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# Sardinia Radio Telescope observations of the Coma cluster

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## ABSTRACT

We present deep total intensity and polarization observations of the Coma cluster at 1.4 and 6.6 GHz performed with the Sardinia Radio Telescope. By combining the single-dish 1.4 GHz data with archival Very Large Array observations, we obtain new images of the central radio halo and of the peripheral radio relic where we properly recover the brightness from the large-scale structures. At 6.6 GHz, we detect both the relic and the central part of the halo in total intensity and polarization. These are the highest frequency images available to date for these radio sources in this galaxy cluster. In the halo, we find a localized spot of polarized signal, with fractional polarization of about 45 per cent. The polarized emission possibly extends along the north-east side of the diffuse emission. The relic is highly polarized, up to 55 per cent, as usually found for these sources. We confirm the halo spectrum is curved, in agreement with previous single-dish results. The spectral index is  $\alpha = 1.48 \pm 0.07$  at a reference frequency of 1 GHz and varies from  $\alpha \simeq 1.1$ , at 0.1 GHz, up to  $\alpha \simeq 1.8$ , at 10 GHz. We compare the Coma radio halo surface brightness profile at 1.4 GHz (central brightness and e-folding radius) with the same properties of the other haloes, and we find that it has one of the lowest emissivities observed so far. Reanalysing the relic's spectrum in the light of the new data, we obtain a refined radio Mach number of  $M = 2.9 \pm 0.1$ .

**Key words:** acceleration of particles – polarisation – galaxies: clusters: individual: Coma Cluster – radio continuum: general.

## 1 INTRODUCTION

Galaxy clusters are unique laboratories for the investigation of turbulent fluid motions, large-scale magnetic fields, and relativistic particles. Radio haloes and relics, respectively, located at the centre and in the outskirts of galaxy clusters, provide direct evidence of the presence of relativistic particles and magnetic fields associated with the intracluster medium. These diffuse sources, with no obvious optical counterparts, are characterized by a faint synchrotron emission, with steep radio spectra<sup>1</sup> ( $\alpha \gtrsim 1$ ), which extends over Mpc scales (e.g. Feretti et al. 2012; Brunetti & Jones 2014; van Weeren et al. 2019).

Radio haloes and relics are usually present in dynamically disturbed galaxy clusters, and their origin and evolution are likely to be associated with the merger history of the clusters. It is supposed that part of the gravitational energy dissipated by merger events is channelled into shocks and turbulence, which can provide the energy for acceleration of the relativistic electrons and protons as well as amplification of magnetic fields on large scales.

Central radio haloes have been observed in a fraction of massive clusters and may probe turbulence dissipation. They are typically not polarized, and so far only a few examples (A2255, MACSJ0717.5+3745, and A523) of large-scale filamentary polarized structures possibly associated with the radio halo emission have been detected (Govoni et al. 2005; Bonafede et al. 2009a; Girardi et al. 2016; Vacca et al. 2022). In the case of A2255, Govoni et al. (2006) suggest that these polarized filaments originate in the periphery of the cluster due to a peculiar steepening of the magnetic field power spectrum with radius. According to Pizzo et al. (2011), however, these structures could alternatively be interpreted as foreground radio relics superimposed on the radio halo due to projection effects. A similar argument has been proposed by Rajpurohit et al. (2021) for the case of the cluster MACSJ0717.5 + 3745, where the relic and a narrow-angle-tailed radio galaxy are interpreted as two different structures projected along the same line of sight.

In contrast to central radio haloes, radio relics are highly polarized (e.g. Clarke & Enßlin 2006; Bonafede et al. 2009b; van Weeren et al. 2010; Loi et al. 2020). It is generally assumed that peripheral radio relics mark the location of shock fronts resulting from cluster merger events. The shock waves can amplify particle energies through the Fermi-I process, as well as amplify the magnetic fields enhancing

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<sup>1</sup>  $S(\nu) \propto \nu^{-\alpha}$ , with  $\alpha$  = spectral index.

the polarized emission (e.g. Enßlin et al. 1998; Kang, Ryu & Jones 2012; Kang & Ryu 2013).

The Coma cluster is one of the nearest galaxy clusters and the first where both a central radio halo (Large, Mathewson & Haslam 1959) and a peripheral radio relic (Jaffe & Rudnick 1979; Ballarati, et al. 1981) have been detected. During the past four decades, these two sources have been extensively analysed at several radio frequencies, allowing a good determination of their radio spectra up to  $\simeq 5$  GHz (e.g. Andernach, Feretti & Giovannini 1984; Thierbach, Klein & Wielebinski 2003). Deep low-frequency observations have shown that the halo and the relic of the Coma galaxy clusters are connected by a bridge of diffuse radio emission (e.g. Kim et al. 1989; Venturi, Giovannini & Feretti 1990; Brown & Rudnick 2011; Bonafede et al. 2021). At 144 MHz, the radio halo extends for more than 2 Mpc (Bonafede et al. 2022). The properties of the Coma radio halo can be explained by models invoking diffuse reacceleration of seed relativistic electrons (e.g. Brunetti et al. 2001; Brunetti & Lazarian 2007; Marchegiani 2019). The presence of even larger-scale diffuse emission around Coma has been suggested by Kronberg et al. (2007), who detected patches of distributed radio ‘glow’ beyond the scale of halo, relic, and bridge.

The study of the spectra of radio haloes and relics is particularly interesting at high frequencies, where important constraints on the physical mechanisms responsible for their formation and evolution can be found (e.g. Loi et al. 2020; Rajpurohit et al. 2020). However, accurate measurement of their integrated spectra over a broad range of frequencies is a difficult task. First, they are usually embedded in a number of discrete sources, whose flux densities need to be carefully subtracted from the total diffuse emission. Secondly, due to their steep spectra, these sources have a low surface brightness at GHz frequencies. Finally, high-frequency observations of extended emission are limited by technical difficulties. Interferometers suffer the so-called missing zero spacing problem, where structures larger than the angular size corresponding to the shortest spacings, are absent, thus making them ‘blind’ to extended structures, while maintaining the high resolution. On the other hand, single dish observations are optimal to detect all the emission up to a scale equal to the size of the scanned region, but will lack emission on angular scales smaller than the primary beam size. One possible solution to these problems is to combine interferometric data with single dish ones to obtain final images with both the high resolution of the interferometer and the short-spacing information provided by the single dish.

