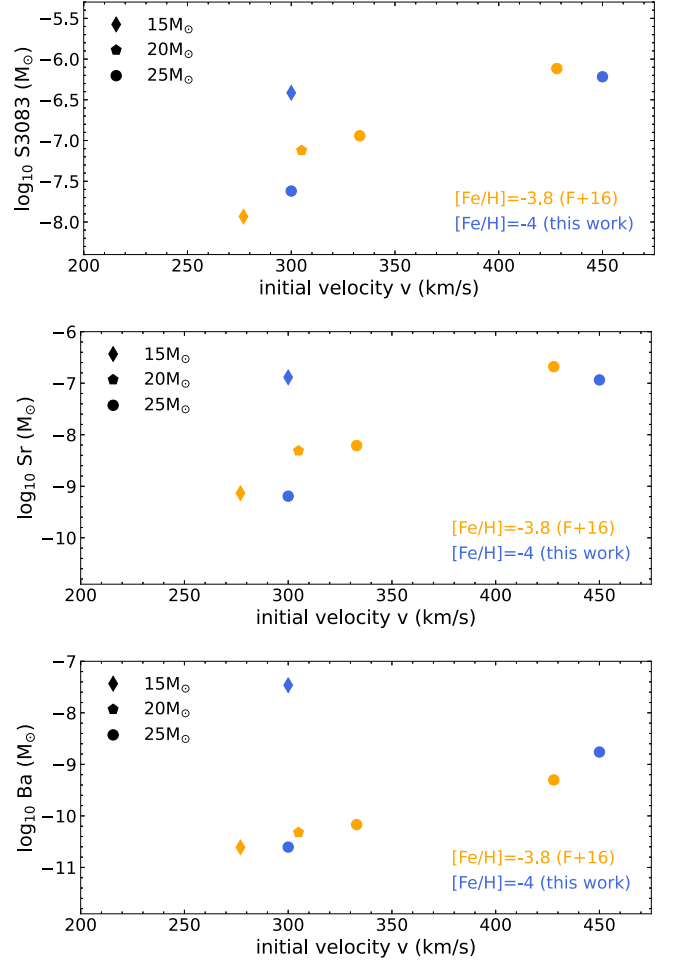


Figure 35. Comparison of the sum of all the yields above Ge between the models computed in this work and the ones presented in Frischknecht et al. (2016) for $[\text{Fe}/\text{H}] = -4$.

- (9) Fluorine is synthesized, as a primary element, in the He convective shell, when it ingests the ^{13}C and ^{14}N present in the CNO pocket left by the entanglement between the He and the H burning. Therefore, its yield scales with the initial rotation velocity.
- (10) The explosion produces iron peak elements as well as intermediate mass elements between Si and Ti. On the contrary, the other elements, i.e., those lighter than Al or heavier than Ni, are very mildly affected by the passage of the shock wave. In particular, the supernova has a negligible effect on the production of the elements heavier than Zn.
- (11) The neutron capture nucleosynthesis leads to a significant overproduction of the elements heavier than Zn in many of the rotating models if the initial velocity exceeds a threshold value that depends both on the initial mass and the initial metallicity. The overabundances are strictly connected to the amount of primary ^{14}N (and hence ^{22}Ne) available in central He burning. A number of models (mostly 15 M_⊙ but also a few 25 M_⊙) produces enough Sr and Ba to fit the range of [Sr/Mg] and [Ba/Mg] observed in a sample of extremely metal-poor stars, already at $[\text{Fe}/\text{H}] = -5$. At zero metallicity, however, the lack of seeds always inhibits an efficient neutron capture nucleosynthesis.

