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A bag of tricks: Using proper motions of Galactic stars to identify the Hercules ultra-faint dwarf galaxy members^{★,★★}

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ABSTRACT

Context. Discovered in the last decade as overdensities of resolved stars, the ultra-faint dwarfs (UFDs) are among the least luminous, most dark-matter dominated, and most metal-poor galaxies known today. They appear as sparse, loose objects with high mass-to-light ratios. Hercules is the prototype of the UFD galaxies. To date, there are still no firm constraints on its total luminosity due to the difficulty of disentangling Hercules bona-fide stars from the severe Galactic field contamination.

Aims. To better constrain Hercules properties, we aim at removing foreground and background contaminants in the galaxy field using the proper motions of the Milky Way stars and the colour–colour diagram.

Methods. We have obtained images of Hercules in the r_{Sloan} , B_{Bessel} and U_{spec} bands with the Large Binocular Telescope (LBT) and LBC-BIN mode capabilities. The r_{Sloan} new dataset combined with data from the LBT archive span a time baseline of about 5 yr, allowing us to measure proper motions of stars in the Hercules direction for the first time. The U_{spec} data along with existing LBT photometry allowed us to use colour–colour diagram to further remove the field contamination.

Results. Thanks to a highly-accurate procedure to derive the r_{Sloan} -filter geometric distortion solution for the LBC-red, we were able to measure stellar relative proper motions to a precision of better than 5 mas yr⁻¹ down to $r_{\text{Sloan}} \simeq 22$ mag and disentangle a significant fraction (>90%) of Milky Way contaminants. We ended up with a sample of 528 sources distributed over a large portion of the galaxy body (~ 0.12 deg²). Of these sources, 171 turned out to be background galaxies and additional foreground stars from the analysis of the $U_{\text{spec}} - B_{\text{Bessel}}$ vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ colour–colour diagram. This leaves us with a sample of 357 likely members of the Hercules UFD. We compared the cleaned colour–magnitude diagram (CMD) with evolutionary models and synthetic CMDs, confirming the presence in Hercules of an old population ($t = 12 \pm 2$ Gyr) with wide spread metallicity ($-3.3 < [\text{Fe}/\text{H}] < -1.8$).

Conclusions. Our procedure to estimate star proper motions proved to be a very effective way to identify likely members for stellar systems as far as 130 kpc. The present selection, based on both proper motions and colour–colour diagram, provides a robust identification of Hercules members and a new target list for more spectroscopic investigations.

Key words. galaxies: dwarf – Local Group – methods: observational

1. Introduction

In the last decade, the ultra-faint dwarf (UFD) galaxies discovered around the Milky Way (MW) and Andromeda spirals have provided new insight in our knowledge to the principles that govern galaxy formation processes. The UFDs show a number of remarkable differences with respect to the “classical” dwarf spheroidal galaxies (dSphs). They are generally fainter than the previously known spheroidals with surface brightnesses typically less than 27 mag arcsec⁻²; thus, they are given the name “ultra-faint dwarfs”. Although UFDs have dimensions comparable to those of the classical dSphs (the typical half-light radius is $r_h \geq 100$ pc), their absolute V magnitude (M_V) is similar to that of the bulk of Galactic globular clusters (GGCs,

[★] Based on data acquired using the Large Binocular Telescope (LBT) at Mt. Graham, Arizona. The LBT is an international collaboration among institutions in the United States, Italy, and Germany. The LBT Corporation partners are: The University of Arizona on behalf of the Arizona university system; Istituto Nazionale di Astrofisica, Italy; LBT Beteiligungsgesellschaft, Germany, representing the Max-Planck Society, the Astrophysical Institute Potsdam, and Heidelberg University; The Ohio State University, and The Research Corporation, on behalf of The University of Notre Dame, University of Minnesota, and University of Virginia.

^{★★} Full Table 2 is only available at the CDS via anonymous ftp to [cdsarc.u-strasbg.fr](ftp://cdsarc.u-strasbg.fr) (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/570/A61>

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$M_V \approx -7$ mag), and some of them are even less luminous with absolute magnitudes as low as $M_V \approx -2$ mag (see e.g. Clementini et al. 2012). All MW UFDs host an ancient population as old as about 10 Gyr and, with only very few exceptions (e.g. Clementini et al. 2012; Okamoto et al. 2012), their color–magnitude diagrams (CMDs) resemble those of metal-poor Galactic clusters (Belokurov et al. 2007; Brown et al. 2012) with no evidence for intermediate-age stellar generations, which are often observed among the classical dSphs instead (e.g. Monelli et al. 2003; Bellazzini et al. 2006). Measurements of the UFDs internal velocity dispersion reveal surprisingly high values ($\sim 3 \div 10 \text{ km s}^{-1}$) in comparison to the luminosity (e.g. Simon & Geha 2007; Walker et al. 2009). Therefore, in contrast to GGCs and even more so in classical dSphs, UFDs appear to be dark-matter dominated with mass-to-light ratios that can reach as large as $M/L \sim 10^{2.3} M_\odot/L_\odot$.

Dwarf spheroidal galaxies have long been thought to be candidate building-blocks in the hierarchical scenario of galaxy formation (e.g. Grebel 2005), where galaxies form via cooling and condensation of gas in dark-matter halos (White 1978). However, the role played by the classical dSphs in shaping the halos of their massive parent galaxies still remains quite controversial, a major issue being the small number of classical dSphs observed in the Local Group (LG). On the other hand, the number of UFDs has increased constantly in the last decade and completeness estimates suggest that many more of these faint satellites are still to be discovered in the LG (Tollerud et al. 2008). They may eventually fill the gap between observed number of satellites and number of relics predicted by the Λ CDM models, the so-called “missing satellite problem” (Moore et al. 1999; Klypin et al. 1999).

The Hercules UFD was discovered by Belokurov et al. (2007) from the analysis of Sloan Digital Sky Survey (SDSS) data. Literature estimates for its distance range from 132 kpc (e.g. Coleman et al. 2007) to 147 kpc (e.g. Adén et al. 2009a) with a value of 132 ± 6 kpc measured from the galaxy RR Lyrae stars (Musella et al. 2012). It has an absolute magnitude of $M_V = -6.6 \pm 0.3$ mag, which places the galaxy among the brightest MW UFDs, and a surface brightness of $\mu_V = 27.2 \pm 0.6 \text{ mag arcsec}^{-2}$ (Martin et al. 2008). Since the earliest ground-based observations, it was recognized that the galaxy CMD resembles that of an old and metal-poor GGC ($t \gtrsim 10 \pm 2$ Gyr and $Z \sim 10^{-4}$, see e.g. Sand et al. 2009; Musella et al. 2012), as recently confirmed by Brown et al. (2012) with Hubble Space Telescope (HST) data. Martin et al. (2008) measured the galaxy half-light radius ($r_h = 8.6'$), and Sand et al. (2009) estimated the tidal radius ($r_t = 35.25'$). Hercules appears highly elongated with an ellipticity $e \gtrsim 0.65$ (Coleman et al. 2007; Martin et al. 2008) and shows indications of a possible tidal disruption (e.g. Martin & Jin 2010). Deason et al. (2012) suggested that some hot horizontal branch (HB) stars once belonged to Hercules may have been tidally stripped and are now unbound. Thus, Hercules may not be a simple bound system in equilibrium (Adén et al. 2009a; Martin & Jin 2010; Deason et al. 2012). If so, its total mass cannot be gauged via measurement of the overall velocity dispersion and size (see e.g. Klimentowski et al. 2007; Łokas 2009), as the streaming of unbound stars could, in principle, inflate the observed mass-to-light ratio.

Unfortunately, the line of sight towards Hercules is heavily contaminated by external sources, making it hard to establish membership from the CMD alone (e.g. Musella et al. 2012). Hercules, as all UFDs, is a very loose stellar system ($\rho = 1.7 \times 10^{-2} M_\odot \text{ pc}^{-3}$, Walker et al. 2009); hence, background galaxies constitute a severe source of contamination.

In addition, this UFD also suffers from a large contamination by MW foreground stars. Even when radial velocities (RV) are considered, the selection of bona-fide members is made rather uncertain by the mean velocity of the galaxy ($\sim 45 \text{ km s}^{-1}$, Adén et al. 2009a) being embedded into the velocity distribution of foreground MW dwarf stars, coinciding with the velocity of the thick disk. For this reason, an estimate of Hercules mass based only on kinematic methods is highly uncertain, as shown by Adén et al. (2009b). Adding a selection based on the Strömgren c_1 index, Adén et al. reduced the radial-velocity dispersion of Hercules stars and decreased the galaxy mass within the half-light radius by a factor of $\sim 1/4$. The rescaled mass is much lower than the common mass scale for MW satellites (Strigari et al. 2008), suggesting that Hercules does not share the halo properties seen in the classical dSphs and other UFDs. The Galactic contamination in the direction of Hercules is a severe problem that needs to be settled before attempting to derive metallicity and radial velocity distributions of Hercules’s stars and, in turn, constrain the galaxy mass and luminosity.

Due to the importance of weeding out any external contaminants, an accurate method to determine the star membership is mandatory to study the stellar population content and the structure of such a poorly-populated and heavily-contaminated system. In this paper, we study the star membership through the analysis of the proper motion (PM) of stars in the Hercules field. Our aim is to remove the foreground contamination by separating Galactic from Hercules stars, according to their PMs. Up to now, such measurements have been conducted in a handful of dSphs using HST data (e.g. Piatek et al. 2003, 2007; Massari et al. 2013), while the Fornax galaxy is the only target studied with ground-based data (Méndez et al. 2010). However, previous works dealt with limited areas of those galaxies, due to the small field-of-view (FoV) of the detectors. Here, we use the Large Binocular Telescope (LBT), whose FoV covers well beyond the half-light radius of Hercules ($r_h = 8.6'$, Martin et al. 2008). We combine new observations specifically obtained for this purpose with archival images and found our membership criteria on PMs and on the colour–colour diagram that involve B_{Bessel} , r_{Sloan} , and U_{spec} data.

The paper is organized as follow: Sect. 2 describes our procedures for the data analysis and to measure PMs and photometry. The results are discussed and compared to previous membership analysis in Sect. 3, while implications for the galaxy stellar population content and for the metallicity and radial-velocity distributions are presented in Sect. 4. A summary and conclusions section close the paper (Sect. 5).

2. Observation and data reduction

2.1. Observations

The Hercules UFD galaxy ($\alpha = 16^{\text{h}}31^{\text{m}}02^{\text{s}}.0$, $\delta = 12^\circ 47' 25''.6$, J2000.0) was observed with the Large Binocular Camera (LBC, Giallongo et al. 2008) at the LBT located on Mount Graham in Arizona. The LBC is a wide field imager (4 CCDs, $2 \text{ K} \times 4.5 \text{ K}$ pixels each) with a FoV of $\sim 23' \times 23'$ and a resolution of $0.225'' \text{ pix}^{-1}$. We employed both archival and proprietary data to have the longest available time baseline. A log of the observations used in this work is reported in Table 1.

The 2007 dataset covers only the central part of the galaxy and was collected during the LBT science demonstration time (March 2007, Coleman et al. 2007) with the LBC-blue, the only active “eye” at that time. Images were taken through B_{Bessel} - and r_{Sloan} -filters with almost no dither. An accurate

Table 1. Log of LBT observations used in the present study.

UT date	LBC	Filter	Exp. time (s)	Seeing (arcsec)	Dither	Field
2007 Mar. 17	Blue	B_{Bessel}	6×300	0.9	Small	Cent
2008 May 29	Red	r_{Sloan}	6×300	0.9	Small	East
2008 May 30	Red	r_{Sloan}	6×300	0.9	Small	West
2008 May 31	Red	r_{Sloan}	6×300	1.2	Small	Cent
2008 Jun. 01	Red	r_{Sloan}	5×300	0.9	Small	Cent
2013 Apr. 04	Red	r_{Sloan}	39×60	0.9	Large	Cent
2013 Apr. 04	Blue	B_{Bessel}	31×60	1.1	Large	Cent
2013 Apr. 04	Blue	U_{spec}	8×60	1.2	Large	Cent

geometric-distortion (GD) solution is available for the B_{Bessel} filter, but not for the r_{Sloan} filter. It was not possible to self-calibrate the GD of the r_{Sloan} filter due to the lack of an adequate dither strategy. For this reason, we selected and used only images in the B_{Bessel} filter from this dataset.

The archival r_{Sloan} exposures are part of the dataset collected between May 29th and June 1st 2008 with the LBC-red and published in Sand et al. (2009), from which we selected the central and lateral fields (see Fig. 1).

