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The X-ray enhancements of radio-loud quasars at high redshift: new results at $z = 4-7$

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ABSTRACT

Highly radio-loud quasars (HRLQs; $\log R > 2.5$) at $z \gtrsim 4$ show apparent enhanced X-ray emission compared to matched HRLQs at lower redshifts, perhaps due to a redshift-dependent fractional contribution to the X-ray luminosity from inverse-Compton scattering of cosmic microwave background photons (IC/CMB). Using new *Chandra* observations and archival X-ray data, we investigate this phenomenon with an optically flux-limited sample of 41 HRLQs at $z = 4-5.5$ all with sensitive X-ray coverage, the largest sample utilized to date by a wide margin. X-ray enhancements are assessed using X-ray-to-optical flux ratios and spectral energy distributions. We confirm the presence of X-ray enhancements at a $4.9-5.3\sigma$ significance level, finding that the median factor of enhancement is ≈ 1.8 at our sample median redshift of $z \approx 4.4$. Under a fractional IC/CMB model, the expected enhancement at lower redshifts is modest; e.g. ≈ 4 per cent at $z \approx 1.5$. We also investigate a sample of seven radio-loud quasars (RLQs; $\log R > 1$) at even higher redshifts of $z = 5.6-6.8$, using new and archival X-ray data. These RLQs also show evidence for X-ray enhancements by a median factor of ≈ 2.7 at a $3.7-4.9\sigma$ significance level. The X-ray spectral and other properties of these $z = 5.6-6.8$ RLQs, however, pose challenges for a straightforward fractional IC/CMB interpretation of their enhancements.

Key words: galaxies: high-redshift – quasars: general – X-rays: galaxies – .

1 INTRODUCTION

Quasars are powered by the accretion process happening in the vicinity of supermassive black holes (SMBHs) located in the central regions of host galaxies. Quasars at high redshifts are of particular interest, since they provide insights into SMBH growth and galaxy formation in the early Universe. The discovery of significant samples of rare high-redshift quasars was made possible by large-scale sky surveys such as the Sloan Digital Sky Survey (SDSS; York et al. 2000). Since Ly α emission is redshifted to the near-infrared (NIR) bands at $z \gtrsim 5.5$, wide-field NIR surveys like the UKIRT Infrared Deep Sky Survey and the VISTA Hemisphere Survey (e.g. Lawrence et al. 2007; McMahon et al. 2013) are also important. As of December 2022, there are 531 quasars with $z \geq 5.3$ in the literature (Fan, Banados & Simcoe 2022). Based on the radio-loudness parameter $R = f_{5\text{GHz}}/f_{4400\text{\AA}}$, where $f_{5\text{GHz}}$ and $f_{4400\text{\AA}}$ are the flux densities at rest frame 5 GHz and 4400 Å (Kellermann et al. 1989), quasars can be

divided into radio-quiet quasars (RQQs; $R \leq 10$) and radio-loud quasars (RLQs; $R > 10$). RLQs harbour strong relativistic jets (e.g. Padovani 2017). The fraction of RLQs remains ~ 10 per cent up to $z \sim 6$ (Bañados et al. 2015). It is well known that the quasar number density peaks at $2 < z < 3$ (e.g. Dunlop & Peacock 1990; Croom et al. 2004; Brown et al. 2006; Yang et al. 2016) and then rapidly declines with increasing redshift. In contrast to the strong redshift dependence of the quasar number density, previous studies have shown that the UV/optical and NIR spectral properties of quasars do not show significant evolution up to $z \sim 6$ (e.g. Fan et al. 2004; Jiang et al. 2007; Shen et al. 2019). Current observations suggest that AGNs and SMBH feeding modes do not show significant evolution after the first billion years of the Universe.

Almost all quasars are bright in the X-ray regime. The X-ray emission from RQQs is proposed largely to be generated by the thermal inverse-Compton (IC) process, where UV/optical photons provided by the accretion disc are upscattered by the hot electrons in a coronal structure (e.g. Haardt & Maraschi 1993). The $L_{\text{UV}}-L_{\text{X}}$ relation of RQQs also does not show significant evolution up to $z \sim 6$ (e.g. Steffen et al. 2006; Vito et al. 2019). Previous studies found that

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the typical X-ray power-law photon index of $z > 6$ RQQs is slightly steeper than that of RQQs at lower redshifts (e.g. Nanni et al. 2017; Vito et al. 2019; Wang et al. 2021). A recent work conducted by Zappacosta et al. (2023) showed that the power-law photon index of a sample of hyperluminous ($L_{\text{bol}} \geq 10^{47}$ erg s $^{-1}$) RQQs seems significantly steeper than that for RQQs at lower redshifts.

The nuclear X-ray emission of RLQs is stronger than that of RQQs with comparable UV/optical luminosities. Historically, this X-ray excess was believed to be produced by an additional jet-linked component (e.g. Zamorani et al. 1981; Worrall et al. 1987). This idea has been challenged by Zhu et al. (2020), Zhu, Timlin & Brandt (2021), and Timlin et al. (2021), who proposed that the X-ray emission from most RLQs is still corona-dominated with stronger coronal X-ray emission caused by a corona–jet connection.

The X-ray luminosity contribution from the jet-linked component is much less important than previously expected for general RLQs. However, the many extended X-ray jets discovered by *Chandra*,¹ often stretching over tens of kpc, demonstrate that some level of jet-linked X-ray emission exists. The radiation mechanisms of this jet-linked X-ray emission have been extensively discussed. One possible mechanism is seed photons being IC scattered by relativistic electrons accelerated in the jet. The seed photons of the IC process may come from the cosmic microwave background (IC/CMB; Tavecchio et al. 2000; Celotti, Ghisellini & Chiaberge 2001); synchrotron emission from the jet (synchrotron self-Compton, or SSC; Bloom & Marscher 1996); or photons radiated from the accretion disc, broad-line region (BLR), or the dusty ‘torus’ (e.g. Dermer & Schlickeiser 1993; Sikora, Begelman & Rees 1994; Błażejowski et al. 2004). The IC/CMB model was used to explain the X-ray knot emission of the kpc-scale jet of PKS 0637–752 (Chartas et al. 2000; Schwartz et al. 2000; Tavecchio et al. 2000) and became a popular explanation for X-ray jets (e.g. Sambruna et al. 2004, 2006; Perlman et al. 2011; Marshall et al. 2018).

Despite the initial success of the IC/CMB model for extended X-ray jets, the lack of strong redshift evolution of RLQ X-ray properties disfavours using IC/CMB to explain the nuclear jet-linked X-ray emission (e.g. Bassett et al. 2004; Lopez et al. 2006; Miller et al. 2011). An X-ray jet-linked component that is dominated by IC/CMB emission would reproduce the $(1+z)^4$ dependence of the CMB energy density. Miller et al. (2011) showed that the relative X-ray brightness of RLQs compared to RQQs with similar UV/optical luminosities does not show significant redshift dependence to $z \sim 4$. However, Wu et al. (2013, Wu13 hereafter) and Zhu et al. (2019, Zhu19 hereafter) showed that the minority subset of highly radio-loud quasars (HRLQs; $\log R > 2.5$) has an X-ray enhancement at $4 < z < 5.5$ compared to their matched low- z counterparts. Zhu19 formed a flux-limited sample of 24 HRLQs at $4 < z < 5.5$ (median $z = 4.4$, $m_i \leq 20.26$) with complete X-ray coverage and compared it with 311 HRLQs at $z < 4$ (median $z = 1.3$) with matched UV/optical luminosities. Zhu19 found the nuclear X-ray emission of $4 < z < 5.5$ HRLQs is ≈ 2 times stronger than that for their low- z counterparts at a 4–5 σ confidence level. The X-ray enhancement factor of ≈ 2 is slightly smaller than that of the ≈ 3 factor found by Wu13 but has a higher confidence level owing to the larger and improved sample. Although the $(1+z)^4$ dependence of the dominant X-ray emission has not been observed, contributions from the IC/CMB process are still expected.

Wu13 and Zhu19 proposed a fractional IC/CMB model to explain the X-ray enhancements of high-redshift HRLQs. In this model, the

IC/CMB process is only dominant on the scale of ≈ 1 –5 kpc, where the CMB energy density starts to dominate those of other radiation fields and the magnetic field. In the inner region, the IC seed photons are dominated by the emission from the accretion process around the central SMBH, such as IR photons emitted by the torus (e.g. Ghisellini & Tavecchio 2009), which does not show a strong redshift dependence. Here, Ghisellini & Tavecchio (2009) assumed a highly relativistic jet with a bulk Lorentz factor $\gamma = 15$. On scales of $\gtrsim 10$ kpc, the likely decelerated jet (e.g. Mullin & Hardcastle 2009; Meyer et al. 2015, 2016; Breiding et al. 2017) can no longer boost CMB photons to X-ray energies. Indeed, if a jet with $\gamma \approx 15$ at ≤ 5 kpc decelerates to $\gamma \approx 1.5$ at a large distance, the X-ray emission produced by the IC/CMB process would decrease by a factor of ≈ 100 . An alternative to the fractional IC/CMB model is that the enhanced star formation in high- z host galaxies might create extra IR photons serving as seed photons for the IC process. It is also possible that high- z jets are slower than those in the low- z universe, leading to a larger fraction of beamed objects at $z > 4$.

If the fractional IC/CMB model is correct, then RLQs at still higher redshifts of $z > 5.5$ are expected to have strong IC/CMB-related X-ray emission due to the $(1+z)^4$ evolution of CMB energy density. Moreover, observations of several individual $z > 5.5$ RLQs reveal inconsistent results regarding their X-ray enhancements (e.g. Belladitta et al. 2020; Medvedev et al. 2020; Connor et al. 2021; Medvedev et al. 2021; Ighina et al. 2022a). Thus, it is important to study the role of the IC/CMB process in the early universe by investigating the X-ray enhancements of a sample of $z > 5.5$ RLQs.

In this work, we investigate a sample of 41 HRLQs at $4 < z < 5.5$ and a sample of 7 RLQs at $z > 5.5$. Our goals include the following: (1) further assess the existence of X-ray enhancements for $4 < z < 5.5$ HRLQs with an enlarged sample, and (2) constrain the X-ray enhancements of RLQs at very high redshifts ($z > 5.5$). In Section 2, we describe the selection of our $4 < z < 5.5$ HRLQ sample and the $z > 5.5$ sample. We report our observations, analysis procedures, and X-ray properties of eight newly observed *Chandra* Cycle 23 objects in Section 3. In Section 4, we present our main results and findings. The discussion and a summary are presented in Sections 5 and 6. Throughout the paper, we use short-hand nomenclature for object names in the text and Table 5. We adopt a flat Λ CDM cosmology with $H_0 = 70.0$ km s $^{-1}$ Mpc $^{-1}$ and $\Omega_m = 0.3$.

2 SAMPLE SELECTION

2.1 The $4 < z < 5.5$ HRLQ sample

Our $4 < z < 5.5$ HRLQ sample was constructed based on the sources selected by Wu13 and Zhu19. Wu13 first selected four $z > 4$ HRLQs from the SDSS Data Release 7 quasar catalogue (Schneider et al. 2010) that covers a sky area of 9380 deg 2 . They then found 24 $z > 4$ HRLQs within the sky area at $\delta > -40^\circ$ from NED.² The sky area they chose was covered by the 1.4 GHz NRAO VLA Sky Survey (NVSS; Condon et al. 1998), which enabled them to determine the radio-loudness of each source. The flux densities of HRLQs ($\log R > 2.5$) with $m_i \leq 21$ at observed-frame 1.4 GHz should be above the NVSS detection limit (≈ 2.5 mJy). The resulting sample contains 28 HRLQs (see Tables 1 and 2 in Wu13 for a full list).³

²<https://ned.ipac.caltech.edu/>

³The 28 HRLQs were revised to 26 by Zhu19. SDSS J003126.79+150739.5 and SDSS J123142.17+381658.9 were removed since they do not satisfy the

¹See, e.g. <https://hea-www.harvard.edu/XJET/>.

Table 1. X-ray observation log of objects analysed in this paper.

Object name	RA (deg)	Dec. (deg)	Instr.	z	Obs. date	Obs. ID	Exp. time (ks)
<i>Chandra</i> Cycle 23 targets							
PSO J055.4244 – 00.8035	55.4244	–0.8035	ACIS-S	5.68	2022/02/03	26029	13.18
SDSS J082511.60 + 123417.2	126.2983	12.5714	ACIS-S	4.377	2021/10/17	26025	6.20
PSO J135.3860 + 16.2518	135.3860	16.2519	ACIS-S	5.63	2022/01/26	26030	12.74
SDSS J104742.57 + 094744.9	161.9274	9.7958	ACIS-S	4.233	2023/03/12	26023	5.02
SDSS J115605.44 + 444356.5	179.0223	44.7301	ACIS-S	4.310	2021/12/21	26027	7.78
SDSS J125300.15 + 524803.3	193.2506	52.8009	ACIS-S	4.115	2021/11/10	26028	9.17
SDSS J153830.71 + 424405.6	234.6280	42.7349	ACIS-S	4.099	2021/12/05	26026	6.67
SDSS J165539.74 + 283406.7	253.9156	28.5685	ACIS-S	4.048	2021/12/05	26024	5.10
Archival objects							
SDSS J083643.85 + 005453.3	129.1829	0.9148	ACIS-S	5.82	2002/01/29	3359	5.68
SDSS J094004.80 + 052630.9	145.0200	5.4419	ACIS-S	4.503	2017/12/31	20476	5.99
PSO J172.3556 + 18.7734	172.3556	18.7734	EPIC-pn	6.82	2020/12/20	0863780101	94.03
					2020/12/22	0863780201	89.73
SDSS J140025.40 + 314910.6	210.1058	31.8196	ACIS-S	4.690	2018/02/07	20480	5.99
CFHQS J142952 + 544717	217.4671	54.7882	ACIS-S	6.18	2021/08/03	22601	30.56
SDSS J154824.01 + 333500.1	237.1000	33.5834	ACIS-S	4.678	2018/02/11	20482	6.11
VIKING J231818.35 – 311346.3	349.5765	–31.2295	ACIS-S	6.44	2022/01/07	25739	19.64
					2022/01/08	26254	9.78
					2022/04/12	25254	9.94
					2022/04/17	26391	17.84
					2022/04/18	26392	9.94
PSO J352.4034 – 15.3373	352.4034	–15.3373	ACIS-S	5.83	2019/08/19	21415	41.52
					2019/08/21	22728	59.28
					2019/08/24	22729	45.46
					2019/08/25	22730	38.24
					2019/09/16	21416	19.06
					2019/09/17	22850	31.44
					2019/09/22	22851	29.88

Based on the HRLQ sample constructed by Wu13, Zhu19 found 17 more $4 < z < 5.5$ HRLQs. Zhu19 first matched the SDSS Data Release 14 quasar catalogue (Pâris et al. 2018) to the Faint Images of the Radio Sky at Twenty-centimetres survey (FIRST; Becker, White & Helfand 1995) for observed-frame 1.4 GHz flux densities and found 16 HRLQs at $4 < z < 5.5$. FIRST should have detected all HRLQs with $m_i \lesssim 21$ with a sensitivity of ≈ 1 mJy. Zhu19 also searched NED following the method used by Wu13 and selected another HRLQ at $z = 4.067$, B3 0254 + 434 (Amirkhanyan & Mikhailov 2006).

We combined the samples constructed by Zhu19 and Wu13, with the two faintest sources ($m_i > 22$) removed, to form a complete sample of $4 < z < 5.5$ HRLQs with 41 sources. 32 out of 41 sources have been analysed by Wu13 and Zhu19. In this paper, we report the data analyses of the remaining nine objects using new and archival *Chandra* observations. The rest-frame UV spectra of the nine newly added HRLQs taken from SDSS are shown in Fig. 1. These objects generally show strong emission lines, indicating that their optical/UV continua are not strongly beamed. SDSS J1538 + 4244, showing an absorption feature on the blue wing of the C IV emission line, was identified as a mini-Broad Absorption Line quasar (mini-BAL; e.g. Hall et al. 2002). Since mini-BALs generally do not show weaker X-ray emission compared to typical quasars (e.g. Gibson et al. 2009; Wu et al. 2010), we did not remove SDSS J1538 + 4244 from the sample.

HRLQ criterion ($\log R > 2.5$) when using the rest frame 2500 Å luminosity from Shen et al. (2011).

We checked the VLA Sky Survey (VLASS; Lacy et al. 2020) Epochs 1 and 2 Quick-look Catalogs (Gordon et al. 2021) for potential source radio variability.⁴ The majority of $4 < z < 5.5$ HRLQs do not show significant source variability during the 32 month time span between Epochs 1 and 2 of VLASS, corresponding to a rest-frame time-scale of ≈ 6.0 months (calculated using the median redshift of $4 < z < 5.5$ HRLQs). All 41 HRLQs at $4 < z < 5.5$ are detected in both epochs. The flux densities at observed-frame 3 GHz of 40 objects fluctuate within 30 per cent between two epochs. The flux density of GB 1508 + 5714 obtained from VLASS Epoch 2 has doubled compared to that from Epoch 1. A ≈ 30 per cent variability corresponds to a ≈ 0.11 fluctuation in $\log R$. The highly-radio-loud nature of $4 < z < 5.5$ HRLQs in our sample is thus not jeopardized by source variability.

We plotted the m_i distribution of the $4 < z < 5.5$ HRLQ sample in Fig. 2 and showed the joint efforts made by Wu13, Zhu19, and this paper to construct a high-redshift HRLQ sample with complete X-ray coverage over the past decade. The optically flux limited sample utilized here is significantly larger than those of past work.

2.2 The $z > 5.5$ RLQ sample

We collected $z > 5.5$ RLQs from the literature (e.g. Belladitta et al. 2020; Bañados et al. 2021; Ighina et al. 2021; Liu et al. 2021) and found 14 objects as of March 2021. Since the quasars selected by radio surveys tend to bias towards those with high

⁴The catalogues were retrieved from <https://cirada.ca/vlascatalogueq10>.

Table 2. X-ray net counts, hardness ratios, and effective photon indices of objects analysed in this paper.