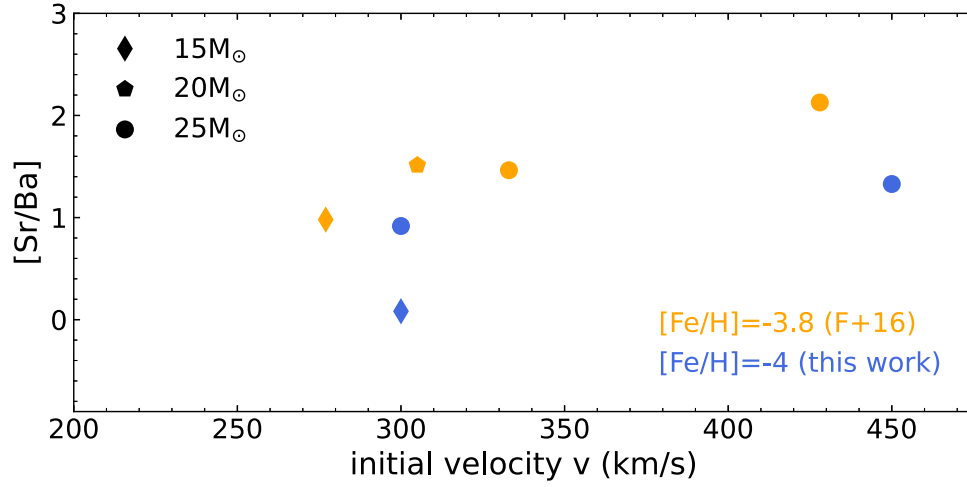


Figure 36. Comparison between the models computed in this work and the ones presented in Frischknecht et al. (2016) for $[\text{Fe}/\text{H}] = -4$.

60Ge ≈ 50 MS	61Ge 39 MS	62Ge 129 MS	63Ge 142 MS	64Ge 63.7 S	65Ge 30.9 S	66Ge 2.26 H	67Ge 18.9 M	68Ge 270.95 D	69Ge 39.05 H	70Ge STABLE 20.37%	71Ge 11.43 D	72Ge STABLE 88Sr 0.6	73Ge STABLE
2P ε	ε 100.00% φ = 80.00%	ε	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%
59Ga	60Ga 70 MS	61Ga 166 MS	62Ga 116.18 MS	63Ga 32.4 S	64Ga 2.627 M	65Ga 15.2 M	66Ga 9.49 H	67Ga 3.2617 D	68Ga 67.71 M	69Ga STABLE 60.108%	70Ga 21.14 M	71Ga STABLE 39.882%	72Ga STABLE 14.095 H
P	ε 96.40% φ = 1.60%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	12.5	β- 99.59% ε 0.41%	11.2	β- 100.00%
58Zn	59Zn 162.0 MS	60Zn 2.35 M	61Zn 89.1 S	62Zn 9.166 H	63Zn 38.47 M	64Zn STABLE 49.63%	65Zn 243.66 D	66Zn STABLE 27.90%	67Zn STABLE 4.10%	68Zn STABLE 18.75%	69Zn 56.4 M	70Zn > 1.3E+16 Y 0.62%	71Zn 2.45 M
ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	5.4	ε 100.00%	3.2	13.9	1.8	6.9	1.9	β- 100.00%
57Cu	58Cu 3.204 S	59Cu 81.5 S	60Cu 23.7 M	61Cu 3.393 H	62Cu 9.67 M	63Cu STABLE 69.17%	64Cu	65Cu STABLE 30.83%	66Cu 5.120 M	67Cu 61.83 H	68Cu 31.1 S	69Cu 2.85 M	70Cu 44.5 S
ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	4 10 ⁹ n/cm ³	22	2.6	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%
56Ni	57Ni 6.075 D	58Ni STABLE 68.077%	59Ni 7.6E+4 Y	60Ni STABLE 26.223%	61Ni STABLE 1.140%	62Ni STABLE 3.634%	63Ni STABLE 0.926%	64Ni	65Ni 2.5172 H	66Ni 54.6 H	67Ni 21 S	68Ni 29 S	69Ni 11.4 S
ε 100.00%	ε 100.00%	3.4	8	2.7	7.4	2.1	2.8	0.7	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%
55Co	56Co 77.233 D	57Co 271.74 D	58Co 70.66 D	59Co STABLE 100%	60Co 1925.28 D	61Co 1.650 H	62Co 1.50 M	63Co 27.4 S	64Co 0.30 S	65Co 1.20 S	66Co 0.16 S	67Co 0.425 S	68Co 0.199 S
ε 100.00%	ε 100.00%	ε 100.00%	ε 100.00%	3.7	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%
54Fe	55Fe STABLE 5.645%	56Fe STABLE 91.754%	57Fe STABLE 2.119%	58Fe STABLE 0.282%	59Fe	60Fe 1.5E+6 Y	61Fe 5.98 M	62Fe 68 S	63Fe 6.1 S	64Fe 2.0 S	65Fe 1.3 S	66Fe 0.44 S	67Fe 0.6 S
2.8	6.9	1	4.1	1.2	2.1	0.5	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%	β- 100.00%
53Mn	54Mn	55Mn	56Mn	57Mn	58Mn	59Mn	60Mn	61Mn	62Mn	63Mn	64Mn	65Mn	66Mn

