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H₂O distribution in the disc of HD 100546 and HD 163296: the role of dust dynamics and planet–disc interaction

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ABSTRACT

Water plays a fundamental role in the formation of planets and their atmospheres. Far-infrared observations with the *Herschel* Space Observatory revealed a surprisingly low abundance of cold-water reservoirs in protoplanetary discs. On the other hand, a handful of discs show emission of hot water transitions excited at temperatures above a few hundred Kelvin. In particular, the protoplanetary discs around the Herbig Ae stars HD 100546 and HD 163296 show opposite trends in terms of cold versus hot water emission: in the first case, the ground-state transitions are detected and the high-*J* lines are undetected, while the trend is opposite in HD 163296. As the different transitions arise from different regions of the disc, it is possible to address the overall distribution of water molecules throughout the disc. We performed a detailed spectral analysis using the thermo-chemical model DALI. We find that HD 163296 is characterised by a water-rich (abundance $\geq 10^{-5}$) hot inner disc (within the snow line) and a water-poor ($< 10^{-10}$) outer disc: the relative abundance of water molecules in the hot inner region may be due to the thermal desorption of icy grains that have migrated inward. Remarkably, the size of the H₂O emitting region corresponds to a narrow dust gap visible in the millimeter continuum at $r = 10$ au observed with the Atacama Large Millimetre Array (ALMA). This spatial coincidence may be due to pebble growth at the border of the snow line. The low-*J* lines detected in HD 100546 instead imply an abundance of a few 10^{-9} in the cold outer disc (> 40 au). The emitting region of the cold H₂O transitions is spatially coincident with that of the H₂O ice previously seen in the near-infrared. Notably, millimetre observations with ALMA reveal the presence of a large dust gap between nearly 40 and 150 au, likely opened by a massive embedded protoplanet. In both discs, we find that the warm molecular layer in the outer region (beyond the snow line) is highly depleted of water molecules, implying an oxygen-poor chemical composition of the gas. We speculate that gas-phase oxygen in the outer disc is readily depleted and its distribution in the disc is tightly coupled to the dynamics of the dust grains.

Key words. protoplanetary disks – planet-disk interactions – astrochemistry – stars: pre-main sequence

1. Introduction

Water is a key element in the physical and chemical evolution of protoplanetary discs and in the formation of planets (e.g. [van Dishoeck et al. 2021](#)). Ro-vibrational and rotational transitions of H₂O and OH in discs have been found by several authors using *Spitzer* (e.g., [Carr & Najita 2008](#); [Salyk et al. 2008](#); [Pontoppidan et al. 2010](#)), *Keck/NIRSPEC* (e.g. [Salyk et al. 2008](#); [Mandell et al. 2008](#); [Doppmann et al. 2011](#)), VLT/CRIRES (e.g., [Fedele et al. 2011](#); [Banzatti et al. 2017](#)), VLT/VISIR ([Pontoppidan et al. 2010](#)), and *Herschel* (e.g., [Hogerheijde et al. 2011](#); [Riviere-Marichalar et al. 2011](#); [Meeus et al. 2012](#); [Fedele et al. 2012, 2013a](#); [Podio et al. 2013](#)). The detection of H₂O and OH triggered intensive modelling campaigns designed to improve our understanding of the origin and abundance of water in discs. Various chemical and physical–chemical models have been developed, including different processes: [Glassgold et al. \(2009\)](#) and [Najita et al. \(2011\)](#) focus on the formation of H₂O in the inner disc and take into account the effect of the energetic radiation (Ultraviolet and X-rays); [Bethell & Bergin \(2009\)](#) and [Ádámkovics et al. \(2014\)](#) included molecular self-shielding to explain the high abundance of H₂O in the inner region of T Tauri discs and the physical–chemical models of [Woitke et al. \(2009\)](#);

[Bruderer et al. \(2012\)](#); [Du & Bergin \(2014\)](#) include gas-phase H₂O formation in the entire disc and in the disc atmosphere including desorption from icy grains.

Observations of multiple transitions of H₂O in protoplanetary discs have the potential to unveil the abundance and distribution of water vapour – both warm and cold – in discs at the time of planet formation, as shown by [Zhang et al. \(2013\)](#) for the disc around TW Hya. These authors find a high concentration of water vapour at $r \sim 4$ au, corresponding to the water condensation front (or snow line). This latter experiment was possible thanks to the combination of low- and high-*J* H₂O transitions from *Herschel* and *Spitzer*.

This paper presents a H₂O ‘line mapping’ of the two Herbig Ae systems where rotational H₂O emission has been detected with *Herschel*, namely HD 100546 and HD 163296. Both discs show substructures (cavities and dust rings) in the dust continuum with ALMA, which may or may not trap icy pebbles in the outer disc that could otherwise drift inward. Our analysis is based on a mixture of H₂O lines targeted with the Photodetector Array Camera and Spectrometer (PACS; [Poglitsch et al. 2010](#)) and the Heterodyne Instrument for the Far Infrared (HIFI; [de Graauw et al. 2010](#)) on *Herschel*. The aim of this paper is to determine the abundance distribution of H₂O vapour in HD 100546 and

HD 163296 by comparing the observed H₂O spectrum to a set of physical–chemical models of discs.

2. Water reservoirs in discs

According to physical–chemical models (e.g. [Woitke et al. 2009](#); [Bruderer et al. 2012](#); [Du & Bergin 2014](#)), there are three main reservoirs of gaseous H₂O in discs:

- s_1 is the inner reservoir (inside the snow line) where H₂O molecules are formed through gas-phase reactions. The high kinetic temperature in this region allows the energy barrier of the radical-H₂ reactions to be overcome (e.g. [Glassgold et al. 2009](#)). At the same time, this reservoir is fully shielded from the ultraviolet (UV) radiation coming from the star, meaning that H₂O molecules are protected from photodissociation. The H₂O abundance in this region can be further enhanced if icy planetesimals migrate inwards through the snow line and H₂O molecules are released via thermal desorption.
- s_2 is the (cold) photodesorption layer in the outer disc where the H₂O vapour is released from the icy grains. The gas temperature in this region is too low (<100 K) and radical H₂ reactions are inhibited, meaning that the H₂O vapour reservoir is only supplied by photodesorption.
- s_3 is the warm reservoir which is located at intermediate layers above the disc midplane and that can extend to several astronomical units (au) from the star. The production of H₂O molecules is driven by gas-phase reactions. UV photons are not fully absorbed and photodissociation of H₂O molecules is relevant in this region: because of this, the amount of H₂O vapour in this layer is also regulated by the self-shielding (e.g. [Bethell & Bergin 2009](#)).

The three H₂O-rich regions are described in Sect. 4. Each region contributes to the H₂O line flux, but while the high- J rotational lines and the ro-vibrational lines arise primarily from reservoirs s_1 and s_3 , the low- J rotational transitions and in particular those connecting to the ground state, are more sensitive to the cold photodesorption layer s_2 .

3. Observations

3.1. PACS spectra

HD 163296 and HD 100546 were observed with *Herschel*/PACS as part of the DIGIT ([Green et al. 2013](#)) and GASPS ([Dent et al. 2013](#)) key programs (Table 1). The PACS spectra used here are from the DIGIT program and the observations are presented in [Fedele et al. \(2012, 2013a\)](#). The spectral window of *Herschel*/PACS (50–200 μ m) includes several rotational H₂O transitions ranging in upper level energy from $E_{\text{up}} = 114$ K ($2_{12}-1_{01}$ at 179.52 μ m) to $E_{\text{up}} = 1552$ K ($9_{18}-9_{09}$ at 62.93 μ m). The fluxes and upper limits of the H₂O transitions are reported in [Fedele et al. \(2012, 2013a\)](#). A number of transitions are detected towards HD 163296 ([Fedele et al. 2012](#); [Meeus et al. 2012](#)), while no H₂O emission is detected in the DIGIT and GASPS programs towards HD 100546 ([Fedele et al. 2013a](#)). The PACS spectrum of HD 100546 was taken early in the mission ([Sturm et al. 2010](#)) and has a lower signal-to-noise ratio (S/N) compared to that of HD 163296. The upper limits reported by [Fedele et al. \(2013a\)](#) are almost an order of magnitude higher than the line fluxes measured for HD 163296.