Name	Net X-ray counts			HR ^a	Γ_X
	Full band (0.5–8 keV)	Soft band (0.5–2 keV)	Hard band (2–8 keV)		
<i>Chandra</i> cycle 23 targets					
PSO J055.4244 – 00.8035	12.6 ^{+3.8} _{–3.2}	8.5 ^{+3.2} _{–2.6}	4.1 ^{+2.4} _{–1.7}	0.49 ^{+0.26} _{–0.31}	2.45 ^{+1.20} _{–0.51}
SDSS J082511.60 + 123417.2	5.2 ^{+2.6} _{–2.0}	2.1 ^{+1.8} _{–1.5}	3.1 ^{+2.1} _{–1.5}	1.49 ^{+0.88} _{–1.31}	1.09 ^{+1.47} _{–0.52}
PSO J135.3860 + 16.2518	8.3 ^{+3.2} _{–2.6}	6.3 ^{+2.8} _{–2.2}	2.0 ^{+1.8} _{–1.2}	0.31 ^{+0.16} _{–0.30}	2.97 ^{+3.77} _{–0.51}
SDSS J104742.57 + 094744.9	27.7 ^{+5.4} _{–4.8}	16.0 ^{+4.2} _{–3.6}	11.7 ^{+3.7} _{–3.0}	0.73 ^{+0.24} _{–0.31}	2.09 ^{+0.68} _{–0.35}
SDSS J115605.44 + 444356.5	5.1 ^{+2.8} _{–2.1}	4.2 ^{+2.6} _{–1.8}	<4.0	<0.94	>1.66
SDSS J125300.15 + 524803.3	10.5 ^{+3.5} _{–2.9}	5.2 ^{+2.6} _{–2.0}	5.2 ^{+2.6} _{–2.0}	1.00 ^{+0.45} _{–0.69}	1.52 ^{+1.40} _{–0.43}
SDSS J153830.71 + 424405.6	<2.46	<2.46	<2.46	–	–
SDSS J165539.74 + 283406.7	15.8 ^{+4.2} _{–3.6}	7.4 ^{+3.0} _{–2.4}	8.4 ^{+3.2} _{–2.6}	1.14 ^{+0.47} _{–0.62}	1.42 ^{+0.92} _{–0.40}
Archival objects					
SDSS J083643.85 + 005453.3	24.4 ^{+5.1} _{–4.5}	20.2 ^{+4.7} _{–4.1}	4.2 ^{+2.4} _{–1.7}	0.21 ^{+0.08} _{–0.13}	2.10 ^{+0.87} _{–0.31}
SDSS J094004.80 + 052630.9	37.1 ^{+6.7} _{–6.0}	26.6 ^{+5.7} _{–5.0}	10.5 ^{+3.8} _{–3.1}	0.39 ^{+0.13} _{–0.16}	2.21 ^{+0.58} _{–0.30}
PSO J172.3556 + 18.7734 ^b	102.1 ^{+21.1} _{–21.0}	38.2 ^{+14.0} _{–13.2}	64.8 ^{+16.2} _{–16.1}	1.62 ^{+2.23} _{–0.35}	1.17 ^{+0.23} _{–0.79}
SDSS J140025.40 + 314910.6	20.1 ^{+5.0} _{–4.3}	12.8 ^{+4.1} _{–3.4}	7.3 ^{+3.2} _{–2.5}	0.58 ^{+0.23} _{–0.29}	1.76 ^{+0.76} _{–0.37}
CFHQS J142952 + 544717	103.7 ^{+9.9} _{–9.8}	63.7 ^{+7.7} _{–7.7}	40.0 ^{+6.5} _{–5.9}	0.63 ^{+0.11} _{–0.15}	2.08 ^{+0.33} _{–0.19}
SDSS J154824.01 + 333500.1	83.2 ^{+8.9} _{–8.8}	64.0 ^{+7.8} _{–7.7}	19.1 ^{+4.6} _{–4.0}	0.30 ^{+0.06} _{–0.10}	2.49 ^{+0.41} _{–0.21}
VIKING J231818.35 – 311346.3	7.9 ^{+3.4} _{–2.8}	6.0 ^{+2.8} _{–2.2}	<3.9	<0.65	>2.12
PSO J352.4034 – 15.3373	122.1 ^{+11.0} _{–10.9}	83.2 ^{+9.0} _{–8.9}	38.8 ^{+6.7} _{–6.0}	0.47 ^{+0.08} _{–0.11}	2.19 ^{+0.19} _{–0.30}

^aHR = $\frac{H}{S}$, where H and S are hard-band and soft-band counts, respectively. The HR values are not directly comparable across different *Chandra* observation cycles (e.g. Wu13 and Zhu19) due to the ACIS low-energy QE degradation.

^bThe full, soft, and hard bands for PSO J172 + 18 are defined to be 0.3–4.5, 0.3–1, and 1–4.5 keV, respectively. See Section 3.2.

radio luminosities, which may show more extreme properties, we removed three radio-selected quasars (McGreer et al. 2006; Zeimann et al. 2011; Belladitta et al. 2020) and focused on optically selected objects. We also removed three optically selected putative RLQs, since they were either not detected in deep follow-up radio observations (Liu et al. 2021) or the radio-loud nature depends on the assumed shape of the radio spectrum (Bañados et al. 2021). Therefore, we found eight bona fide optical-selected RLQs at $z > 5.5$, among which seven objects with $m_{1450} < 21.68$ have sensitive (new and archival) *Chandra* or *XMM-Newton* coverage. The remaining object with $m_{1450} = 24.05$ still lacks sensitive X-ray data.

We plotted the radio and optical/UV luminosities against redshift for $4 < z < 5.5$ HRLQs, $z > 5.5$ RLQs, and general RLQs from the full sample of Zhu et al. (2020) in Fig. 3. Compared to objects studied by Wu13 and Zhu19, our objects are fainter in both the radio and optical/UV bands.

We repeated the VLASS radio variability analysis described in Section 2.1. Three out of seven RLQs at $z > 5.5$ were detected in both Epochs of VLASS and all of them show flux density fluctuations within 15 per cent on a rest-frame time-scale of ≈ 4.7 months (calculated using the median redshift of $z > 5.5$ RLQs). Only one object (VIK J2318 – 3113) was detected in one Epoch but not another. Observations at other radio frequencies further suggest that VIK J2318 – 3113 is probably a highly variable source. It is possible that such variability is extrinsic rather than intrinsic (Ighina et al. 2022b). The typical ≈ 15 per cent radio variability of $z > 5.5$ RLQs translates to a ≈ 0.06 fluctuation in $\log R$, which does not jeopardize their radio-loud nature.

3 OBSERVATIONS AND DATA ANALYSES

In this section, we describe the data analyses of nine HRLQs at $4 < z < 5.5$ and seven RLQs at $z > 5.5$ (see Table 1 for their observation logs).

Among the nine $4 < z < 5.5$ HRLQs, six have been awarded *Chandra* Cycle 23 observation time and three are archival objects (Snios et al. 2020) that are reanalysed for consistency. Among the seven $z > 5.5$ RLQs, two (PSO J055 – 00 and PSO J135 + 16) are *Chandra* Cycle 23 objects. Two archival objects (VIK J2318 – 3113 and PSO J172 + 18) are analysed and reported for the first time in this paper. Three additional objects with sensitive X-ray coverage reported in previous studies (Brandt et al. 2002; Connor et al. 2021; Medvedev et al. 2021) are reanalysed for consistency.

3.1 *Chandra* data reduction and analysis

All objects reported in Table 1 were observed with the Advanced CCD Imaging Spectrometer (ACIS) on board *Chandra* except for PSO J172 + 18.⁵ We utilized *Chandra* Interactive Analysis of Observations (CIAO) version 4.14.0 to conduct X-ray data reduction. We first ran the `chandra_repro` tool to reprocess and recalibrate the

⁵CFHQS J1429 + 5447 has been observed by both *Chandra* and *XMM-Newton*. We used the most recent observation conducted by *Chandra* in our analyses. However, the 0.5–2 keV flux derived from the *Chandra* data is ≈ 40 per cent fainter than that inferred from the *XMM-Newton* data (Medvedev et al. 2021), suggesting the source is probably variable in X-rays on a rest-frame time-scale of ≈ 52 d. The *Chandra* observation also gave a flatter X-ray spectral index.

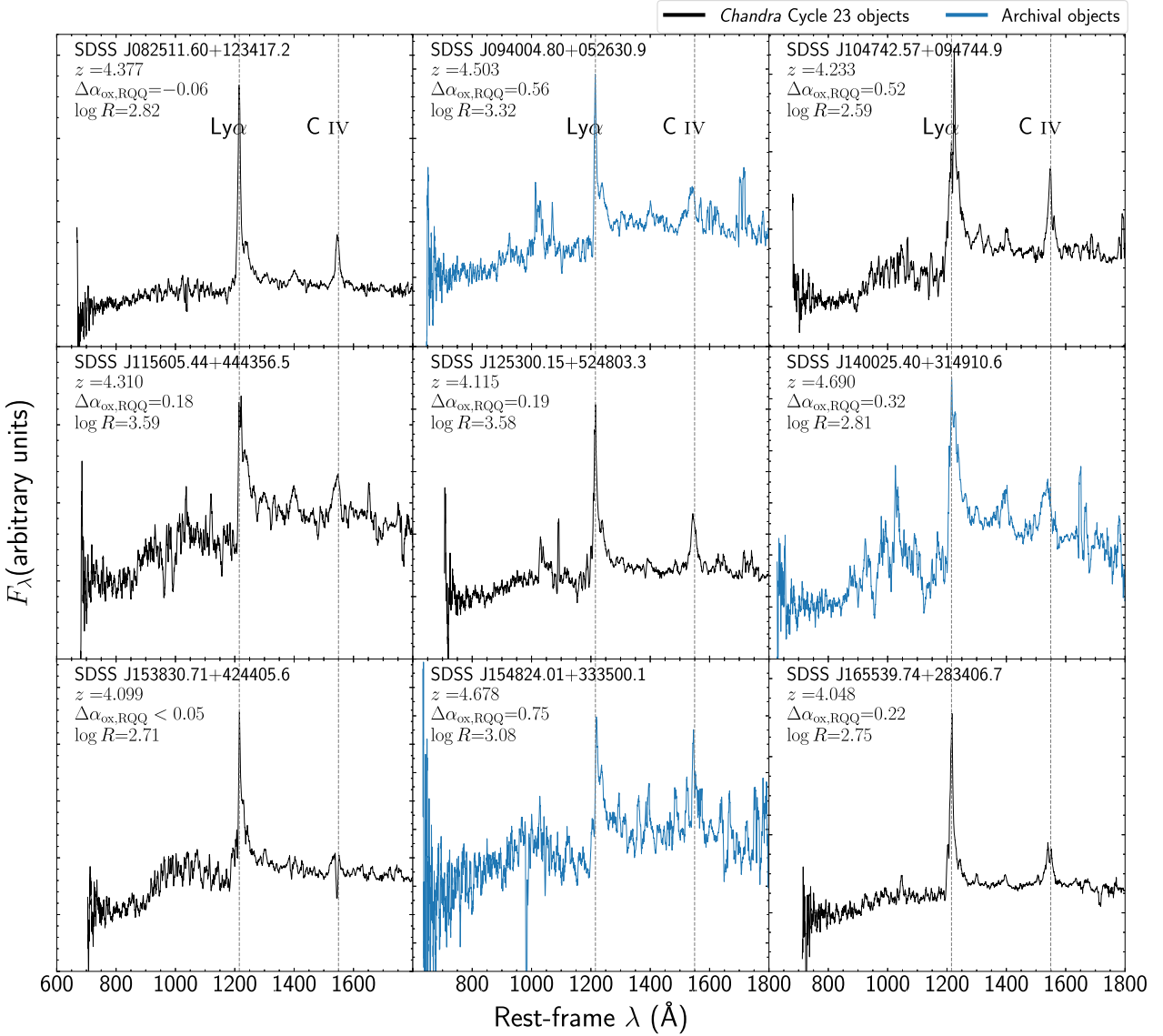


Figure 1. The rest-frame UV spectra of the new sources added to our sample, ordered by ascending RA. All spectra are taken from SDSS. The object name, redshift, $\Delta\alpha_{\text{ox,RQQ}}$, and logarithm of the radio-loudness parameter are listed in each panel. The x-axis is the rest-frame wavelength in units of \AA . The y-axis is on a linear scale with arbitrary units. Each spectrum has been smoothed with a boxcar filter. Ly α ($\lambda = 1215.24 \text{ \AA}$) and C IV ($\lambda = 1549.48 \text{ \AA}$) are labelled with the dotted vertical lines.

observation data with CALDB version 4.9.7. We did not see any object showing extended X-ray structures based on visual inspections. After that, we ran `fluximage` to generate exposure-corrected X-ray images in the full band (0.5–8 keV), soft band (0.5–2 keV), and hard band (2–8 keV). Here, we define the effective energy of each band to be the geometric mean of the energy limits. We then performed source detection by running `wavdetect` on the full-band image with a 10^{-6} significance threshold and wavelet scales 1, $\sqrt{2}$, 2, $2\sqrt{2}$, and 4. All sources but SDSS J1538 + 4244 and VIK J2318 – 3113 were detected by `wavdetect`. We adopted `wavdetect` positions for the detected sources and the optical position for the undetected sources as source positions. We then applied the `deflare` procedure to background light curves to remove background flares and periods when the count rate was anomalously low. The `method` parameter is set to be `sigma` to adopt the `lc.sigma.clip` method with the default `sigma` value of 3, which iteratively deletes any point

outside $\pm 3\sigma$ about the mean until all points are in this range. When running `deflare`, regions of detected sources were masked out. Then, we filtered the event file with the good time interval (GTI) file produced by `deflare`. None of our observations was affected by flaring except for SDSS J1400 + 3149, whose exposure time has been reduced by 4 per cent.

We defined the source region to be a circle with a radius of 2.0 arcsec centred at the source position (corresponding to a ≈ 94 per cent encircled-energy fraction, or EEF, of the PSF at 2 keV) and the background region to be an annulus centred at the source position, with inner and outer radii of 5.0 and 20.0 arcsec, respectively. We visually inspected the X-ray images to ensure that the background regions of reported objects are free of other X-ray sources. After that, we extracted the source and background counts of all three bands using `dmextract` with the source and background regions. We added the raw counts in the source and background regions

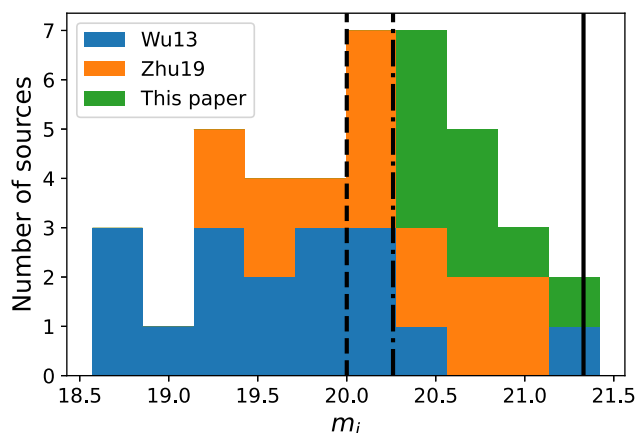


Figure 2. The m_i distribution for the $4 < z < 5.5$ HRLQ sample with 41 sources. The histogram is colour coded by the papers that provide X-ray analyses. The blue, orange, and green bars represent sources analysed by Wu13, Zhu19, and this paper, respectively. The dashed, dash-dotted, and solid vertical lines are the flux limits applied in Wu13, Zhu19, and this paper, respectively. The flux-limited samples of Wu13, Zhu19, and this paper contain 12, 24, and 41 sources with sensitive X-ray coverage, respectively.

of all five observations of VIK J2318 – 3113 together to get its raw source and background counts. We adopted the likelihood-ratio test developed by Li & Ma (1983) for source detection. The null hypothesis is $s = 0$, and the alternative hypothesis $s \neq 0$, where s is the true source counts. Following Li & Ma (1983), we defined a likelihood ratio, λ , which is the ratio of the likelihoods that all X-ray counts are produced by the background over that there exists an actual X-ray source. The likelihood ratio, λ , satisfies equation (1), where N_{src} and N_{bkg} are source and background counts, and B is background area to source area ratio:

$$\ln \lambda = - \left(N_{\text{src}} \ln \left((1+B) \frac{N_{\text{src}}}{N_{\text{bkg}} + N_{\text{src}}} \right) + N_{\text{bkg}} \ln \left(\frac{1+B}{B} \frac{N_{\text{bkg}}}{N_{\text{bkg}} + N_{\text{src}}} \right) \right). \quad (1)$$

The statistic $Z = \sqrt{-2 \ln \lambda}$ is the Z-score of the source-detection test. That is, the likelihood-ratio test has a $Z \sigma$ significance level. If the source counts are smaller than the estimated background counts, i.e. $N_{\text{src}} < N_{\text{bkg}}/B$, we flip the sign of Z for this scenario. We rejected the null hypothesis if $Z \gtrsim 2.576$, or equivalently $p < 0.01$, and considered a source to be detected in the tested energy band. Here, the p -value is calculated as $p = P(T > Z)$, where T follows a standard normal distribution. The 0.01 threshold is suitable for source-detection tests with pre-specified positions.

We calculated Z for all three bands of all our sources. For detected bands, we used a Bayesian method `aprates`⁶ (e.g. Primini & Kashyap 2014) and set the `conf` parameter to 0.68 to calculate the net counts and their 1σ credible intervals for all three bands, which are shown in Table 2. For each undetected band, the upper bound of a 90 per cent confidence interval of net counts is reported. Only a fraction of the source counts is included in the source aperture. We corrected the effects of non-ideal PSF by setting the parameters `alpha` and `beta` of `aprates` to be the PSF fraction in the source aperture and background region, which are calculated using `src_psffrac`.

We ran the `specextract` tool to extract source and background spectra. The `specextract` tool automatically generates ancillary response files (ARFs) and response matrix files (RMFs) except for SDSS J1538 + 4244, which does not have counts in the full band. We ran `mkacisrmf`, with the weight map provided by `specextract`, to create the weighted RMF and `mkarf` to create the ARF for SDSS J1538 + 4244. For VIK J2318 – 3113, we ran `combine_spectra` to combine its spectra and response files from all five observations. We used the combined spectrum in the following analyses.

We also calculated hardness ratios and their 1σ confidence intervals using the Bayesian estimation method developed by Park et al. (2006). In this paper, hardness ratio HR is defined as $\frac{H}{S}$, where H and S are net counts in the hard and soft bands, respectively. For each object detected in the soft band but undetected in the hard band, we reported an upper limit on the hardness ratio to be the hard count upper limit divided by soft counts. We then estimated the effective power-law photon index Γ_X using SHERPA. For each object, we generated a series of Galactic-absorbed power-law spectra using the `xsphabs.abs1*powlaw1d.p1` model implemented in SHERPA, which is the multiplication of an absorption model and a power-law model, with fixed Galactic neutral hydrogen column density (N_{H}^7) and varying Γ_X . We then used `calc_model_sum` to calculate the soft-band and hard-band counts of each model. With X-ray counts, we calculated the hardness ratio of each model and used interpolation to determine the desired Γ_X whose hardness ratio matches the observed value.