Figure 37. Nuclide chart.

- (12) A couple of fast rotating models, i.e., the 015f600 and the 015e700, give a $[\text{Sr}/\text{Ba}] < 0$, value usually attributed to the operation of the AGB stars.

We conclude that rotation at zero and very low metallicity may play a crucial role in the early pollution of the interstellar medium, especially for the production of ^{14}N , ^{19}F , and the heavy elements. Of course, the computation of a larger grid of masses is required to investigate the impact of these findings on the early evolution of the Universe. We aim to address this in a future work.

Acknowledgments

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Appendix A The FRANEC Code

In this section, we briefly recall the main relevant features and input physics for this work of the FRANEC evolutionary code. A complete discussion is presented in detail in Chieffi & Limongi (2013) and Limongi & Chieffi (2018). We define the borders of the convective zones according to the Ledoux criterion in H-burning regions, and according to the Schwarzschild criterion elsewhere. We treat semiconvection as discussed in Langer (1991), setting the free parameter to the value $\alpha_{\text{semi}} = 0.02$. This choice allows all the (solar) models to become RSG at the very beginning of core He burning (Chieffi & Limongi 2013). In addition, we assume 0.2 H_p of overshooting at the outer edge of the convective core only during the core H-burning phase. As in Limongi & Chieffi (2018), in the present work, we do not include any thermohaline mixing nor any effect of magnetic fields. The effect of rotation on the structure of the star has been included following the *shellular rotation* approach. The transport of angular momentum due to meridional circulation and shear turbulence

has been treated by means of an advective–diffusive equation (Chaboyer & Zahn 1992; Talon et al. 1997; Limongi & Chieffi 2018). Conversely, the transport of the chemical species has been treated using a pure diffusive approach (Chaboyer & Zahn 1992; Zahn 1992). Note that the meridional circulation dominates the transport of the chemical species and of the angular momentum in the inner part of the radiative mantle, while the secular shear controls the transport in the outer layers (Chieffi & Limongi 2013; Limongi & Chieffi 2018). Since rotation is a multidimensional physical phenomenon, its inclusion in a 1D stellar evolution code implies necessarily a certain number of assumptions. Therefore, the diffusion coefficients that drive both the angular momentum transport and the mixing of the chemicals are intrinsically uncertain and require a proper calibration. Following the procedure of Pinsonneault et al. (1989), Heger et al. (2000), and Brott et al. (2011); Chieffi & Limongi (2013), Limongi & Chieffi (2018) considered two free parameters, namely f_c and f_μ , such that $D_{\text{rot}} = f_c \times (D_{\text{m.c.}} + D_{\text{shear}})$, and $\nabla_\mu^{\text{adopted}} = f_\mu \times \nabla_\mu$. This means that f_c controls the efficiency of the chemical mixing due to rotation, while f_μ regulates the influence of the gradient of the molecular weight on the mixing of both the chemical composition and the angular momentum. They calibrated $f_c = 1.5$, and $f_\mu = 0.01$ in order to reproduce the main trend of the observed surface N enhancements as a function of the rotation velocity in LMC samples of the FLAMES survey (Hunter et al. 2008). In this work, we maintain such a choice. Note that a different calibration of these two parameters, as well as different choices for the convection, semiconvection, and convective boundary mixing, may drastically affect the convective histories of these stars and therefore lead to significantly different results in terms of *s*-process nucleosynthesis and possibly on convective shell mergers in the very latest stages of evolution of massive stars. Mass loss has been