The archival images were combined with 25 new images acquired on April 4th 2013¹. We adopted a large dither pattern (70'', ~30% of the FoV) specifically designed to calibrate the GD in the r_{Sloan} -filter of the LBC-red. The right panel of Fig. 1 shows the dither pattern and the depth-of-coverage map of the proprietary r_{Sloan} -exposures. The total area covered is 0.69 deg². Images were collected using both the LBC-blue and LBC-red arms in r_{Sloan} (39 exposures), B_{Bessel} (31), and U_{spec} (8).

The new observations completely cover the central field and partially overlap the lateral fields of Sand et al. (2009), as shown in the left panel of Fig. 1.

2.2. Data reduction

Data were reduced using the procedures described in Bellini et al. (2010). A main asset of our reduction process was the derivation of an ad-hoc GD correction for the LBC-red in the r_{Sloan} -filter, starting from the recipes described in Bellini & Bedin (2010) and improving the polynomial solution that follows prescriptions provided in Libralato et al. (2014). Here, we briefly outline the key points of the reduction process while referring to the aforementioned papers for more details.

2.2.1. Astrometric and photometric reduction

The pre-reduction procedure included standard operations such as de-biasing, flat-fielding, pixel-area correction, and cosmic rays-removal (Bellini et al. 2010). The reduction software is able to find bright, isolated star-like sources in each CCD of each exposure and obtain spatially varying empirical point-spread functions (PSFs in an array of 3×4 elements for each chip). These PSFs were then used to measure positions and fluxes of sources in each chip of each exposure that were then collected into individual catalogues.

2.2.2. The master frame

All stellar positions in the B_{Bessel} -filter catalogues were corrected using the B_{Bessel} -filter geometric-distortion correction

available from Bellini & Bedin (2010). We cross-identified stars in common between catalogues and derived average position and magnitude for each source onto a distortion-free reference system (hereafter, the master frame). To build the master frame, we proceeded as follows. We started from the GD-corrected positions of the first catalogue and identified all catalogues that have stars in common. We then transformed the stellar positions of these overlapping catalogues to the first-catalogue reference system by means of conformal transformations (two rigid shifts in the two coordinates, one rotation and one change of scale), using only bright, unsaturated stars in common to compute transformation coefficients. The average transformed positions and fluxes of common stars defined a new, larger, and improved master frame. We iteratively increased and improved the master frame by adding additional overlapping catalogues.

Once stars from all catalogues have been added to the master frame list, we improved single-catalogue transformations by means of more general, 6-parameter linear transformations (to minimize the residuals in the linear terms). The final master frame contains average positions and fluxes of all stars measured in at least three exposures.

2.2.3. r_{Sloan} -filter geometric distortion solution for the LBC-red

The blue and red LBC arms have the same optical design, and their cameras are made by the same detectors arranged in the same way. This means that both the blue and the red cameras have a similar geometric distortion to the 0th order, and, therefore, the distortion solution found for the blue-arm should represent a good first-guess solution also for the red-arm.

Hence, to derive the geometric-distortion solution of the r_{Sloan} exposures for the LBC-red, we started by correcting the stellar positions of the 2013 dataset with the V -filter GD correction of Bellini & Bedin (2010).

We cross-identified stars in different catalogues to put them in the same reference frame of the B_{Bessel} -filter master frame by means of conformal transformations. Even if the V -filter correction for the LBC-blue is not perfectly adequate to correct the r_{Sloan} -filter LBC-red images, systematic errors on their positions have a random amplitude from one exposure to the other due to the adopted observing strategy (dither pattern). Hence, the average r_{Sloan} star positions in the master frame provide a good first-guess approximation of their true positions in a distortion-free frame.

The GD solution for the r_{Sloan} -filter of the LBC-red is made by three parts: (i) a linear transformation to put all images on the master frame; (ii) a polynomial correction; and (iii) a table of residuals.

The polynomial correction was mostly performed, as described in Bellini & Bedin (2010). The only difference is that we used a fifth-order polynomial instead of a third-order one to fit the residual trends. At the first iteration, the cubic part of the polynomial was the same of the V -filter third-order polynomial of Bellini & Bedin, while higher-order terms were set to zero. Then, we iterated the procedure to derive new polynomial coefficients and improve the master frame until the star positional r.m.s. did not change significantly from one iteration to the next.

The last part of our correction consisted of four look-up tables (one for each CCD) to minimize the residuals of the geometric distortion left by the polynomial correction. We followed the method described in Bellini et al. (2011) for the WFC3/UVIS detector of the HST.

¹ INAF-DT no. 38, P.I.: Brocato.

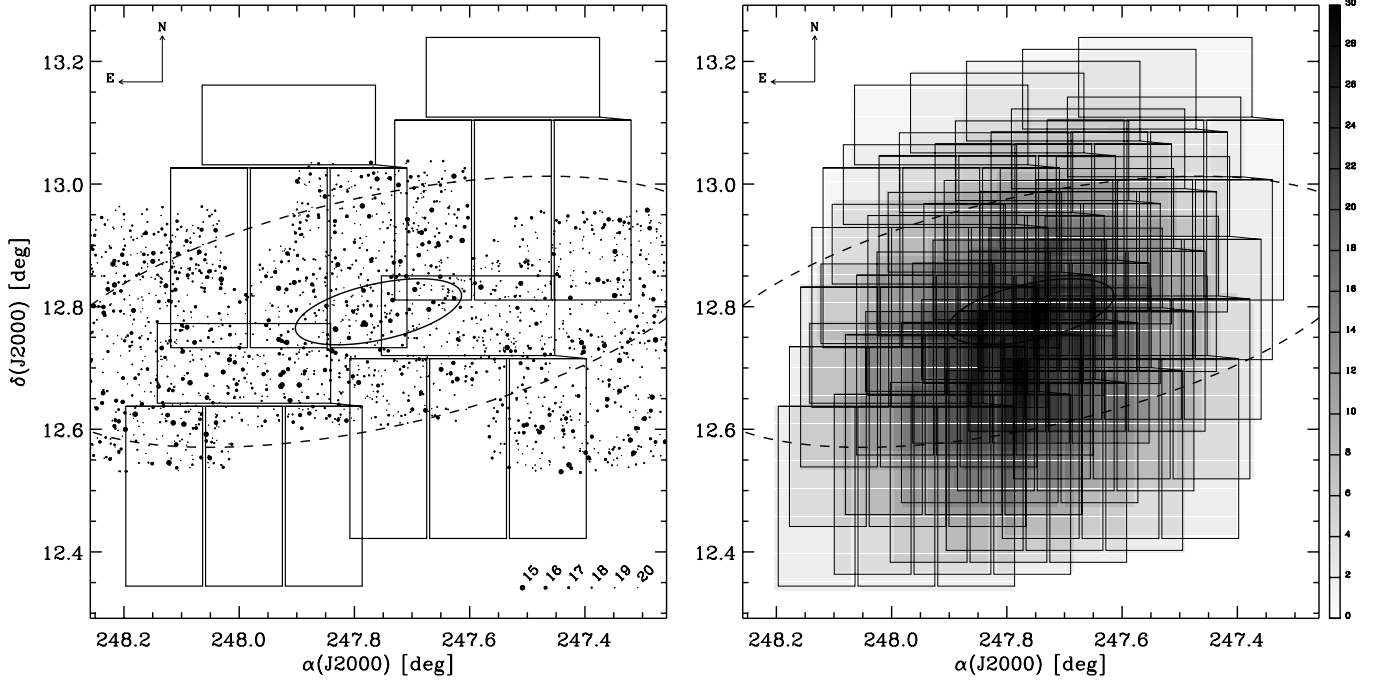


Fig. 1. *Left:* map of Hercules UFD showing the regions covered by the proprietary and archive LBT observations used in the present study. The solid lines display the contours of the most external LBC pointings of the dither pattern adopted during the April 2013 observations. The black points show the position of the photometric sources in the central and lateral fields observed by Sand et al. (2009). Symbol size is inversely proportional to the source r_{Sloan} magnitude. The solid and dashed ellipses mark the galaxy half-light and tidal radii, respectively. *Right:* footprints of the 5×5 dither pattern adopted during the April 2013 observations. The depth-of-coverage map for the r_{Sloan} -images is also shown in grey scale.

In our correction, we subdivided each chip of the 4-CCDs LBT mosaic in 11×25 elements. The table correction was built at a given location of the chip using a bi-linear interpolation among the surrounding grid points. We iterated this procedure by applying 75% of the suggested correction, building a new master frame, and computing new, improved grid points. The convergence was reached when the change in the suggested correction was negligible from one iteration to the next.

In Figs. 2 and 3, we show the distortion maps before and after applying the distortion corrections, respectively. Figure 4 shows the $\sigma(\text{Positional residuals})$, computed as in Libralato et al. (2014) after each step of our correction. In the bottom panel, we show the $\sigma(\text{Positional residuals})$ for a master frame derived using general 6-parameter linear transformations. By applying all corrections, the $\sigma(\text{Positional residuals})$ improve from ~ 74.2 mas to ~ 9.5 mas.

2.2.4. Geometric-distortion corrected and cleaned catalogues

To build the final master frames for the U_{spec}^2 , B_{Bessel} , and r_{Sloan} filters, we cross-identified all stars in our GD-corrected catalogues using 6-parameter linear transformations to absorb uncorrected distortion and atmospheric effects (see e.g. Libralato et al. 2014) and to further improve the general astrometric accuracy.

The master lists (one for each filter) were purged from false detections as in Anderson et al. (2008). We selected stellar sources according to their photometric errors and the quality of the PSF-fit (QFIT, derived from the absolute value of the residuals of the PSF-fit for each star scaled by the flux) by considering the 65th percentile of the quoted quantities as a function of

magnitude. We ended up with master lists of 15 217 sources in r_{Sloan} , 7700 in B_{Bessel} and 5759 in U_{spec} .

2.2.5. Astrometric and photometric calibration

The astrometric calibration was also derived with the purpose of obtaining the match with the SDSS (DR9, Ahn et al. 2012) and the Sand et al.'s catalogues. We used the UCAC 4 catalogue (Zacharias et al. 2013) to convert our pixel-based coordinates into equatorial coordinates by cross-identifying the stars in common between the two catalogs using 6-parameter linear transformations.

The photometric calibration was performed using a set of sources extracted from the SDSS catalogue. The B_{Bessel} magnitudes were obtained by applying the relations by Jordi et al. (2006) and Jester et al. (2005), as described in Sand et al. (2009). The U_{spec} filter has a response curve very similar to the SDSS u' ; therefore, we calibrated it against the SDSS magnitudes without any further colour transformation. The zero point and the colour term of the calibration relations were obtained using only the best stellar-type sources (i.e. QFIT < 0.15) where the r.m.s. of the photometric residuals around the mean magnitude is smaller than 0.03 mag. For the r_{Sloan} and U_{spec} filters, a zero point was sufficient to calibrate the instrumental magnitudes, and no significant colour term was found. For the B_{Bessel} filter, both $U_{\text{spec}} - B_{\text{Bessel}}$ and $B_{\text{Bessel}} - r_{\text{Sloan}}$ colours were used to derive calibration relations. We obtained a good fit with both colours but used the equation in $B_{\text{Bessel}} - r_{\text{Sloan}}$ in the end, which has smaller scatter. The calibration results were checked against Sand et al. (2009) for the two filters in common (B_{Bessel} , r_{Sloan}), finding a close agreement with an r.m.s. scatter below ~ 0.03 mag for magnitudes brighter than $B_{\text{Bessel}} \sim 20$ mag and $r_{\text{Sloan}} \sim 21$ mag. For the U_{spec} -filter, the check was

² The GD correction in B_{Bessel} was adopted also for the U_{spec} filter.