Our data reduction ends with running `calc_energy_flux` on the `xsphabs.abs1*powlaw1d.p1` model combining ARF and RMF files, Γ_X , and N_{H} to derive the Galactic-absorption corrected soft-band flux. The model is normalized so that the result of running `calc_model_sum` on the soft-band equals the soft-band net counts or upper limit.

3.2 XMM–Newton data reduction and analysis

There are two archival X-ray observations of PSO J172 + 18 using EPIC onboard the XMM–Newton observatory. We report the results of these observations (see Table 1 for the observation logs) for the first time. We used the SAS package (v21.0.0) and the most recent Current Calibration Files to reprocess the XMM–Newton data. We used the `EPPROC` command to produce calibrated event lists and filtered the resulting event lists using good time intervals created with single-event (i.e. pattern zero), and high-energy (10–12 keV) light curves with a criterion of ‘RATE <= 0.4’. We extracted source spectra from a circular aperture with a radius of 15 arcsec centred at the optical position of PSO J172 + 18. We also chose a circular source-free region with a radius of 65 arcsec on the same CCD as the background region. We then extracted background spectra following the method we used to extract source spectra. The net counts, hardness ratio, and Γ_X are calculated following the steps described in Section 3.1. The results are reported in Table 2. The flux of PSO J172 + 18 appears only slightly above the sensitivity of these XMM–Newton observations. To achieve the best signal-to-noise ratio, we only considered counts below 4.5 keV and defined soft, hard, and full bands as 0.3–1, 1–4.5, and 0.3–4.5 keV, respectively.

The X-ray emission of PSO J172 + 18 might suffer from additional absorption, given the flatness of the observed spectrum

⁶<https://cxc.cfa.harvard.edu/ciao/ahelp/aprates.html>.

⁷<https://heasarc.gsfc.nasa.gov/cgi-bin/Tools/w3nh/w3nh.pl>

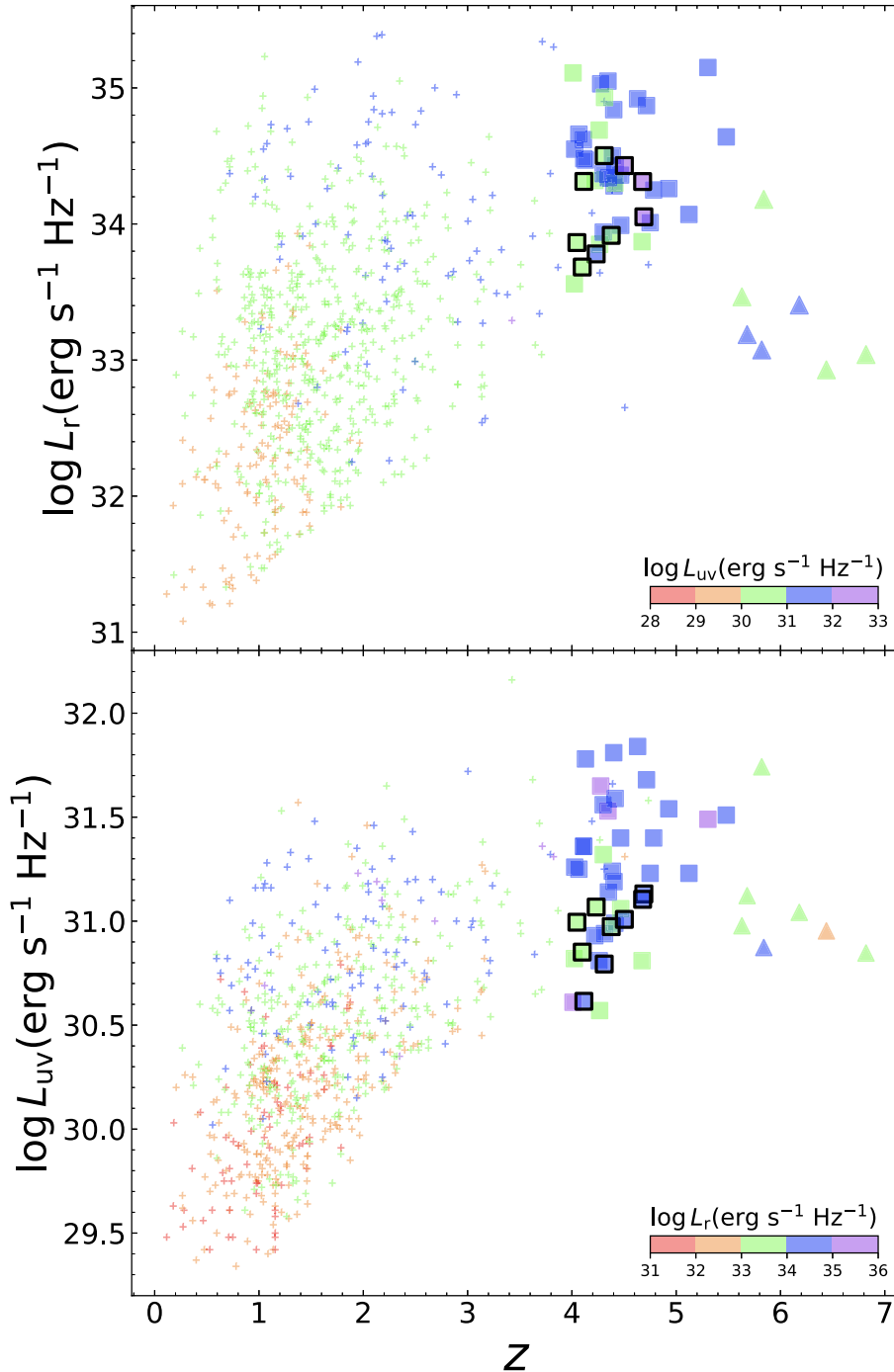


Figure 3. Radio (rest frame 5 GHz, upper panel) and UV (rest frame 2500 Å, lower panel) monochromatic luminosities versus redshift. The upper and lower panels are colour-coded by $\log L_{\text{uv}}$ and $\log L_r$, as indicated by the respective colour bars. The squares represent 41 HRLQs at $4 < z < 5.5$ from Zhu19, Wu13, and this paper. Squares encircled by black boundaries are those newly added $4 < z < 5.5$ HRLQs. The triangles represent seven RLQs at $z > 5.5$. The plus signs represent optically selected radio-loud quasars from Zhu et al. (2020). Symbols in the upper and lower panels are colour-coded based on their UV and radio monochromatic luminosities, respectively.

($\Gamma_X \approx 1.17$; see Table 2) and the faintness of the flux.⁸ Since the 0.3–4.5 keV band probes 2.3–35 keV photons in the rest

⁸We examined the rest-frame optical/UV spectrum of PSO J172 + 18 provided by Bañados et al. (2021). The optical/UV spectrum is similar to that of typical quasars, with prominent emission lines and a rest-frame UV power-law slope $\alpha_v = -0.48$. Thus, there is no apparent obscuration in the rest-frame optical/UV band.

frame, the column density must be high if the putative absorber is intrinsic to PSO J172 + 18. To assess the column density of the absorber and its impact on the X-ray fluxes, we fit a power-law model with intrinsic photoelectric absorption in addition to the Galactic absorption. The spectra from the two observations were fitted jointly. Due to the limited number of net counts, the photon index and column density cannot be constrained simultaneously. We thus fixed Γ_X to 2.0 (e.g. Vito et al. 2019; Zhu, Timlin &

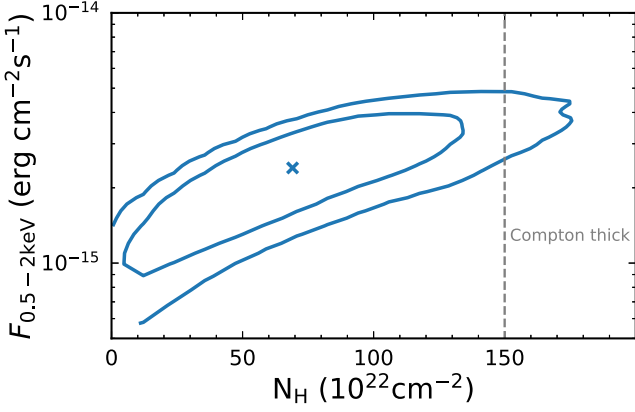


Figure 4. The 68 per cent (inner) and 90 per cent (outer) confidence regions of the 0.5–2 keV flux of the power-law continuum and the column density of the intrinsic absorber for PSO J172 + 18. The photon index is fixed at $\Gamma_X = 2.0$. The cross symbol indicates the best-fitting model for $\Gamma_X = 2.0$, where the absorber is likely Compton thin with best-fitting $N_H = 6.9 \times 10^{23} \text{ cm}^{-2}$. The observed X-ray flux is probably suppressed by a factor of ≈ 3 .

Brandt 2021), leaving the power-law normalization factor and the column density of the absorber free to vary. We performed a Markov chain Monte Carlo analysis to obtain a sample of 10^4 sets of free parameters using SHERPA. The results are plotted in Fig. 4, where the normalization factor is replaced by absorption-corrected 0.5–2 keV flux. If $\Gamma_X = 2.0$, the absorber is likely Compton thin with best-fitting $N_H = 6.9 \times 10^{23} \text{ cm}^{-2}$. We use the best-fitting 0.5–2 keV flux, $2.40 \times 10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$, in later calculations.

Another possible explanation for the flat X-ray spectrum of PSO J172 + 18 is that it is a highly beamed object (or blazar). However, the steep radio spectrum ($\alpha_r = -1.31$, Bañados et al. 2021) and the modest radio loudness ($\log R = 2.07$) of PSO J172 + 18 disfavors this scenario.

3.3 X-ray, optical/UV, and radio properties

In this section, we elaborate on selected columns of Tables 3 and 4, which report X-ray, optical/UV, and radio properties for our sample of $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs. The captions of Tables 3 and 4 contain brief explanations of all columns.

The absolute i -band magnitude of the quasar is listed in column (3) of Table 3. To be consistent with Zhu19, they are calculated from Galactic-extinction corrected m_i using equations (1) and (4) in section 5 of Richards et al. (2006) and K -corrections from the same paper.

We adopted a new method to calculate the flux density observed at $2500(1+z) \text{ \AA}$ for $z > 5.5$ RLQs since Richards et al. (2006) did not provide K -corrections for $z > 5.5$ quasars. We used the SYNPHOT (STScI Development Team 2018) package to simulate the photometry of quasars observed in certain filters and adopted the composite quasar spectrum from Vanden Berk et al. (2001) as the quasar spectrum template. We inspected the rest-frame optical/UV spectra of all seven $z > 5.5$ RLQs and did not identify any objects with unusual continuum spectra. It is thus appropriate to use the composite spectrum given by Vanden Berk et al. (2001) in our calculations. We then normalized the composite spectrum to the photometric data in the selected band and determined the flux density at $2500(1+z) \text{ \AA}$ from the normalized composite spectrum. Since rest-frame 2500 \AA is in the observed-frame NIR band at $z > 5.5$,

Table 3. X-ray, optical/UV, and radio properties of newly added $4 < z < 5.5$ HRLQs. Objects are sorted by ascending RA. (1) Object name. (2) Apparent i -band magnitude. (3) Absolute i -band magnitude. (4) Galactic neutral hydrogen density (HI4PI Collaboration et al. 2016) in units of 10^{20} cm^{-2} . (5) Count rate in the observed-frame 0.5–2 keV band in units of 10^{-3} s^{-1} . (6) Galactic absorption-corrected flux in the observed 0.5–2 keV band, in units of $10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$. (7) Flux density at $2/(1+z) \text{ keV}$ in units of $10^{-32} \text{ } 10^{\text{erg cm}^{-2} \text{ s}^{-1} \text{ Hz}^{-1}}$. (8) Effective X-ray power-law photon index. If there is no available Γ , we take $\Gamma = 1.5$. (9) Flux density observed at $2500(1+z) \text{ \AA}$, in units of $10^{-27} \text{ } 10^{\text{erg cm}^{-2} \text{ s}^{-1} \text{ Hz}^{-1}}$. (10) Logarithm of the monochromatic UV luminosity at rest frame 2500 \AA , in units of $10^{\text{erg s}^{-1} \text{ Hz}^{-1}}$. (11) Radio spectral index calculated near observed 1.4 GHz (see Section 5.1 for details). (12) Logarithm of monochromatic radio luminosity at rest frame 5 GHz in units of $10^{\text{erg s}^{-1} \text{ Hz}^{-1}}$, extrapolated from the observed-frame 1.4 GHz flux density assuming a power-law spectrum $f \propto \nu^{\alpha_r}$. (13) Logarithm of the radio-loudness parameter. (14) Optical–X-ray spectral index. (15) The difference between the measured α_{ox} and that expected for RLQs with similar UV luminosity. (16) The difference between the measured α_{ox} and that expected for RQQs with similar UV luminosity.

Object name (1)	m_i (2)	M_i (3)	N_H (4)	C.R. (5)	F_X (6)	f_{keV} (7)	Γ_X (8)	$f_{2500\text{\AA}}$ (9)	$\log L_{2500\text{\AA}}$ (10)	α_r (11)	$\log L_r$ (12)	$\log R$ (13)	α_{ox} (14)	$\Delta\alpha_{\text{ox, RQQ}}$ (15)	$\Delta\alpha_{\text{ox, RLQ}}$ (16)
<i>Chandra</i> Cycle 23 objects															
SDSS J082511.60 + 123417.2	20.71	-26.44	4.47	0.34 $^{+0.32}_{-0.20}$	0.34 $^{+0.29}_{-0.19}$	1.03 $^{+0.88}_{-0.59}$	1.09 $^{+1.47}_{-0.52}$	0.27	30.97	-0.82	33.92	2.82	-1.69 $^{+0.10}_{-0.14}$	-0.06 $^{+0.10}_{-0.14}$	-0.27 $^{+0.10}_{-0.14}$
SDSS J104742.57 + 094744.9	20.32	-26.67	2.51	3.19 $^{+0.84}_{-0.71}$	4.91 $^{+1.29}_{-1.09}$	41.91 $^{+11.04}_{-9.33}$	2.09 $^{+0.68}_{-0.35}$	0.35	31.07	0.17	33.78	2.59	-1.12 $^{+0.04}_{-0.04}$	0.52 $^{+0.04}_{-0.04}$	0.33 $^{+0.04}_{-0.04}$
SDSS J1115605.44 + 444356.5	21.06	-25.99	1.24	0.56 $^{+0.34}_{-0.24}$	0.61 $^{+0.38}_{-0.26}$	3.44 $^{+2.09}_{-1.47}$	> 1.66	0.18	30.79	-0.83	34.50	3.59	-1.43 $^{+0.08}_{-0.09}$	0.18 $^{+0.08}_{-0.09}$	-0.09 $^{+0.08}_{-0.09}$
SDSS J125300.15 + 524803.3	21.33	-25.54	1.20	0.57 $^{+0.32}_{-0.24}$	0.64 $^{+0.32}_{-0.25}$	3.05 $^{+1.53}_{-1.17}$	1.52 $^{+1.40}_{-0.43}$	0.13	30.61	-0.37	34.31	3.58	-1.39 $^{+0.07}_{-0.08}$	0.19 $^{+0.07}_{-0.08}$	-0.07 $^{+0.07}_{-0.08}$
SDSS J153830.71 + 424405.6	20.76	-26.13	2.36	< 0.40	< 0.42	< 1.98	-	0.22	30.85	-0.71	33.68	2.71	< -1.56	< 0.05	< -0.14
SDSS J165539.74 + 283406.7	20.41	-26.49	4.58	1.45 $^{+0.62}_{-0.47}$	1.58 $^{+0.64}_{-0.51}$	6.75 $^{+2.74}_{-2.19}$	1.42 $^{+0.92}_{-0.40}$	0.32	30.99	-0.04	33.86	2.75	-1.41 $^{+0.06}_{-0.07}$	0.22 $^{+0.06}_{-0.07}$	0.02 $^{+0.06}_{-0.07}$
Archival objects															
SDSS J094004.80 + 052630.9	20.77	-26.52	4.07	4.44 $^{+0.95}_{-0.83}$	4.08 $^{+0.87}_{-0.78}$	41.40 $^{+8.87}_{-7.78}$	2.21 $^{+0.58}_{-0.30}$	0.28	30.98	-0.72	34.43	3.32	-1.08 $^{+0.03}_{-0.03}$	0.56 $^{+0.03}_{-0.03}$	0.31 $^{+0.03}_{-0.03}$
SDSS J140025.40 + 314910.6	20.28	-26.83	1.15	2.23 $^{+0.71}_{-0.59}$	1.77 $^{+0.57}_{-0.47}$	11.74 $^{+3.76}_{-3.12}$	1.76 $^{+0.76}_{-0.37}$	0.35	31.13	-0.76	34.05	2.81	-1.33 $^{+0.05}_{-0.05}$	0.32 $^{+0.05}_{-0.05}$	0.12 $^{+0.05}_{-0.05}$
SDSS J154824.01 + 333500.1	20.35	-26.76	2.40	10.66 $^{+1.43}_{-1.41}$	10.52 $^{+1.28}_{-1.27}$	146.46 $^{+17.85}_{-17.62}$	2.49 $^{+0.41}_{-0.21}$	0.32	31.10	-0.71	34.31	3.08	-0.90 $^{+0.02}_{-0.02}$	0.75 $^{+0.02}_{-0.02}$	0.51 $^{+0.02}_{-0.02}$

Table 4. X-ray, optical/UV, and radio properties of $z > 5.5$ RLQs. Objects are sorted by ascending RA. (2) AB magnitude at observed frame 1450 (1 + z) Å, extrapolated from the flux density at rest frame 2500 Å assuming $\alpha_v = -0.5$. (3) Absolute magnitude at rest frame 1450 Å. (7) Flux density at $2(1 + z)$ keV in units of $10^{-31} \text{ } 10^{\text{erg cm}^{-2} \text{ s}^{-1} \text{ Hz}^{-1}}$. The remaining columns are identical to those in Table 3.