A deep PACS observation of HD 100546 was executed as part of a calibration program targeting the H₂O transition

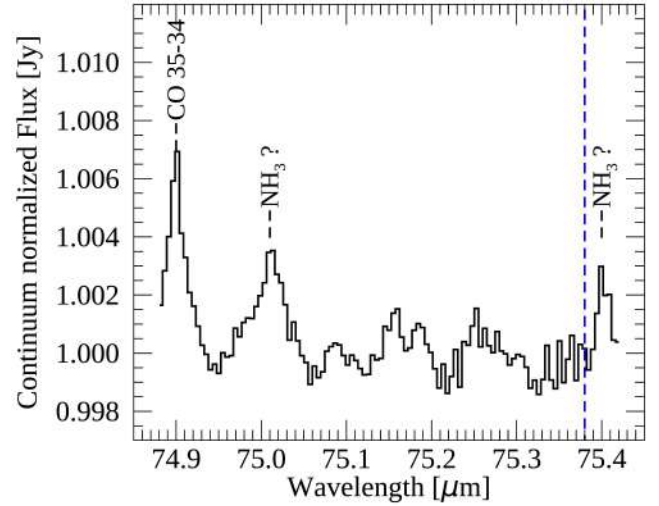


Fig. 1. *Herschel*/PACS deep integration of HD 100546 at 75 μ m. The CO $J = 35-34$ line is detected along with two other emission lines likely due to NH₃. The blue dashed line indicates the position of the H₂O $3_{21}-2_{12}$ transition.

Table 1. Observations log.

Source	Date	Obs ID	PI
HIFI - $1_{10}-1_{01}$			
HD 163296	2012-10-12	1342253130	L. Podio
HD 100546	2011-12-23	1342235094	M. Hogerheijde
HD 100546	2011-12-24	1342235095	M. Hogerheijde
HIFI - $1_{11}-0_{00}$			
HD 163296	2012-10-17	1342253594	M. Hogerheijde
HD 163296	2012-10-18	1342253595	M. Hogerheijde
HD 100546	2012-07-24	1342248515	M. Hogerheijde
HD 100546	2012-12-04	1342256430	M. Hogerheijde
HD 100546	2012-12-27	1342257850	M. Hogerheijde
PACS - $3_{21}-2_{12}$			
HD 100546	2013-02-10	1342263460	Calibration
PACS - Others			
HD 163296	2011-04-03	1342217819	N. Evans
HD 163296	2011-04-03	1342217820	N. Evans
HD 100546	2009-12-11	1342188037	N. Evans
HD 100546	2009-12-11	1342188038	N. Evans

$3_{21}-2_{12}$ at 75.38 μ m. Figure 1 shows the pipeline-reduced spectrum (taken in ‘linespec’ mode). The CO $J = 35-34$ transition at 74.9 μ m is detected along with two other emission lines at 75.01 μ m and 75.41 μ m. These two emission lines could be due to ro-vibrational transitions of NH₃ or SO₂ (further analysis is deferred to a forthcoming paper). Notably, the H₂O $3_{21}-2_{12}$ is not detected. The 3σ upper limit (Table 2) is computed adopting a line FWHM of 0.019 μ m as measured on the CO $J = 35-34$ transition and accounting for the flux calibration error provided by the *Herschel* pipeline.

3.2. HIFI spectra

The H₂O ground state transitions were observed with *Herschel*/HIFI during an open call proposal (Table 1). The line fluxes and upper limits were published by [Du et al. \(2017\)](#). Here we report a new, more stringent upper limit to the $1_{10}-1_{01}$ transition towards

Table 2. H₂O line fluxes.

Transition	λ [μm]	E_{up} [K]	F_{obs} [10^{-17} W m $^{-2}$]	
			HD 163296	HD 100546
1 ₁₀ –1 ₀₁	538.30	61	<0.08	0.10 \pm 0.01
1 ₁₁ –0 ₀₀	269.54	53	<0.49	0.30 \pm 0.02
2 ₂₁ –1 ₁₀	108.07	194	0.7 \pm 0.5	<10.2
3 ₂₁ –2 ₁₂	75.38	305	<2.5	<1.09
4 ₁₄ –3 ₀₃	113.54	324	0.7 \pm 0.4	<7.7
4 ₂₃ –3 ₁₂	78.74	432	1.8 \pm 0.4	<14.7
4 ₃₁ –3 ₂₂	56.31	552	2.7 \pm 1.6	<23.6
7 ₀₇ –6 ₁₆	71.95	843	2.2 \pm 0.5	<11.8
8 ₁₈ –7 ₀₇	63.32	1070	2.0 \pm 0.6	–

Notes. The H₂O 8₁₈–7₀₇ transition in HD 100546 is blended with the [O I] line.

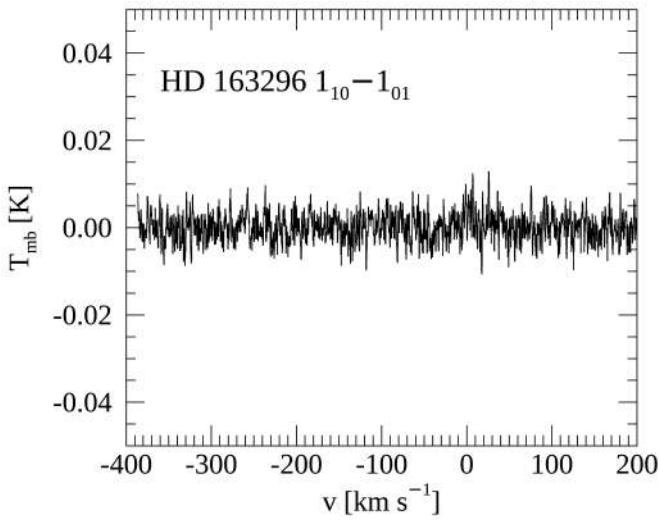


Fig. 2. *Herschel*/HIFI spectrum of HD 163296 1₁₀–1₀₁ (at 556 GHz) at rest-frame velocity.

HD 163296 based on deeper integration (Table 1). We downloaded the level 2 data product from the data archive. The WBS spectrum is converted from antenna temperature to mean-beam temperature after correcting for the beam and forward efficiency (Roelfsema et al. 2012). Finally, the spectra of the horizontal and vertical polarization are averaged together. The reduced and flux-calibrated spectrum is presented in Fig. 2. The ground-state H₂O line remains undetected even in this case. We compute the upper limit and converted from K km s^{−1} to W m^{−2} using the formula

$$\int F_{\nu} d\nu = 2.73 \times 10^{-29} \nu^3 \theta^2 \int T_{\nu} d\nu, \quad (1)$$

where ν is the line frequency (GHz) and θ the half power beam width (arcsec). Following Du et al. (2017), we adopted a line full width at half maximum of 9 km s^{−1} (e.g. Thi et al. 2004), which is similar to the low- J CO lines, and the line upper limits include a 20% flux calibration uncertainty.

4. Analysis

The analysis presented in this paper is based on simulations with the DALI thermo-chemical models of discs (Bruderer et al. 2012; Bruderer 2013).