included following the prescriptions of Vink et al. (2000, 2001) for the BSG phase; de Jager et al. (1988), van Loon et al. (2005) for the RSG phase; and Nugis & Lamers (2000) for the Wolf–Rayet phase. In rotating models, mass loss is enhanced following the prescription of Maeder & Meynet (2000):

$$\dot{M}(\Omega) = \dot{M}(\Omega = 0) \times \frac{(1 - \Gamma)^{\frac{1}{\alpha}-1}}{\left[1 - \frac{\Omega^2}{2\pi G \rho_m} - \Gamma\right]^{\frac{1}{\alpha}-1}} \quad (\text{A1})$$

where Ω is the angular rotation velocity, $\Gamma = L_{\text{rad}}/L_{\text{EDD}}$ is the Eddington factor, ρ_m is the density, and α is an empirical force multiplier. For α , we adopted the values presented in Table 1 of Maeder & Meynet (2000). As the metallicity decreases, the mass loss significantly reduces because it scales as $Z/Z_{\text{sol}}^{0.85}$ (Vink et al. 2001) and $Z/Z_{\text{sol}}^{0.50}$ (Maeder 1990). We consider the dynamical mass loss caused by the approach of the luminosity of the star to the Eddington limit ($L_{\text{EDD}} = 4\pi cGM/k$, with k the stellar opacity) by removing all the zones where $\Gamma > 1$. Let us recall that, as it is well known, the luminosity L_{rad} that enters in the Eddington factor Γ is the radiative one and not the total one (Langer 1997). We furthermore include the dynamical mass loss caused by the approach of the angular rotation velocity to the breakout limit. In this latter case, we consider unbound and therefore remove all the mass layers with $\Omega/\Omega_{\text{crit}} > 0.99$.

Appendix B Evolutionary Properties

We present the main properties of the models during the evolution (Table 5) and at the onset of the core collapse (Table 6).

Table 5
Main Evolutionary Properties of $[\text{Fe}/\text{H}] = -\infty, -5, -4$ Models

Phase	Time	M_{CC}	$\text{Log}(T_{\text{eff}})$	$\text{Log}(L/L_{\odot})$	M	M_{He}	M_{CO}	v_{equa}	Ω_{sup}	$\Omega/\Omega_{\text{crit}}$	J_{tot}	H_{sup}	He_{sup}	N_{sup}
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	Mass Fraction	Mass Fraction	Mass Fraction
$15M_{\odot},$ $[\text{Fe}/\text{H}] = -\infty$ 0 km s^{-1}														
MS	6.77(+6)	6.84	4.76	4.47	15.00	0.00	0.00	0.00(+0)	0.00(+0)	0.00(+0)	0.00(+0)	7.55(−1)	2.45(−1)	0.00(+00)
H	1.31(+7)	6.84	4.67	4.77	15.00	3.59	0.00	0.00(+0)	0.00(+0)	0.00(+0)	0.00(+0)	7.55(−1)	2.45(−1)	0.00(+00)
He	6.47(+5)	2.83	4.60	4.86	15.00	4.21	2.82	0.00(+0)	0.00(+0)	0.00(+0)	0.00(+0)	7.55(−1)	2.45(−1)	0.00(+00)
C	3.56(+3)	0.63	4.37	4.83	15.00	4.23	3.01	0.00(+0)	0.00(+0)	0.00(+0)	0.00(+0)	7.55(−1)	2.45(−1)	0.00(+00)
Ne	8.84(−1)	0.79	4.37	4.83	15.00	4.23	2.99	0.00(+0)	0.00(+0)	0.00(+0)	0.00(+0)	7.55(−1)	2.45(−1)	0.00(+00)
O	1.31(+0)	0.97	4.37	4.83	15.00	4.23	2.97	0.00(+0)	0.00(+0)	0.00(+0)	0.00(+0)	7.55(−1)	2.45(−1)	0.00(+00)
Si	1.11(−1)	1.09	4.37	4.83	15.00	4.23	2.96	0.00(+0)	0.00(+0)	0.00(+0)	0.00(+0)	7.55(−1)	2.45(−1)	0.00(+00)
$25M_{\odot},$ $[\text{Fe}/\text{H}] = -4$ 700 km s^{-1}														
MS	6.24(+4)	0.00	4.66	4.79	25.00	0.00	0.00	6.88(+2)	2.34(−4)	8.95(−1)	7.62(−1)	7.55(−1)	2.45(−1)	6.95(−08)
H	9.53(+6)	13.00	4.60	5.40	24.50	9.45	0.00	3.86(+2)	4.90(−5)	8.61(−1)	4.31(−1)	6.32(−1)	3.68(−1)	1.97(−06)
He	6.00(+5)	8.58	3.86	5.57	12.70	12.20	1.58	4.44(−3)	1.65(−1)	1.03(−4)	3.15(−2)	5.01(−1)	4.98(−1)	1.56(−04)
C	2.13(+2)	0.00	4.40	5.66	12.50	12.30	9.51	1.13(−1)	4.63(−9)	7.97(−4)	3.12(−2)	2.87(−1)	7.00(−1)	1.15(−02)
Ne	1.58(−1)	0.43	4.38	5.67	12.50	12.30	9.51	2.89(−1)	1.06(−8)	2.14(−3)	3.12(−2)	2.87(−1)	7.00(−1)	1.15(−02)
O	1.69(−1)	1.35	4.39	5.67	12.50	12.30	9.51	2.94(−1)	1.10(−8)	2.17(−3)	3.12(−2)	2.85(−1)	7.02(−1)	1.19(−02)
Si	1.08(−2)	1.67	4.40	5.67	12.50	12.30	9.51	3.11(−1)	1.21(−8)	2.24(−3)	3.12(−2)	2.83(−1)	7.03(−1)	1.22(−02)