Object name (1)	m_{1450} (2)	M_{1450} (3)	N_H (4)	CR (5)	F_X (6)	f_2 keV (7)	Γ_X (8)	$f_{2500 \text{ Å}}$ (9)	$\log L_{2500 \text{ Å}}$ (10)	α_r (11)	$\log L_r$ (12)	$\log R$ (13)	α_{ox} (14)	$\alpha_{\text{ox}}^{\text{RQQ}}$ (15)	$\Delta\alpha_{\text{ox, RQQ}}$ (15)	$\Delta\alpha_{\text{ox, RLQ}}$ (16)
<i>Chandra</i> cycle 23 obejects																
PSO J055.4244 – 00.8035	20.70	–25.91	5.89	$0.64^{+0.24}_{-0.19}$	$1.02^{+0.38}_{-0.31}$	$1.71^{+0.64}_{-0.52}$	$2.45^{+1.20}_{-0.51}$	0.25	31.12	–0.99	33.19	1.94	$-1.22^{+0.05}_{-0.06}$	$0.44^{+0.05}_{-0.06}$	$0.30^{+0.05}_{-0.06}$	
PSO J135.3860 + 16.2518	21.04	–25.55	3.50	$0.50^{+0.22}_{-0.17}$	$0.92^{+0.41}_{-0.32}$	$2.71^{+1.20}_{-0.95}$	$2.97^{+3.77}_{-0.51}$	0.18	30.98	–0.55	33.46	2.36	$-1.09^{+0.06}_{-0.07}$	$0.55^{+0.06}_{-0.07}$	$0.38^{+0.06}_{-0.07}$	
Archival objects																
SDSS J083643.85 + 005453.3	18.77	–27.07	4.81	–	$1.40^{+0.33}_{-0.28}$	$1.61^{+0.37}_{-0.33}$	$2.10^{+0.87}_{-0.31}$	1.48	31.91	–0.55	33.07	1.21	$-1.52^{+0.03}_{-0.04}$	$0.24^{+0.03}_{-0.04}$	$0.16^{+0.03}_{-0.04}$	
PSO J172.3556 + 18.7734	21.68	–25.22	3.48	–	$0.24^{+0.09}_{-0.08}$	$0.28^{+0.10}_{-0.10}$	–	0.10	30.85	–1.31	33.04	2.07	$-1.37^{+0.05}_{-0.07}$	$0.24^{+0.05}_{-0.07}$	$0.10^{+0.05}_{-0.07}$	
CFHQS J142952 + 544717	21.03	–25.71	1.15	$2.08^{+0.25}_{-0.25}$	$2.72^{+0.33}_{-0.33}$	$3.23^{+0.39}_{-0.39}$	$2.08^{+0.33}_{-0.19}$	0.19	31.04	–0.54	33.40	2.24	$-1.06^{+0.02}_{-0.02}$	$0.58^{+0.02}_{-0.02}$	$0.42^{+0.02}_{-0.02}$	
VIKING J231818.35 – 311346.3	21.32	–25.49	1.10	$0.09^{+0.04}_{-0.03}$	$0.13^{+0.06}_{-0.05}$	$0.16^{+0.07}_{-0.06}$	>2.12	0.14	30.95	–0.80	32.76	1.69	$-1.51^{+0.06}_{-0.08}$	$0.12^{+0.06}_{-0.08}$	$0.00^{+0.06}_{-0.08}$	
PSO J352.4034 – 15.3373	21.36	–25.29	1.67	–	$0.34^{+0.04}_{-0.04}$	$0.43^{+0.05}_{-0.05}$	$2.19^{+0.30}_{-0.19}$	0.14	30.89	–0.95	34.18	3.18	$-1.35^{+0.02}_{-0.02}$	$0.27^{+0.02}_{-0.02}$	$0.05^{+0.02}_{-0.02}$	

^aFlux in the observed frame 0.5–2 keV is calculated from the hard band (1–4.5 keV) count rate assuming $\Gamma_X = 2.0$.

we used H -band magnitudes to calculate $f_{2500 \text{ Å}}$, whenever possible. For objects without H -band observations, we used J -band (CFHQS J1429 + 5447 and PSO J352 – 15) or Pan-STARRS y -band (PSO J135 + 16) photometric data instead (see Section 4.3). The results are shown in column 9 of Table 4.

We calculated the radio spectral indices α_r around observed-frame 1.4 GHz, with $f_\nu \propto \nu^{\alpha_r}$. The results are shown in column 11 of Table 3 for HRLQs and column 11 of Table 4 for $z > 5.5$ RLQs. The 1.4 GHz flux densities were obtained from the FIRST or NVSS surveys. We also obtained flux densities at observed-frame 150 MHz, 326 MHz, 366 MHz, 3 GHz, and 5 GHz (See Section 4.3). We calculated α_{low} and α_{high} , the radio spectral index between 1.4 GHz and a lower or higher frequency. We take the average value of α_{low} and α_{high} to be α_r .

The power-law spectral indices connecting rest frame 2500 Å and 2 keV, defined by

$$\alpha_{\text{ox}} = \frac{\log(f_{2\text{keV}}/f_{2500 \text{ Å}})}{\log(\nu_{2\text{keV}}/\nu_{2500 \text{ Å}})}, \quad (2)$$

are shown in column 14 of Table 3 for HRLQs and column 14 of Table 4 for $z > 5.5$ RLQs.

We present differences between the measured α_{ox} and the expected α_{ox} value of RQQs ($\alpha_{\text{ox, RQQ}}$) in column (15) of Table 3 for $4 < z < 5.5$ HRLQs and column (15) of Table 4 for $z > 5.5$ RLQs. More explicitly,

$$\Delta\alpha_{\text{ox, RQQ}} = \alpha_{\text{ox}} - \alpha_{\text{ox, RQQ}}. \quad (3)$$

Here, $\alpha_{\text{ox, RQQ}}$ is calculated using equation (3) of Just et al. (2007):

$$\alpha_{\text{ox, RQQ}} = -0.140 \log L_{2500 \text{ Å}} + 2.705. \quad (4)$$

We also present differences between the measured α_{ox} and the expected α_{ox} of low- z RLQs ($\alpha_{\text{ox, RLQ}}$) in column 16 of Table 3 for $4 < z < 5.5$ HRLQs and column 16 of Table 4 for $z > 5.5$ RLQs. More explicitly,

$$\Delta\alpha_{\text{ox, RLQ}} = \alpha_{\text{ox}} - \alpha_{\text{ox, RLQ}}. \quad (5)$$

Here, $\alpha_{\text{ox, RLQ}}$ is calculated from the $L_{2\text{keV}}-L_{2500 \text{ Å}}-L_{5\text{GHz}}$ relation for the full RLQ sample given by model I in table 4 of Zhu et al. (2020), which is equivalent to

$$\alpha_{\text{ox, RLQ}} = -0.203 \log L_{2500 \text{ Å}} + 0.084 \log L_{5\text{GHz}} + 2.015. \quad (6)$$

4 RESULTS

4.1 X-ray enhancements of $4 < z < 5.5$ HRLQs

To qualitatively assess the X-ray enhancements of $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs, we plotted α_{ox} , $\Delta\alpha_{\text{ox, RQQ}}$, and $\Delta\alpha_{\text{ox, RLQ}}$ against $\log R$ for our full sample of $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs in the upper, middle, and lower panels of Fig. 5, respectively. We also included optically selected radio-loud quasars from Zhu et al. (2020) in Fig. 5 for comparison. The full sample of Zhu et al. (2020) has 729 RLQs, among which 657 (90.1 per cent) objects have X-ray detections. The redshift of the comparison sample has a median of 1.5 and an interquartile range (IQR) of 1.0. We plotted horizontal dashed lines with $\Delta\alpha_{\text{ox, RQQ}} = 0$ and $\Delta\alpha_{\text{ox, RLQ}} = 0$ in the middle and lower panels of Fig. 5. The positions of $4 < z < 5.5$ HRLQs (stars, squares, and diamonds) in the middle and lower panels of Fig. 5 are generally higher than the low- z comparison RLQs, implying enhanced X-ray emission. More specifically, 39 out of 41 HRLQs at $4 < z < 5.5$ have positive $\Delta\alpha_{\text{ox, RQQ}}$, and 29 have positive $\Delta\alpha_{\text{ox, RLQ}}$.

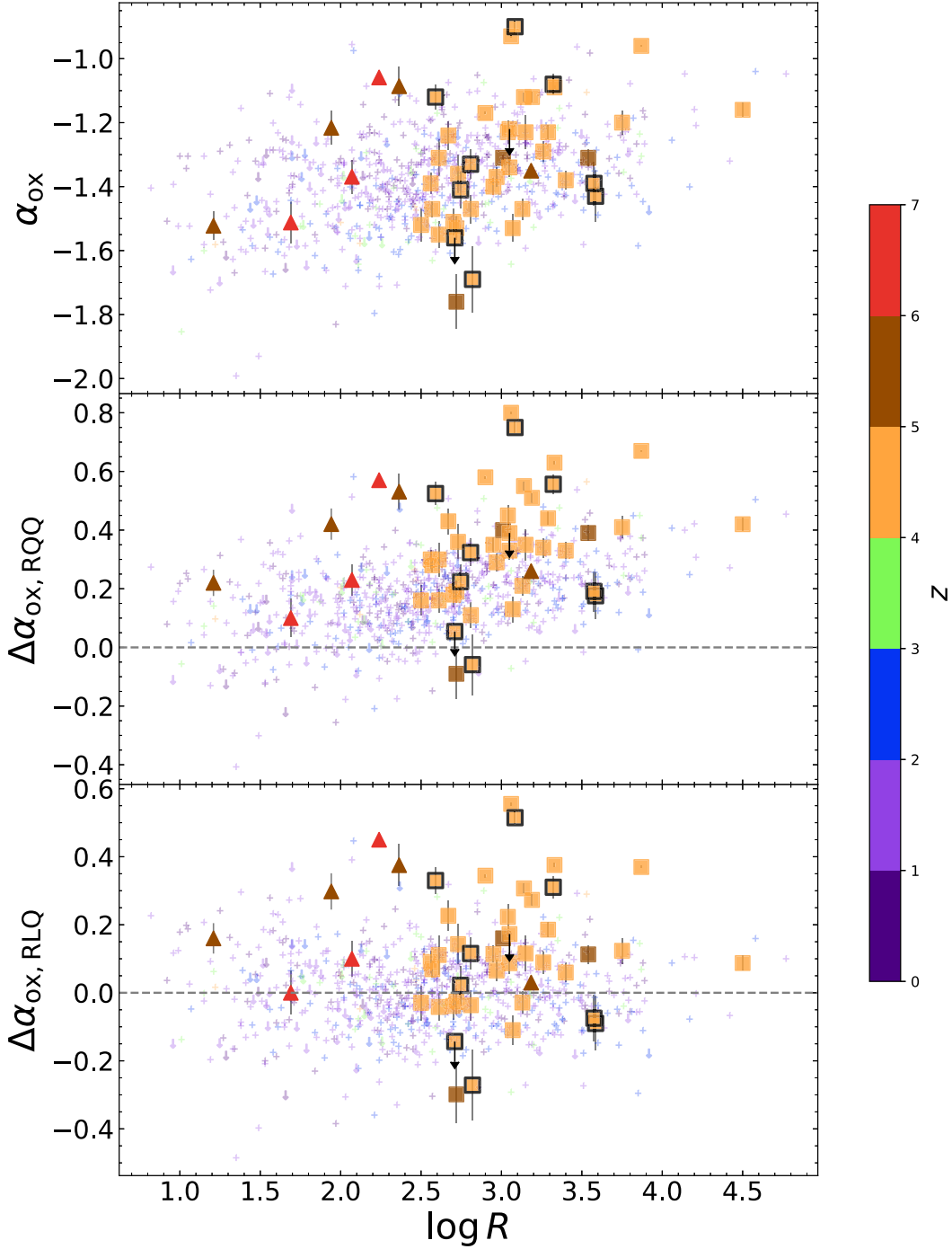


Figure 5. The α_{ox} (upper panel), $\Delta\alpha_{\text{ox,RQQ}}$ (middle panel), and $\Delta\alpha_{\text{ox,RLQ}}$ (lower panel) parameters against logarithm of radio-loudness ($\log R$). The squares represent 41 HRLQs at $4 < z < 5.5$ from Zhu19, Wu13, and this paper. Squares encircled by black boundaries are those newly added $4 < z < 5.5$ HRLQs. The triangles represent seven RLQs at $z > 5.5$. The plus signs represent optically selected radio-loud quasars from Zhu et al. (2020) that are detected in X-rays. The downward arrows represent objects with only X-ray upper limits. All symbols are colour-coded based on their redshifts. The data points in the lower two panels are not merely zero-point shifts. Compared to $\Delta\alpha_{\text{ox,RQQ}}$, $\Delta\alpha_{\text{ox,RLQ}}$ has an additional contribution from $\log L_{5\text{GHz}}$ (see equations 3–6).

We then applied three conditions ($z < 4$, $m_i < 21.33$, $\log R > 2.5$) to the full sample of Zhu et al. (2020) to form a sample of $z < 4$ HRLQs that are comparable to $z > 4$ HRLQs in the optical/UV and radio bands. Here, we adopted an upper limit of 21.33 for m_i since all objects in our $4 < z < 5.5$ HRLQ sample are optically brighter than $m_i = 21.33$. We plotted the distributions of $\Delta\alpha_{\text{ox,RQQ}}$ and $\Delta\alpha_{\text{ox,RLQ}}$ for the low- z HRLQ comparison sample and the $4 <$

$z < 5.5$ HRLQ sample in Fig. 6 for quantitative analysis. The low- z HRLQ sample contains 377 objects with a median redshift of 1.5 and an IQR of 1.0. The logarithm of the radio-loudness parameter ($\log R$) of the comparison sample has a median of 3.0 and an IQR of 0.6.

Since our data include upper limits, we adopted survival analysis methods implemented in the PYTHON package LIFELINES (Davidson-

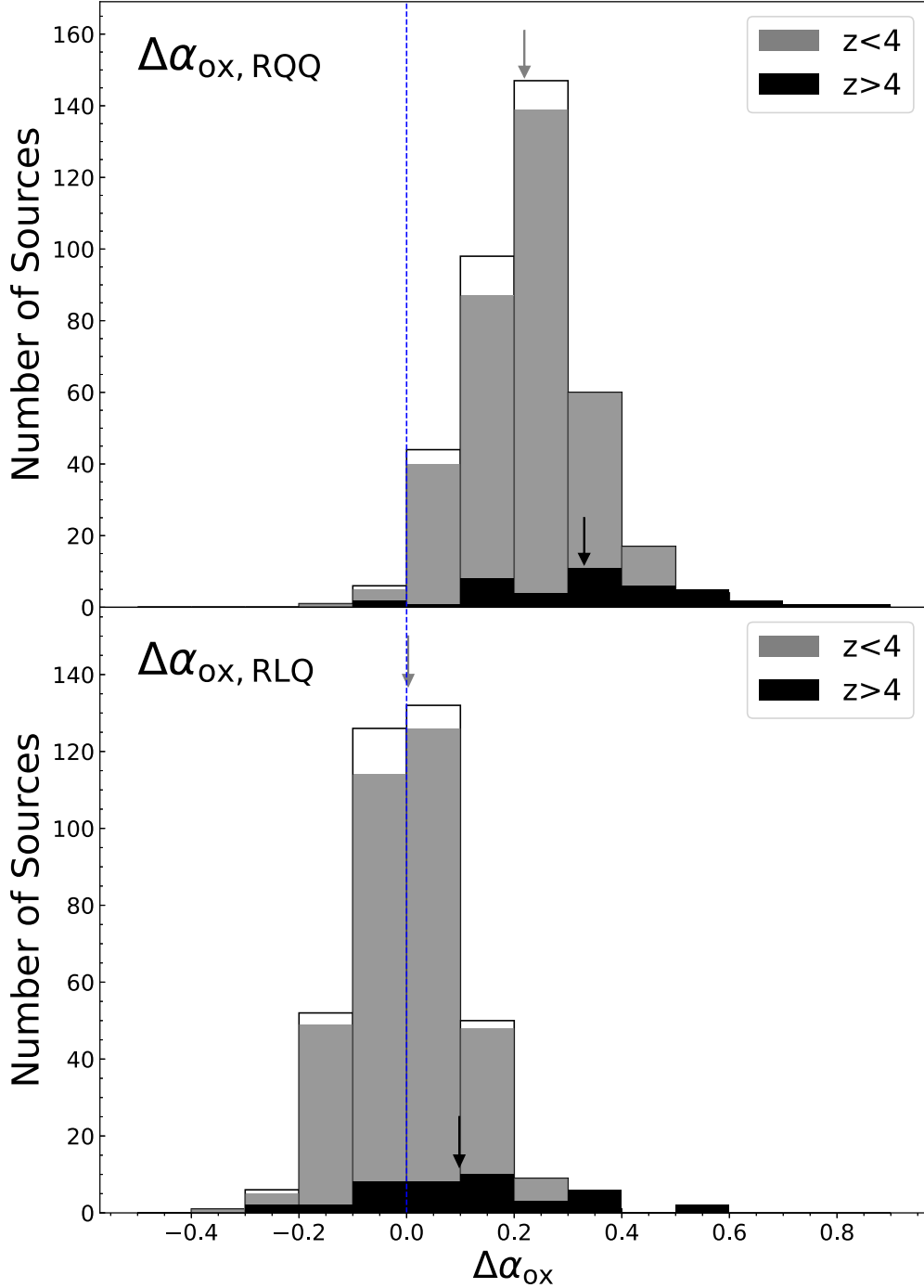


Figure 6. The grey and open bars are histograms of $\Delta\alpha_{\text{ox,RQQ}}$ (upper panel) and $\Delta\alpha_{\text{ox,RLQ}}$ for the optically selected RLQs from Zhu et al. (2020) with $z < 4$, $m_i < 21.33$, and $\log R > 2.5$, where grey bars are X-ray-detected objects and open bars are X-ray undetected objects. The black bars are sources from the combined sample of Wu13, Zhu19, and this work. The downward arrows indicate the medians of $\Delta\alpha_{\text{ox}}$ distributions for HRLQs at $z < 4$ and $z > 4$, respectively.