4.1. Disc physical setup

DALI takes as input the stellar spectrum (in this case corresponding to the blackbody emission at $T = T_{\text{eff}}$) and a power-law surface density structure with an exponential tail:

$$\Sigma_{\text{gas}}(R) = \Sigma_c \left(\frac{R}{R_c} \right)^{-\gamma} \exp \left[- \left(\frac{R}{R_c} \right)^{2-\gamma} \right], \quad (2)$$

where R is the radial distance from the star, R_c the critical radius, and Σ_c is the gas surface density at $R = R_c$. The dust surface density is $\Sigma_{\text{gas}}/\Delta_{\text{gd}}$, where Δ_{gd} is the gas-to-dust-mass ratio. The density in the vertical direction is assumed to follow a Gaussian distribution with scale height $h = H/R$:

$$h = h_c \left(\frac{r}{R_c} \right)^{\psi}, \quad (3)$$

where h_c is the scale height at $R = R_c$ and ψ the flaring angle. The dust grain size distribution is described using two grain size populations as in D’Alessio et al. (2006), and dust mass absorption cross sections from Andrews et al. (2011). The grain size distribution is approximated by a power-law distribution with exponent q (equal for both populations). The settling of the large grains is controlled by the parameters χ (scale height of the large grain population compared to the gas one) and f_{large} (small-to-large grain mass ratio).

DALI solves the 2D dust continuum radiative transfer and determines the dust temperature and radiation field strength at each disc position. In the standard procedure, DALI iteratively solves the gas thermal balance and chemistry. The H₂O spectrum is obtained by computing the non-local thermodynamic equilibrium (NLTE) level populations, including infrared pumping and by fixing the ortho-to-para ratio to 3. The collisional rate coefficients are from the LAMDA database (Schöier et al. 2005, and references therein).

4.1.1. The spectral energy distribution

The goal of this first step is to constrain the disc dust temperature and density gradients using the spectral energy distribution (SED) as an indicator. A reference physical model is obtained from the comparison of the observed SEDs with a grid of synthetic SEDs based on a grid of DALI models.

The initial setup for the parameterisation of HD 163296 is taken from Kama et al. (2020). From the reported disc gas mass of $6.7 \times 10^{-2} M_{\odot}$ we derive a value of $\Sigma_c = 6.8 \text{ g cm}^{-2}$ at $R_c = 125 \text{ au}$, which was obtained by solving the mass integral. The stellar parameters have been changed to $L = 17 L_{\odot}$ and $M = 2 M_{\odot}$, adapted from Vioque et al. (2018). With this setup, a first grid of simulations changing Σ_c , Δ_{gd} , h_c , and ψ was run to determine the disc reference model. The SED is shown in Fig. 3 (lower left panel).

In the case of HD 100546, the initial setup is taken from Kama et al. (2016). The initial values are $\Sigma_c = 18.2 \text{ g cm}^{-2}$ at $R_c = 50 \text{ au}$ and $\Delta_{\text{gd}} = 40$ which yield a total gas mass of $3.2 \times 10^{-2} M_{\odot}$ and total dust mass of $8.1 \times 10^{-4} M_{\odot}$. The Kama et al. (2016) setup was derived using a distance of 97 pc; the stellar and disc parameters were updated to account for the new distance estimate of $d = 108 \text{ pc}$ (Gaia Collaboration 2021). The setup includes an inner dust gap between 4 au and 13 au. Recently, Fedele et al. (2021) reported a new analysis of ALMA 870 μm dust continuum observations that reveals the presence of an outer gap in the disc extending from ~ 40 to $\sim 150 \text{ au}$ (hinted

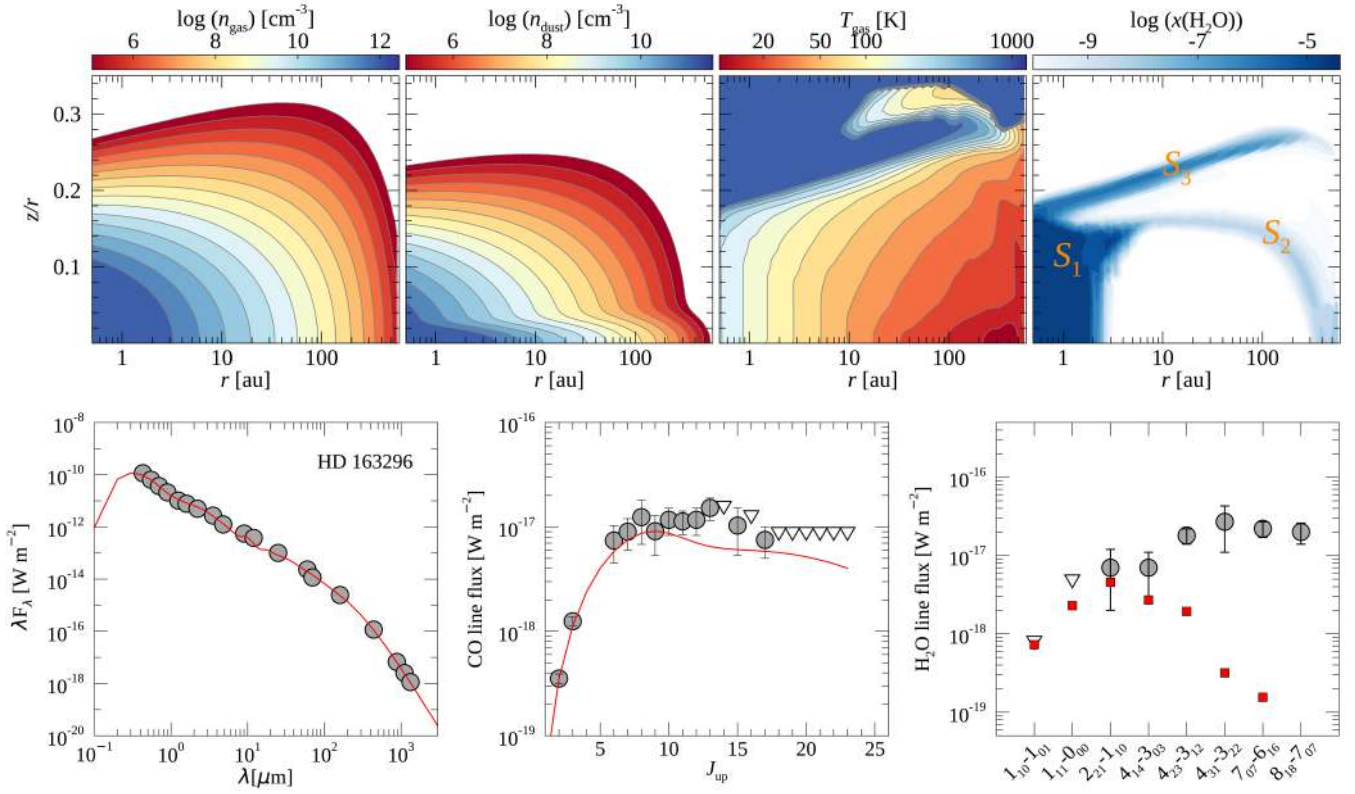


Fig. 3. DALI disc structure for HD 163296. *Top panels:* gas and dust density structure, the gas temperature, and the H₂O abundance structure. The three main H₂O reservoirs are indicated by the labels s_1 , s_2 , and s_3 . *Bottom panels:* model predictions of the SED (*left*), CO ladder (*middle*), and H₂O fluxes (*right*). The observed fluxes and 3σ upper limits are shown as (grey) circles and open triangles, respectively. The representative model shown as a red line and red squares) reproduces the SED (*left*) and the CO rotational ladder (*middle*) well but is not able to reproduce the H₂O line fluxes and upper limits. We note that the H₂O abundances shown here are those of the representative disc model based on the full gas-grain chemistry calculation.