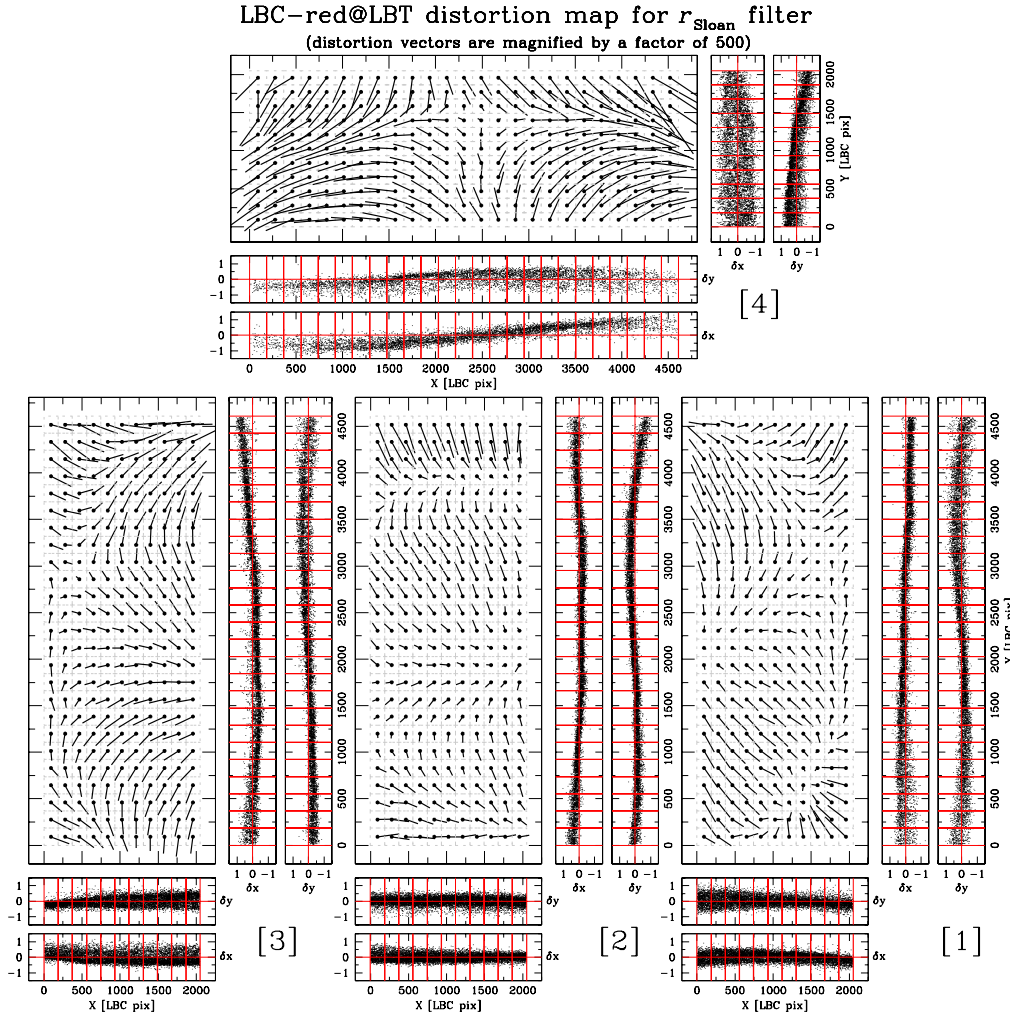


Fig. 2. Residual trends of the four chips for uncorrected star positions and single residual trends along the X and Y axes. The size of the residual vectors is magnified by a factor of 500. Units are expressed in LBC-raw pixels.

performed by comparing the calibration results obtained from the $U_{\text{spec}} - B_{\text{Bessel}}$ and the $U_{\text{spec}} - r_{\text{Sloan}}$ colours to fit the colour term, which was negligible in both cases, as already mentioned. The check was performed by using a set of ~ 1500 stars from the SDSS survey having a magnitude brighter than $u' \sim 20$ mag in the colour range $1 < u' - r' [\text{mag}] < 3$. The results of the fit provide calibrated U_{spec} magnitudes that are in good agreement with each other. In the following, we adopt the calibrated U_{spec} magnitudes coming from the $U_{\text{spec}} - r_{\text{Sloan}}$ transformation equation.

2.3. Proper motions

The r_{Sloan} images were used to measure the stellar PMs. The Hercules r_{Sloan} -band datasets define a time baseline of 4.94 years and cover a common area of 0.30 deg^2 . To measure the stellar displacements between the two epochs, we followed the prescriptions given in [Anderson et al. \(2006\)](#). To do this, it is mandatory to select a set of reference objects against which to compute relative PMs. An absolute reference frame is not required here. We measure star motions with respect to other stars in our field. From basic considerations on the expected internal motions of stars belonging to Hercules as opposed to the Galactic field stars, we can expect that the internal velocity dispersion of the formers is much smaller than that of the latters. Indeed, according to the internal velocity dispersion measured by [Adén et al. \(2009a\)](#) and the galaxy distance, we expect the Hercules

stars to have an internal velocity dispersion of $\sim 0.01 \text{ mas yr}^{-1}$. This is a factor of 10^3 smaller than our random measurement errors ($\sim 10 \text{ mas yr}^{-1}$). Furthermore, according to what is observed for other dSphs located at similar distance, such as Carina ($\sim 100 \text{ kpc}$, [Piatek et al. 2003](#)) and Fornax ($\sim 135 \text{ kpc}$, [Piatek et al. 2007](#)), we expect an absolute PM of the Hercules stars of the order of tenths of mas yr^{-1} . Therefore, Hercules stars represent the best choice to define our reference list.

We started by identifying Hercules stars within an ellipse with a semi-major axis of $7''$ centered on the galaxy center, ellipticity, and inclination values from [Martin et al. \(2008\)](#) (to mitigate the fraction of field contaminants). Stars within this region were then plotted on the r_{Sloan} vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ CMD, on which we isolated two regions containing bona-fide Hercules red giant branch (RGB) and HB stars. The CMD selections were then extended to the whole FoV. The initial list of reference stars includes 323 objects.

We used this starting reference list to transform stellar positions of each catalog onto the master frame following the local transformation approach described in [Anderson et al. \(2006\)](#). This allows us to map the coordinate system of one frame into that of another and transform the position of each individual star measured in one frame into that of the other. Because of the low stellar density in the Hercules field, we used the nearest 25 reference stars found on the same chip as the target star in both images. Of these 25 stars, we reject the five with the largest transformation residuals. The final best 20 reference stars

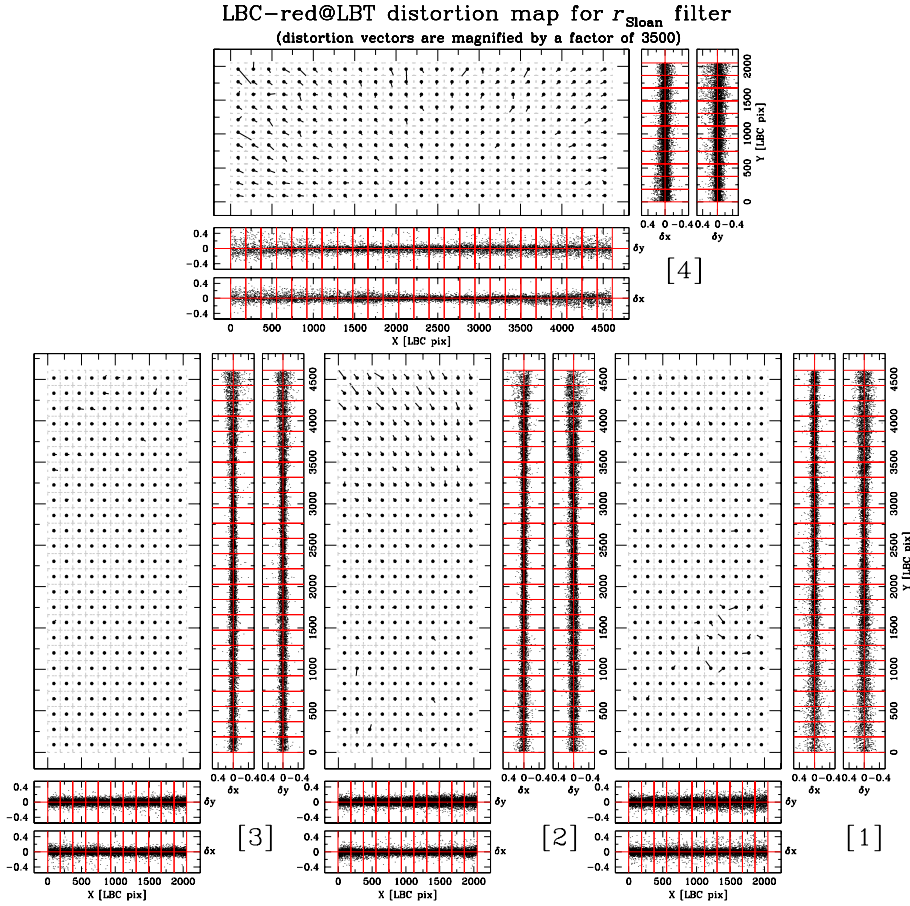


Fig. 3. Positional residuals after all corrections have been applied. The size of the vectors is now magnified by a factor of 3500.

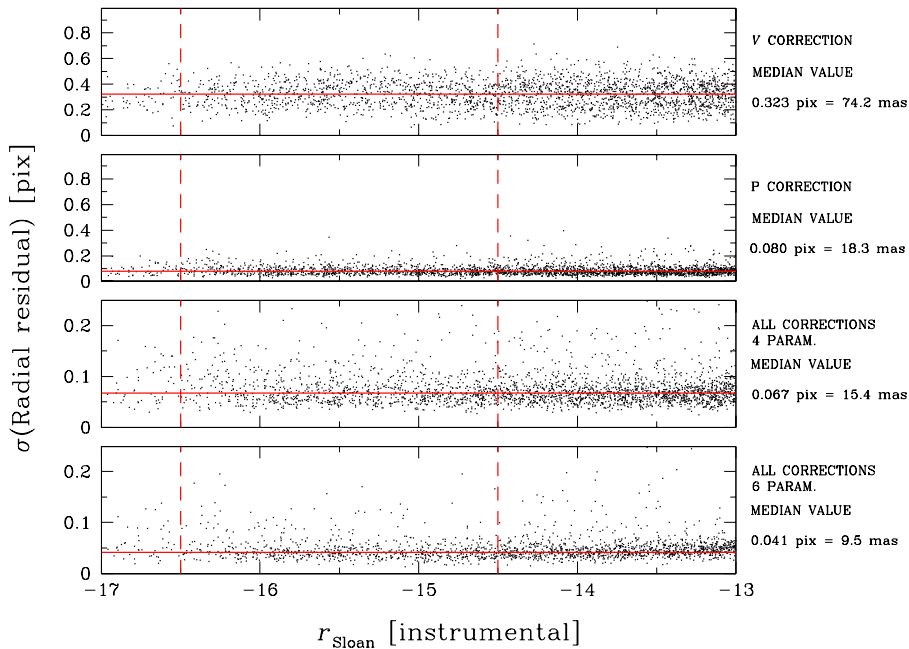


Fig. 4. $\sigma(\text{Radial residuals})$ versus instrumental r_{Sloan} magnitudes after each step of our solution. The red solid horizontal lines show the median value of $\sigma(\text{Radial residual})$ between red dashed vertical lines.

will then define the local transformation parameters that map the coordinate system of one frame into that of another. Then, for each star, we computed the displacement on the master frame as the average of the displacements obtained by comparing each pair of transformed positions (one from the first epoch and one

from the second epoch). Once we have obtained a first estimate of the stellar PMs, we can improve the reference list by rejecting those stars, which motion is not consistent with the Hercules mean motion (i.e. with a displacement larger than 1 pixel). We iterated the process of improving the reference list and measuring