Pilon 2023) in the following calculations. We used the Kaplan–Meier estimator to estimate the cumulative distribution functions of all data sets. We then calculated the medians of all distributions from the cumulative distribution functions. We used bootstrap (1000 times) to estimate the 1σ uncertainties of the medians we calculated in the previous step. The medians of $\Delta\alpha_{\text{ox,RQQ}}$ for low- z and high- z HRLQs are $0.219^{+0.005}_{-0.004}$ and $0.334^{+0.016}_{-0.034}$, respectively. The medians of $\Delta\alpha_{\text{ox,RLQ}}$ for low- z and high- z HRLQs are $0.003^{+0.005}_{-0.004}$ and $0.098^{+0.016}_{-0.011}$, respectively. The difference between the medians of the

$\Delta\alpha_{\text{ox,RLQ}}$ distributions at $4 < z < 5.5$ and $z < 4$ is $0.095^{+0.017}_{-0.012}$. Our results imply that the X-ray emission of high- z HRLQs is $1.77^{+0.19}_{-0.12}$ times stronger than that of their low- z counterparts. After that, we used the Peto–Peto test implemented in the LIFELINES package to test the significance of the difference between $\Delta\alpha_{\text{ox}}$ distributions of low- z and high- z HRLQs. The statistical test shows a 5.33σ ($p = 5.01 \times 10^{-8}$) difference for $\Delta\alpha_{\text{ox,RQQ}}$ distributions and a 4.90σ ($p = 4.74 \times 10^{-7}$) difference for $\Delta\alpha_{\text{ox,RLQ}}$ distributions. To illustrate the redshift evolution of $\Delta\alpha_{\text{ox,RLQ}}$, we plotted $\Delta\alpha_{\text{ox,RLQ}}$ versus redshift

for the low redshift HRLQ comparison sample (grey plus signs) and the $4 < z < 5.5$ HRLQ sample (black squares) in the left panel of Fig. 7.

We performed a two-sample Kolmogorov–Smirnov (KS) test on the $\log R$ distributions of the $4 < z < 5.5$ HRLQ sample and the $z < 4$ HRLQ comparison sample. With the null hypothesis that the $\log R$ distributions from the two samples are the same, the KS test gave a p -value of 0.95. We also performed a similar KS test on the radio flux distributions and found a p -value of 0.30. The medians (σ_{NMAD}^9) of the $\log R$ distributions of $4 < z < 5.5$ HRLQs and $z < 4$ HRLQs are $3.04_{-0.09}^{+0.02}$ (0.43) and $2.98_{-0.03}^{+0.04}$ (0.44), respectively. Similarly, for the \log radio flux distributions of the high- z and low- z HRLQs, the medians (σ_{NMAD}) are $-24.16_{-0.03}^{+0.03}$ (0.65) and $-24.19_{-0.01}^{+0.07}$ (0.52), respectively. Therefore, both the $\log R$ values and radio fluxes are consistent among the two samples. Thus, we do not need an explicit cut on $\log R$ or radio fluxes.

The results from Zhu19 indicate that the X-ray enhancement of high- z HRLQs is a factor of $1.9_{-0.4}^{+0.5}$ at a 4.07σ significance level considering the differences between $\Delta\alpha_{\text{ox,RLQ}}$ distributions of low- z and high- z HRLQs. Compared to Zhu19, our results indicate a slightly lower X-ray enhancement factor (though statistically consistent within uncertainties) at a higher significance level. The X-ray enhancement factor for our results is smaller because only five out of nine newly added $4 < z < 5.5$ HRLQs have positive $\Delta\alpha_{\text{ox,RLQ}}$. However, since the sample size has been improved from 24 (the flux-limited sample in Zhu19) to 41, the significance level of the X-ray enhancement has been improved.

4.2 X-ray enhancements of $z > 5.5$ RLQs

Referring to the middle and lower panels of Fig. 5, the positions of the seven $z > 5.5$ RLQs are generally higher than the comparison sample. All seven objects have positive $\Delta\alpha_{\text{ox,RQQ}}$ and non-negative $\Delta\alpha_{\text{ox,RLQ}}$. Five of them have $\Delta\alpha_{\text{ox,RLQ}} \geq 0.10$, and three stand out with $\Delta\alpha_{\text{ox,RLQ}} \geq 0.30$.

We used the sample of optically selected RLQs from Zhu et al. (2020) with $m_i \approx m_{1450} < 21.68$ as the comparison sample. Here, the flux limit is the m_{1450} of the faintest $z > 5.5$ RLQ. The low-redshift comparison sample of $z > 5.5$ RLQs differs from that of $4 < z < 5.5$ by removing the $\log R > 2.5$ and $z < 4$ conditions and changing the flux limit. We then followed the methods used in Section 4.1 to calculate the medians of the $\Delta\alpha_{\text{ox}}$ distributions and test the significance levels of the differences between the $\Delta\alpha_{\text{ox}}$ distributions for RLQs at $z \lesssim 5$ and $z > 5.5$. The medians of $\Delta\alpha_{\text{ox,RQQ}}$ at $z \lesssim 5$ and $z > 5.5$ are $0.173_{-0.006}^{+0.007}$ and $0.269_{-0.025}^{+0.167}$, respectively. The medians of $\Delta\alpha_{\text{ox,RLQ}}$ at $z \lesssim 5$ and $z > 5.5$ are $-0.007_{-0.006}^{+0.005}$ and $0.160_{-0.060}^{+0.140}$, respectively. The difference between the medians of the $\Delta\alpha_{\text{ox,RLQ}}$ distributions at $z > 5.5$ and $z \lesssim 5$ is $0.167_{-1.47}^{+0.140}$. This corresponds to an X-ray enhancement factor of $2.72_{-1.47}^{+3.58}$. The large uncertainties are due to the small sample size at $z > 5.5$. The statistical test shows a 3.65σ ($p = 1.30 \times 10^{-4}$) difference for the $\Delta\alpha_{\text{ox,RQQ}}$ distributions and a 4.91σ ($p = 4.61 \times 10^{-7}$) difference for the $\Delta\alpha_{\text{ox,RLQ}}$ distributions. The results are not significantly affected if the potentially heavily absorbed source, PSO J172 + 18, is removed. Following Section 4.1, we plotted $\Delta\alpha_{\text{ox,RLQ}}$ versus redshift for the

low-redshift RLQ comparison sample (grey plus signs) and the $z > 5.5$ RLQ sample (black triangles) in the right panel of Fig. 7.

A KS test on the $\log R$ distributions of the $z > 5.5$ RLQ sample and its low-redshift comparison sample gives a p -value of 0.07. A similar KS test on radio flux distributions gives a p -value of 0.003. The KS tests suggest that the $\log R$ values, as well as the radio fluxes, are marginally different among the two samples. If such differences do exist, the low-redshift comparison sample could only bias towards higher $\log R$ (see Fig. 5) and radio fluxes. Since objects with lower $\log R$ and radio fluxes are expected to have less jet-linked X-ray emission, we conservatively did not apply an upper limit on $\log R$ or radio fluxes for the comparison sample.

4.3 Spectral energy distributions

To compare the broadband spectral energy distributions (SEDs) of HRLQs at $4 < z < 5.5$ and RLQs at $z > 5.5$ with their low- z counterparts, we constructed the SEDs for the nine newly added $4 < z < 5.5$ HRLQs and the seven $z > 5.5$ RLQs. The SEDs of the remaining $4 < z < 5.5$ HRLQs can be found in Wu13 and Zhu19. This comparison serves as an additional test of X-ray enhancements of $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs. The multiwavelength photometric data were collected from the following sources:

(i) Radio: See Table 5 and its footnotes for detailed information about the available radio frequencies for each source.

(ii) Submillimetre: We included submillimetre photometry for $z > 5.5$ RLQs. The flux densities at 1.2 mm of CFHQS J1429 + 5447 and PSO J352 – 15 are taken from Khusanova et al. (2022). The flux densities at 1.2 mm of VIK J2318 – 3113 and SDSS J0836 + 0054 are taken from Venemans et al. (2020) and Petric et al. (2003), respectively. The flux densities at 850 μm of PSO J055 – 00 and PSO J135 + 16 are taken from Li et al. (2020). PSO J055 – 00 is a non-detection; we took its 2σ upper limit.

(iii) Mid-infrared: The mid-infrared flux densities are taken from the *WISE* all-sky catalogue (Wright et al. 2010) except for SDSS J1548 + 3335, PSO J055 – 00, VIK J2318 – 3113, PSO J352 – 15, and PSO J172 + 18, which are non-detections in the *WISE* all-sky catalogue. We retrieved the *W1* and *W2* magnitudes of the first four sources from the CatWISE 2020 catalogue (Marocco et al. 2021). We used the *WISE* all-sky catalogue whenever possible since the CatWISE catalogue did not provide *W3* and *W4* magnitudes. Following Bañados et al. (2021), we took the *W1* and *W2* magnitudes of PSO J172 + 18 from the DESI Legacy Imaging Surveys (DECaLS; Dey et al. 2019).

(iv) Near-infrared: The flux densities in NIR bands are taken from the UKIRT Hemisphere Survey (UHS; Dye et al. 2018), the VISTA Kilo-degree Infrared Galaxy Survey (VIKING; Edge et al. 2013), the VISTA Hemisphere Survey (VHS; McMahon et al. 2013), or dedicated follow-up observations. SDSS J1253+5248 and SDSS J1655 + 2834 only have *J*-band detections from UHS. PSO J055 – 00 has *J*, *H*, and *K* band detections from VHS. SDSS J0836 + 0054 and VIK J2318 – 3113 have *J*, *H*, and *K* band detections from VIKING. PSO J352 – 15 has *Y* and *J* band detections from VHS. CFHQS J1429 + 5447 has *J*-band detection from the Canada–France High- z Quasar Survey (CFHQS; Willott et al. 2010). SDSS J1548 + 3335 was covered by UHS but not detected in any band. Due to our particular interest in this source, we set an upper limit for its *J*-band flux by taking the maximum *J*-band magnitude among all detections within 1 arcmin of it. We took *J*, *H*, and *K* band magnitudes for PSO J172 + 18 from follow-up observations reported by Bañados et al. (2021).

⁹ $\sigma_{\text{NMAD}} = 1.4826 \times \text{median absolute deviation (MAD)}$. This is a robust estimator of standard deviation.

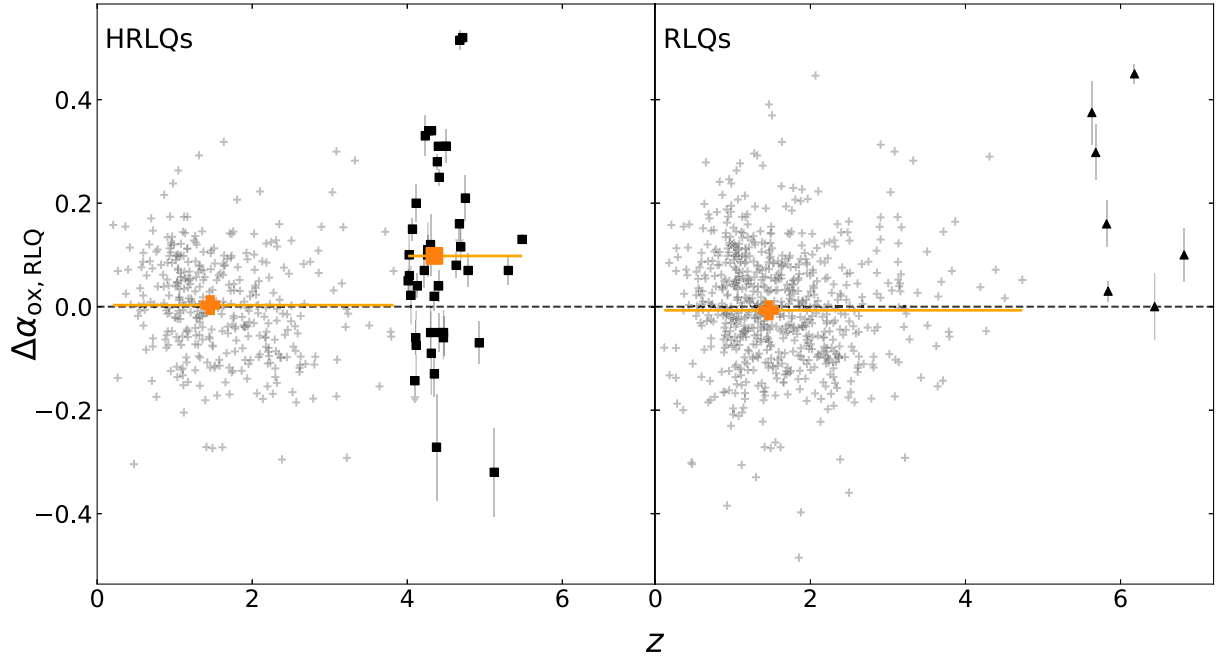


Figure 7. $\Delta\alpha_{\text{ox,RLQ}}$ versus redshift for HRLQs (left panel) and RLQs (right panel). **Left:** The grey plus signs represent the low-redshift HRLQ comparison sample. The squares are 41 HRLQs at $4 < z < 5.5$. The orange plus sign represents the median $\Delta\alpha_{\text{ox,RLQ}}$ of the low-redshift HRLQ comparison sample. The orange square represents the median $\Delta\alpha_{\text{ox,RLQ}}$ of the $4 < z < 5.5$ HRLQ sample. **Right:** The grey plus signs represent the low-redshift RLQ comparison sample. The triangles are seven RLQs at $z > 5.5$. The orange plus sign represents the median $\Delta\alpha_{\text{ox,RLQ}}$ of the low-redshift RLQ comparison sample. The orange triangle represents the median $\Delta\alpha_{\text{ox,RLQ}}$ of the $z > 5.5$ RLQ sample. For both panels, orange horizontal error bars represent redshift ranges of relevant data sets. Orange vertical error bars represent 1σ uncertainties of the medians estimated using the bootstrap.

(v) Optical: Considering the effects of the Ly α forest, we took SDSS r , i , and z magnitudes and Pan-STARRS y magnitudes for $4 < z < 5.5$ objects. For objects with larger redshift ($z > 5.5$), we took Pan-STARRS z and y magnitudes. VIK J2318 – 3113 is not covered by Pan-STARRS.

(vi) X-ray: The flux densities at observed-frame 2 keV of SDSS J0836 + 0054, CFHQS J1429 + 5447, and PSO J352 – 15 were retrieved from Brandt et al. (2002), Medvedev et al. (2021), and Connor et al. (2021), respectively. The observed-frame 2 keV flux densities of all other sources are from this paper.

We calculated the monochromatic luminosities using flux densities and distances, which are derived from redshifts. The constructed SEDs for $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs are shown in Figs 8 and 9. Both figures are ordered by ascending RA. Following Wu13 and Zhu19, the composite SEDs for the 10 HRLQs from Shang et al. (2011) with comparable optical luminosity ($\log \lambda L_{\lambda}(3000 \text{ \AA}) > 45.9$) and radio loudness ($2.9 < \log R < 3.7$) are plotted for comparison in Figs 8 and 9. Considering the radio-loudness of $z > 5.5$ RLQs ($1.21 < \log R < 3.18$), we also plotted the composite spectrum for RQQs retrieved from Shang et al. (2011) using dotted lines in Fig. 9. The composite SEDs are normalized to the observed fluxes at 2500 \AA .

Four out of nine newly added HRLQs have higher luminosities at rest frame 2 keV (the rightmost dotted vertical grey line of each panel) than the comparison SEDs. The X-ray luminosities of the remaining five sources are comparable to the comparison SED if the uncertainties of Γ_{X} are considered. Combining the SED comparison results from Wu13, Zhu19, and our work, 20 out of 41 HRLQs show apparent X-ray excesses. Indeed, all 20 objects have $\Delta\alpha_{\text{ox,RLQ}} \geq 0.05$, indicating that the SED comparison method is consistent

with the method described in Section 3.3. Nearly all of them have X-ray luminosities that are at least comparable to the comparison SED.

The rest frame 2 keV luminosities for three out of seven $z > 5.5$ RLQs are higher than the comparison composite SED of RLQs. The three objects that show apparent X-ray enhancements under the SED comparison are those with the largest $\Delta\alpha_{\text{ox,RLQ}}$ values among the $z > 5.5$ RLQs.

5 DISCUSSION

5.1 Implications for the fractional IC/CMB model

Historically, it has been thought that the small-scale X-ray core emission of RLQs is dominated by a jet-linked component (e.g. Worrall et al. 1987). To accommodate the mild X-ray enhancements of high- z HRLQs, Wu13 proposed a *fractional IC/CMB* model, where the IC/CMB process mainly operates within a few kpc from the central SMBH and the contribution from the IC/CMB process is only a small fraction of the total X-ray emission at low redshifts. None of the objects in our sample shows extended X-ray emission. Considering that the 0.5 arcsec angular resolution of *Chandra* corresponds to a physical size of 3.4 kpc at $z = 4.35$ (the median redshift of the $4 < z < 5.5$ HRLQ sample), the X-ray jets (if present) are likely smaller than ≈ 5 kpc. This is consistent with the assumptions of the fractional IC/CMB model. X-ray observations with higher spatial resolution are required to constrain the scale of the jet. An alternative approach is to observe gravitationally lensed RLQs at high redshifts, whose X-ray emission is expected to have a significant contribution from the jet. However, only a

Table 5. Multiwavelength properties of the 41 HRLQs at $4 < z < 5.5$ (Wu13, Zhu19; this work) and 7 RLQs at $z > 5.5$. (1) Object name. (2) Flux density at observed-frame 150 MHz, taken from the TIFR GMRT Sky Survey alternative data release (TGSS ADR; Intema et al. 2017). (3) Flux density at observed-frame 326 MHz, taken from the Westerbork Northern Sky Survey (Rengelink et al. 1997). (4) Flux density at observed-frame 366 MHz, taken from the Texas Survey of Radio Sources (Douglas et al. 1996). (5) Flux density at observed-frame 1.4 GHz, taken from FIRST or NVSS. (6) Flux density at observed-frame 3 GHz, taken from the VLASS Epoch 1 Quick Look Catalog (Gordon et al. 2021) (7) Flux density at observed-frame 5 GHz, taken from the Green Bank 6-cm survey (GB6; Gregory et al. 1996) unless otherwise specified. (8) Radio spectral index between observed-frame 1.4 GHz and a lower frequency. (9) Radio spectral index between observed-frame 1.4 GHz and a higher frequency. (10) Radio spectral index at observed-frame 1.4 GHz, taking the average of α_{low} and α_{high} . (11) VLBI observed band that is closest to 1.4 GHz. (12) VLBI flux density observed at the band in (11). (13) The flux density at corresponding VLBI bands inferred from $f_{1.4\text{GHz}}$ assuming radio spectral slope to be α_{high} . (14) Angular size of the compact component of the VLBI image. If the best-fitting Gaussian component is elliptical, we adopt $\theta_{\text{VLBI}} = \sqrt{\theta_{\text{maj}}\theta_{\text{min}}}$, where θ_{maj} and θ_{min} are angular sizes of the major and minor axes, respectively. θ_{VLBI} is not provided if the source does not have available size estimation (observed by astrometric calibration surveys or not explicitly reported by authors) or extended structures have significant contributions to the total flux. (15) VLBI references: (a) Coppejans et al. (2016), (b) Petrov (2013), (c) Gordon et al. (2016), (d) Krezinger et al. (2022), (e) Petrov (2021), (f) Frey et al. (2010), (g) Frey et al. (2018), (h) Momjian, Petric & Carilli (2004), (i) Frey et al. (2015), (j) Hunt et al. (2021), (k) Cao et al. (2017), (l) Pushkarev & Kovalev (2012), (m) Frey et al. (2003), (n) Momjian et al. (2021), (o) Frey et al. (2011), (p) Zhang et al. (2022), (q) Momjian et al. (2018), (r) Astrogeo: <http://astrogeo.org>.