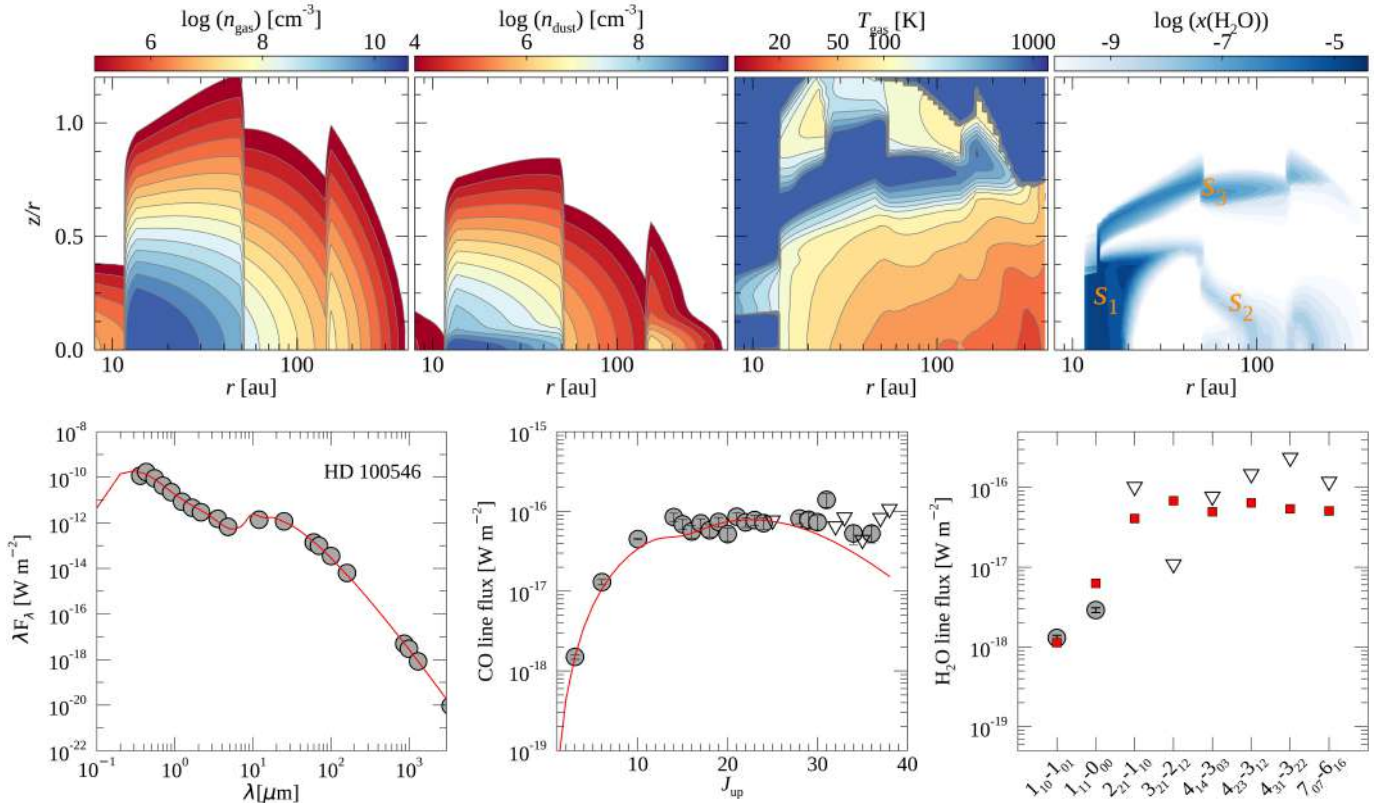


Fig. 4. Same as Fig. 3 but for HD 100546.

Table 3. DALI model parameters.

Parameter	Unit	HD 163296	HD 100546	Description
M_\star	$[M_\odot]$	2.0	2.5	Stellar mass
T_{eff}	[K]	9000	10 500	Stellar (blackbody) temperature
L_{bol}	$[L_\odot]$	17	28	Stellar luminosity
Σ_c	$[\text{g cm}^{-2}]$	1.55	18	Σ_{gas} at R_c
Δ_{gd}		30	90	Gas-to-dust mass ratio
ψ		0.10	0.23	Flaring angle
h_c	[radians]	0.07	0.18	Scale height at R_c
γ		0.9	1	Power-law exponent of $\Sigma(r)$
R_c	[au]	125	50	Critical radius
R_{in}	[au]	0.35	0.25	Dust inner radius
R_{out}	[au]	600	400	Disc outer radius
M_{gas}	$[10^{-2} \times M_\odot]$	1.54	1.57	Disc gas mass
M_{dust}	$[10^{-4} \times M_\odot]$	5.15	1.68	Disc dust mass
χ			0.2	Degree of settling
f_{large}			0.85	Large-to-small dust mass ratio
a_{min}	$[\mu\text{m}]$	0.02	0.05	Minimum grain size
q		3.0	3.5	Power-law exponent of grain size population
PAHs	[%]	0.01	1.0	PAH abundance in gas with respect to the ISM
$R_{\text{cav,in}} - R_{\text{cav,out}}$	[au]		4.0–13.0	Dust cavity
$\delta_{\text{gas,cav}}$			10^{-5}	Gas density drop for $R_{\text{cav,in}} < R < R_{\text{cav,out}}$
$\delta_{\text{small,cav}}$			10^{-5}	Small dust density drop for $R_{\text{cav,in}} < R < R_{\text{cav,out}}$
$\delta_{\text{large,cav}}$			0	Large dust density drop for $R_{\text{cav,in}} < R < R_{\text{cav,out}}$
$R_{\text{gap,in}} - R_{\text{gap,out}}$	[au]		50–150	Dust gap
$\delta_{\text{gas,gap}}$			10^{-1}	Gas density drop for $R_{\text{gap,in}} < R < R_{\text{gap,out}}$
$\delta_{\text{small,gap}}$			10^{-1}	Small dust density drop for $R_{\text{gap,in}} < R < R_{\text{gap,out}}$
$\delta_{\text{large,gap}}$			0	Large dust density drop for $R_{\text{gap,in}} < R < R_{\text{gap,out}}$

at by Walsh et al. 2014) that divides the disc inner bright ring, centred at nearly 28 au, and the disc outer faint ring, centred at ~ 200 au. To reproduce the observed double-ring structure, the density structure was modified using different scaling factors (δ) for the gas and the small and the large dust grains to reduce the densities in the inner dust cavity and in the outer gap:

$$n_i = \begin{cases} n_i \times \delta_{i,\text{cav}} & \text{if } R_{\text{cav,in}} < R < R_{\text{cav,out}} \\ n_i & \text{if } R_{\text{cav,out}} \leq R \leq R_{\text{gap,in}} \\ n_i \times \delta_{i,\text{gap}} & \text{if } R_{\text{gap,in}} < R < R_{\text{gap,out}} \\ n_i & \text{if } r \geq R_{\text{gap,out}} \end{cases} \quad (4)$$

where $i = \text{gas, small grains, large grains}$. The values of all the δ factors are reported in Table 3, while the obtained gas and dust densities are shown in the top left panels of Fig. 4. The small dust grains are assumed to be dynamically coupled to the gas, and so we impose $\delta_{\text{gas}} = \delta_{\text{small}}$ at every radius, while $\delta_{\text{large,cav}} = \delta_{\text{large,gap}} = 0$ to clear the inner cavity and the outer gap from the large dust grains. ALMA observations of CO isotopologues suggest a gas density drop of one order of magnitude in the outer gap (Booth private communication) and so we reduced the gas density by the same amount. With this density setup, a grid of simulations was created varying Σ_c , Δ_{gd} , h_c , and ψ to match the observed SED.

We note that the disc around HD 163296 is also characterised by dust gaps and rings (e.g. Isella et al. 2016; Andrews et al. 2018), but in contrast to HD 100546, the gaps are relatively narrow and their presence does not seem to affect the H_2O distribution (see discussion further below).