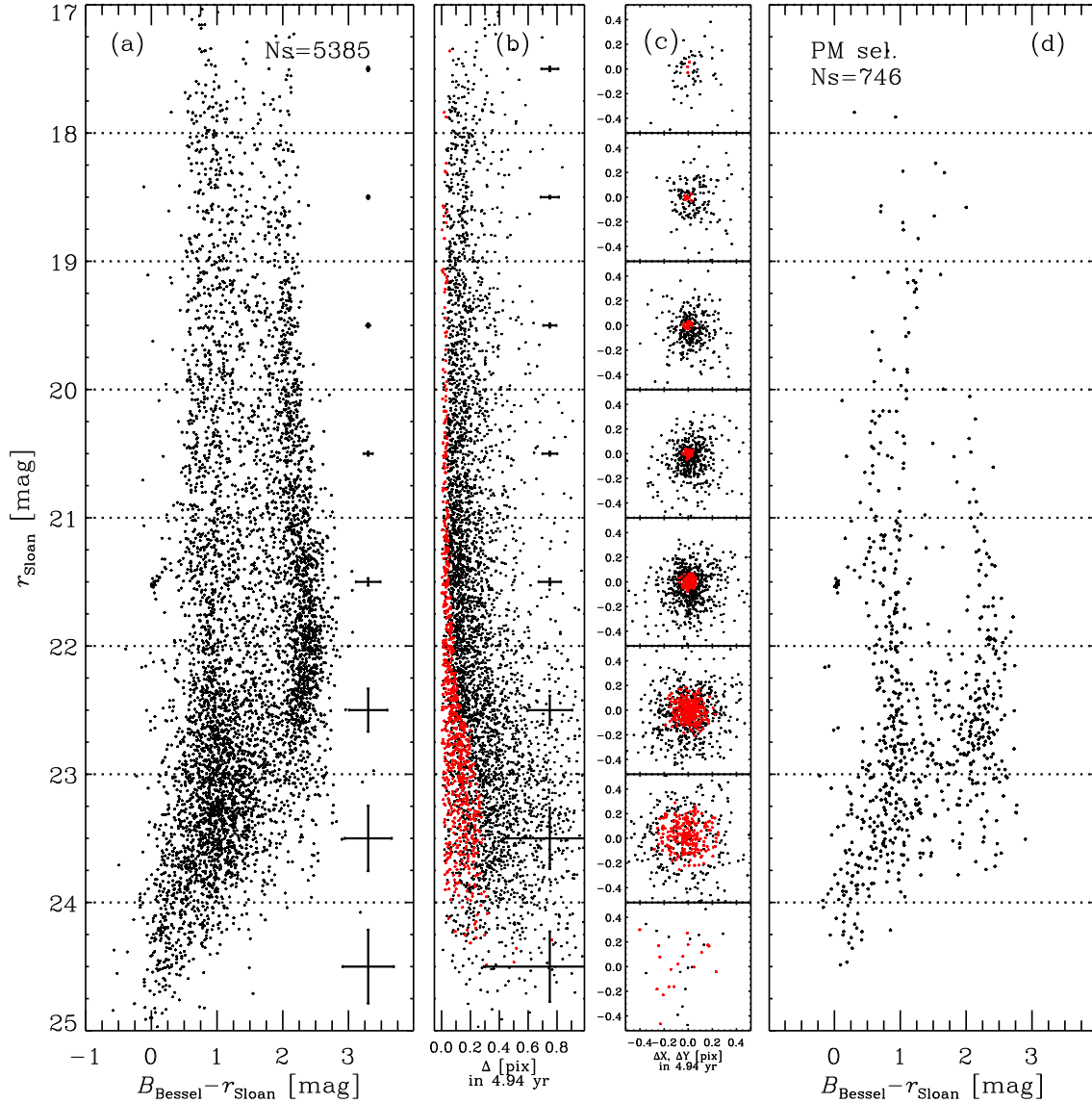


Fig. 5. Panel **a**) r_{Sloan} vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ CMD-cleaned, according to the photometric selection criteria described in the text. Mean errors are also shown on the right for each magnitude bin. Panel **b**) Displacement based on the r_{Sloan} -filter as a function of magnitude. Mean errors are also shown. Red symbols mark proper-motion (PM) selected stars (see text). Panels **c**) Vector-point diagrams for each magnitude bin. Symbols are the same as in panel **b**). Panel **d**): r_{Sloan} vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ PM-selected CMD.

more accurate PMs three times. A further iteration proved to offer negligible improvements. The final list of reference stars includes 255 objects.

Because of the low surface density of Hercules stars and the severe Galactic field star contamination, some of the reference stars used in the local transformation between epochs are actually not members of Hercules. In particular, the fraction of Galactic stars is expected on the basis of Besançon model to increase from $\sim 20\%$ to $\sim 50\%$, which moves from the center to the outer regions of the field. However, the inclusion of these stars in the reference list does not sizably affect the astrometric reference, since the mean PM of such stars is comparable to that of Hercules within the measurement errors but with a larger dispersion.

We were able to measure PMs for 5385 objects that have both r_{Sloan} and B_{Bessel} photometry. Panel a of Fig. 5 shows the r_{Sloan} vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ CMD of these sources. Similar,

but less accurate, results were obtained using probable background galaxies with $23.5 < r_{\text{Sloan}}$ [mag] < 24.5 and $-0.5 < B_{\text{Bessel}} - r_{\text{Sloan}}$ [mag] < 1.0 as the reference list. The disadvantage of this approach is in the much lower signal-to-noise of these sources (higher random errors) that leads unavoidably to a poorer accuracy in the PM determination.

2.3.1. Proper motion selection

The displacements ($\Delta = \sqrt{\Delta X^2 + \Delta Y^2}$) for the 5385 stars, which have a PM measure, are reported as black dots in panel b of Fig. 5. The mean uncertainties of magnitude and displacement in each magnitude bin are also shown. Unlike what is commonly found for Galactic stellar clusters, panel b does not show a clear dichotomy in the PM star distribution. Therefore, to distinguish field stars from Hercules members, we can only select those stars with a PM compatible with a null value. For this reason, we

took the dependence of the PM uncertainty on magnitude into account by computing a running 65th percentile of the r.m.s. displacement ($\sigma_{\Delta} = \sqrt{\sigma_{\Delta X}^2 + \sigma_{\Delta Y}^2}$) as a function of the r_{Sloan} magnitude. We, then, adopted its half as PM selection radius (R_{sel}). Moreover, we chose only stars that have a number of couples of measurements (N_c) larger than 50. These selection criteria represent a compromise between including contaminants that have velocity equal to the Hercules' mean PM and missing galaxy members with larger PM errors. The resulting selections are shown as red symbols in panel b. The same colour coding is adopted in panel c of Fig. 5, where we show the vector-point diagram (VPD) for each magnitude bin. In other words, the selected stars have a displacement lower than the (magnitude dependent) uncertainty; thus, their displacement is assumed to be nil.

The final PM-selected catalogue consists of 746 sources, and we show their CMD in panel d of Fig. 5. The RGB and HB of Hercules stars are clearly defined, compared to the unselected CMD in panel a. In both panels, the main sequence (MS) turn-off of Hercules ($r_{\text{Sloan}} \sim 24$ mag, Sand et al. 2009) is not reached with an adequate signal-to-noise ratio, although we have used the same data of Sand et al. (2009). This effect is caused by the lower (by a factor of 5) total exposure time of the second-epoch data compared to the first-epoch, and it is even enhanced by the different approach to the data reduction and analysis. Sand et al. performed their photometry on the co-added images; we instead measured the stars positions and fluxes on the individual exposures.

The PM selection allows us to disentangle a significant fraction of MW stars. To better highlight our results in Fig. 6, we compare the CMD within Hercules half-light radius before and after the PM-selection procedure. The left panel of Fig. 6 shows that a selection merely based on the stars radial distribution still suffers from a large contamination by field stars. This is significantly reduced by PM-motion selecting Hercules members (right panel of Fig. 6). Nevertheless, panel d of Fig. 5 shows that a Galactic sequence at colour $1.9 < B_{\text{Bessel}} - r_{\text{Sloan}}$ [mag] < 2.8 is still present in our PM-selected CMD. To provide a rough estimate of the residual Galactic contamination, we selected two boxes on this sequence and compared the star counts with the unselected catalogue. In the first box, which are located around the HB magnitude level ($21 < r_{\text{Sloan}}$ [mag] < 22), we found that about 8% of Galactic stars survive our proper motion selection, while 25% are in the second box, located at a fainter magnitude level ($22 < r_{\text{Sloan}}$ [mag] < 23). We note that similar fractions are expected from a Galactic simulation taken from the Besançon stellar population synthesis models (Robin et al. 2003, 2004) after applying the same PM-selection criteria described above. The same simulation allows us to estimate the residual fraction of Galactic stars expected at the same levels of magnitude as above, but for the Galactic blue plume in the colour range $-0.5 < B_{\text{Bessel}} - r_{\text{Sloan}}$ [mag] < 1.8 . They are expected to be $\sim 10\%$ and 40% , respectively. In Table 2, we list the final catalogue of 528 PM-selected sources. From left to right, we report the source identity (Col. 1), right ascension, and declination (Cols. 2, 3), U_{spec} , B_{Bessel} and r_{Sloan} magnitudes with their uncertainty (Cols. 4–6), displacement with its uncertainty (Col. 7).

We recall that the selection described above is based on the assumed selection radius for the allowed displacement and on the number of couples. We performed several tests to evaluate the dependence of our results on these quantities. We found that a 30% increment (decrement) of R_{sel} produces an increase of 25% (decrease of 40%) in the number of sources, while

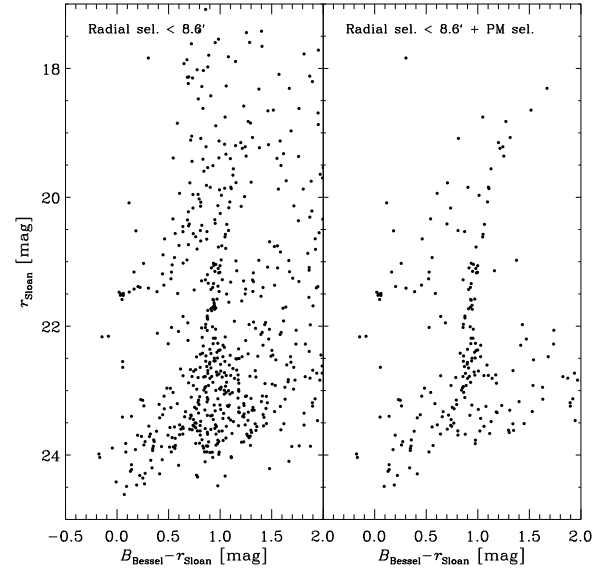


Fig. 6. CMD of stars within an elliptical region with $r_h = 8.6'$ before (left) and after (right) applying the PM selection procedure.

the contamination increases (decreases) more than 35%. On the other hand, the number of sources increases by 70% for $N_c = 10$, but the residual contamination doubles. In contrast, by adopting $N_c = 100$, the field contamination and sources are reduced to half the number. We can conclude that the parameters adopted in Fig. 5 are assured to have a reasonable number of stars and marginal contamination.

2.4. Completeness tests

The comparison between our unselected photometric catalogues and those of Sand et al. (2009) shows similar luminosity functions down to magnitudes of $r_{\text{Sloan}} \sim 23$ mag and $B_{\text{Bessel}} \sim 24$ mag, respectively (Fig. 7). We recall that the magnitude depth is limited by the exposure times of the second-epoch observations, which are about five times shorter than the first-epoch time exposures. Moreover, given the different data reduction and photometric procedures, there are differences between our stellar counts and those found by Sand et al. even for bright stars. However, such differences, due to the differing photometric reductions, are of the order of the sampling uncertainty and fully accounted by the Poisson noise (Fig. 7), since $\Delta N / \sqrt{N} \lesssim 1$, where ΔN is the difference in counts between us and Sand et al. Fainter than the above-mentioned magnitude limits, stellar counts differ by more than 1σ . This implies that our photometry is nearly complete for sources brighter than $r_{\text{Sloan}} \sim 23$ mag and $B_{\text{Bessel}} \sim 24$ mag, and, consequently, the photometric completeness does not represent an issue in our study, given the magnitude intervals for the analysed science objects.

3. Membership analysis and comparison to previous works

To date, attempts to identify Hercules members have been mainly based on CMD-selection techniques, sometimes combined with radial velocity studies. Coleman et al. (2007) selected Hercules candidate members by comparing the V vs. c_1 CMD (where $c_1 = 0.944[B - V] + 0.330[V - r_{\text{Sloan}}]$) of the

Table 2. PM-selected stars of Hercules UDF.

ID	α (J2000) (deg)	δ (J2000) (deg)	U_{spec} (mag)	B_{Bessel} (mag)	r_{Sloan} (mag)	Δ (pix in 4.94 yr)
001	247.8386	12.8540	18.92 ± 0.03	18.17 ± 0.01	17.36 ± 0.02	0.06 ± 0.09
002	247.8689	12.7897	18.14 ± 0.01	18.14 ± 0.01	17.84 ± 0.02	0.02 ± 0.06
003	247.9269	12.7312	19.81 ± 0.02	18.80 ± 0.01	17.88 ± 0.01	0.03 ± 0.04
004	247.9150	12.8006	21.59 ± 0.03	19.77 ± 0.01	18.24 ± 0.01	0.03 ± 0.07
005	247.8111	12.8634	20.30 ± 0.04	19.34 ± 0.01	18.30 ± 0.01	0.02 ± 0.06
006	247.7385	12.7891	21.88 ± 0.04	19.98 ± 0.04	18.31 ± 0.04	0.03 ± 0.03
007	247.7318	12.7109	19.98 ± 0.00	19.28 ± 0.01	18.57 ± 0.01	0.01 ± 0.07
008	247.5811	12.8411	20.04 ± 0.03	19.32 ± 0.01	18.61 ± 0.01	0.04 ± 0.03
009	247.8457	12.7467	21.82 ± 0.05	20.16 ± 0.01	18.65 ± 0.01	0.02 ± 0.05
010	247.7372	13.0069	...	19.74 ± 0.01	18.70 ± 0.01	0.03 ± 0.07

Notes. This table is available entirely in machine-readable form at the CDS.