To study in detail the high-frequency properties of the diffuse radio emission in the Coma cluster, in this paper we present new Sardinia Radio Telescope (SRT; Bolli et al. 2015; Prandoni et al. 2017) observations in *C* band (6.6 GHz) and *L* band (1.4 GHz). We combined *L* band SRT observations with Very Large Array (VLA) interferometric observations to obtain a final image with both the high resolution of the interferometer and the short-spacing information provided by SRT. We observed the Coma cluster in *L* and *C* bands as part of the SRT Multifrequency Observations of Galaxy Clusters (SMOG) project. The SMOG project (PI: M. Murgia; SRT Project S0001) is an SRT early science program focusing on wideband and wide-field single dish spectral-polarimetric studies of a sample of galaxy clusters. The aim of this project is to use SRT observations of a sample of nearby galaxy clusters known from the literature to harbour diffuse radio haloes, relics, or extended radio galaxies to investigate the intracluster media on large scales and to understand the interplay between relativistic particles and magnetic fields and the life-cycles of cluster radio galaxies (Murgia et al. 2016; Govoni et al. 2017; Loi et al. 2017; Brienza et al. 2018; Vacca et al. 2018).

We also added to the SMOG data of the Coma cluster the *C*-band observations collected during the commissioning of the SARDARA (Sardinia Roach2-based Digital Architecture for Radio Astronomy) backend (Melis et al. 2018).

We describe the radio observations and the data reduction in Section 2. We present the resulting total intensity and the polarized diffuse emission of the Coma cluster in Section 3. The analysis of the halo, and comparison with literature data, is presented in Section 4. The analysis of the relic, and comparison with literature data, is presented in Section 5. In Section 6, we discuss our findings and give the conclusions in Section 7. In Appendix A, we provide details of the imaging stacking algorithm used in the SRT data reduction. In Appendix B, we report a consistency check of the SRT flux density scale. In Appendix C, we look for possible counterparts the halo polarized spot at different frequencies. In Appendix D, we report the parameters of the SRT beam at 6.6 GHz.

Throughout this paper, we assume a Lambda cold dark matter cosmology with  $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ,  $\Omega_m = 0.27$ , and  $\Omega_\Lambda = 0.73$ . At the Coma redshift ( $z = 0.0231$ ; Struble & Rood 1999), 1 arcsec corresponds to 0.46 kpc.

## 2 RADIO OBSERVATIONS AND DATA REDUCTION

The *C*-band observations were taken between 2015 May and 2016 July, with a total of about 90 h on source. The *L*-band observations were taken in 2016 July, with a total of 14 h on source. A summary of the SRT observations is shown in Table 1. The data reduction and imaging were done with the Single-dish Spectral-polarimetry Software (SCUBE; Murgia et al. 2016).

### 2.1 C-band observations

We observed with the SRT an area of  $2 \text{ deg} \times 2 \text{ deg}$  in the field of the Coma cluster centred at  $\text{RA}_{J2000} = 12^{\text{h}}57^{\text{m}}17^{\text{s}}$  and  $\text{Dec.}_{J2000} = +27^{\circ}47'49''$ , using the *C*-band receiver (Peverini et al. 2009). Full-stokes parameters were acquired with the SARDARA backend in the frequency range of 6000–7200 MHz, at a spectral resolution of 1.46 MHz per channel. We performed several on-the-fly (OTF; Mangum, Emerson & Greisen 2007) mapping in the equatorial frame, alternating the RA and Dec. directions. The telescope scanning speed was set to  $6 \text{ arcmin s}^{-1}$  and the scans were separated by 0.7 arcmin to properly sample the SRT beam, whose FWHM is 2.9 arcmin in this frequency range. We recorded the data stream by acquiring 33 full bandwidth spectra per second. Individual samples (each consisting of an independent spectrum) are spaced across the sky by 11 arcsec along the scan direction. Using this set-up, the beam FWHM is sampled with four cells in the direction orthogonal to the scan direction, and is greatly over sampled along the scan direction, but this is averaged out in the final pixelization. Bandpass, flux density, and polarization calibrators were done with at least four cross scans on source calibrators performed at the beginning and at the end of each observing run.

We used a standardized pipeline for the calibration and imaging. We excised all the RFI at well-known specific frequencies. Bandpass and flux density calibration were performed by observing 3C 286, assuming the flux density scale of Perley & Butler (2017). After a first bandpass and flux density calibration cycle, we flagged spectral channels affected by persistent RFI. We then repeated a second round of bandpass and the flux density calibration. We applied the gain-elevation curve correction to account for the gain variation with elevation due to the telescope structure gravitational stress

**Table 1.** Details of the SRT observations centred on  $RA_{J2000} = 12^{\text{h}}57^{\text{m}}17^{\text{s}}$ ;  $Dec_{J2000} = +27^{\circ}47'49''$ . Column 1: Frequency range; Column 2: spectral resolution; Column 3: observing time (calibrators included); Column 4: date of observation; Column 5: number of images on the source; Column 6: calibrators; Column 7: SRT project name.