4.1.2. CO rotational ladder

In a second step, we modelled the CO rotational ladder to constrain the 2D gas temperature structure: the fluxes of the optically thick CO rotational transitions are indeed a powerful tool to trace the gas temperature throughout the radial and vertical extent of the disc (Fedele et al. 2013b, 2016). Observational data of the CO rotational emission in HD 163296 are taken from Fedele et al. (2016), while data of HD 100546 are taken from Meeus et al. (2013); van der Wiel et al. (2014); Fedele et al. (2016). The CO collisional rate coefficients are from Yang et al. (2010).

To model the CO rotational ladders, a grid of DALI models was created starting from the parameters that best fit the SED and by changing parameters that mostly affect the gas structure, namely: Σ_c , Δ_{gd} , and ψ . These parameters mostly change the shape of the CO rotational ladder; Σ_c and Δ_{gd} are changed simultaneously to lower the total gas mass, maintaining the disc dust mass at a constant level, thus fixing the shape of the SED. The parameters of the reference models are given in Table 3 and the synthetic CO ladders are presented in Figs. 3 and 4 (middle panels) for the two discs, respectively.

4.2. The H_2O line fluxes

Figures 3 and 4 (lower right panel) show the flux of the H_2O rotational transitions obtained with the reference thermo-chemical models compared to the observational data. The DALI chemical network used here is based on the UMIST06 database (Woodall et al. 2007) and contains ten elements (H, He, C, N, O, Mg, Si, S, Fe, and PAH), 109 species, and 1463 reactions. The chemical network is initialised with atomic abundances, with a carbon-to-oxygen abundance ratio of 0.468.

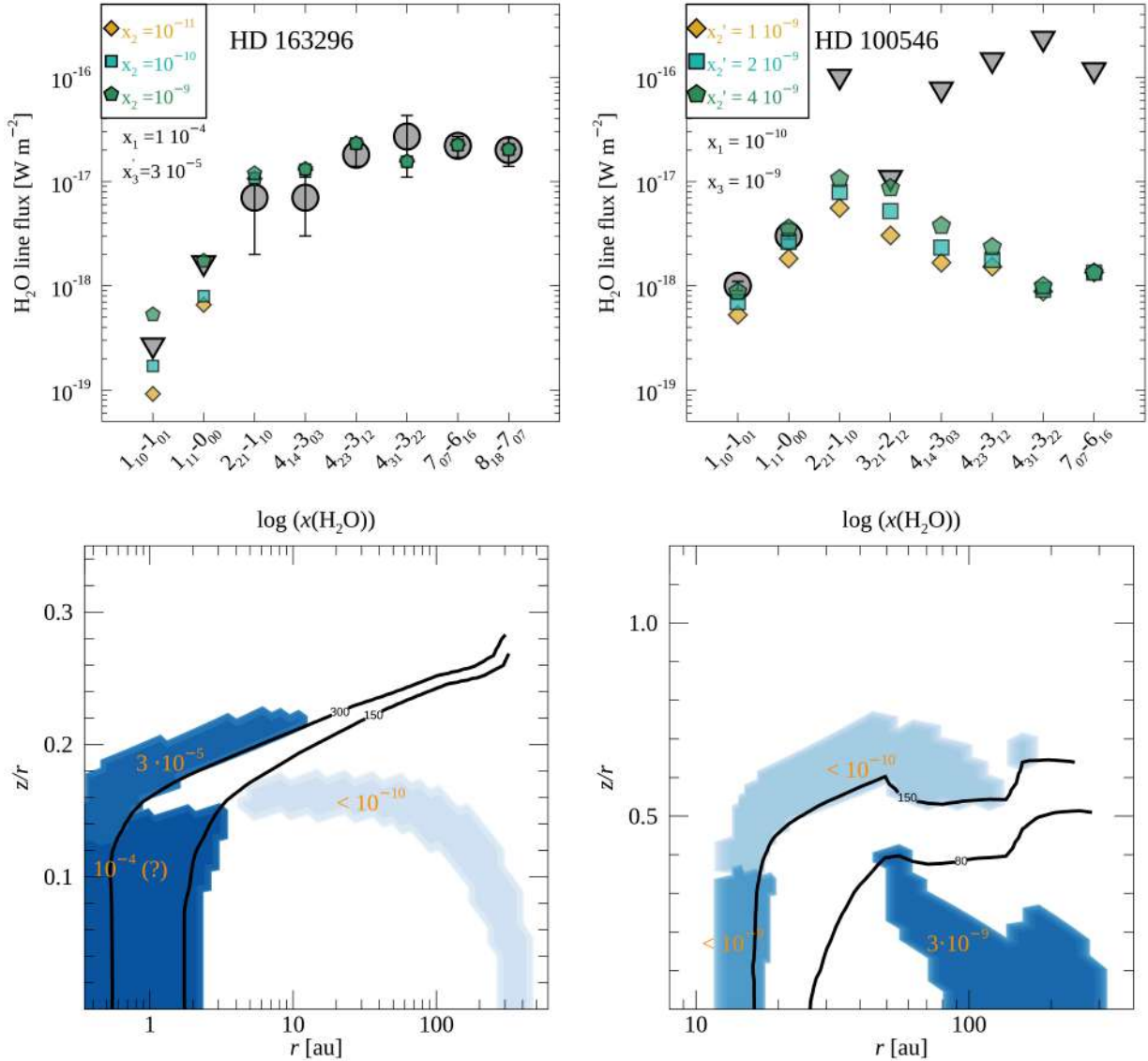


Fig. 5. *Top:* results of the H₂O parametric models: (*left*) HD 163296: the models that best reproduce the observations are those with a low H₂O content in the cold reservoir ($x_3 \leq 10^{-9}$) and with no H₂O in the warm layer beyond the snow line; (*right*) HD 100546: models with $x_2' \sim 2\text{--}4 \times 10^{-9}$ and low values of x_1 ($\leq 10^{-9}$) and x_3 ($\leq 10^{-10}$) match the observed flux of the ground state transitions as well as the upper limit of the high- J lines. *Bottom:* H₂O abundance structure based on the final parametric model showing the three H₂O reservoirs.

In the case of HD 163296, the reference thermo-chemical model (red squares) almost matches the low flux of the ground-state transitions but it underestimates the flux of the excited transitions by up to two orders of magnitude. On the other hand, the HD 100546 reference model predicts an overly strong emission in the 3₂₁–2₁₂ transition, while it almost matches the flux of the ground-state transitions.

The mismatch between the observed and synthetic H₂O line fluxes cannot be due to the global physical properties, such as the density and temperature structures, as these are constrained by the SED and by the CO ladder. Similarly, the discrepancy cannot be ascribed to the global chemical composition or to the initial chemical abundances (such as the carbon/oxygen mass ratio) as in this case all lines would change accordingly. The two opposite trends of the H₂O rotational fluxes are most likely the outcome of a difference in H₂O abundance structure. To verify this hypothesis, we modelled the H₂O line fluxes adopting a parametric abundance distribution rather than a full gas-grain chemistry.

4.2.1. Water abundance parametric distribution

Starting from the dust and gas temperatures derived above, we switched off the chemical solver and the thermal balance modules. This allows us to parametrise the H₂O abundance. The three H₂O reservoirs can be parametrised as follows:

$$x(\text{H}_2\text{O}) = \begin{cases} x_1 & \text{for } T_{\text{dust}} > 150 \text{ K}, n_{\text{gas}} > 10^9 \text{ cm}^{-3} \\ x_2 & \text{for } T_{\text{dust}} < 100 \text{ K}, A_V > 3.0 \text{ mag} \\ x_3 & \text{for } T_{\text{gas}} > 300 \text{ K}, n_{\text{gas}} > 10^6 \text{ cm}^{-3} \end{cases}, \quad (5)$$

where x_1 , x_2 , and x_3 correspond to the H₂O abundance in s_1 , s_2 , and s_3 , respectively. Such a parametrisation is tuned to match the prediction of thermo-chemical models (Figs. 3 and 4). Once the three abundance regions had been defined, we performed a grid of DALI simulations varying the values x_1 , x_2 , and x_3 .