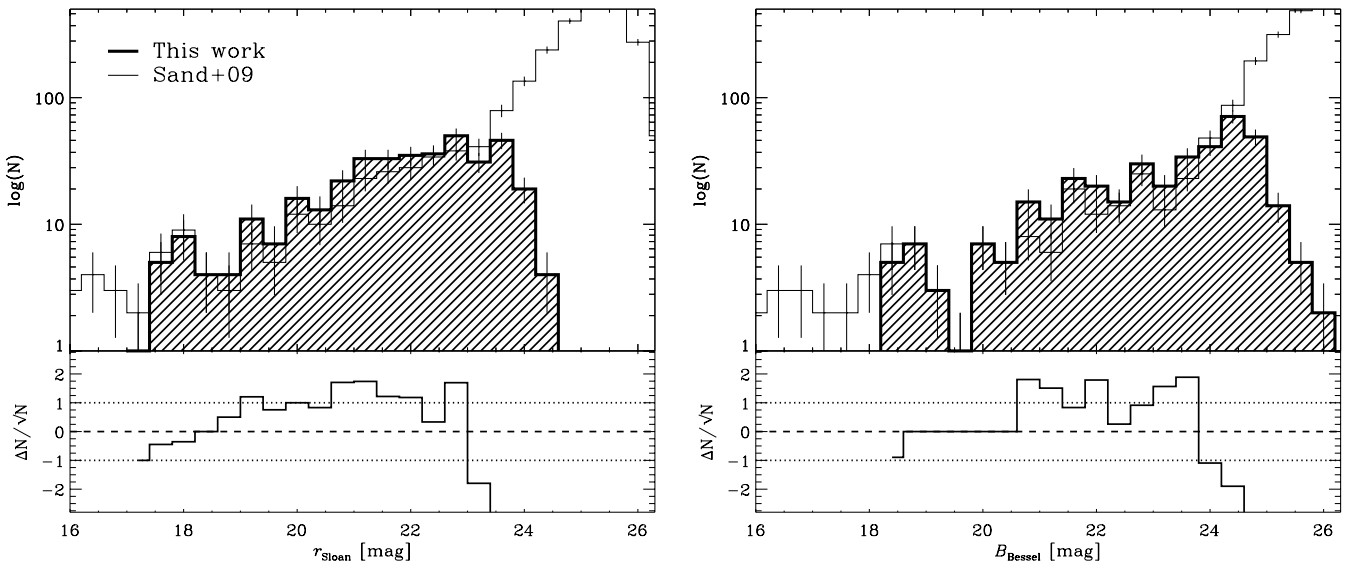


Fig. 7. Top panels: luminosity functions in the r_{Sloan} (left panel) and B_{Bessel} (right panel) bands for our unselected photometric catalogue (thick histogram) and for Sand et al. (2009, thin histogram). Bottom panels: ratio between differential star counts for the two distributions and Poisson noise. The dotted lines refer to the 1σ level.

galaxy central region with the CMD of an adjacent field. Adén et al. (2009a) separated the foreground Galactic dwarf stars from Hercules RGB giants by means of Strömgen photometry and the $c_{1,0}$ vs. $(b - y)_0$ diagram as a function of magnitude. A similar approach was followed by Simon & Geha (2007) and Deason et al. (2012), who selected galaxy candidates from the SDSS data on the basis of the colours and proximity to Hercules.

Figure 8 shows the spatial distribution and the CMD of our PM-selected catalogue and the evolved stars with spectroscopic measurements. Red (blue) symbols mark the position of the spectroscopic targets included (non-included) in our final catalogue. The RR Lyrae stars identified by Musella et al. (2012) are also marked. In detail, 41 sources of Adén et al. (2009a)’s list have a counterpart in our complete photometric catalogue; however, only 25 are cross-identified in our PM-selected list. Three stellar sources in Deason et al. (2012) sample are located outside our FoV. Nine of the remaining 14 sources are present in our PM-selected catalogue. As for the sample of Adén et al. (2011), two stars are not present in our final FoV, and we recovered eight of the nine sources, while 25 (red circles) of the 30 sources in Simon & Geha (2007) are part of our PM-selected

catalogue. We note that this latter sample was also analysed by Kirby et al. (2008, 2013). The list of cross-identified spectroscopic sources and variables is presented in Table 3. In a recent study, using radial velocity measurements Koch et al. (2014) confirmed the star named Her-3 in Koch et al. (2008, 2014) (#41082 in Adén et al. 2009a, #009 in this work) to be a binary system. We confirm that this star (marked by an arrow in the right panel of Fig. 8) is indeed present in our PM-selected catalogue.

The majority of the sources from Adén et al. (2009a), Simon & Geha (2007), and Adén et al. (2011) catalogues that were PM rejected are located on Hercules RGB and HB loci (right panel of Fig. 8). All these sources have a displacement larger than 0.05 pixels, where the maximum value is allowed to be Hercules members as described in the Sect. 2.3 (Fig. 9). For the sake of clarity, we note that seven un-matched spectroscopic targets show a displacement larger than 0.12 ± 0.01 pixel (one from Simon & Geha 2007, four from Adén et al. 2009a, and two from Deason et al. 2012). Therefore, we can firmly exclude them from the Hercules members. We also note that a 30% increase of R_{sel} and the adoption of $N_c = 20$, result in the inclusion of

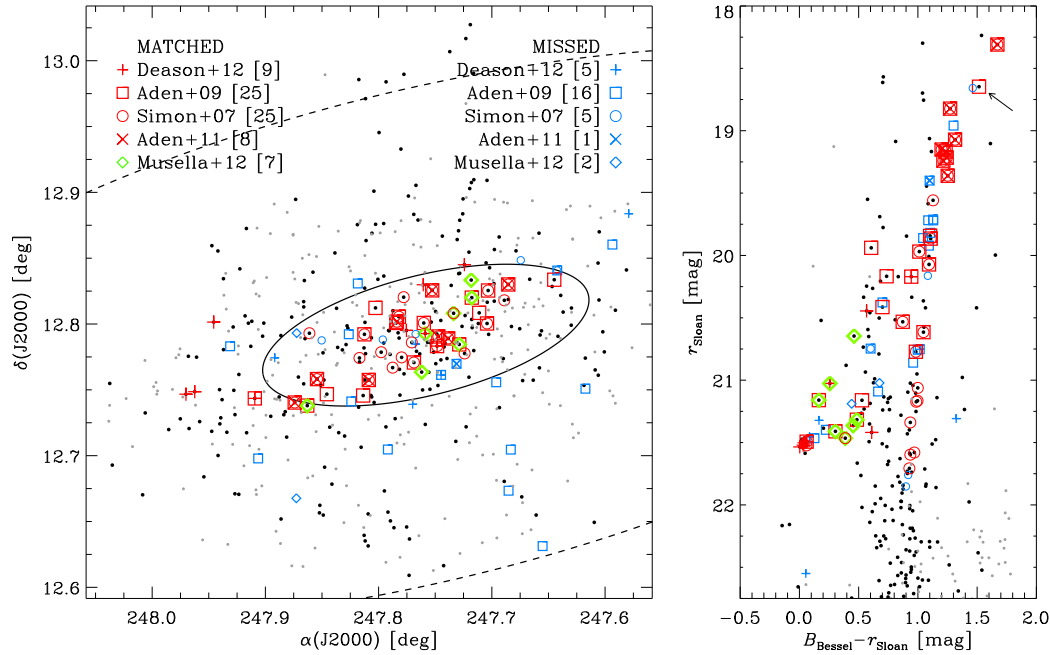


Fig. 8. *Left:* spatial distribution of Hercules PM-selected stellar sources (black filled circles). Spectroscopic targets are marked as pluses (Deason et al. 2012), squares (Adén et al. 2009a), circles (Simon & Geha 2007) and crosses (Adén et al. 2011). Red (blue) symbols represent spectroscopic targets cross-identified (non-cross-identified) in the PM-selected catalogue. RR Lyrae stars studied by Musella et al. (2012) are marked as green (blue) diamonds. The numbers in parentheses are referred to the numbers of spectroscopic targets and variables cross-identified (non-cross-identified). Sources excluded by the colour-colour selection are shown as grey dots (see Fig. 10). *Right:* PM-selected r_{Sloan} vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ CMD. Symbols are the same as in the left panel. An arrow indicates the binary star Her-3 discovered by Koch et al. (2014).

only two stars from Deason et al. (2012), four stars from Adén et al. (2009a), one star from Musella et al. (2012), and three stars from Simon & Geha (2007).

We further investigated the Hercules membership with another powerful tool: the colour-colour diagram. In Fig. 10, we plot the star distribution in the $U_{\text{spec}} - B_{\text{Bessel}}$ vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ plane. We superimposed a metal-poor ($[\text{Fe}/\text{H}] = -2.27$) isochrone with age $t = 13$ Gyr and the corresponding zero-age horizontal branch (ZAHB) from the stellar model database BaSTI (Pietrinferni et al. 2004, 2006, 2013)³ as reference. In this diagram, PM-selected stars with spectroscopic measurements and RR Lyrae variables are located near the isochrone and the ZAHB, following the evolutionary phase prescriptions also in the colour-colour diagram. Sources located far from these regions are marked by grey dots and are not expected to belong to the Hercules UFD. In particular, the grey dots in the upper-right part of the two-colour diagram are mainly background galaxies, while grey dots in the lower regions are foreground Galactic stars (e.g., see Fig. 1 in Bono et al. 2010). In conclusion, we are confident that stars selected according to our PM analysis and the colour-colour diagram are likely Hercules members.

4. Stellar population analysis

4.1. Metallicity distribution

Spectroscopic studies have shown the stars in the FoV of Hercules to exhibit a broad metallicity distribution spanning from $[\text{Fe}/\text{H}] = -3.5$ up to -1.5 (Adén et al. 2011; Kirby et al. 2013, see Fig. 11). This evidence is also supported by photometric metallicity estimators, such as Strömgen indices (Adén et al. 2009a) and Fourier analysis of light curves of

RR Lyrae (Musella et al. 2012). This behavior seems quite common among dwarf galaxies (among the UFDs, in particular) and is interpreted as the sign of a complex chemical evolution. However, up to now, the high foreground contamination in the Hercules field has hampered any detailed analysis. We have now recomputed the weighted mean and the standard deviation of Hercules $[\text{Fe}/\text{H}]$ distribution using our PM-selected sample, which is only marginally contaminated by Galactic stars and background galaxies. The metallicity spread is confirmed, as shown in Fig. 11, where dashed-line histograms refer to original data, whereas shaded histograms show the metallicity distribution of the PM-selected stars. We note that the iron abundances, derived by Adén et al. (2009a) and based on Strömgen photometry, were corrected by adopting the new calibration provided by Adén et al. (2011). The cumulative $[\text{Fe}/\text{H}]$ distribution, obtained by merging the three samples, is also shown in the bottom panel. From the PM-selected stars, a weighted mean metallicity value of $[\text{Fe}/\text{H}] = -2.46 \pm 0.04$ and a dispersion of $\sigma = 0.48$ dex are obtained.

4.2. Kinematics and structure

We applied the same cleaning procedure to the RV distributions provided by Adén et al. (2009a) and Simon & Geha (2007) and obtained mean RV and dispersion values that agree with the unselected ones. We also analysed the cumulative RV distribution by applying a weighted mean to the stars in common between both authors and we obtained very similar results. Furthermore, we estimated mean systemic velocity and dispersion using the maximum likelihood approach described in Walker et al. (2006). We derived a mean velocity of $45.02 \pm 0.97 \text{ km s}^{-1}$ with a dispersion of $4.29 \pm 1.17 \text{ km s}^{-1}$ using 26 stars. We used our velocity dispersion and Eq. (11) of Walker et al. (2009) to estimate the

³ Available at: <http://albione.oa-teramo.inaf.it>

Table 3. List of cross-identified Hercules spectroscopic sources and variables.