Frequency range (MHz)	Spectral resolution (MHz/channel)	Time on source (h)	Observing date	OTF Mapping	Calibrators	SRT project
<b>C band</b>						
6000–7200	1.46	3	2015 May 2	1RA × 1Dec.	3C 286, 3C 84	SARDARA comm.
		3	2015 Jul 3	1RA × 1Dec.	3C 286, PKS1830-21	SARDARA comm.
		3	2015 Jul 16	1RA × 1Dec.	3C 286, PKS1830-21	SARDARA comm.
		3	2015 Jul 31	1RA × 1Dec.	3C 286, PKS1830-21	SARDARA comm.
		3	2015 Aug 7	1RA × 1Dec.	3C 286, PKS1830-21	SARDARA comm.
		9	2015 Dec 5	3RA × 3Dec.	3C 286, 3C 84	SARDARA comm.
		3	2016 Feb 2/3	1RA × 1Dec.	3C 286, 3C 84	S0001
		9	2016 Feb 6/7	3RA × 3Dec.	3C 286, 3C 84	S0001
		7.5	2016 Mar 14/15	2RA × 3Dec.	3C 286, 3C 84	S0001
		7.5	2016 Mar 15/16	3RA × 2Dec.	3C 286, 3C 84	S0001
		7.5	2016 Mar 17/18	2RA × 2Dec.	3C 286, 3C 84	S0001
		7.5	2016 Mar 18/19	3RA × 2Dec.	3C 286, 3C 84	S0001
		7.5	2016 Mar 19/20	3RA × 2Dec.	3C 286, 3C 84	S0001
		7.5	2016 Mar 20/21	2RA × 3Dec.	3C 286, 3C 84	S0001
		7.5	2016 Jul 27	2RA × 2Dec	3C 286, 3C 84	S0001
<b>L band</b>						
1300–1800	0.0916	7	2016 Jul 08/09	3RA × 3Dec.	3C 147, 3C 286, 3C 84, 3C 138	S0001
		7	2016 Jul 18	3RA × 3Dec	3C 147, 3C 286, 3C 84, 3C 138	S0001

change. We performed the polarization calibration by correcting the instrumental on-axis polarization and the absolute polarization angle. The on-axis instrumental polarization was determined through observations of the bright unpolarized sources 3C 84 or PKS 1830-21. The leakage of Stokes  $I$  into  $Q$  and  $U$  is in general less than 2 per cent across the band, with an RMS scatter of 0.7–0.8 per cent. We fixed the absolute position of the polarization angle using as reference the primary polarization calibrator 3C 286. The difference between the observed and predicted position angle according to Perley & Butler (2013) was determined, and corrected channel-by-channel. The calibrated position angle was within the expected value of  $33^{\circ}$  for 3C 286, with a RMS scatter of  $\pm 1^{\circ}$ .

Our primary goal is to image the emission of the diffuse emission and the discrete sources in the field of view (FoV) of the Coma cluster. Since we are not interested in retaining any large-scale foreground emission, we removed the baseline scan by scan by fitting a second-order polynomial to the ‘cold-sky’ regions devoid of both discrete sources and of the galaxy cluster extended emission (relic and halo). These cold-sky regions were identified using a mask created with the NRAO VLA Sky Survey (NVSS; Condon et al. 1998) image at 1.4 GHz, convolved with a beam FWHM of 2.9 arcmin and including those sources with a brightness  $>0.5$  mJy beam $^{-1}$ . In this way, we removed the base level related to the receiver noise, the atmospheric emission, and the large-scale foreground sky emission. We then imaged the spectral cubes of the  $L$ ,  $R$ ,  $U$ , and  $Q$  polarizations of all the observing slots. To increase the sensitivity, for each polarization, we stacked all spectral cubes separately for the RA and Dec. directions. We used a weighted stacking to take into account of the different noises of the scans and to taper the region affected by residual RFI (see Appendix A for details).

Finally, we combined all the RA and Dec. scans by mixing their stationary wavelet transform (SWT) coefficients (see Murgia et al. 2016). The de-stripping resulting from the SWT stacking is effective in isolating and removing the characteristic noise oriented along the scanning direction.

The images of the total intensity  $I$ , polarized intensity  $P$ , and the polarization angle  $\Psi$  have been derived from the circular polarizations  $R$  and  $L$ , and from Stokes parameters  $U$  and  $Q$ , according to

$$I = R + L, \quad (1)$$

$$P = \sqrt{U^2 + Q^2}, \quad (2)$$

$$\Psi = 0.5 \cdot \arctan(U/Q). \quad (3)$$

We also corrected the polarization images for the Rician bias (Killeen, Bicknell & Ekers 1986).

## 2.2 L-band observations

We observed with the SRT an area of 3 deg × 3 deg centred at  $RA_{J2000} = 12^{\text{h}}57^{\text{m}}17^{\text{s}}$  and  $Dec_{J2000} = +27^{\circ}47'49''$  in the field of the Coma cluster using the  $L$ - and  $P$ -band dual-frequency coaxial receiver for primary-focus operations (Valente et al. 2022). We used the  $L$ -band component only covering the frequency range of 1.3–1.8 GHz. The data stream was recorded with the SARDARA backend. The configuration used had 1500 MHz of bandwidth and 16 384 channels  $\sim 91.6$  kHz each, full-Stokes parameters, and sampling at 10 spectra per second. We opted for the OTF mapping strategy scanning the sky alternatively along the RA and Dec. direction with a telescope scanning speed of 6 arcmin s $^{-1}$  and an angular separation of 3 arcmin between scan. This choice guarantees a proper sampling of the SRT beam whose full width at half-maximum (FWHM) is about 14 arcmin at 1550 MHz, the central frequency of these observations. Since the sampling time is 100 ms, the individual samples are separated in the sky by 36 arcsec along the scanning direction, but the uneven beam sampling will be compensated for by averaging in the final pixelization.

The SRT  $L$ -band receiver is native linear, and we acquire the vertical and horizontal polarizations,  $X$  and  $Y$ , and the Stokes parameters  $U$  and  $V$ . We used 3C 147 as bandpass and flux density

calibrator and the flux density scale of Perley & Butler (2017) was assumed.