In parallel with the DALI model grid, we investigated the H₂O line flux ratios by performing a set of NLTE simulations with RADEX (van der Tak et al. 2007). This is useful for

checking the trend of different molecular transitions at different densities and temperatures and can be used to properly set the DALI model grid.

4.2.2. H₂O abundance in HD 163296

In the case of HD 163296, the non-detection of the ground-state H₂O transitions points to a low H₂O abundance in the cold photodesorption (s_2) layer. On the other hand, the detection of high- J H₂O lines suggests a medium-to-high abundance in the warm and hot layers. We run an initial grid of models varying x_1 and x_3 (between 10^{-4} – 10^{-8}) and x_2 (10^{-8} – 10^{-12}). The results are reported in Appendix A. In all cases, the models do not match the observed trend. Models with high H₂O abundance ($\geq 10^{-5}$) in s_1 and s_3 almost match the flux of the most energetic transitions (though they still do not match the observations) but these models overestimate the upper limits of the low- J lines independently of the value of x_2 (Fig. A.1). This implies that the warm layer s_3 contributes substantially to the ground-state transitions. Using RADEX we investigated how the physical conditions (gas temperature and density) affect the line flux ratio between the detected mid- J (e.g. 4_{14} – 3_{03}) and undetected low- J (1_{10} – 1_{01}) lines: the line flux ratio increases with increasing gas temperature and decreasing gas density. In particular, we find reasonable agreement with the observed flux ratio lower limit (≥ 10) at $n_{\text{gas}} \geq 10^8 \text{ cm}^{-3}$ and $T_{\text{gas}} \geq 250 \text{ K}$; these conditions are met only in s_1 and in the innermost part of the warm layer s_3 , at $r \lesssim 10 \text{ au}$ within the snow line, right above the hot inner reservoir s_1 . For HD 163296, we therefore modified the parametrisation of x_3 as follows:

$$x(\text{H}_2\text{O}) = x'_3 \text{ for } T_{\text{gas}} > 300 \text{ K}, n_{\text{gas}} > 10^8 \text{ cm}^{-3}, \quad (6)$$

and we performed a new grid of models varying x_1 , x_2 , and x'_3 . Fig. 5 (left panels) shows the grid results: models with $x'_3 \sim 3 \times 10^{-5}$ and $x_2 < 10^{-10}$ are in good agreement with the observed trend. We note that the line fluxes are now insensitive to the value of x_1 , and so the actual abundance in s_1 is unconstrained.

In conclusion, we find that HD 163296 hosts a H₂O-rich inner disc inside the H₂O snow line ($r \sim 5 \text{ AU}$), while the disc outer region is H₂O-poor. The high- J H₂O lines detected by PACS require a warm inner reservoir with a H₂O abundance x'_3 of a few 10^5 . On the contrary, from the non-detection of the low- J H₂O lines, we constrain the H₂O abundance in the photodesorption layer – defined for $3 < A_V < 5$ outside the disc snow line – to be $x_2 < 10^{-9}$ and the H₂O abundance in the disc warm layer to be negligible. Based on the revised parametrisation, we computed the synthetic spectrum of H₂O with DALI. The results are reported in Appendix B.

4.2.3. H₂O abundance in HD 100546

In the case of HD 100546, the detection of the ground-state H₂O lines implies a contribution from the cold photodesorption layer (s_2). Contrary to HD 163296, the high- J transitions in the PACS range remain undetected with flux upper limits of the order of a few $10^{-17} \text{ W m}^{-2}$ (Meeus et al. 2012; Fedele et al. 2013a). The deep PACS observation of the 3_{21} – 2_{12} transition at $75.38 \mu\text{m}$ is an order of magnitude more sensitive than the previous observations and yet the line is not detected. These non-detections suggest a low H₂O abundance in the warm layer of HD 100546. We ran an initial grid of parametric models, varying the H₂O abundance in the three reservoirs in the ranges 10^{-8} – 10^{-12} (in s_1 and s_3) and 10^{-8} – 10^{-10} (in s_2). The results of the model grid are

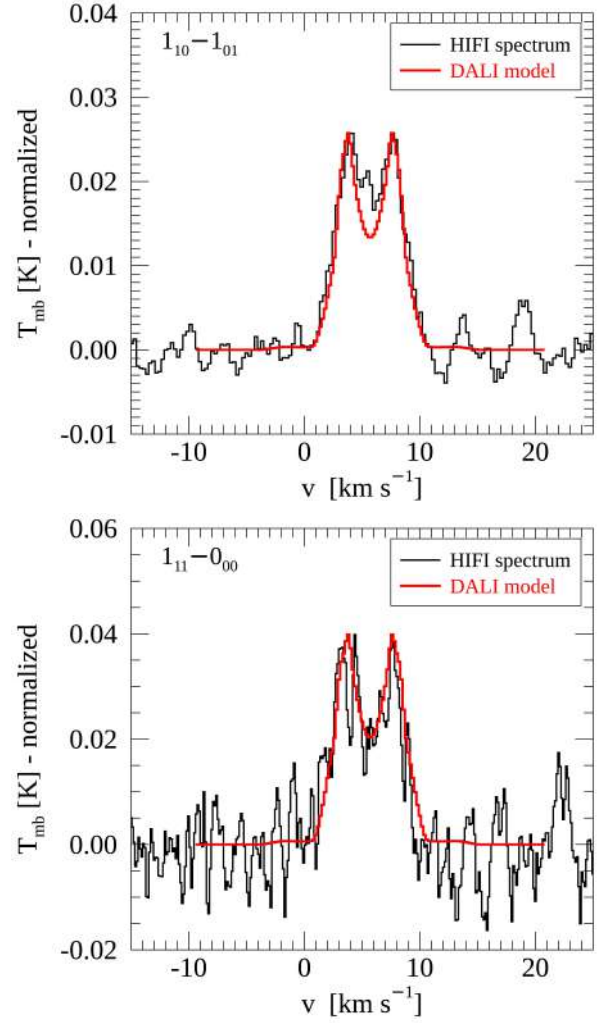


Fig. 6. Velocity profile of the ground-state H₂O lines in HD 100546 and comparison with the DALI model spectrum. The spectra are continuum-subtracted and normalised. The DALI model nicely reproduces the observed profile of both transitions.

shown in Fig. A.2. As expected, the fluxes of the lowest transitions (up to the 3_{21} – 2_{12}) are mostly dominated by the abundance in the cold reservoir, while both s_1 and s_3 contribute to the flux of the high- J lines.