ID	S&G07	A09	A11	D12	K13	M12
006	308 205	42241 ^a	42 241 ^a	...	308 205 ^a	...
009	...	41 082 ^a	...	...	...	...
012	308 613	42 149 ^a	42 149 ^a	...	308 613 ^a	...
014	308 686	41 743 ^a	41 743 ^a	...	308 686 ^a	...
018	308 457	42 795 ^a	42 795 ^a	...	308 457 ^a	...
020	309 528	40 789 ^a	40 789 ^a	...	309 528 ^a	...
021	308 596	42 096 ^a	42 096 ^a	...	308 596 ^a	...
022	309 397	41 460 ^a	41 460 ^a	...	309 397 ^a	...
023	309 487	40 993 ^a	40 993 ^a	...	309 487 ^a	...
026	308 324	...	...	...	...	...
030	...	41 737 ^a	...	...	...	...
032	308 627	42 008 ^a	...	...	308 627 ^a	...
033	...	43 167	...	...	...	...
034	308 674	41 912 ^a	...	...	308 674 ^a	...
037	308 671	41 758 ^a	...	...	308 671 ^a	...
039	...	41 401	...	...	...	...
041	...	40 435	...	F1-16	...	...
049	...	41 532	...	...	...	...
052	...	...	...	F2-01	...	...
057	308 524	42 621	...	...	308 524 ^a	...
060	308 829	42 637 ^a	...	...	308 829 ^a	...
061	...	...	...	...	...	V2
064	309 655	41 423 ^a	...	...	309 655 ^a	...
073	...	...	...	F2-07	...	V1 ^a
075	309 663	...	...	...	309 663 ^a	...
083	...	42 484	...	...	...	V5 ^a
084	...	42 550	...	...	...	...
085	308 1382	...	...	...	308 1382 ^a	...
086	308 327	...	...	...	308 327 ^a	...
097	...	40 911	...	...	...	V8 ^a
098	308 477	...	...	...	...	...
100	...	...	...	...	...	V6 ^a
105	...	42 355	...	...	...	V3 ^a
106	...	...	...	F1-21	...	...
108	308 190	...	...	...	...	V4 ^a
111	308 256	42 134	...	F2-17	...	...
113	...	...	...	F1-10	...	...
114	...	...	...	F2-16	...	...
117	...	...	...	F2-06	...	...
118	309 470	...	...	...	...	...
120	...	...	...	F1-09	...	...
122	308 1556	...	...	...	308 1556 ^a	...
125	308 751	...	...	...	...	...
131	308 1473	...	...	...	...	...

Notes. Star identity from this work (Col. 1), Simon & Geha (2007, Col. 2); Adén et al. (2009a, Col. 3); Adén et al. (2011, Col. 4); Deason et al. (2012, Col.5); Kirby et al. (2013, Col. 6); Musella et al. (2012, Col. 7).

^a Available iron abundance value.

galaxy total mass for which we found the value of $M_{\text{tot}} = 3.5 \pm 2.4 \times 10^6 M_{\odot}$, which agrees with literature estimates (e.g. Walker et al. 2009; Adén et al. 2009b). As noted by Adén et al. 2009b, this value is significantly lower than the *common mass scale* found by Strigari et al. (2008, $M_{\text{dyn}} = 1.4^{+0.5}_{-0.4} \times 10^7 M_{\odot}$), suggesting that Hercules does not share the halo properties seen in other dSphs.

The poor statistics of the RV distribution does not allow us to find firm evidence for possible kinematic sub-structures in Hercules. On the other hand, our data cover a significant fraction of the galaxy body, and our selection procedures allowed us to confidently identify likely members. For these reasons, we were able to investigate the galaxy structural properties. In particular,

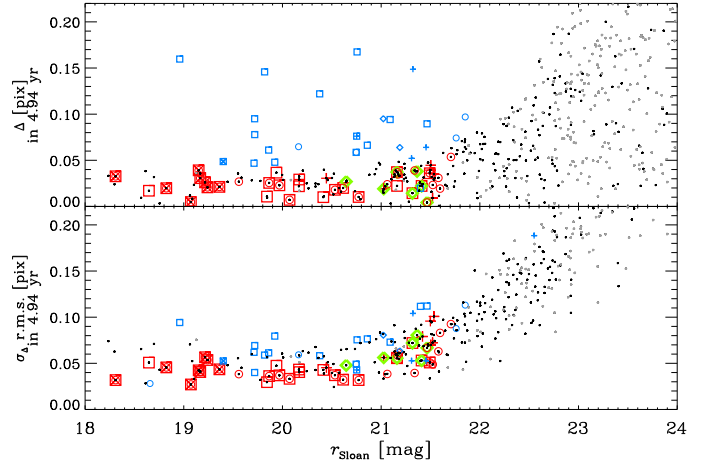


Fig. 9. Displacement (Δ , upper panel) and displacement error (σ_{Δ} , lower panel) as a function of r_{Sloan} magnitude. Symbols are the same as in Fig. 8. For graphical reasons, two spectroscopic sources (non-cross-identified) are not shown in the upper panel, since they have $\Delta > 0.2$ pix.

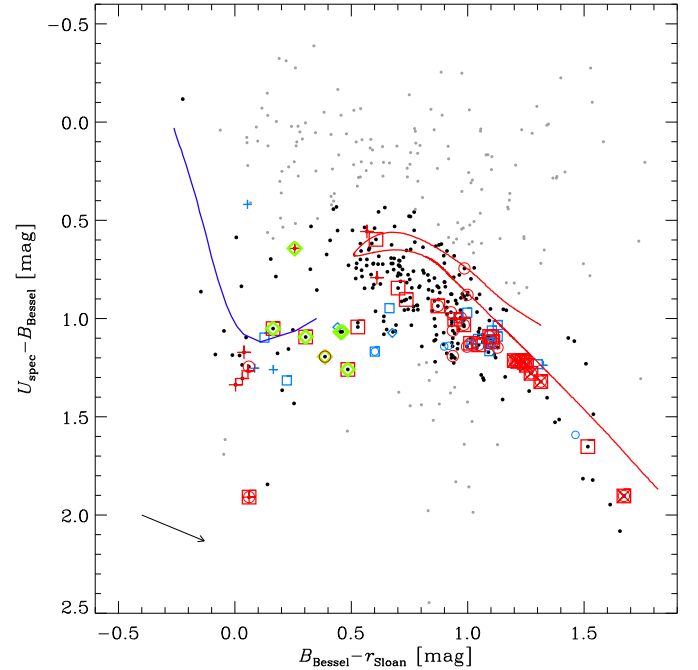


Fig. 10. Colour-colour diagram of Hercules PM-selected stars and spectroscopic targets. Symbols are the same as in the Fig. 8. The isochrone with age $t = 13$ Gyr and $[\text{Fe}/\text{H}] = -2.27$ from the BaSTI database (see text) and the corresponding ZAHB are also shown as red and blue lines, respectively. An arrow indicates the reddening vector.

the left panel of Fig. 8 shows that stars selected according to the PM and colour-colour diagram criteria appear strikingly distributed along the galaxy major axis. We repeated the analysis of Martin et al. (2008) and confirm the large ellipticity ($\epsilon \simeq 0.68$, $\text{PA} \simeq -74^\circ$) of this MW satellite. Deason et al. (2012) suggested a tidal stripping process to explain the high elongation value, a hypothesis supported by the systemic velocity gradient in the outskirts of Hercules. We note that our PM selection confirmed two probable tidal stripped stars (Deason et al. 2012, F1-09 and F1-10 in their Table 2) as Hercules members. Nevertheless, new spectroscopic data, covering a larger area and a larger sample of

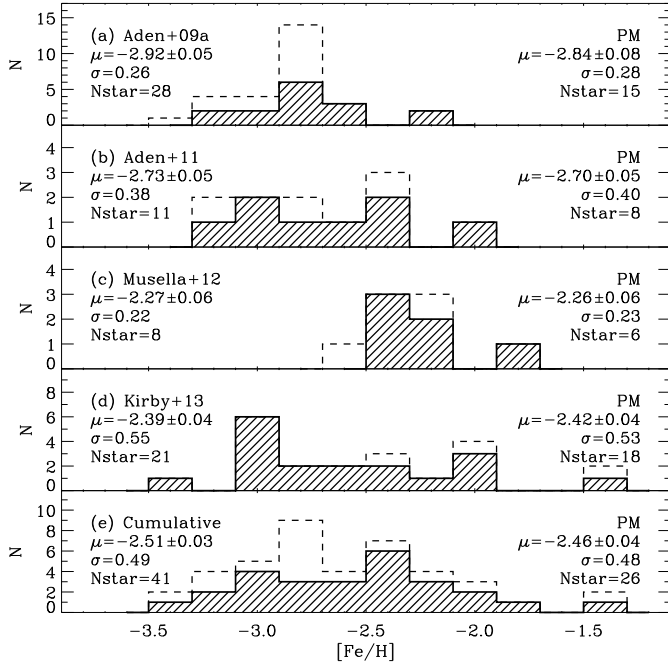


Fig. 11. Metallicity distribution of Hercules stars (dashed lines) according to **a)** Adén et al. (2009a); **b)** Adén et al. (2011); **c)** Musella et al. (2012); and **d)** Kirby et al. (2013). The shaded histograms show the metallicity distributions of the PM-selected stars. Weighted mean and dispersion values are also labelled for the original (on the left) and selected (on the right) distributions, respectively. Panel **e)**: comparison of the whole sample of $[\text{Fe}/\text{H}]$ measurements available in the literature before (dashed histogram) and after (shaded histogram) the PM selection (see text for more details).

stars, are needed to put firm constraints on the Hercules tidal disruption. Our study now provides a robust identification of Hercules members and a solid target list for further spectroscopic investigations.

4.3. Colour-magnitude diagrams

Hercules appears as a very sparsely and poorly populated system (see for instance Fig. 8). In spite of this, the RGB is well-defined, and the HB appears characterised by (i) a group of moderately blue stars easily recognizable at $B_{\text{Bessel}} - r_{\text{Sloan}} \sim 0$ mag; (ii) a handful of stars that are candidate to be extreme blue HB stars; and (iii) a number of stars redder than the RR Lyrae variables and nearly at same magnitude level. The colour-extension of Hercules HB was interpreted by Belokurov et al. (2007) early as a signature of possible multiple stellar populations in the galaxy, since a metal-rich population, possibly 1–3 Gyr younger than the bulk of stars might be responsible for the red HB stars. Such a component was not ruled out by Brown et al. (2012) on the basis of HST photometry. However, we recall that the morphology of the HB can be driven by a complex interplay of different effects (e.g., see Lee 1994; Buonanno et al. 1997; Pasquato et al. 2013).

In Fig. 12, we compare Hercules PM- and colour-colour-selected CMD with theoretical prescriptions. We overplotted isochrones and ZAHBs from the BaSTI database for metallicities compatible with the spectroscopic estimates (i.e. $[\text{Fe}/\text{H}] = -3.27, -2.27, -1.79$). For each metallicity, two sets of isochrones were considered: solar-scaled and α -enhanced

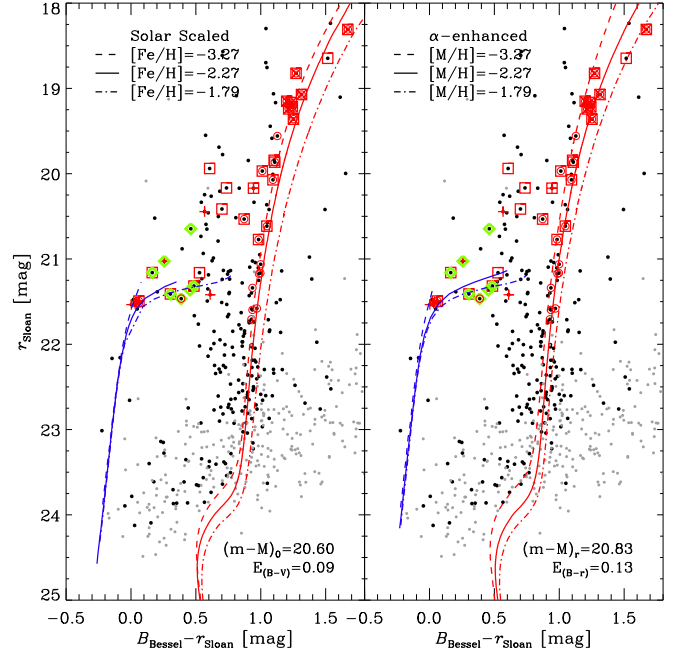


Fig. 12. Solar-scaled (left) and α -enhanced (right) isochrones overplotted to the observed r_{Sloan} vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ CMD of PM and colour-colour-selected members. Symbols are the same as in the Fig. 8.