(This table is available in its entirety in machine-readable form.)

Table 6
Physical Properties of the Models at the Onset of the Core Collapse (Psn Model)

v_i (km s ⁻¹)	$\log_{10} T_{\text{eff}}$ (K)	$\log_{10} L/L_{\odot}$	M_{Fe} (M_{\odot})	J_{Fe} (g cm s ⁻¹)	$\xi_{2.5}$ ($M_{\odot}/10^3$ km)	ξ_{CO} ($M_{\odot}/10^3$ km)
Set Z, $Z = 0$						
15 M_{\odot}						
0	4.37	4.83	1.07	...	0.13	0.07
150	3.67	5.15	1.35	2.33(+49)	0.24	0.09
300	4.70	5.25	1.53	4.48(+49)	0.31	0.12
450	4.93	5.27	1.73	6.74(+49)	0.40	0.15
600	4.51	5.24	1.54	4.60(+49)	0.32	0.13
700	5.07	5.22	1.61	6.34(+49)	0.34	0.14
800	5.10	5.23	1.67	6.27(+49)	0.30	0.11
25 M_{\odot}						
0	4.46	5.20	1.18	...	0.12	0.06
150	4.14	5.41	1.37	1.90(+49)	0.29	0.11
300	4.32	5.13	1.38	2.70(+49)	0.32	0.13
450	3.67	5.58	1.39	3.04(+49)	0.39	0.12
600	4.58	5.64	1.48	3.71(+49)	0.39	0.12
700	4.25	5.54	1.35	3.21(+49)	0.53	0.17
800	4.36	5.52	1.43	3.19(+49)	0.50	0.16
Set F, $[\text{Fe}/\text{H}] = -5$						
15 M_{\odot}						
0	3.79	4.57	1.01	...	0.18	0.08
150	4.43	5.16	1.53	3.77(+49)	0.28	0.09
300	3.67	5.18	1.72	6.22(+49)	0.30	0.13
450	4.23	5.10	1.56	4.32(+49)	0.28	0.12
600	3.67	5.24	1.54	5.11(+49)	0.30	0.13
800	4.32	5.21	1.55	3.91(+49)	0.31	0.11
25 M_{\odot}						
0	4.74	4.88	1.41	...	0.31	0.11
150	3.88	5.39	1.62	4.37(+49)	0.49	0.16
300	4.66	5.65	1.62	4.34(+49)	0.38	0.12
600	4.37	5.65	1.87	6.54(+49)	0.57	0.14
800	4.47	5.67	1.75	5.99(+49)	0.43	0.13
Set E, $[\text{Fe}/\text{H}] = -4$						
15 M_{\odot}						
0	3.67	5.05	1.27	...	0.14	0.07
300	4.41	5.22	1.77	6.97(+49)	0.32	0.13
600	3.68	5.21	1.73	5.97(+49)	0.31	0.13
700	3.68	5.24	1.65	5.52(+49)	0.31	0.13
25 M_{\odot}						
0	3.67	5.44	1.43	...	0.34	0.13
300	4.76	5.64	1.75	5.39(+49)	0.40	0.12
450	4.43	5.67	1.77	5.99(+49)	0.57	0.14
600	4.45	5.66	1.72	5.66(+49)	0.52	0.13
700	4.39	5.67	1.81	6.69(+49)	0.52	0.14