Of key importance is the upper limit of the 3_{21} – 2_{12} transition as all the models in the initial grid overestimate the upper limit (Fig. A.2). Using RADEX, we inspected how the line flux ratios (e.g. 3_{21} – $2_{12}/1_{10}$ – $1_{01} \lesssim 8$) vary with gas temperature and density, and H₂O column density. The only way to match the observed flux ratio is to lower the gas temperature ($\leq 80 \text{ K}$) in the line-emitting region. This imposes a very low abundance in s_3 (otherwise the upper level is easily populated) as its upper layers are known to be warm from the analysis of the CO ladder. Interestingly, the independent analysis of the line velocity profile of the HIFI H₂O spectra allows us to pose a robust constraint on the line-emitting region in the cold reservoir: as reported by van Dishoeck et al. (2021), the ground-state H₂O emission comes from $\sim 40 \text{ au}$ outward. Based on this observational finding, we slightly modified the parametrisation of s_2 to be limited beyond 40 au (equivalent to $T_{\text{dust}} < 80 \text{ K}$):

$$x(\text{H}_2\text{O}) = x'_2 \text{ for } T_{\text{dust}} < 80 \text{ K}, A_V > 3.0 \text{ mag}. \quad (7)$$

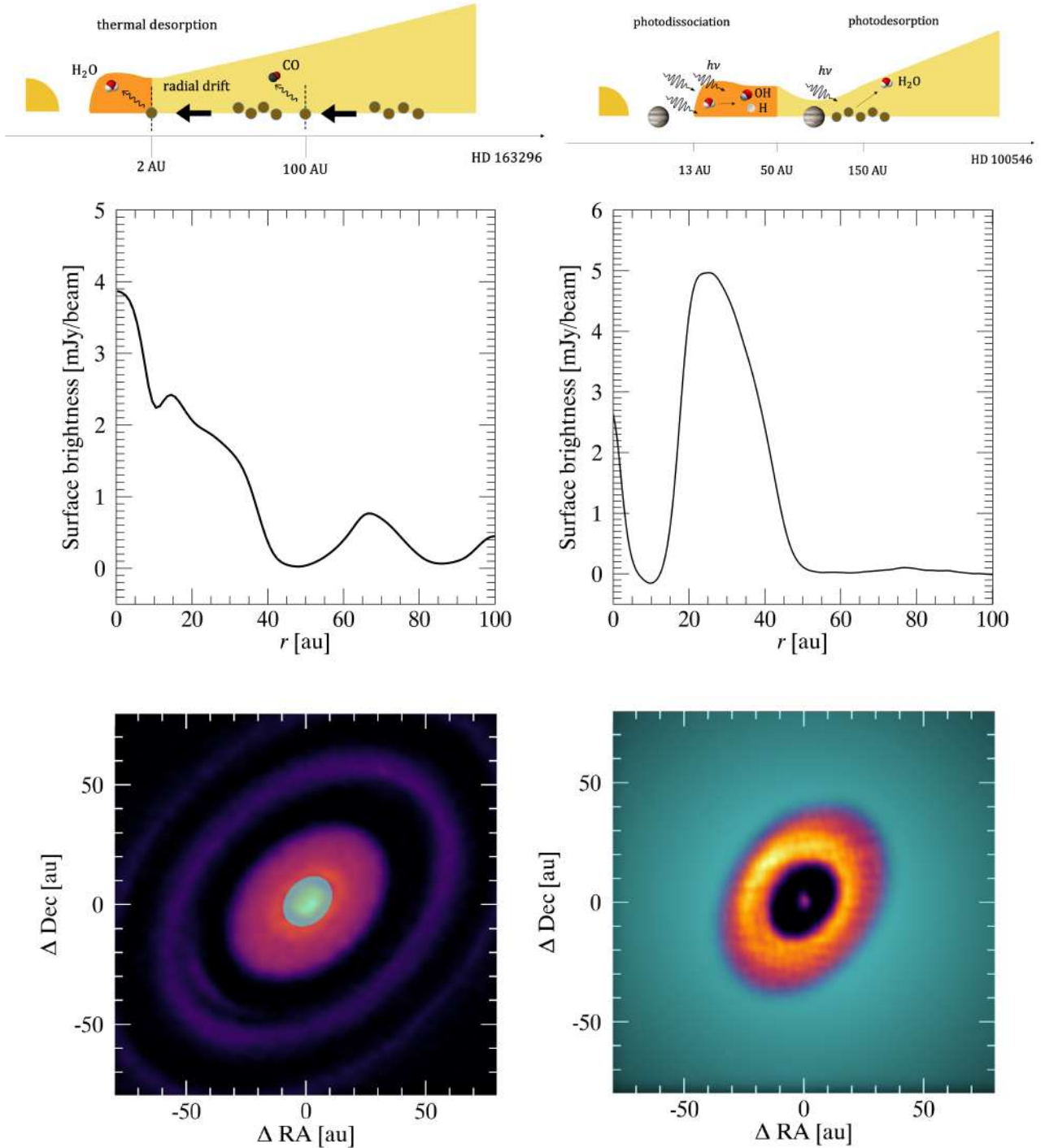


Fig. 7. *Top:* schematic of the H₂O distribution in the two discs. *Middle:* surface brightness profile (azimuthally averaged) of the millimetre dust continuum at 1.2 mm for HD 163296 (from DSHARP survey, [Andrews et al. 2018](#); [Huang et al. 2018](#)) and at 0.87 mm for HD 100546 ([Pineda et al. 2019](#); [Fedele et al. 2021](#)) in the inner 100 au. *Bottom:* water-emitting region (cyan) overlaid on the ALMA dust continuum image. Notably in the case of HD 163296, the size of the H₂O-emitting region corresponds to the narrow dust gap at 10 au. This may be due to dust growth at the border of the snow line.

With this assumption, the models with $x'_2 \sim 3 \times 10^{-9}$ and low values of x_1 ($\leq 10^{-9}$) and x_3 ($\leq 10^{-10}$) are in good agreement with the observational trend (Fig. 5, right). Figure 6 shows the observed and synthetic line velocity profile of the ground-state transitions. The DALI synthetic spectra nicely reproduce the observed line profile. Also, in this case we computed the H₂O spectrum based on the parametrised distribution and the result is shown in Appendix B.

5. Discussion and conclusion

The dichotomy of the gas-phase H₂O abundance structure in HD 163296 and HD 100546 can be explained through the dynamical history of the two discs, which influences their chemistry.

[Banzatti et al. \(2020\)](#) proposed a link between the inner disc chemistry and the migration of solid pebbles for H₂O while [Booth et al. \(2019\)](#) and [Zhang et al. \(2021\)](#) speculate that

the enhanced CO column density in the disc inner 100 au of HD 163296 is due to the inward drift of icy dust particles that release the CO to the gas phase when they cross the CO frost line at $r \approx 100$ au. A similar mechanism might explain the high H₂O abundance within the disc snow line. Notably, a narrow dust gap is visible in the ALMA dust continuum at $r = 10$ au (Fig. 7). This spatial coincidence might be due to dust growth at the border of the snow line as suggested by Zhang et al. (2015) in the case of HL Tau. Further analysis is needed to verify such a hypothesis. In this regard, Notsu et al. (2019) find that we should observe a change in the millimetre dust opacity at the snow line position.

In HD 100546, the H₂O emission region overlaps with a disc outer gap between $r \sim 40$ au and $r \sim 150$ au detected with ALMA at 870 μm (Fedele et al. 2021). Notably, this is spatially coincident with the 3 μm H₂O ice absorption band detected by Honda et al. (2016) that extends from $r \sim 40$ au to $r \sim 120$ au. The high H₂O abundance in the photodesorption layer can be explained through the spatial coincidence of the dust gap and the H₂O-emitting region: the presence of the outer disc gap lets the UV stellar photons penetrate to the colder layers to make H₂O ice sublimate through photodesorption. This is shown in the schematics presented in Fig. 7. This scenario can also explain the origin of the crystalline forsterite emission at 69 μm : the blackbody fitting suggests that the emission arise from dust grains at ~ 70 K at radial distances $r > 50$ au (Sturm et al. 2010). As for the H₂O ice, the crystalline forsterite is directly illuminated by the stellar UV photons that enter in the dust gap.

Interestingly, Booth et al. (2021) report the detection of gas-phase CH₃OH towards HD 100546: contrary to H₂O, the CH₃OH emission peaks in the inner 60 au of the disc and extends out to nearly 300 au. According to Booth et al. (2021), the CH₃OH emission is due to desorption of the primordial ice inherited from the cold dark cloud: in particular, the bulk of the emission from the inner disc is due to thermal desorption mostly from the inner cavity at 13 au, while the spatially extended emission is due to photodesorption, similarly to the scenario proposed here for H₂O.

It is worth noting that the only other disc with a detection of cold gas-phase H₂O, TW Hya (Hogerheijde et al. 2011), also shows CH₃OH emission (Walsh et al. 2016).