The RFI contamination in the  $L$  band is substantial, and it is necessary to refine the data reduction by iterating RFI flagging and calibration. The pipeline starts by flagging all spectral regions known to be affected by the presence of persistent RFI. This is done using a fixed flag table. An automatic flag algorithm is then used to search both along time and frequency for any other RFI not included in the initial flag table. An initial set of band pass and flux density scale solutions are then obtained. Using this first calibration, we flagged all calibrators' data outside a specific flux density range (from  $-1$  to  $15$  Jy) and we repeated the entire procedure to obtain refined bandpass and flux density solutions. At the end of the process, about 25 per cent of the data were flagged.

We ran the automatic flag algorithm in the calibrated data of the Coma cluster. A 'cold-sky' model for the Coma field is obtained using the NVSS, smoothed at SRT resolution. We masked out all point sources above an intensity level of  $2\sigma$ , the halo, the bridge, and the relic regions, and we used the remaining portion of the FoV to model the subscan baseline with a first-order polynomial (linear fit). We subtracted the baseline from the data to remove receiver noise, atmospheric contributions, and all unwanted sky emission on scales larger than our FoV. We then flagged all data outside a specific flux density range (from  $-0.2$  to  $2$  Jy) and we repeated the procedure to obtain a refined baseline subtraction. Finally, the baseline-subtracted data were then projected on to a regular three-dimensional grid with a spatial resolution of  $3$  arcmin  $\text{pixel}^{-1}$ . These steps were performed in each frequency channel for both the  $X$  and  $Y$  polarizations. We calibrated and analysed only the total intensity of the Coma cluster at  $L$  band.

The frequency cubes for  $X$  and  $Y$  polarizations were stacked separately for RA and Dec. scans, following the same weighted average technique described in the Appendix A. As for the  $C$ -band observations, the final RA and Dec. cubes were merged and de-stripped by mixing the SWT coefficients.

As a last step, the total intensity cube,  $I$ , was formed by summing the two polarizations:  $I = X + Y$ .

### 3 RESULTS

#### 3.1 C-band total intensity and polarization images

In the top panel of Fig. 1, we show the 6.6 GHz SRT total intensity image resulting from the average of all spectral channels in the 1.2 GHz bandwidth. The beam FWHM is 2.9 arcmin. We estimated the image noise level using 100 circular regions of exactly one beam in size scattered all over the background in the FoV. We calculated the dispersion of the average intensity between all the boxes, and found an RMS noise of  $\sigma_I = 0.33$  mJy  $\text{beam}^{-1}$ . This value is very close to the expected confusion noise limit of  $\sigma_c = 0.36$  mJy  $\text{beam}^{-1}$  expected at this frequency and angular resolution, for a spectral index  $\alpha = 0.8$  (Condon 2002). We draw solid contours from  $3\sigma_I$  increasing by a factor of  $\sqrt{2}$ , while light-grey contours are the negative  $-3\sigma_I$  contours. We clearly detect the emission associated to the brightest radio sources in the field, part of the diffuse radio halo (Coma C) at the cluster centre and the peripheral radio relic (B1253+275) located on the south-west of the cluster centre. The detection of the central radio halo and the peripheral relic at 6.6 GHz presented in this work are the images at the highest frequency ever obtained for these diffuse sources in the Coma cluster.

In the SRT 6.6 GHz image, the radio halo diffuse emission is elongated in the north-south direction and the largest linear size,

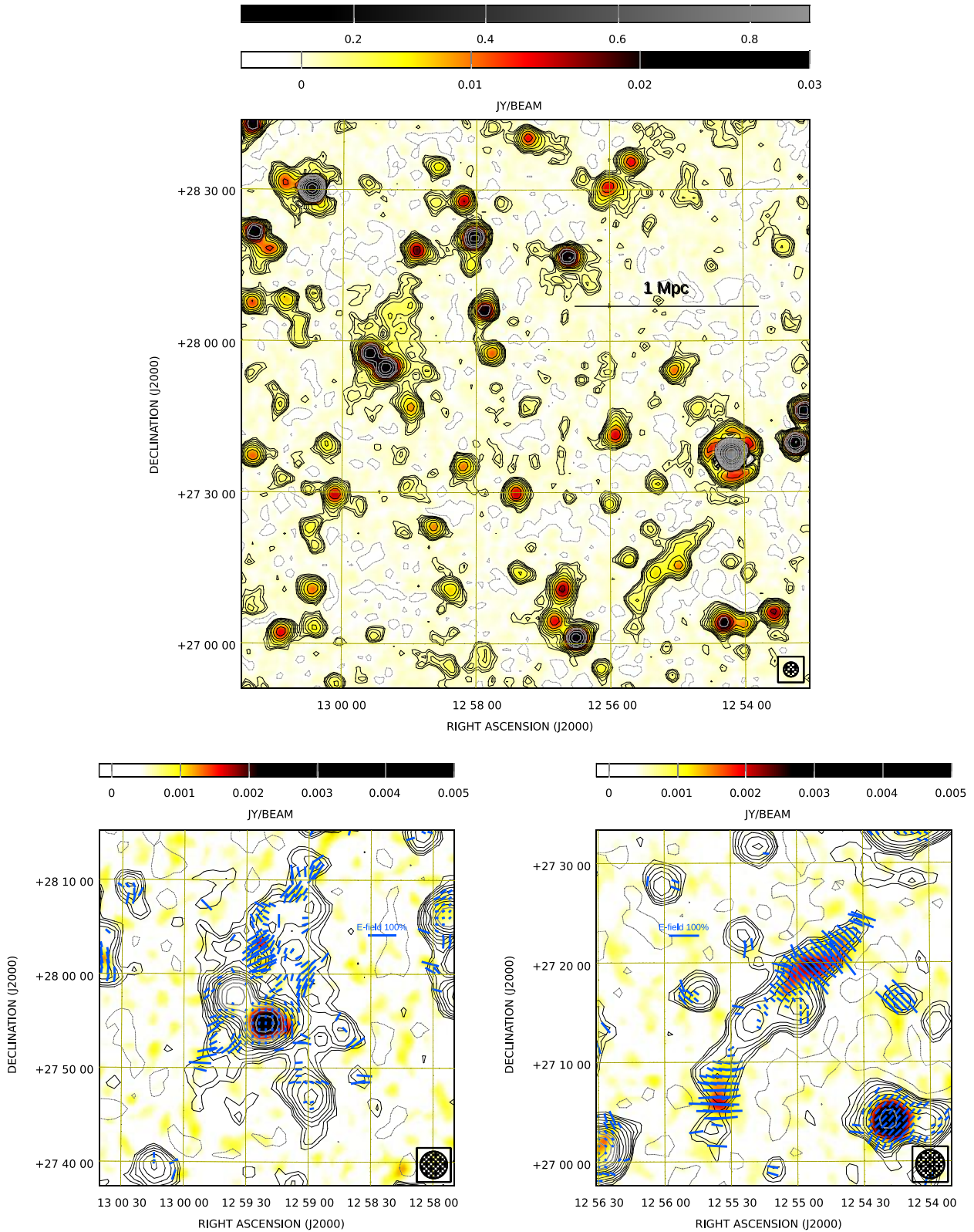
measured from the  $3\sigma_I$  isophote, is approximately 30 arcmin, corresponding to 830 kpc. The overall shape and elongation of the radio halo are broadly consistent with the images at 2.675 and 4.85 GHz obtained at a similar resolution with the Effelsberg 100-m telescope by Thierbach, Klein & Wielebinski (2003). However, the elongation of the halo toward north-west is due in part to a series of point sources incorporated in the diffuse emission, and is analysed in detail in Section 4.1. The radio relic has an elongated structure with a fairly uniform brightness, which extends over a linear length of 770 kpc (or 28 arcmin in angular size) with a deconvolved width of  $\sim 80$  kpc.