Object name	z	$f_{150\text{MHz}}$ (mJy)	$f_{326\text{MHz}}$ (mJy)	$f_{366\text{MHz}}$ (mJy)	$f_{1.4\text{GHz}}$ (mJy)	$f_{5\text{GHz}}$ (mJy)	$f_{5\text{GHz}}$ (mJy)	α_{low}	α_{high}	α_r	$\log R$	Γ_X	α_{ox}	$\Delta\alpha_{\text{ox,ROQ}}$	$\Delta\alpha_{\text{ox,RLQ}}$	VLBI band (GHz)	f_{VLBI} (mJy)	f_{lowes} (mJy)	θ_{VLBI} (mas)	Ref.	
(1)		(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)					(11)	(12)	(13)	(14)	(15)		
HRLQs at $4 < z < 5.5$ from this paper																					
SDSS J0825 + 1234	4.377	-	-	-	16.68 ± 0.15	8.96 ± 0.12	-	-	-0.82	-0.82	2.82	1.09 ^{+1.47} _{-0.52}	-1.69	-0.08	-0.27	-	-	-	-	-	
SDSS J0940 + 0526	4.503	432.7 ± 44.1	-	-	55.66 ± 0.14	37.68 ± 0.14	-	-0.92	-0.51	-0.72	3.32	2.21 ^{+0.58} _{-0.38}	-1.07	0.55	0.31	1.7	18.3	50.4	1.91	(a)	
SDSS J1047 + 0947	4.233	21.0 ± 3.3	-	-	18.89 ± 0.15	25.47 ± 0.12	-	-0.05	0.39	0.17	2.59	-	-	-	-	-	-	-	-	-	
SDSS J1156 + 4443	4.310	282.9 ± 28.6	220.0 ± 4.0	-	66.23 ± 0.14	35.13 ± 0.14	-	-0.82	-0.83	-0.83	3.59	>1.66	-1.46	0.14	-0.12	-	-	-	-	-	-
SDSS J1253 + 5248	4.115	91.9 ± 10.5	89.0 ± 3.3	-	55.92 ± 0.15	40.52 ± 0.18	-	-0.32	-0.42	-0.37	3.58	1.52 ^{+1.40} _{-0.43}	-1.39	0.18	-0.07	-	-	-	-	-	-
SDSS J1400 + 3149	4.690	-	-	-	20.16 ± 0.14	11.33 ± 0.13	-	-	-0.76	-0.76	2.81	1.76 ^{+0.76} _{-0.38}	-1.33	0.31	0.12	1.7	10.7	17.4	3.01	(a)	
SDSS J1538 + 4244	4.099	-	-	-	11.71 ± 0.13	6.80 ± 0.13	-	-	-0.71	-0.71	2.71	-	-1.56	<-0.04	-	-	-	-	-	-	
SDSS J1548 + 3335	4.678	135.1 ± 14.9	107.0 ± 3.6	-	37.62 ± 0.14	22.01 ± 0.11	-	-0.72	-0.70	-0.71	3.08	2.49 ^{+0.41} _{-0.21}	-0.90	0.73	0.51	1.7	10.0	32.8	1.76	(a)	
SDSS J1655 + 2834	4.048	-	-	-	23.01 ± 0.14	23.63 ± 0.11	22 ± 4	-	-0.04	-0.04	2.75	1.42 ^{+0.92} _{-0.40}	-1.41	0.21	0.02	-	-	-	-	-	-
HRLQs at $4 < z < 5.5$ from Wu13 and Zhu19																					
PSS 0121 + 0347	4.130	-	-	-	72.95 ± 0.20	58.11 ± 0.17	51 ± 7	-	-0.28	-0.28	2.57	2.10 ^{+0.40} _{-0.30}	-1.47	0.28	0.04	2.2	65.0	64.3	-	(b)	
R3 0254 + 434	4.067	72.2 ± 7.6	108.0 ± 3.9	-	148.10 ± 5.30	325.16 ± 1.42	159 ± 14	0.22	1.03 ^a	0.63	3.29	1.44 ^{+0.21} _{-0.11}	-1.23	0.44	0.15	2.3	353.0	246.8	-	(c)	
SDSS J0304 + 0046	4.266	36.2 ± 5.7	-	-	20.64 ± 0.11	16.33 ± 0.09	-	-0.25	-0.31	-0.28	3.15	>1.79	-1.23	0.35	0.11	1.7	15.0	19.4	4.78	(d)	
PMN J0324 - 2918	4.630	51.7 ± 6.8	-	-	236.50 ± 7.10	177.33 ± 1.09	-	0.68	-0.38	0.15	2.95	1.80 ^{+0.40} _{-0.40}	-1.40	0.35	0.08	2.3	238.0	199.2	-	(a)	
PMN J0525 - 3343	4.401	73.5 ± 11.7	-	-	188.30 ± 5.70	107.93 ± 1.01	-	0.42	-0.73	-0.15	2.90	1.67 ^{+0.02} _{-0.02}	-1.17	0.58	0.31	4.3	71.0	83.0	-	(e)	
SDSS J0813 + 3508	4.929	175.1 ± 18.8	153.0 ± 3.8	-	48.99 ± 0.16	23.94 ± 0.14	-	-0.78	-0.94	-0.86	2.61	1.35 ^{+0.44} _{-0.17}	-1.55	0.16	-0.07	1.6	17.1	43.2	1.18	(f)	
SDSS J0835 + 1825	4.412	72.8 ± 7.9	-	-	51.49 ± 0.13	56.16 ± 0.13	40 ± 5	-0.16	-0.20	-0.18	3.19	1.56 ^{+0.11} _{-0.11}	-1.12	0.51	0.25	-	-	-	-	-	
Q0906 + 6930	5.480	-	35.0 ± 3.9	-	92.80 ± 2.80	106.27 ± 0.66	106 ± 10	0.67	0.10	0.39	3.01	1.60 ^{+0.10} _{-0.10}	-1.31	0.40	0.13	2.3	118.3	97.5	0.98	(g)	
SDSS J0913 + 5919	5.122	-	-	-	17.45 ± 0.16	9.40 ± 0.11	-	-	-0.81	-0.81	2.72	>0.71	-1.76	-0.09	-0.32	1.4	19.0	17.4	1.3	(h)	
SDSS J1021 + 2209	4.262	444.5 ± 44.7	-	-	134.67 ± 0.47	127.64 ± 0.20	108 ± 10	-0.53	-0.17	-0.35	3.75	>1.30	-1.20	0.41	0.10	4.3	97.0	111.2	-	(e)	
SDSS J1026 + 2542	5.304	422.9 ± 42.4	-	406 ± 24	230.81 ± 0.14	143.33 ± 0.18	142 ± 13	-0.42	-0.38	-0.40	3.54	1.73 ^{+0.32} _{-0.31}	-1.31	0.39	0.07	1.7	137.5	213.6	-	(i)	
RX J1028 - 0844	4.276	127.4 ± 13.3	-	-	269.20 ± 8.10	124.38 ± 0.16	-	0.33	-1.01	-0.34	3.33	1.40 ^{+0.03} _{-0.03}	-1.09	0.63	0.34	2.3	147.0	163.0	-	(j)	
SDSS J1113 + 4645	4.468	34.0 ± 4.2	-	-	24.91 ± 0.25	22.13 ± 0.12	20 ± 4	-0.14	-0.17	-0.16	2.81	1.51 ^{+0.59} _{-0.21}	-1.47	0.11	-0.05	-	-	-	-	-	
PMN J1155 - 3107	4.300	-	-	-	82.00 ± 2.50	163.71 ± 1.48	-	-	0.91	0.91	2.73	>1.33	-1.36	0.36	0.12	2.3	129.9	128.8	-	(c)	
SDSS J1235 - 0003	4.673	-	-	-	18.27 ± 0.15	11.61 ± 0.15	-	-	-0.59	-0.59	3.05	-	-1.22	0.39	0.16	1.4	18.8	18.3	<3.3	(h)	
SDSS J1237 + 6517	4.301	115.5 ± 11.7	81.0 ± 3.3	-	25.50 ± 0.90	15.70 ± 0.24	-	-0.79	-0.64	-0.71	2.50	1.92 ^{+0.90} _{-0.30}	-1.52	0.16	-0.05	-	-	-	-	-	
SDSS J1242 + 5422	4.750	19.7 ± 3.1	30.0 ± 2.8	-	19.74 ± 0.13	10.41 ± 0.12	-	-0.29	-0.84	-0.56	2.67	2.38 ^{+1.13} _{-0.33}	-1.24	0.43	0.21	1.6	17.7	17.7	0.67	(f)	
CLASS J1325 + 1123	4.415	-	-	-	69.39 ± 0.14	53.02 ± 0.14	62 ± 8	-	-0.09	-0.09	2.72	1.80 ^{+0.50} _{-0.40}	-1.53	0.19	-0.05	1.7	62.7	68.2	0.76	(d)	

Table 5 – continued

Object name	z	f_{150} MHz (mJy)	f_{326} MHz (mJy)	f_{566} MHz (mJy)	$f_{1.4}$ GHz (mJy)	f_{5} GHz (mJy)	f_{5} GHz (mJy)	f_{5} GHz (mJy)	α_{low}	α_{high}	α_r	$\log R$	Γ_X	α_{ox}	$\Delta\alpha_{\text{ox,ROQ}}$	$\Delta\alpha_{\text{ox,RLO}}$	VLBI band (GHz)	f_{VLBI} (mJy)	f_{lowes} (mJy)	θ_{VLBI} (mas)	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)	(16)	(17)	(18)	(19)	(20)	(21)	(22)
SDSS J1348 + 1935	4.404	52.1 ± 6.9	–	–	49.25 ± 0.15	42.75 ± 0.13	38 ± 5	–0.03	–0.20	–0.11	2.97	1.56 ^{+0.34} _{–0.17}	–1.37	0.29	0.04	–	–	–	–	–	–
SDSS J1412 + 0624	4.467	122.8 ± 16.2	–	–	43.04 ± 0.14	27.97 ± 0.15	34 ± 6	–0.47	–0.19	–0.33	2.70	1.33 ^{+0.43} _{–0.38}	–1.51	0.18	–0.06	1.7	18.8	41.5	<2.66	(d)	
SDSS J1420 + 1205	4.027	403.7 ± 40.5	–	248 ± 29	83.77 ± 0.14	48.41 ± 0.45	47 ± 6	–0.81	–0.45	–0.63	3.05	1.61 ^{+0.35} _{–0.32}	–1.34	0.33	0.06	1.7	47.9	76.8	–	(k)	
GB 1428 + 4217	4.715	174.3 ± 18.0	238.0 ± 3.2	222 ± 18	211.27 ± 0.15	125.79 ± 0.13	337 ± 30	–0.08	0.37	0.14	3.06	1.73 ^{+0.08} _{–0.05}	–0.93	0.80	0.52	2.3	150.0	253.9	–	(l)	
GB 1508 + 5714	4.313	202.2 ± 20.7	218.0 ± 3.6	222 ± 15	248.07 ± 0.14	243.22 ± 1.44	292 ± 26	0.09	0.13	0.11	3.87	1.55 ^{+0.05} _{–0.05}	–0.96	0.67	0.34	2.3	276.6	264.6	–	(l)	
SDSS J1535 + 0254	4.388	150.1 ± 15.3	–	–	78.82 ± 0.15	46.13 ± 0.16	53 ± 7	–0.29	–0.31	–0.30	3.14	1.32 ^{+0.10} _{–0.09}	–1.12	0.55	0.28	5	68.0	53.1	–	(r)	
SDSS J1605 + 2728	4.024	43.6 ± 4.9	–	–	11.66 ± 0.14	6.16 ± 0.23	–	–0.59	–0.84	–0.71	2.61	–	–1.31	0.30	0.10	–	–	–	–	–	–
SDSS J1612 + 4702	4.350	139.2 ± 14.6	118.0 ± 3.6	–	52.26 ± 0.15	44.01 ± 0.13	30 ± 4	–0.56	–0.44	–0.50	3.07	> 1.50	–1.53	0.13	–0.13	–	–	–	–	–	–
SDSS J1659 + 2101	4.784	27.1 ± 4.0	–	–	28.73 ± 0.15	23.43 ± 1.10	–	0.03	–0.27	–0.12	2.56	1.75 ^{+0.40} _{–0.36}	–1.39	0.30	0.07	1.6	29.3	27.7	3.07	(f)	
GB 1713 + 2148	4.011	1080.6 ± 108.1	–	1118 ± 50	446.40 ± 14.90	248.42 ± 1.58	306 ± 27	–0.68	–0.30	–0.49	4.50	1.63 ^{+0.24} _{–0.23}	–1.16	0.42	0.05	4.3	55.0	318.8	–	(e)	
PMN J1951 + 0134	4.114	47.4 ± 7.8	–	–	99.10 ± 3.00	254.90 ± 0.22	151 ± 14	0.33	1.24 ^a	0.79	3.04	1.54 ^{+0.33} _{–0.30}	–1.23	0.45	0.20	2.3	259.0	183.4	–	(c)	
PMN J2134 – 0419	4.346	554.4 ± 56.2	–	622 ± 58	303.79 ± 0.15	313.74 ± 2.09	–	–0.53	0.04	–0.25	3.40	1.70 ^{+0.38} _{–0.18}	–1.38	0.33	0.02	1.7	236.6	306.2	1.42	(k)	
SDSS J2220 + 0025	4.220	644.7 ± 64.5	–	–	92.65 ± 0.10	40.24 ± 0.45	37 ± 7	–0.87	–0.72	–0.79	3.26	> 1.76	–1.29	0.34	0.07	1.7	8.2	80.6	–	(k)	
PMN J2314 + 0201	4.110	103.8 ± 11.7	–	–	117.83 ± 0.12	87.81 ± 0.14	84 ± 9	0.06	–0.27	–0.10	3.13	1.33 ^{+0.33} _{–0.15}	–1.47	0.21	–0.06	5	77.6	83.6	–	(r)	
PSO J055 – 00	5.68	–	–	–	2.14 ± 0.14	1.01 ± 0.13 ^b	–	–	–0.99	–0.99	1.94	2.45 ^{+1.20} _{–0.51}	–1.22	0.42	0.30	–	–	–	–	–	–
SDSS J0836 + 0054	5.82	–	–	–	1.53 ± 0.15	–	0.58 ± 0.06 ^c	–0.76 ^d	–0.33	–0.55	1.21	1.97 ^{+0.85} _{–0.32}	–1.53	0.19	0.12	1.6	1.1	1.5	–	(m)	
PSO J135 + 16	5.63	–	–	–	3.99 ± 0.15	2.62 ± 0.21	–	–	–0.55	–0.55	2.36	2.97 ^{+3.77} _{–0.51}	–1.09	0.53	0.38	–	–	–	–	–	–
PSO J172 + 18	6.82	<8.5 ^e	–	–	1.02 ± 0.14	–	–	–	–1.31 ^f	–1.31	–	–	–	–	–	–	1.5	0.50	0.51 ^g	5.9	(n)
CFHQS J1429 + 5447	6.18	–	–	–	2.93 ± 0.15	2.07 ± 0.11	–	–0.62 ^h	–0.45	–0.54	2.24	2.50 ^{+0.20} _{–0.20}	–0.88	0.75	0.60	1.6	3.3	2.8	2.63	(o)	
VIK J2318 – 3113	6.44	–	–	–	0.52 ± 0.17 ⁱ	0.40 ± 0.15 ^j	0.104 ± 0.034 ^k	–0.44 ^l	–1.16	–0.80	–	–	–	–	–	–	1.57	0.48	0.44	2.3	(p)
PSO J352 – 15	5.84	163.1 ± 20.7	–	–	14.90 ± 0.70	7.89 ± 0.15	–	–1.07	–0.83	–0.95	3.18	1.99 ^{+0.29} _{–0.28}	–1.41	0.20	–0.03	1.5	6.57	14.1	–	(q)	

Notes. ^a $f_{5\text{GHz}}$ of these objects are substantially larger than $f_{1.4\text{GHz}}$ and $f_{5\text{GHz}}$. Use $f_{5\text{GHz}}$ to calculate α_{high} rather than the preferred $f_{5\text{GHz}}$.

^b Forced photometry using AEGEAN.

^c $f_{5\text{GHz}}$ of SDSS J083643.85 + 005453.3 is taken from Petric et al. (2003).

^d α_{low} is calculated from $f_{1.4\text{GHz}}$ and $f_{326\text{MHz}}$ (2.47 mJy; Shao et al. 2020).

^e A 3 σ upper limit obtained from Bañados et al. (2021).

^f α_{high} is calculated from flux densities at observed-frame 1.52 and 2.87 GHz obtained from simultaneous follow-up radio observations reported by Bañados et al. (2021) instead of extrapolating from FIRST observation at 1.4 GHz to avoid possible variability.

^g f_{lowes} is the flux density at observed-frame 1.52 GHz taken from Bañados et al. (2021) instead of extrapolating from FIRST observation at 1.4 GHz to avoid possible variability.

^h α_{low} is calculated from $f_{1.4\text{GHz}}$ and $f_{440\text{MHz}}$ (Shimwell et al. 2022).

ⁱ $f_{1.4\text{GHz}}$ of VIK J2318 – 3113 is the flux density at observed-frame 1367 MHz taken from the Rapid ASKAP Continuum Survey (RACS; McConnell et al. 2020).

^j $f_{5\text{GHz}}$ of VIK J2318 – 3113 is taken from Ighina et al. (2022b), calculated from the VLASS Epoch 2 Quick Look Image.

^k $f_{5\text{GHz}}$ of VIK J2318 – 3113 is the flux density at observed-frame 5500 MHz taken from Ighina et al. (2022b).