The low H₂O abundance in the outer warm molecular layer in both HD 163296 and HD 100546 implies an O-poor molecular layer compared to the standard thermochemical predictions. This is in agreement with the findings of low gas-phase CO abundances and large carbon/oxygen mass ratios observed in several discs (e.g. Bergin et al. 2010; Favre et al. 2013; McClure et al. 2016; Kama et al. 2016; Miotello et al. 2017; Semenov et al. 2018).

In both cases, oxygen in the outer disc is incorporated into dust particles settled to the midplane (e.g. Krijt et al. 2020). In the case of HD 163296, the radial migration of icy pebbles to the inner disc decreases the H₂O content in the outer disc and enhances the gas-phase reservoir inside the H₂O snow line. On the other hand, in HD 100546, the presence of the outer wide gap (see Fig. 7 bottom panels) prevents or slows down the radial drift of the ice dust grains towards the high-temperature region, resulting in a (relatively) high gas-phase H₂O abundance in the outer disc. Compared to the wide and deep gap of HD 100546, the three outer gaps observed in HD 163296 (Fig. 7) are not wide and deep enough to stop the inward drift of icy grains. Our results show how the chemistry of discs is strictly connected to the dynamical history of the system and to the presence of giant protoplanets.

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Appendix A: H₂O model grid

The results of the parametric model grid for HD 163296 and HD 100546 are shown in Figures A.1 and A.2. The models shown here refer to the original definition of the H₂O reservoir (Equation 5). Only a portion of the grid is shown here.

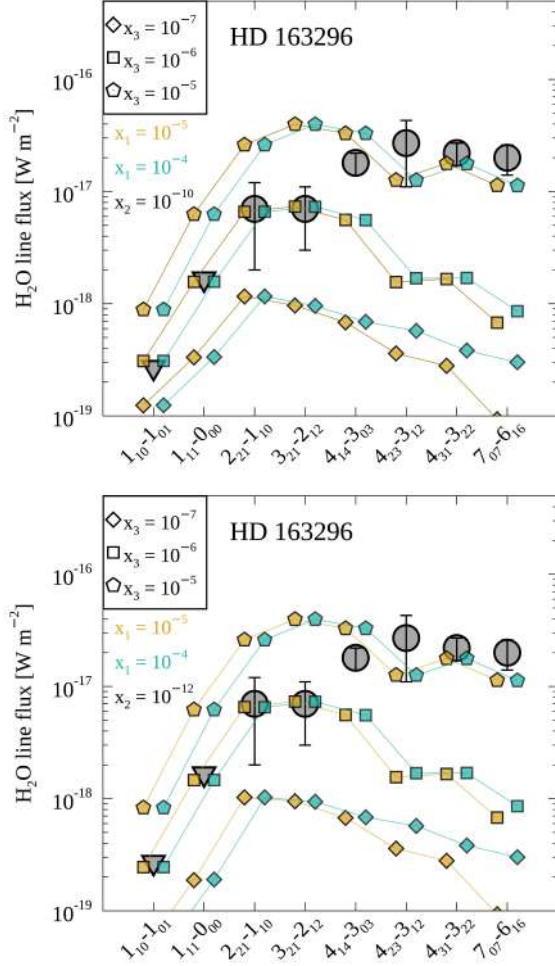


Fig. A.1. Results of the parametric model grid for HD 163296.

In the case of HD 163296, none of the models are able to reproduce the observed trend: on the one hand, the high- J line requires an high abundance ($\gtrsim 10^{-5}$, Figure A.1) in the warm layer (s_3) but these models overestimate the upper limit of the two ground-state transitions. Lowering the value of x_2 does not help.

Figure A.2 shows a subset of the model grid for two different values of x_2 , 10^{-9} and 4×10^{-9} . In the first case, the models underestimate the flux of the ground-state transitions. Increasing the H₂O abundance in s_2 is better suited to fit the flux of the cold transitions but note that these models fail to reproduce the upper limit to the $3_{21} - 2_{12}$ transition.

Appendix B: Synthetic H₂O spectrum

Figure B.1 shows the synthetic H₂O spectra for both discs based on the DALI parametric distribution reported in Figure 5. The spectroscopic data for the ray tracing are from the LAMDA database (Schöier et al. 2005, and reference therein). Submillimetre observations with e.g. ALMA are potentially able to detect emission of H₂O isotopologues, such as H₂¹⁸O. According to our predictions, the brightest H₂O submillimetre transition

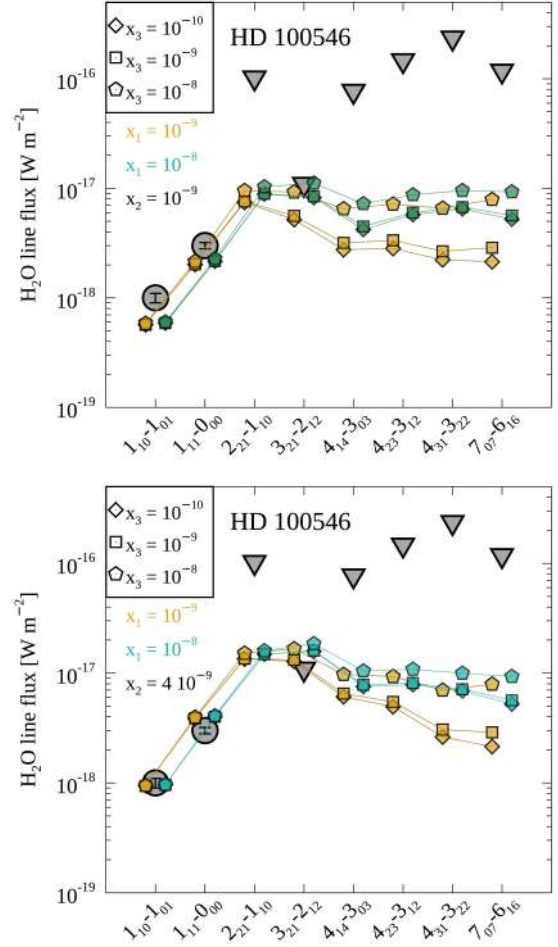


Fig. A.2. Same as Figure A.1 but for HD 100546.

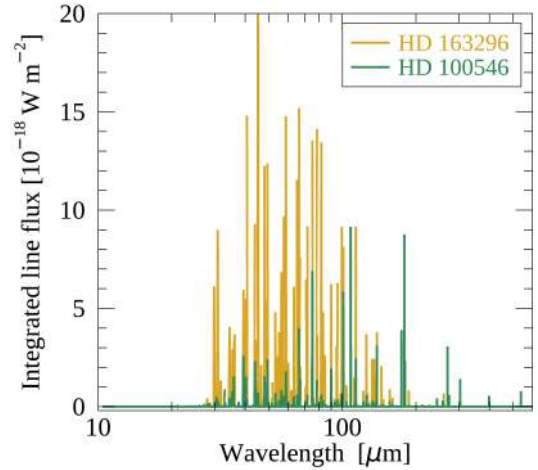


Fig. B.1. Synthetic H₂O spectrum of HD 163296 and HD 100546 based on the H₂O parametric distribution reported in Figure 5.

is the $4_{14} - 3_{21}$ (lower energy level of 212 K); while the main isotopologue cannot be observed from the ground because of atmospheric absorption, the corresponding H₂¹⁸O transition at 390,607 GHz falls in the ALMA band 8. Assuming a H₂O / H₂¹⁸O abundance ratio of 560, the predicted flux of the H₂¹⁸O $4_{14} - 3_{21}$ transition is $7.5 \times 10^{-24} \text{ W m}^{-2}$ and $1 \times 10^{-24} \text{ W m}^{-2}$ for HD 163296 and HD 100546, respectively. These lines are too faint to be detected with current instrumentation in a reasonable amount of time.