We checked the consistency of the calibration of the flux density scale using Coma-A (alias 3C 277.3; RA:  $12^{\text{h}}54^{\text{m}}12^{\text{s}}$ , Dec.:  $+27^{\text{d}}37^{\text{m}}34^{\text{s}}$ ), the strongest radio source in the FoV. Coma-A is an ideal radio source to cross-check the calibration since its emission is dominated by two radio lobes and, given its angular size of  $\text{LAS} \simeq 1$  arcmin, is unresolved by the SRT at 6.6 GHz. By considering all the fifteen observing sessions, the systematic uncertainty for the SRT flux density measurements at 6.6 GHz is estimated to be about 1 per cent. See Appendix B for details.

In the bottom left panel of Fig. 1 we show a zoom of the cluster centre where we have overlaid the radio halo total intensity contours on the 6.6 GHz SRT polarized intensity image obtained by the average of all spectral channels in the 1.2 GHz bandwidth. The polarization noise level, after correction for the positive bias, is  $\sigma_P = 0.25$  mJy  $\text{beam}^{-1}$ . We show the polarization vectors of the  $\vec{E}$ -field where the fractional polarization, defined as  $\text{FPOL} = P/I$ , is detected with  $\text{S/N} > 3$ . We did not correct the polarization vectors for the Rotation Measure effect. The Coma cluster Galactic coordinates are  $l = 58^\circ$  and  $b = 88^\circ$ . The cluster is close to the galactic North Pole and the galactic RM is so low,  $\sim 0.3$  rad  $\text{m}^{-2}$  (Oppermann et al. 2011), that its effect on the observed polarization angle is completely negligible at 6.6 GHz. The bright polarized intensity peak, close to the centre of the halo, is due to the head-tail source 5C 4.81 which is nearly point-like to the SRT beam. The fractional polarization of 5C 4.81 is  $\text{FPOL} \simeq 5$  per cent at 6.6 GHz. This fractional polarization level is significantly less than that measured by Bonafede et al. (2010) at 1.5 arcsec resolution, most likely because of the significant beam depolarization affecting the SRT image. The close-by source to the north-east, 5C 4.85, is completely unpolarized in the SRT image for the same reason. With the VLA at 1.5 arcsec resolution, Bonafede et al. (2010) measured fractional polarization levels of 18 per cent and 10 per cent for 5C 4.81 and 5C 4.85, respectively.

A localized spot of polarization is observed in the radio halo at RA:  $12^{\text{h}}59^{\text{m}}24^{\text{s}}$ , Dec.:  $+28^{\text{d}}03^{\text{m}}00^{\text{s}}$  with an intensity  $I = 2$  mJy  $\text{beam}^{-1}$  and  $P = 0.9$  mJy  $\text{beam}^{-1}$  ( $\text{FPOL} \simeq 45$  per cent). There is a hint that the polarized emission extends along the north-east side of the halo at a level of  $\text{FPOL} \simeq 35$  per cent. We checked for the presence of a discrete source (such as a fossil steep spectrum source) at the position of the spot that could explain the observed level of polarization. We inspected the LOFAR (LoTSS; Shimwell et al. 2022) and GMRT (TGSS; Intema et al. 2017) images at 144 and 150 MHz, but we do not find the presence of any discrete radio source, embedded in the halo diffuse emission in this position. We also verified in the VLA Sky Survey (VLASS; Lacy et al. 2020) at 2–4 GHz for a possible source visible only at high frequency due to of an inverted radio spectrum, but we find none (see Appendix C).