($[\alpha/\text{Fe}] = +0.4$)⁴. An age of 13 Gyr, the distance modulus $(m - M)_0 = 20.60$ mag and the reddening value $E(B - V) = 0.09$ mag were adopted (Musella et al. 2012). The extinction coefficients are from McCall (2004)⁵. To account for the decrease in the He-core mass caused by the use of more updated conductive opacities, the ZAHB magnitude level was increased by 0.05 mag (Cassisi et al. 2007). Agreeing with spectroscopic measurements, we found that the RGB stars fit either solar-scaled models or α -enhanced chemical mixture models. In particular, the two redder stars at the RGB-tip ($B_{\text{Bessel}} - r_{\text{Sloan}} > 1.4$ mag) match well the most metal-rich isochrones.

Even after cleaning for external sources, there is a number of stars around $B_{\text{Bessel}} - r_{\text{Sloan}} \sim 0.5$ mag spread over one magnitude (from $r_{\text{Sloan}} \sim 20.3$ to 21.3 mag). In our total FoV, we counted about 21 of such stars (see dotted line box in Fig. 13). The feature extended above the HB level was first recognized by Adén et al. (2009b), who also suggested it might be populated by variable stars. However, Musella et al. (2012) identified only one anomalous Cepheid (AC, star V2 in their Table 2, $r_{\text{Sloan}} = 20.64$ mag) in that region of the CMD, which is consistent with a stellar evolution model with $M \sim 1.35 M_{\odot}$ ($Z = 0.0001$). We confirm that this star (the most luminous variable in Fig. 12) with a displacement $\Delta \sim 0$ pix in 4.94 yr is a likely member of the Hercules UFD. The nature of ACs is still debated (e.g. see Marconi et al. 2004). The most widely accepted scenarios are that they could be young (≤ 5 Gyr) single stars belonging to a recent star formation episode or they could be massive stars formed via a mass transfer in binary systems, but as old as the other stars in the stellar system. Therefore, Hercules' AC might be again an indication of the presence of an intermediate-age

⁴ The evolutionary models were constructed assuming a helium-to-metal enrichment ratio $\Delta Y/\Delta Z = 1.4$ and a fixed mass-loss rate described by the mass-loss Reimers parameter $\eta_{\text{R}} = 0.4$ (Pietrinferni et al. 2004).

⁵ $R_U = 4.80, R_B = 4.07, R_r = 2.58$.

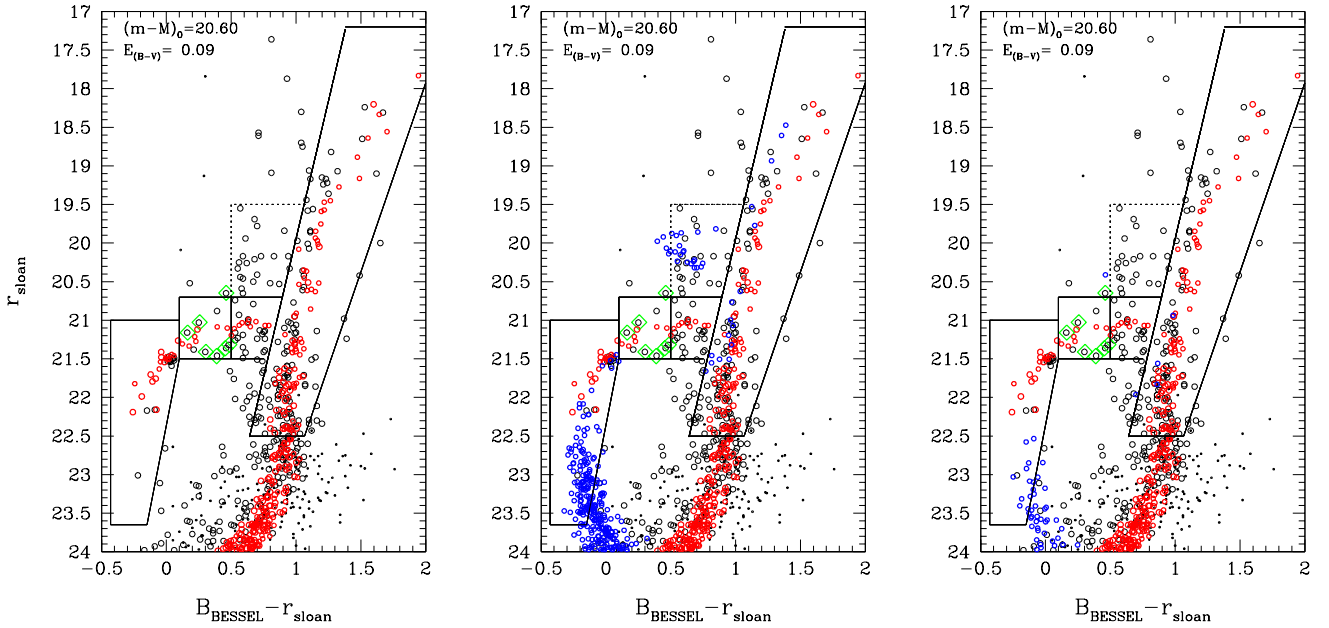


Fig. 13. *Left:* observed CMD of likely Hercules stars (large open black circles) compared to a synthetic CMD composed by three stellar populations (red circles) with $t = 14, 13$, and 10 Gyr and $[\text{Fe}/\text{H}] = -3.27, -2.27$, and -1.79 , respectively. Four boxes (solid lines) are used to count stars on the blue, intermediate and red part of the galaxy HB and RGB+AGB. Observed star counts in boxes are $N = 12, 9, 20$, and 98 (from left to right, respectively). In the dotted line box, the star count is 21 . Observed variables are marked with green diamonds. Small grey circles are background galaxies and Galactic stars discarded via the colour-colour diagram. *Middle:* a stellar population with $[\text{Fe}/\text{H}] = -1.79$ and $t = 1$ Gyr (blue circles) is over plotted to obtain the same stellar count in the dotted box. *Right:* a stellar population with $[\text{Fe}/\text{H}] = -2.27$ and $t = 1.9$ Gyr (blue circles) is over plotted to obtain one star almost located in the same position of the AC.

population that is as old as $\sim 2\text{--}3$ Gyr, as speculated by Musella et al. (2012).

To further investigate this issue and to study stellar counts and distributions in the CMD in general, even in case of a complex population scenario, the stellar population synthesis code SPoT⁶ (Raimondo et al. 2005; Raimondo 2009, and references therein) was used to simulate a series of synthetic CMDs. We constructed a library of CMDs for single-age, single-metallicity stellar populations spanning the metallicity range $-3.27 \leq [\text{Fe}/\text{H}] \leq -1.5$ and the age range $1 \leq t [\text{Gyr}] \leq 14$. The synthetic CMDs were randomly populated using Monte Carlo methods with the initial mass function (IMF) of Kroupa (2001) in the mass interval $0.1 \div 100 M_{\odot}$. This procedure assures a proper study of poorly populated stellar systems, such as the Hercules UFD. For each star, the luminosity and effective temperature were derived according to evolutionary tracks by the BaSTI database, then magnitudes in the photometric bands of the LBT/LBC channels (both red and blue) were computed using colour-temperature relations derived from the stellar atmospheres by Castelli & Kurucz (2003, and references therein). The LBC-filter response curves were taken from Giallongo et al. (2008) and Speziali et al. (2008). We explored different assumptions on stellar population parameters, such as total mass, age, metallicity, and different parameterizations of the HB star distribution (the Reimers mass-loss parameter η_R , its dispersion σ_R , etc.). Each simulation also included a realistic photometric error.

In Fig. 13, we show the comparison between the observed and a synthetic CMD composed by three stellar populations with $t = 14, 13, 10$ Gyr and $[\text{Fe}/\text{H}] = -3.27, -2.27, -1.79$, respectively. The mass fraction of each subpopulation was derived from the spectroscopic metallicity distribution. In the middle

panel of the same figure, we also over plot a stellar population with $[\text{Fe}/\text{H}] = -1.79$ and $t = 1$ Gyr (blue circles). From the simulations, we would expect a corresponding number of stars in the MS phase, to have 21 stars in the dotted line box above the red HB. It appears that HST observations (see Fig. 1 of Brown et al. 2012) and our data, although not suitable for studying the TO region of the galaxy due to the poor signal-to-noise, tend to exclude such a possibility. This agrees with the general finding that UFD galaxies host mainly old stellar populations (Belokurov et al. 2007; Musella et al. 2012; Brown et al. 2012). Hence, a fraction of stars in that region should belong to the MW, in spite of them having a displacement ~ 0 pix in 4.94 yr (i.e. within our magnitude dependent PM uncertainty, see Sect. 2.3.1). On the other hand, the possibility that a few stars in the aforementioned region might be Hercules intermediate-age stars is not totally ruled out. The right panel of Fig. 13 shows the example of a population that produces a star with photometric properties comparable to those of the only one luminous AC known in Hercules. This specific population has $[\text{Fe}/\text{H}] = -2.27$, $t = 1.9$ Gyr, and a total stellar mass (including white dwarfs and neutron stars see Sect. 4.4) of $8 \times 10^2 M_{\odot}$. From the figure, it is clear that the upper part of the younger MS and the HB blue-tail of the older population occupy the same region on the CMD, where we count just a small number of stars. Moreover, the bulk of the younger MS stars is fainter than $r_{\text{Sloan}} \sim 23$ mag, the value at which, unfortunately, our data begins to suffer from incompleteness effects. Therefore, we cannot exclude such a small fraction of an intermediate-age population in the galaxy. We emphasize that the very low number of stars involved in the analysis should deserve a more accurate statistical investigation. On the other side, deeper data covering a larger portion of the galaxy are needed to reach a firmer conclusion. Interestingly, Cusano et al. (2013) recently identified a number of pulsating variables brighter than

⁶ www.oa-teramo.inaf.it/spot

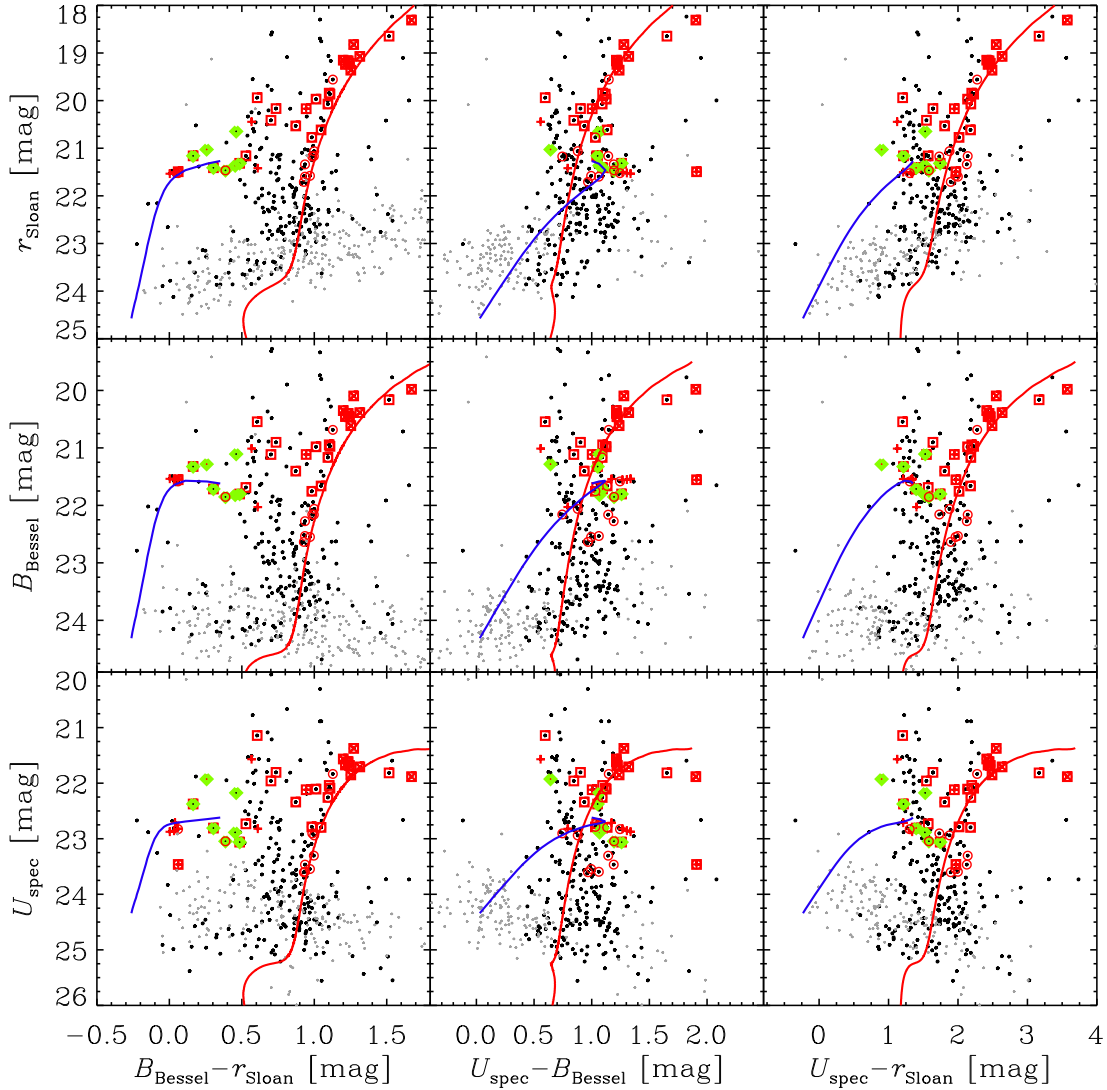


Fig. 14. PM-selected CMDs in different filter combinations with superimposed a solar-scaled isochrone with $t = 13$ Gyr and $[\text{Fe}/\text{H}] = -2.27$ from the BaSTI database and the corresponding ZAHB. The *three panels on the left-hand side* show, from top to bottom, the r_{Sloan} , B_{Bessel} and U_{spec} magnitudes vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ colour, the *middle panels* show the magnitudes vs. $U_{\text{spec}} - B_{\text{Bessel}}$ colour, and the *right panels* the magnitudes vs. $U_{\text{spec}} - r_{\text{Sloan}}$ colour. Symbols are the same as in the Fig. 8.

the RR Lyrae stars in And XIX, a new dwarf satellite of the Andromeda galaxy, raising the question of whether this galaxy was still forming stars up to 1 Gyr ago.