^l α_{low} is calculated from $f_{399\text{MHz}}$ (0.89 mJy; EMU, Norris et al. 2011) and $f_{1.4\text{GHz}}$.

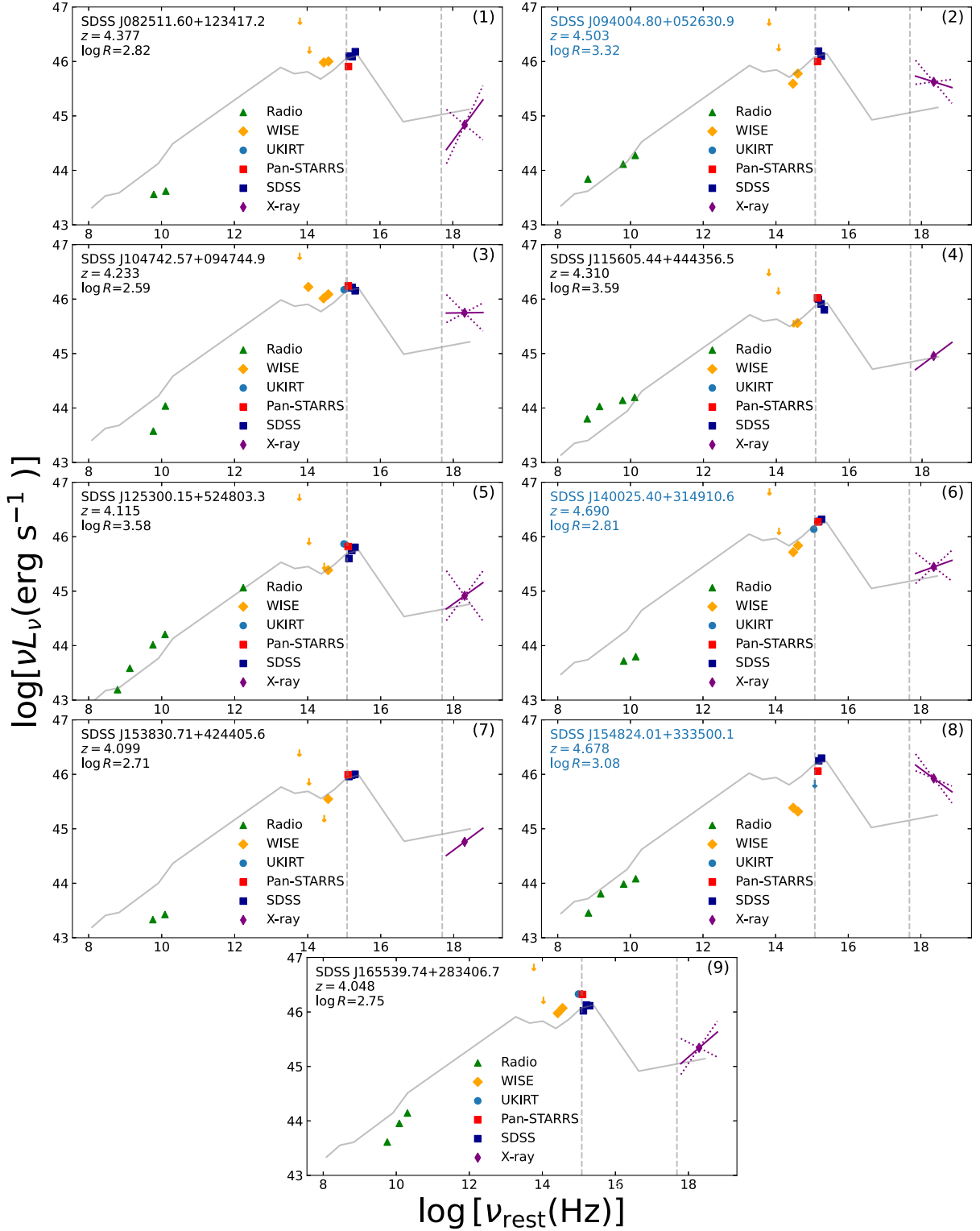


Figure 8. SEDs of the nine newly added $4 < z < 5.5$ HRLQs, ordered by ascending RA. Downward arrows represent upper limits. Objects with black text are *Chandra* Cycle 23 objects. Those with blue text are archival objects. The purple diamonds are located at observed-frame 2 keV . The solid purple lines are X-ray power-law spectra around observed-frame 2 keV derived from photon indices reported in Table 3. Their uncertainties are represented by the dotted purple lines. The solid grey curves are composite SEDs for the 10 HRLQs at $z < 1.4$ from Shang et al. (2011) with comparable optical luminosity and radio loudness, scaled to the flux density at rest frame 2500 \AA . The dotted grey vertical lines are at rest frame 2500 \AA and 2 keV . The name, redshift, and $\log R$ of each object are shown at the upper left of each panel.

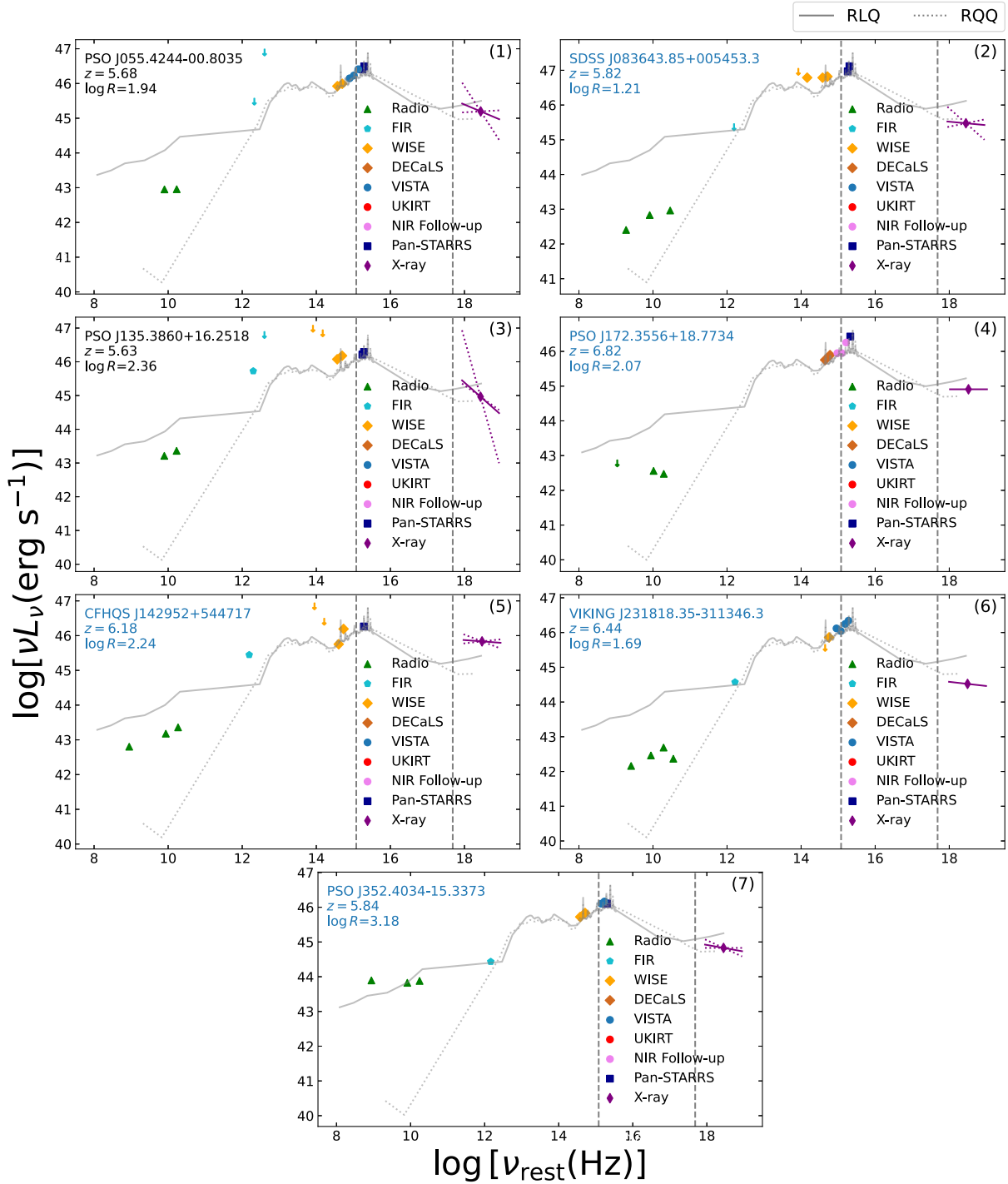


Figure 9. SEDs of the $z > 5.5$ RLQ sample, ordered by ascending RA. Downward arrows represent upper limits. Objects with black text are *Chandra* Cycle 23 objects. Those with blue text are archival objects. The purple diamonds are located at the observed-frame 2 keV. The solid purple lines are X-ray power-law spectra around observed-frame 2 keV derived from photon indices reported in Table 4. Their uncertainties are represented by the dotted purple lines. The solid grey curves are composite SEDs for RLQs from Shang et al. (2011). The dotted grey lines are composite SEDs for RQQs from Shang et al. (2011). All solid grey curves are scaled to the flux density at rest frame 2500 Å. The dotted grey vertical lines are at rest frame 2500 Å and 2 keV. The name, redshift, and $\log R$ of each object are shown at the upper left of each panel.

few gravitationally lensed RLQs, limited to $z \lesssim 3.6$, have been observed in X-rays. Those with the highest redshifts are either only moderately radio loud (Dadina et al. 2016; Dogruel et al. 2020) or have ambiguities in physical interpretation (Schwartz, Spingola & Barnacka 2021). Besides, none of the gravitationally lensed systems

mentioned above shows apparent X-ray enhancements compared to typical RLQs.

The results from Zhu et al. (2020) and Zhu, Timlin & Brandt (2021) may suggest a simpler explanation. Zhu et al. (2020) found that the contribution of the jet-linked component to the X-ray core

emission of RLQs is generally small, with a mean fraction of ≈ 5 per cent. The median redshift of the RLQ sample utilized by Zhu et al. (2020) is 1.5. The small contribution from the jet-linked component could readily explain the X-ray enhancements of high- z HRLQs.

We then modelled the factor of X-ray enhancement as $1 + A[(1 + z)^4 - 1]$, containing a constant component and an IC/CMB component that evolves with redshift following $(1 + z)^4$, to constrain the contribution from the IC/CMB process at different redshifts. A is set to 9.41×10^{-4} to obtain the X-ray enhancement factor of 1.77 at $z = 4.35$. At $z \approx 1.5$, the predicted factor of X-ray enhancement is ≈ 4 per cent, which is consistent with previous studies (e.g. Wu13; Zhu19; Ighina et al. 2019) and the contribution from the jet-linked component found by Zhu et al. (2020). This is also roughly consistent with the jet-to-core X-ray ratio reported by Marshall et al. (2005, 2011, 2018).

5.2 The X-ray enhancements of RLQs at $z > 5.5$

At $z > 5.5$, the X-ray emission of moderately radio-loud quasars may be enhanced as a manifestation of the IC/CMB process in the dense CMB photon field. Indeed, the $z > 5.5$ RLQs show X-ray enhancements as expected if the IC/CMB mechanism plays an important role. However, the $z > 5.5$ RLQs show properties different from the HRLQs at $4 < z < 5.5$.

We compiled multiwavelength radio data for 41 HRLQs at $4 < z < 5.5$ and seven RLQs at $z > 5.5$ in Table 5. We calculated the radio spectral index between 1.4 GHz and a lower frequency, α_{low} , and the radio spectral index between 1.4 GHz and a higher frequency, α_{high} . We then took the average of α_{low} and α_{high} to get α_r , the radio spectral index around observed-frame 1.4 GHz defined as $f \propto \nu^{\alpha_r}$. When calculating α_{low} and α_{high} , we preferred to use frequencies that are further from 1.4 GHz to reduce the effects of measurement uncertainties with the exception that 150 MHz has the lowest priority since it is too far away from 1.4 GHz and the radio spectra of some objects are peaked at frequencies between 150 MHz and 1.4 GHz. The radio data we collected cover rest-frame frequencies of ≈ 0.9 –27 GHz and ≈ 1 –34 GHz for typical $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs (calculated using the median redshift of each sample), respectively. Thus, the redshift difference between the two samples does not significantly affect the rest-frame radio frequencies probed. In Table 5, we used boldface to label GHz peaked sources (GPSs) identified based on the radio data we collected, whose α_r should be treated with caution.

To explore the correlation between X-ray enhancements and radio spectral index, we plotted $\Delta\alpha_{\text{ox,RLQ}}$ versus α_r in Fig. 10 for $4 < z < 5.5$ HRLQs (left panel) and $z > 5.5$ RLQs (right panel). The medians of $\Delta\alpha_{\text{ox,RLQ}}$ of $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs with $\alpha_r < -0.5$ are $0.06_{-0.13}^{+0.04}$ and $0.16_{-0.13}^{+0.14}$, respectively.

Our results suggest that RLQs at $z > 5.5$ with $\alpha_r < -0.5$ tend to have stronger X-ray enhancements than HRLQs at $4 < z < 5.5$ with similar radio spectral indices. Considering that RLQs at $4 < z < 5.5$ do not show X-ray enhancements (e.g. Miller et al. 2011), the X-ray enhancements of RLQs apparently rise significantly at $z \gtrsim 5.5$. It is worth noting that although radio-selected blazars that should have the strongest jet-linked X-ray components have been deliberately removed (see Section 2.2), the X-ray enhancement of our optically selected $z > 5.5$ RLQ sample is still strong. We also note that there is no apparent correlation between $\log R$ and X-ray enhancements for $z > 5.5$ RLQs. The only HRLQ in our $z > 5.5$ RLQ sample (PSO J352 – 15) only shows a marginal X-ray enhancement with $\Delta\alpha_{\text{ox,RLQ}} = 0.03_{-0.02}^{+0.02}$. This does not support the idea that X-ray emission for $z > 5.5$ RLQs is dominated by jets. However, the

lack of correlation between $\log R$ and X-ray enhancements is only suggestive since the $z > 5.5$ RLQ sample is very small.

We also found that the X-ray spectra of $z > 5.5$ RLQs are steeper than those of their low-redshift counterparts while such an X-ray steepening is not found in $4 < z < 5.5$ HRLQs. We plotted Γ_X versus redshift for 333 optically selected RLQs with $z \leq 4.73$ analysed by Zhu, Timlin & Brandt (2021) (small dots) and median Γ_X in four redshift bins ($z = 0$ –1, 1–2, 2–3, and 3–4; large orange dots) in the right panel of Fig. 11.¹⁰ The Zhu, Timlin & Brandt (2021) sample was built upon the Zhu et al. (2020) sample by selecting objects with high-quality X-ray data that could produce reliable Γ_X values. Throughout Fig. 11, blue labels represent objects with $\alpha_r > -0.5$ and green labels represent those with $\alpha_r \leq -0.5$. The median(σ_{NMAD}) of Γ_X for low-redshift RLQs given by Zhu, Timlin & Brandt (2021) is $1.84_{-0.01}^{+0.01}(0.30)$. We then included the six $z > 5.5$ RLQs with available Γ_X values (small triangles) and their median Γ_X (large orange triangle) in Fig. 11 for comparison. The potentially heavily absorbed object, PSO J172 + 18 (see Section 3.2), was not included. We used the Kaplan–Meier estimator to derive the median(σ_{NMAD}) of Γ_X for $z > 5.5$ RLQs, $2.19_{-0.07}^{+0.26}(0.10)$, which is significantly larger than that for low-redshift RLQs.

The small dots in the left panel of Fig. 11 are HRLQs from the Zhu, Timlin & Brandt (2021) sample and the large orange dots are median Γ_X values of HRLQs in redshift bins similar to the right panel. The squares represent $4 < z < 5.5$ HRLQs. The large yellow square represents the median Γ_X value of $4 < z < 5.5$ HRLQs. 38 out of 41 objects in our $4 < z < 5.5$ HRLQ sample have available Γ_X values. The median(σ_{NMAD}) of Γ_X for HRLQs at $z < 4$ and $4 < z < 5.5$ are $1.80_{-0.09}^{+0.08}(0.26)$ and $1.63_{-0.07}^{+0.10}(0.27)$, respectively. The 1σ error bars were calculated using bootstrap. The X-ray spectra of HRLQs at $4 < z < 5.5$ are not steeper compared to their low-redshift counterparts. The steepening of X-ray spectra of $z > 5.5$ RLQs and the lack of it for $4 < z < 5.5$ HRLQs indicate $z > 5.5$ RLQs may be in a different evolutionary stage.

The evolution of X-ray spectral properties of RQQs up to $z \gtrsim 6$ has been investigated by recent studies. Vito et al. (2019) jointly fitted the X-ray spectra of 12 RQQs at $z > 6$ with < 30 net counts and 6 with > 30 net counts from 0.5 to 7 keV. They found an average $\Gamma_X = 2.20_{-0.34}^{+0.39}$ for the sample with < 30 net counts and an average $\Gamma_X = 2.13_{-0.08}^{+0.08}$ for the sample with > 30 net counts. Zappacosta et al. (2023) reported an average $\Gamma_X = 2.4_{-0.1}^{+0.1}$ for a sample of $z > 6$ hyperluminous RQQs ($L_{\text{bol}} \geq 10^{47}$ erg s $^{-1}$). Compared to the canonical value of $\Gamma_X \approx 1.9$ for RQQs at lower redshifts, both studies suggest, although at different significance levels, the steepening of X-ray spectra of $z \gtrsim 6$ RQQs. Zappacosta et al. (2023) proposed that the steepening of X-ray spectra is a manifestation of lower coronal temperature due to disc truncation caused by radiatively driven winds. The Γ_X evolution trend of RQQs (see also fig. 7 in Vito et al. 2019 and fig. 5 in Zappacosta et al. 2023) is similar to that

¹⁰We notice that there is an apparent Γ_X versus redshift trend for $z < 4$ RLQs and HRLQs as is shown in both panels of Fig. 11, which is probably caused by selection biases. The radio-loud nature of objects in Zhu, Timlin & Brandt (2021) is determined using radio data at observed-frame 1.4 GHz, whose rest-frame frequency increases with redshift. At higher rest-frame frequencies, objects with steep radio spectra may drop below detection limits. Thus, objects in the Zhu, Timlin & Brandt (2021) sample tend to have flatter radio spectra at higher redshifts, which suggests more jet contribution and hence flatter X-ray spectra. Aside from that, only bright radio sources can be detected at higher redshifts, resulting in higher $\log R$ values and probably flattening X-ray spectra.