Although many radio haloes have been imaged well in total intensity, their polarized signals are still very difficult to detect, and so far, only a few radio haloes have been imaged in polarization. Using magneto-hydro-dynamical cosmological simulations, Govoni et al. (2013) demonstrated that most radio haloes could be intrinsically polarized, but the resolution and sensitivity of current instruments



**Figure 1.** Top panel: SRT total intensity image at 6.6 GHz of the Coma cluster, resulting from the average of all spectral channels in the 1.2 GHz bandwidth. Contours start at  $3\sigma_I$  where  $\sigma_I = 0.33 \text{ mJy beam}^{-1}$  and increment with a  $\sqrt{2}$  factor. Dotted light-gray contours are negative contours drawn at  $-3\sigma_I$ . The beam FWHM is 2.9 arcmin, as shown in the bottom right corner of the images. Bottom panels: SRT linearly polarized intensity image for the radio halo (left) and relic (right) obtained from the spectral average. The polarization noise level, after the correction for the positive bias, is  $\sigma_P = 0.25 \text{ mJy beam}^{-1}$ . Contours refer to total intensity, while vectors represent the orientation of the polarization angle and are proportional in length to the fractional polarization  $\text{FPOL} = P/I$ . Polarization vectors refer to the radio wave  $\vec{E}$ -field and are traced only where  $\text{FPOL} > 3\sigma_{\text{FPOL}}$ . The reference bar corresponds to a 100 per cent polarized signal.

hinder the detection of this signal. In particular, for the Coma cluster, where the power spectrum of intracluster magnetic field fluctuations extends at most to a maximum scale of a few tens of kpc (Bonafede et al. 2010), we do not expect large-scale polarization associated with the radio halo. However, simulations have shown that, even if most of the polarized emission drops below the noise level, localized spots could be detectable in Coma-like haloes (see e.g. fig. 3 in Govoni et al. 2013).

In the bottom-right panel of Fig. 1, we show a zoom of the radio relic region with the total intensity contours overlaid on the 6.6 GHz SRT polarized intensity image. The radio relic is highly polarized, from  $\text{FPOL} \simeq 40$  per cent in the north-west tip up to  $\text{FPOL} \simeq 50$  per cent in the south-east tip. The polarization vectors are perpendicular to the relic ridge line, as typically observed for these radio sources. At 2.675 GHz and 4.3 arcmin resolution, Thierbach, Klein & Wielebinski (2003) observed the same polarization angle distribution but slightly lower fractional polarization levels of  $\text{FPOL} \simeq 30$  per cent in the north and  $\text{FPOL} \simeq 40$  per cent in the south of the relic, respectively. The fractional polarization levels they measured are in good agreement with those measured with the SRT when considering the beam depolarization effect that could be caused by the coarser angular resolution of their observation.

### 3.2 L-band total intensity images

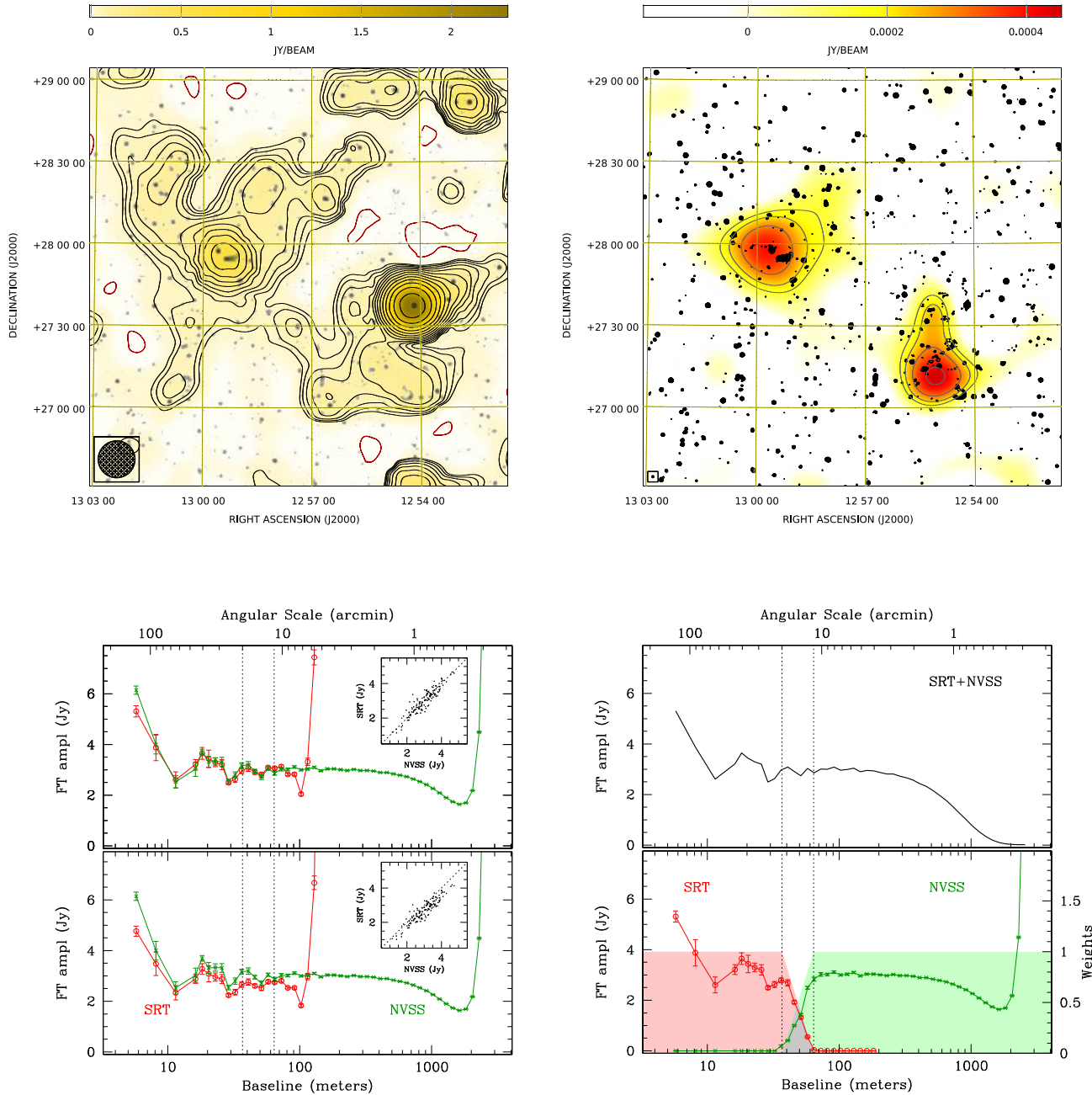
In the top-left panel of Fig. 2, we present the 1.4 GHz SRT total intensity image, represented by contour levels and yellow tones, overlaid on the NVSS image, represented by grey tones. The SRT image is obtained by averaging all spectral channels in a bandwidth of 200 MHz centred at 1.4 GHz. The FWHM beam size is 13.5 arcmin and the image is confusion limited with  $\sigma_c \simeq 30 \text{ mJy beam}^{-1}$ .