Appendix C

Supernova Properties

We present the main features of the explosion of the models (Table 7).

Table 7
Main Supernova Properties of $[\text{Fe}/\text{H}] = -\infty, -5, -4$ Models

Model	M_{Fe} (M_{\odot})	M_{rem} (M_{\odot})	Explosion Kinetic Energy (foe)
015z000	1.07	1.75	3
015z150	1.35	1.86	3
015z300	1.53	1.99	3
015z450	1.73	2.32	4
015z600	1.54	2.09	4
015z700	1.61	2.04	3
015z800	1.67	2.15	3
015f000	1.01	1.68	5
015f150	1.53	2.49	9
015f300	1.72	2.28	7
015f450	1.56	2.66	9
015f600	1.54	2.69	9
015f800	1.55	3.23	9
015e000	1.27	3.08	9
015e300	1.77	1.71	2
015e600	1.73	1.93	3
015e700	1.65	1.91	3
025z000	1.18	1.90	3
025z150	1.37	1.87	3
025z300	1.38	2.07	3
025z450	1.39	2.13	4
025z600	1.48	3.08	9
025z700	1.35	2.66	9
025z800	1.43	3.14	9
025f000	1.41	2.87	12
025f150	1.62	1.54	1.5
025f300	1.62	1.98	3
025f600	1.87	2.00	3
025f800	1.75	2.07	3
025e000	1.43	2.31	4
025e300	1.75	2.70	9
025e450	1.77	3.15	10
025e600	1.72	2.94	9
025e700	1.81	3.16	10

Appendix D

Tables of Explosive Yields

We present the explosive yields from Set Z (Tables 8 and 9), Set F (Tables 10 and 11), and Set E (Tables 12 and 13).

Table 8
Summary of the Explosive Yields for the 15 M_{\odot} Models at Zero Metallicity

Isotope	Z	A	015z000 (M_{\odot})	015z150 (M_{\odot})	015z450 (M_{\odot})	015z700 (M_{\odot})	015z800 (M_{\odot})
H	1	1	6.9377E+00	5.7716E+00	4.8249E+00	4.2531E+00	4.2634E+00
H2	1	2	6.9934E-17	1.1775E-16	7.6080E-17	7.4622E-17	7.6302E-17
He3	2	3	4.7003E-05	1.6064E-05	6.9627E-06	4.1563E-06	4.2143E-06
He4	2	4	5.0304E+00	4.8150E+00	4.3347E+00	4.4478E+00	4.4204E+00
Li6	3	6	7.3342E-24	3.0079E-22	2.1498E-23	8.2389E-24	1.8664E-23
Li7	3	7	8.8337E-11	2.7036E-12	1.5064E-12	5.6079E-12	6.4483E-12
Be9	4	9	1.3250E-39	1.3122E-39	4.6371E-40	4.6747E-40	5.4374E-33
B10	5	10	2.8963E-22	2.6565E-21	5.1278E-22	3.0037E-23	2.3259E-22
B11	5	11	1.1512E-20	2.6069E-17	1.4468E-18	2.2282E-18	1.0572E-17
C12	6	12	2.2845E-01	3.6602E-01	2.6887E-01	3.9726E-01	5.8994E-01
C13	6	13	1.1121E-08	2.4279E-06	1.1371E-04	7.3141E-04	3.0065E-03

(This table is available in its entirety in machine-readable form.)