Figure 14 shows the PM-selected CMDs in various filter combinations with superimposed a solar-scaled isochrone with $[\text{Fe}/\text{H}] = -2.27$ and the corresponding ZAHB. The combination of different bands and CMDs allow us to investigate the real membership of the extreme blue-HB stars. We found good agreement of the blue-HB stars with the ZAHB loci in the CMDs, thus supporting their membership to Hercules. Interesting to note is also the HB red incursion in the panels involving the $U_{\text{spec}} - B_{\text{Bessel}}$ colour (see for a discussion Momany et al. 2003).

4.4. Hercules stellar mass

We have used our PM-decontaminated sample to estimate Hercules' stellar mass. The number of member stars above $r_{\text{Sloan}} \geq 22.5$ mag (about half a magnitude brighter than our completeness limit) is quite firm, since the contamination by

Galactic stars and background galaxies is only a few percent at this magnitude level (Sect. 2.3). By contrast, in the region around $B_{\text{Bessel}} - r_{\text{Sloan}} \sim 0.5$ mag and above the red HB, there is still a significant field star contamination, as discussed in Sect. 2.3.1. We considered stellar counts in the different boxes shown in Fig. 13 and restricted our analysis to the area within the galaxy r_h . The observed star counts in the different boxes are $N = 8, 6, 4$, and 57, which move from blue to red in the CMD, specifically the red giants are $N_{\text{RGB}} = 57$.

For each set of parameters (age, chemical composition, IMF, HB parameters, etc.), we constructed a grid of simulated CMDs by changing the total stellar mass to count the desired number of giant stars (N_{RGB}) in a certain number of simulations. In particular, the mass value changes from a few tens of solar masses up to $M_* = 5 \times 10^4 M_{\odot}$. The former value is appropriate to produce very few red giant stars if Hercules is considered to host multiple generations of stars with different metal contents (and ages), as suggested by both photometric and spectroscopic observations. The lowest N_{RGB} (i.e. $N_{\text{RGB}} = 0 \div 5$) considered in the simulation is related to a generation of stars

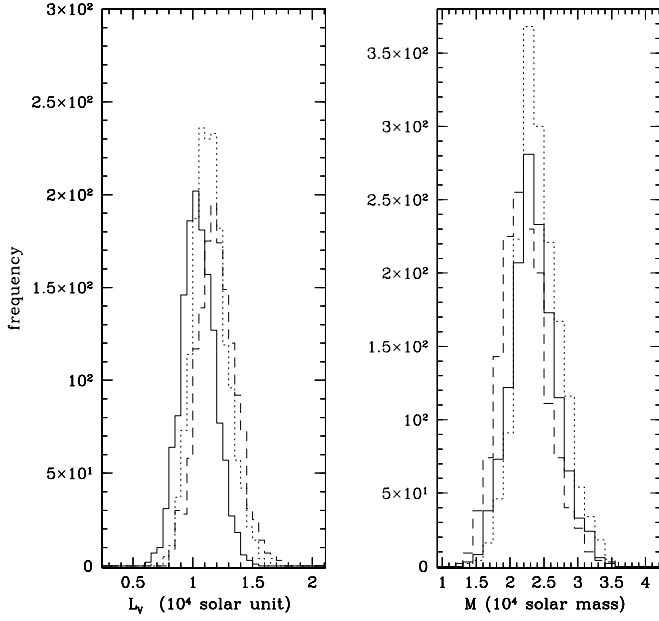


Fig. 15. Frequency distribution of L_V and M_* for simulations containing $N_{\text{RGB}} = 57$. Different lines correspond to stellar populations with $[\text{Fe}/\text{H}] = -3.27$ and $t = 14$ Gyr (solid line), $[\text{Fe}/\text{H}] = -2.27$ and $t = 13$ Gyr (dotted line), and $[\text{Fe}/\text{H}] = -1.79$, $t = 10$ Gyr (dashed line).

with $[\text{Fe}/\text{H}] \sim -1.79$, contributing with a mass fraction as low as a few percent of the total stellar content according to the spectroscopic measurements (see the previous section). The higher mass value corresponds to the mass of a single-age and single-metallicity population accounting for 100% of observed red giants (i.e. $N_{\text{RGB}} = 57 \pm 5$). For each set of parameters and each mass value, we generated 500 simulations. Then, we selected only those simulations with a number of giant stars equal to the observed N_{RGB} . For each set of simulations computed with the same set of parameters and the appropriate number of reference stars (N_{RGB}), we computed the median of the distribution of the integrated total stellar mass (M_*), the luminosity (L) and the magnitudes. This procedure assured us to accurately recover the mass and luminosity of this sparsely populated faint satellite, whose luminosity can be affected by the number and luminosity of individual stars, which is close to the RGB-tip. The total mass included all the evolving stars from the hydrogen-burning limit up to the asymptotic giant branch and stars along the white dwarf (WD) cooling sequence. In addition, stars with an initial mass higher than M_{up} ⁷ were assumed to leave a neutron star (NS) as remnant. To evaluate the maximum contribution of NS stars to the total mass, we set the NS mass at its upper limit ($\sim 2 M_{\odot}$, see e.g. Fagiolini et al. 2007). We found that the NS mass fraction constitutes a few percent of the galaxy mass at most. We did not take into account the contribution of black holes, which assumes on the mass of the remnant and the IMF. However, for a Kroupa-like IMF in metal-poor old stellar populations it is expected that the mass fraction of both NS and black holes does not exceed 5–10% (Maraston 2005, and references therein). This procedure resulted in more than 2000 realizations for each set of

parameters, depending on the expected numbers of stars N_{RGB} , which is over more than 10^4 total simulations.

In Fig. 15, we show, the distributions of L_V and M_* obtained from simulations containing $N_{\text{RGB}} = 57$, and stellar populations with $[\text{Fe}/\text{H}] = -3.27$ and $t = 14$ Gyr; $[\text{Fe}/\text{H}] = -2.27$ and $t = 13$ Gyr and $[\text{Fe}/\text{H}] = -1.79$, $t = 10$ Gyr, as an example.

We assumed that Hercules hosts a single-age, single-metallicity population. In such a case, for a population with $[\text{Fe}/\text{H}] = -2.27$, $t = 13$ Gyr, and the Kroupa’s IMF (i.e. $\alpha_{\text{Kroupa}} = 2.3$ for stars with mass greater than $0.5 M_{\odot}$), we found a total stellar mass of $M_* = (2.5 \pm 0.2) \times 10^4 M_{\odot}$. As expected, the mass does not significantly depend on metallicity in the $[\text{Fe}/\text{H}]$ range considered and at fixed age (e.g. 13 Gyr), being $M_* = (2.3 \pm 0.2) \times 10^4 M_{\odot}$ for $[\text{Fe}/\text{H}] = -3.27$ and $M_* = (2.6 \pm 0.2) \times 10^4 M_{\odot}$ for $[\text{Fe}/\text{H}] = -1.79$. At fixed metallicity (e.g. $[\text{Fe}/\text{H}] = -2.27$), if the age increases to 14 Gyr, the mass does not change, while it decreases of $\sim 0.3 \times 10^4 M_{\odot}$ when $t = 10$ Gyr. We also explored the possibility that the exponent of the Kroupa’s IMF α_{Kroupa} varies: for $\alpha_{\text{Kroupa}} = 1.8$ and 2.8, we found a variation on mass values of $\sim 8\%$, which is compatible with the mass uncertainty due to the small number of red giants in Hercules. Finally, adopting a Salpeter-like IMF (i.e. $\alpha_{\text{Salp}} = 2.35$ down to $0.1 M_{\odot}$, Salpeter 1955) results in a mass value of $M_* = (4.1 \pm 0.4) \times 10^4 M_{\odot}$. The luminosity is much less dependent on the population parameters. The V-luminosity is $L_V = (1.1 \pm 0.1) \times 10^4 L_{V,\odot}$ and the bolometric luminosity is $L_{\text{bol}} = (1.4 \pm 0.1) \times 10^4 L_{\odot}$; changes of the IMF-shape or ages do not give significant variations ($\sim 10\%$). If we rescaled the number of RGB stars to that adopted by Martin et al. (2008) and discard WD and NS stars in our simulations, we find results similar to Martin et al. (2008).

5. Summary and conclusions

We have presented LBT/LBC observations in the r_{Sloan} , B_{Bessel} and U_{spec} -filters obtained in the direction of the Hercules UFD galaxy using both arms of the LBC. Combined with LBT archive data, the r_{Sloan} -filter observations covered a time baseline of 4.94 yr (2008–2013). This allowed us to measure the proper motion of stars in the Hercules field over an area about six times the galaxy half-light radius.

We derived a new precise r_{Sloan} -filter geometric distortion solution for the LBC-red. This allowed us to accurately correct star positions for geometric distortion, resulting in a final catalogue of 5385 stars in r_{Sloan} (and B_{Bessel}) and covering $\sim 0.25 \text{ deg}^2$ of the sky. We measured star relative proper motions with a precision better than 5 mas yr^{-1} ($\sim 0.10 \text{ pix}$ in 4.94 yr) for stars down to $r_{\text{Sloan}} \simeq 22 \text{ mag}$. Finally, we selected 528 sources over an area of $\sim 0.12 \text{ deg}^2$, which is a large portion of the galaxy body.

The present procedure allowed us to disentangle a significant fraction ($>90\%$ up to $r_{\text{Sloan}} \simeq 22 \text{ mag}$) of MW stars from Hercules members. We further improved the CMD cleaning by selecting sources, according to their location in the $U_{\text{spec}} - B_{\text{Bessel}}$ vs. $B_{\text{Bessel}} - r_{\text{Sloan}}$ diagram and removing foreground stars and fainter background galaxies. We finally obtained a sample of 357 likely Hercules stars.

We have compared our PM-selected final catalogue with photometrically and spectroscopically selected literature samples. Our selection criteria allowed us to clear the literature spectroscopic samples from non-members; however, it did not affect the weighted mean and dispersion of the $[\text{Fe}/\text{H}]$ and RV distributions. Our PM selection provides a set of robustly

⁷ M_{up} is defined as the critical stellar mass over which carbon ignition occurs in non-degenerate conditions, marking the boundary between intermediate-mass and massive stars. M_{up} is $\sim 6.0 M_{\odot}$ for the used metallicities (Pietrinferni et al. 2004).

identified Hercules members and a new target list for further spectroscopic observations.

The comparison of our PM and colour–colour selected CMD with isochrones and synthetic CMDs confirmed the presence in Hercules of an old and metal-poor stellar population with a possible spread in metallicity consistent with that derived from spectroscopic observations and the age range $\Delta t \sim 1\text{--}3$ Gyr. Unfortunately, our photometric data do not reach the turn-off point preventing more precise estimates of age. However, we tend to exclude, although cannot totally rule out, that the overabundance of stars in the region above the red HB is due to the presence in Hercules of an intermediate-age population as old as 1 Gyr.

Finally, we have proven that our procedure to estimate star proper motions, based on the LBT, can be extended and applied to stellar systems out to large distances with high accuracy and with significant improvement on the membership identification.

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