We combined our single-dish SRT data together with interferometric data to improve the angular resolution while maintaining the sensitivity to large-scale structures present in the FoV. We computed the combination in the Fourier transform plane using task `ISD_COMBO` in SCUBE.

As a first step, we perform a fine calibration of the SRT flux density scale in the Fourier space to match that of the NVSS in the spatial scale interval common to the two images, as illustrated in the bottom-left plot of Fig. 2. Since processing of the single-dish scans involves fitting a baseline level, this data set may be the one with the most uncertain calibration and a multiplicative factor is used for a finer correction of image values. The same single-dish scaling factor is implemented in the analogous tasks `AIPS IMERG` and `MIRIAD IMMERGE`. The NVSS is effective to determine the scaling factor of the SRT image, given the large number of point sources contained in the mosaic. The plots represent the azimuthally averaged radial profiles of the Fourier amplitudes for the SRT (red dots) and the NVSS (green crosses). The vertical dotted lines delimit the ring in the two-dimensional Fourier space, where the SRT and the NVSS spatial scales overlap. The corresponding baselines range from  $D = 35 \text{ m}$  to  $D = 64 \text{ m}$ , that correspond to angular scales,  $\lambda/D$ , ranging respectively from 21 arcmin to 11 arcmin. The range of spatial scales contained in the images goes from the angular size of the SRT FoV ( $\simeq 3 \text{ deg}$ ), down to the resolution of the NVSS (45 arcsec). Note that the Fourier amplitude profile of NVSS at short baselines ( $< 10 \text{ m}$ ) is comparable to that of SRT, although the NVSS contains no information on these scales due to the lack of short spacings. Indeed, this is a non-physical flux density caused by the convolution in Fourier space with the square window function transform determined by the FoV of the SRT image. However, this does not affect the result of the combination of the two Fourier transforms because we

set the same FoV window function in the NVSS image as well. In fact, SRT does contain more large-scale flux density and actually helps recover extended structures from the Coma cluster, as will be shown below, but it is difficult to see the contribution directly on the amplitude profiles as this is small compared to the flux density of the numerous point sources in the field. Finally, for proper combining, before merging we deconvolved the Fourier transforms of the SRT and NVSS images from the respective Gaussian beams. This causes the steep increase of the amplitude's spectra noticeable at high wavenumbers, which however will be compensated by the final re-convolution with the interferometer's synthesized beam. The SRT amplitude must be increased by a factor of 11 per cent to match the NVSS flux density. The upper panel, in the bottom-left plot of Fig. 2, shows the Fourier amplitude profiles after applying the scale factor to the SRT data. The insets show the consistency of the NVSS and SRT flux density in the ring. In the bottom-right plot of Fig. 2, we present the merging of the Fourier transforms. We used a linear weighting of the interferometer and single-dish amplitudes across the overlap ring, as represented in the lower panel by the shaded regions and the right-axis scale. The upper panel shows the final merged Fourier amplitude re-convolved to the 45 arcsec angular resolution of the NVSS. The black contours in the top-right panel of Fig. 2 represent the combination of the SRT and NVSS images after their merging in the Fourier space. Neither the radio halo nor the relic are detected at 45 arcsec resolution in the SRT+NVSS image. The sensitivity of the NVSS is not enough to detect these extended sources. The red tones and the grey contours show the residual contribution from the SRT data alone, obtained by subtracting the NVSS image from the SRT+NVSS image at 45 arcsec resolution. It is clear that there is a significant contribution to the large-scale flux density from the SRT to both the radio halo region at the cluster centre ( $S_v \sim 400 \text{ mJy}$ ) and the peripheral relic region ( $S_v \sim 200 \text{ mJy}$ ). However, in terms of surface brightness, these contributions are fainter than  $\leq 0.45 \text{ mJy beam}^{-1}$  at 45 arcsec resolution, which happens to be exactly the NVSS 1- $\sigma$  noise level. Therefore, the NVSS is useful for providing a reliable calibration correction factor for the single-dish image, but cannot help detect the Coma radio halo and relic.