Table 9
Summary of the Explosive Yields for the 25 M_{\odot} Models at Zero Metallicity

Isotope	Z	A	025z000 (M_{\odot})	025z150 (M_{\odot})	025z300 (M_{\odot})	025z600 (M_{\odot})	025z800 (M_{\odot})
H	1	1	1.1038E+01	9.5070E+00	8.9251E+00	7.6770E-02	7.5261E+00
H2	1	2	9.7691E-17	2.2546E-16	8.8163E-17	4.4676E-19	8.5274E-17
He3	2	3	2.2449E-05	1.3648E-05	2.8545E-06	2.0871E-09	7.8699E-07
He4	2	4	7.7707E+00	8.0226E+00	6.8354E+00	1.6223E+00	8.5668E+00
Li6	3	6	6.3545E-20	1.0737E-19	1.8910E-20	3.4109E-21	1.4538E-21
Li7	3	7	9.7520E-09	2.2644E-11	3.2323E-08	2.6896E-12	4.4803E-11
Be9	4	9	1.9211E-30	1.3944E-37	4.6855E-32	9.9426E-40	2.2008E-39
B10	5	10	1.6156E-17	3.3247E-19	1.1839E-20	3.4880E-21	2.3027E-20
B11	5	11	3.8122E-13	4.5678E-17	1.1724E-13	2.1378E-17	6.4746E-18
C12	6	12	5.2445E-01	6.0427E-01	7.5239E-01	1.0495E+00	7.3120E-01
C13	6	13	9.6339E-04	1.0051E-05	1.3363E-02	2.0039E-04	5.3721E-06

(This table is available in its entirety in machine-readable form.)

Table 10
Summary of the Explosive Yields for the 15 M_{\odot} Models at $[\text{Fe}/\text{H}] = -5$

Isotope	Z	A	015f000 (M_{\odot})	015f150 (M_{\odot})	015f300 (M_{\odot})	015f450 (M_{\odot})	015f600 (M_{\odot})	015f800 (M_{\odot})
H	1	1	7.0908E+00	5.9400E+00	5.3713E+00	4.7299E+00	4.9347E+00	3.8229E+00
H2	1	2	4.4549E-06	1.1907E-10	1.1904E-10	1.1684E-10	1.2014E-10	1.3193E-10
He3	2	3	1.2263E-04	4.2956E-05	1.9056E-05	3.5541E-06	7.3833E-06	4.8993E-06
He4	2	4	4.7552E+00	4.6562E+00	4.4978E+00	5.4257E+00	4.4629E+00	6.0950E+00
Li6	3	6	2.0192E-11	1.1435E-14	5.3749E-15	3.9364E-15	5.0802E-15	1.5986E-12
Li7	3	7	2.8931E-10	1.7239E-12	1.0669E-11	1.5417E-10	4.6503E-13	7.8107E-11
Be9	4	9	2.4046E-14	2.1815E-17	9.8170E-18	6.9375E-18	8.3584E-18	3.0691E-15
B10	5	10	1.1109E-13	1.2629E-16	5.5972E-17	3.9325E-17	4.6223E-17	1.4998E-14
B11	5	11	1.8565E-12	3.1724E-14	6.4675E-16	4.9734E-16	5.0253E-16	7.8128E-14
C12	6	12	2.7146E-01	2.8086E-01	3.2330E-01	3.4313E-01	4.3962E-01	3.0305E-01
C13	6	13	2.6925E-08	1.7882E-05	1.8461E-04	6.6015E-06	9.3410E-05	1.3624E-06

(This table is available in its entirety in machine-readable form.)

Table 11
Summary of the Explosive Yields for the 25 M_{\odot} Models at $[\text{Fe}/\text{H}] = -5$