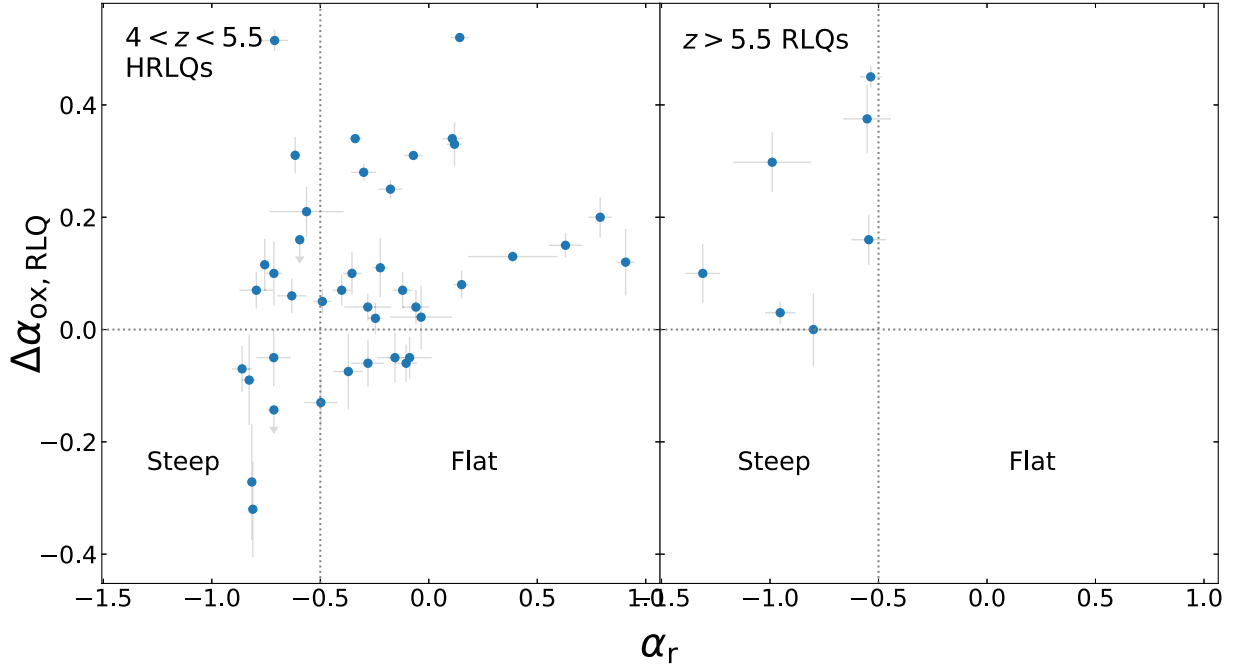


Figure 10. $\Delta\alpha_{\text{ox,RLQ}}$ versus radio spectral index α_r for $4 < z < 5.5$ HRLQs (left panel) and $z > 5.5$ RLQs (right panel). The dotted horizontal line represents $\Delta\alpha_{\text{ox,RLQ}} = 0$. The dotted vertical line represents $\alpha_r = -0.5$, the typical boundary between steep and flat radio spectra.

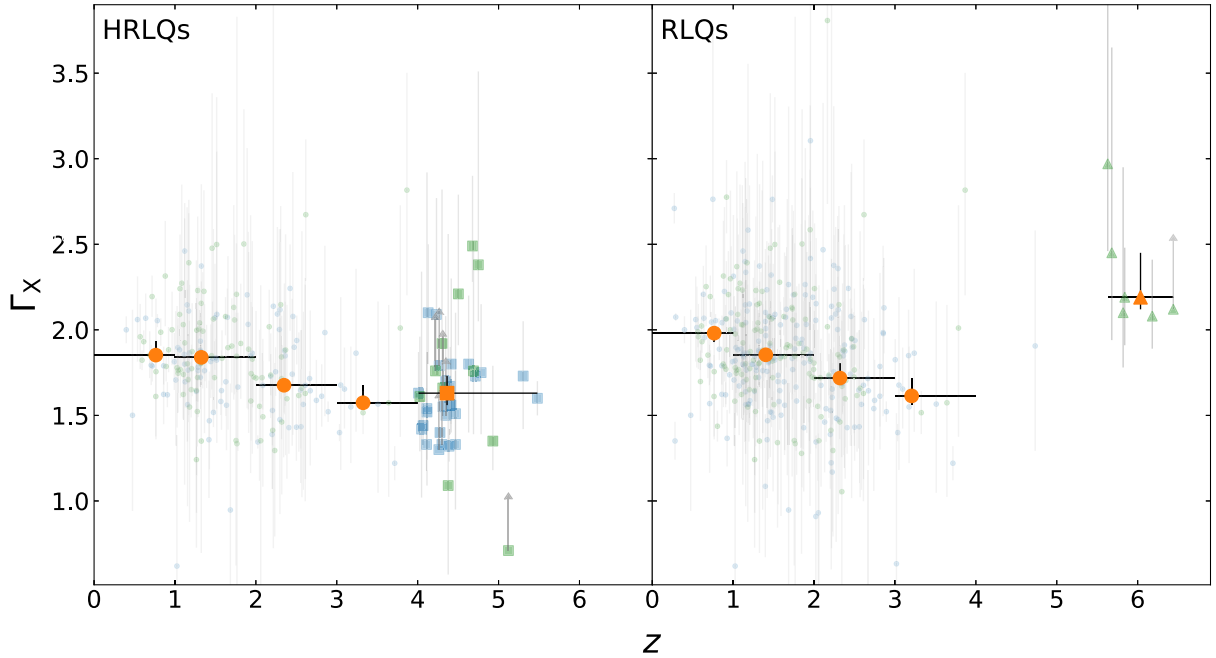


Figure 11. X-ray power-law photon index Γ_X versus redshift for HRLQs (left panel) and RLQs (right panel). 38 out of 41 HRLQs at $4 < z < 5.5$ and six out of seven RLQs at $z > 5.5$ have available Γ_X values. In both panels, blue and green symbols represent objects with $\alpha_r > -0.5$ and $\alpha_r \leq -0.5$, respectively. The large orange dots are the median Γ_X values of objects from four redshift bins ($z = 0-1, 1-2, 2-3, \text{ and } 3-4$) in both panels (see Footnote¹⁰ for further relevant discussion). The z coordinates of orange dots represent the median z of redshift bins with horizontal error bars representing the ranges of redshift bins. The vertical error bars of orange symbols are 1σ uncertainties obtained via bootstrapping. Left: The squares and dots (both blue and green) represent HRLQs at $4 < z < 5.5$ and HRLQs from Zhu, Timlin & Brandt (2021), respectively. The orange square represents the median Γ_X value of $4 < z < 5.5$ HRLQs. The z coordinate of the orange square is the median redshift of the $4 < z < 5.5$ HRLQ sample with its horizontal error bar representing the redshift range of the $4 < z < 5.5$ HRLQs sample. Right: The triangles and dots (both blue and green) represent RLQs at $z > 5.5$ and RLQs from Zhu, Timlin & Brandt (2021), respectively. The orange triangle is the median Γ_X value of $z > 5.5$ RLQs and is slightly displaced in the horizontal direction to avoid overlapping with green triangles. The horizontal error bar of the orange triangle indicates the redshift range of $z > 5.5$ RLQs with available Γ_X values.

of RLQs presented in the right panel of Fig. 11. This suggests that RLQs may undergo similar physical transitions as RQQs at $z \sim 6$.

The X-ray spectral and other properties discussed above indicate $z > 5.5$ RLQs are at a different evolutionary stage. RLQs at $z > 5.5$ feature steep radio and X-ray spectra and relatively strong X-ray enhancements. The X-ray steepening mechanism proposed by previous studies, which was mentioned in the previous paragraph, could probably shed light on the evolution of RLQs. However, a larger sample of $z > 5.5$ RLQs is needed to determine the physical mechanisms that are responsible for the X-ray enhancements of RLQs at very high redshifts and the role of the IC/CMB process in them.

5.3 Milli-arcsecond scale properties

We also investigated if there is a relation between the milliarcsecond-scale radio-jet properties and the X-ray enhancements of high redshift HRLQs/RLQs. We used the ratio between the flux densities given by VLBI observations and observations with lower resolution (NVSS/FIRST) at matched frequencies, $f_{\text{VLBI}}/f_{\text{lowres}}$, as an indicator of source compactness. An $f_{\text{VLBI}}/f_{\text{lowres}}$ that is close to one indicates a compact radio-emitting region while a ratio that is much smaller than one indicates the existence of diffuse emission extending beyond the scale of a few hundred pc.

We collected available VLBI observations from the literature (see Table 5). 29 out of 41 HRLQs at $4 < z < 5.5$ and five out of seven RLQs at $z > 5.5$ have available VLBI observations. If an object has VLBI observations in more than one band, the band closest to observed-frame 1.4 GHz was selected. The frequencies of all the bands we selected are greater than 1.4 GHz. We then used α_{high} (see Table 5) to extrapolate the NVSS/FIRST flux densities from 1.4 GHz to the VLBI frequencies we selected. Since the VLBI and NVSS/FIRST observations were not taken simultaneously, variability of the sources may influence the values of $f_{\text{VLBI}}/f_{\text{lowres}}$. Based on the VLASS radio variability analyses presented in Section 2, the typical radio variability of $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs is within ≈ 30 per cent over a rest-frame period of ≈ 5 –6 months. Although some VLBI and NVSS/FIRST observations are separated by over a decade in the observed frame ($\gtrsim 2$ yr in the rest frame), the available VLASS radio variability analyses over a shorter time period do not suggest strong variability effects upon $f_{\text{VLBI}}/f_{\text{lowres}}$.

We plotted $\Delta\alpha_{\text{ox}}$ versus $f_{\text{VLBI}}/f_{\text{lowres}}$ for $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs that have VLBI observations in Fig. 12. We did not find an apparent dependence between the amount of X-ray enhancement and the source compactness, or the scale and size of radio jets.

Since the $f_{\text{VLBI}}/f_{\text{lowres}}$ value reaches as high as ≈ 1.5 , we expect that source variability and flux uncertainties may affect $f_{\text{VLBI}}/f_{\text{lowres}}$ by ≈ 0.5 . This is roughly consistent with a combination of the suggestive $\lesssim 30$ per cent radio variability mentioned in the previous paragraph and measurement uncertainties, considering that objects with longer time gaps between VLBI and NVSS/FIRST observations may show stronger radio variability. It is thus appropriate to consider objects with $f_{\text{VLBI}}/f_{\text{lowres}} > 0.5$ as relatively compact. The majority of objects in Fig. 12 are considered to be compact and have radio jets at scales smaller than a few hundred pc, which are smaller than typical X-ray jets. This is consistent with the expectation that X-ray jets produced via the IC/CMB process are larger than radio jets since the electrons that are responsible for X-ray emission have a longer cooling time than those responsible for radio emission (e.g. Harris & Krawczynski 2007; Worrall 2009).

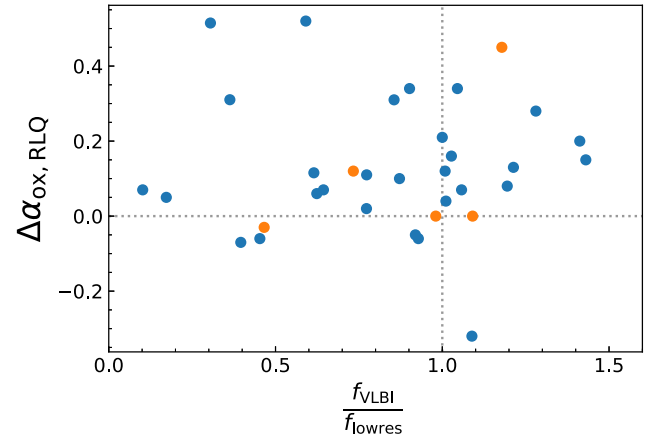


Figure 12. X-ray enhancement strength versus compactness of the $4 < z < 5.5$ HRLQ sample and the $z > 5.5$ RLQ sample. 29 out of 41 $4 < z < 5.5$ HRLQs (blue dots) and five out of seven $z > 5.5$ RLQs (orange dots) have VLBI coverage. f_{VLBI} is the observed flux density at the VLBI band closest to 1.4 GHz. f_{lowres} is the flux density at corresponding VLBI bands inferred from $f_{1.4\text{GHz}}$ assuming the radio spectral slope to be α_{high} . The vertical and horizontal dotted lines represent $f_{\text{VLBI}}/f_{\text{lowres}} = 1$ and $\Delta\alpha_{\text{ox,RLQ}} = 0$, respectively. There is no apparent correlation between X-ray enhancement and compactness.

6 SUMMARY AND FUTURE WORK

6.1 Summary

We have investigated and confirmed the X-ray enhancements of $z > 4$ HRLQs compared to their low-redshift counterparts using new and archival *Chandra* observations. We also found such X-ray enhancements in $z > 5.5$ RLQs for the first time. Our key findings are summarized as the following:

(i) We combined the $4 < z < 5.5$ HRLQs selected by Wu13 and Zhu19 to construct a sample of 41 HRLQs at $4 < z < 5.5$ with complete X-ray coverage, pushing the optical flux limit to $m_i = 21.33$ compared with previous studies (see Section 2.1). We obtained new *Chandra* Cycle 23 observations of six HRLQs at $4 < z < 5.5$. Along with three archival objects, we analysed the *Chandra* observations of nine HRLQs at $4 < z < 5.5$ and reported their X-ray properties in Table 3 (see Section 3.1).

(ii) We searched the literature and constructed a sample of optically selected $z > 5.5$ RLQs. The sample consists of the seven brightest (in rest-frame optical/UV bands) optically selected RLQs at $z > 5.5$ with complete X-ray coverage (see Section 2.2). We also obtained new *Chandra* Cycle 23 observations of two RLQs at $z > 5.5$. Along with five archival objects, we analysed and reported the X-ray properties of seven RLQs at $z > 5.5$ in Table 4. Among the five archival objects, two (VIK J2318 – 3113 and PSO J172+18) have not been reported in the literature previously. The remaining three objects have been reanalysed for consistency. All objects except for PSO J172 + 18, which only has *XMM-Newton* coverage (see Section 3.2), were observed by *Chandra* (see Section 3.1).

(iii) The X-ray enhancement of HRLQs at $4 < z < 5.5$ compared to matched HRLQs at $z < 4$ has been further confirmed. The $\Delta\alpha_{\text{ox}}$ distributions of $4 < z < 5.5$ HRLQs are shown to be different from those of $z < 4$ HRLQs at a 4.90–5.33 σ statistical significance level. The factor of X-ray enhancement of $4 < z < 5.5$ HRLQs is constrained to be $1.77^{+0.19}_{-0.12}$ (see Section 4.1).

(iv) We found an X-ray enhancement of RLQs at $z > 5.5$ compared to matched RLQs at $z \lesssim 5$ for the first time. The $\Delta\alpha_{\text{ox}}$ distributions

of $z > 5.5$ RLQs are shown to be different from those of $z \lesssim 5$ RLQs at a $3.65\text{--}4.91\sigma$ statistical significance level. The factor of X-ray enhancement of $z > 5.5$ RLQs is $2.72_{-1.47}^{+3.58}$ (see Section 4.2).

(v) We constructed broad-band SEDs of the nine newly added $4 < z < 5.5$ HRLQs and seven $z > 5.5$ RLQs. We compared these with suitable composite SEDs at lower redshifts. The comparison results further support the X-ray enhancements of $4 < z < 5.5$ HRLQs and $z > 5.5$ RLQs (see Section 4.3). The broad-band SEDs of the remaining 32 HRLQs at $4 < z < 5.5$ can be found in Wu13 and Zhu19.

(vi) We found that the RLQs at $z > 5.5$ have a median X-ray power-law spectral index (Γ_X) of $2.19_{-0.07}^{+0.26}$, which is significantly steeper than that of RLQs at lower redshifts, $1.84_{-0.01}^{+0.01}$, given by Zhu, Timlin & Brandt (2021).

6.2 Future work

The number of luminous RLQs at very high redshifts ($z \gtrsim 6$) has been increasing rapidly with the aid of wide-field sky surveys in the optical-to-NIR bands (e.g. Pan-STARRS, Chambers et al. 2016; UKIDSS, Lawrence et al. 2007; and VHS, McMahon et al. 2013) and at radio frequencies (e.g. RACS, McConnell et al. 2020; and LoTSS-DR2, Shimwell et al. 2022). During the writing process of this paper, several new RLQs at $z \gtrsim 6$ have been identified (Bañados et al. 2023; Ighina et al. 2023). The upcoming Vera C. Rubin Observatory Legacy Survey of Space and Time (Ivezić et al. 2019), together with *Euclid* and the *Roman Space Telescope*, are expected to discover even more quasars, pushing the redshift frontier of quasars to $z \approx 9\text{--}10$. Their radio properties could be constrained by ongoing sensitive radio surveys including VLASS (Lacy et al. 2020) and EMU (Norris et al. 2021). Thus, the number of RLQs at $z \gtrsim 6$ is expected to be significantly increased in the near future. With the increasing number of RLQs, one could possibly form a sample of HRLQs at $z \gtrsim 6$ as well.

While our results for $4 < z < 5.5$ HRLQs can still be explained by the fractional IC/CMB model, it is possible that there are additional mechanisms that are responsible for the X-ray enhancement of $z > 5.5$ RLQs. Our understanding of RLQs/HRLQs at $z \gtrsim 6$ is greatly limited by low X-ray count numbers and the small sample size. Deeper X-ray observations of objects in our $z > 5.5$ sample will be valuable to set tighter constraints on their X-ray spectral properties. In addition, investigating the X-ray properties of larger samples of $z \gtrsim 6$ RLQs/HRLQs with *Chandra* and *XMM-Newton* could provide insights into the X-ray emission mechanisms of RLQs/HRLQs and the evolution of SMBHs in the first billion years of the Universe.

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DATA AVAILABILITY

The raw data of all objects except SDSS J104742.57 + 094744.9 are publicly available in the *Chandra* Data Archive (<https://cx.cfa.harvard.edu/cda/>) and the *XMM-Newton* Science Archive (<http://nxsas.esac.esa.int/nxsas-web/#home>). The raw data of SDSS J104742.57 + 094744.9 will be shared on reasonable request to the corresponding author. The reduced data generated in this research will be shared on reasonable request to the corresponding author.

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