Isotope	Z	A	025f000 (M_{\odot})	025f150 (M_{\odot})	025f300 (M_{\odot})	025f600 (M_{\odot})	025f800 (M_{\odot})
H	1	1	1.0479E+01	9.2190E+00	8.2383E+00	8.2848E+00	8.0325E+00
H2	1	2	5.2687E-08	2.8238E-10	2.8418E-10	2.8786E-10	2.8419E-10
He3	2	3	1.5036E-04	2.8950E-05	6.1156E-06	6.6427E-06	7.5860E-06
He4	2	4	7.7320E+00	7.2501E+00	5.9065E+00	6.1575E+00	5.7309E+00
Li6	3	6	2.3880E-13	4.5468E-15	2.9703E-15	3.5637E-15	9.9245E-13
Li7	3	7	1.3589E-07	2.2726E-10	4.1190E-12	2.0164E-12	1.9723E-11
Be9	4	9	2.8437E-16	7.6964E-18	4.6601E-18	5.5784E-18	1.4387E-15
B10	5	10	1.3149E-15	4.2812E-17	2.5105E-17	3.0138E-17	7.0210E-15
B11	5	11	2.7589E-12	6.8296E-15	2.6443E-16	3.1154E-16	5.4293E-14
C12	6	12	6.7443E-01	6.3049E-01	1.0028E+00	7.1193E-01	8.8205E-01
C13	6	13	1.8463E-02	2.7189E-05	1.4493E-04	5.8292E-05	6.2138E-05

(This table is available in its entirety in machine-readable form.)

Table 12
Summary of the Explosive Yields for the 15 M_{\odot} Models at $[\text{Fe}/\text{H}] = -4$

Isotope	Z	A	015e000 (M_{\odot})	015e300 (M_{\odot})	015e600 (M_{\odot})	015e700 (M_{\odot})
H	1	1	6.9414E+00	5.1828E+00	4.6574E+00	4.4780E+00
H2	1	2	8.3378E-07	3.8771E-10	3.9043E-10	3.9094E-10
He3	2	3	1.6574E-04	2.8955E-05	5.9298E-06	8.4794E-06
He4	2	4	4.7321E+00	4.3088E+00	5.0540E+00	5.1361E+00
Li6	3	6	3.7789E-12	1.7679E-14	2.0799E-14	1.7093E-12
Li7	3	7	5.4203E-11	5.6861E-13	1.0967E-11	9.5385E-11
Be9	4	9	4.5002E-15	3.6244E-17	3.5223E-17	2.9501E-15
B10	5	10	2.0880E-14	2.1717E-16	1.9372E-16	1.4500E-14
B11	5	11	2.3427E-12	2.7624E-15	3.0723E-15	9.5753E-14
C12	6	12	2.3567E-01	3.1451E-01	3.9399E-01	3.6063E-01
C13	6	13	7.6166E-08	1.1131E-04	6.0284E-04	2.1025E-04




(This table is available in its entirety in machine-readable form.)

Table 13
Summary of the Explosive Yields for the 25 M_{\odot} Models at $[\text{Fe}/\text{H}] = -4$

Isotope	Z	A	025e000 (M_{\odot})	025e300 (M_{\odot})	025e450 (M_{\odot})	025e600 (M_{\odot})	025e700 (M_{\odot})
H	1	1	1.0232E+01	8.1114E+00	8.0705E+00	8.1749E+00	7.6932E+00
H2	1	2	7.4351E-06	9.0561E-10	9.1666E-10	9.1669E-10	9.0865E-10
He3	2	3	1.9231E-04	7.9284E-06	5.7955E-06	5.9342E-06	6.3600E-06
He4	2	4	7.5529E+00	6.2019E+00	5.9278E+00	5.9217E+00	6.3052E+00
Li6	3	6	3.3703E-11	1.6474E-14	1.4323E-14	2.2375E-14	1.4779E-13
Li7	3	7	4.8513E-10	8.4690E-12	5.3097E-12	2.7903E-12	1.7102E-11
Be9	4	9	4.0136E-14	2.7583E-17	2.4212E-17	3.7528E-17	2.2978E-16
B10	5	10	1.8547E-13	1.5280E-16	1.3568E-16	2.0845E-16	1.2422E-15
B11	5	11	3.8557E-12	1.5819E-15	1.5446E-15	2.3294E-15	2.2272E-14
C12	6	12	8.3501E-01	8.9375E-01	7.2727E-01	7.6615E-01	7.2707E-01
C13	6	13	8.5519E-07	2.2296E-04	5.6759E-05	5.6921E-05	5.6802E-05
...		

(This table is available in its entirety in machine-readable form.)

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