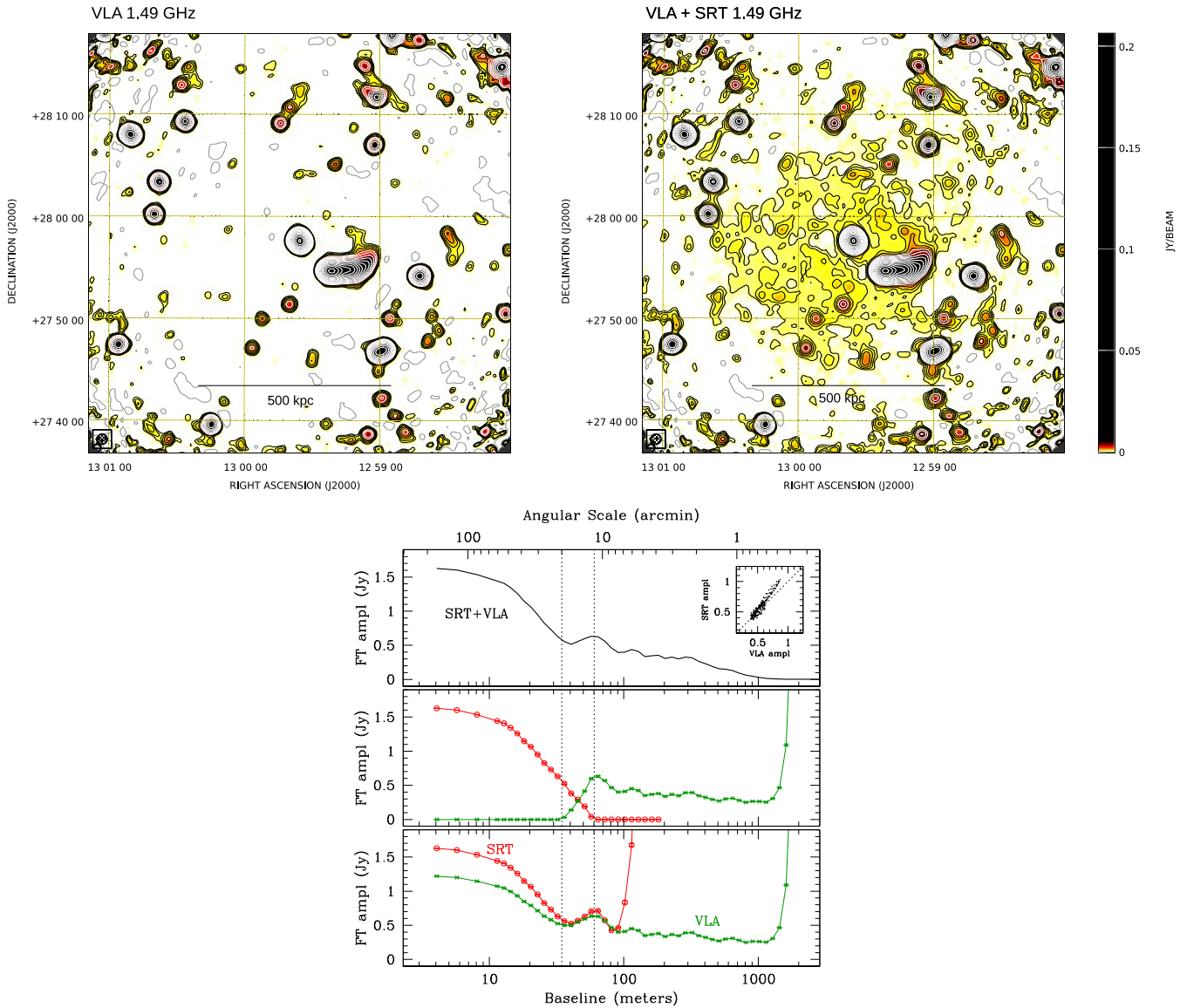
To obtain the deeper images necessary to reveal the halo and the relic, we combined the SRT image with pointed VLA observations by keeping fixed the calibration correction derived from the NVSS. For the radio halo, we used the VLA pointed D-configuration archival observation at 1.49 GHz (project AG200) centred on 5C 4.81. We present the Fourier combination of the VLA and SRT images in Fig. 3. Note that the FoV is smaller than in Fig. 2. For this purpose, we produced an SRT image at a central frequency of exactly 1.49 GHz and a bandwidth of 100 MHz, to match the frequency coverage of the VLA observation. In the top-left panel, we show the VLA D-configuration image at 1.49 GHz corrected for the primary beam attenuation. Before the combination, we tapered the SRT image exactly as the VLA image, basically by zeroing all pixels outside a circle of  $1^\circ$  in diameter centred in the VLA pointing. We show the Fourier merging in the bottom panel. We kept fixed the scale factor of 11 per cent for the SRT flux density scale, as derived from the NVSS, and then we merged the Fourier amplitudes using the same linear weighting scheme as in Fig. 2. The SRT and VLA amplitudes match in the overlapping ring, but now the SRT provides a substantial contribution to angular scales larger than 20 arcmin. We show the result in the top-right panel of Fig. 3, where we present the combined VLA+SRT image at a resolution of 60 arcsec. This image reveals a diffuse low-surface brightness halo at the cluster centre. The halo has a surface brightness of about  $\sim 0.5 \text{ mJy beam}$  at an angular



**Figure 2.** Top-left: SRT image of the Coma cluster at 1.4 GHz represented in contours and yellow tones over the NVSS image (grey-scale). Contours start at  $30 \text{ mJy beam}^{-1}$  (confusion limit) and increase by  $\sqrt{2}$ . The beam FWHM is  $13.5 \text{ arcmin}$ . Top-right: Black contours refer to the combination of the SRT and NVSS images after their merging in the Fourier space. Levels start at  $1.5 \text{ mJy beam}^{-1}$  ( $45 \text{ arcsec beam}$ ) and increase by  $\sqrt{2}$ . The colour image and the gray contours represent the contribution to the extended emission due to the SRT data only, with levels starting at  $3\sigma$ , or  $0.15 \text{ mJy beam}^{-1}$  ( $45 \text{ arcsec beam}$ ), and increasing by  $\sqrt{2}$  (see the text). Bottom left: Azimuthally averaged radial profiles of the Fourier amplitudes for the SRT (red dots) and the NVSS (green crosses). The vertical dotted lines delimit the ring in the Fourier space, where the SRT and the NVSS spatial scales overlap (baselines from 35 to 64 m). The lower panel shows the initial amplitudes of the Fourier transforms deconvolved from the respective observing beam. The SRT amplitude needs to be increased by a factor of 11 per cent to match the NVSS flux density. The upper panel shows the Fourier amplitude profiles after the application of the scaling factor to the SRT data. The insets show the consistency of the NVSS and SRT flux density inside the ring. Bottom right: The lower panel shows the linear weighting of the interferometer and single-dish amplitudes, as represented by the shaded regions and the right-axis scale. The upper panel shows the final merged Fourier amplitude re-convolved to the  $45 \text{ arcsec}$  angular resolution of the NVSS.

resolution of  $1 \text{ arcmin}$  FWHM beam and a linear size of about  $500 \text{ kpc}$  (or  $20 \text{ arcmin}$  in angular size). We discuss how the properties of the Coma radio halo compare to those of other haloes from previous studies in Section 6.1. The intensity is slightly above the  $3\sigma_l$  level

of the VLA D-array image but below the sensitivity of the NVSS, which explains why it was not detected in the image shown in Fig. 2. The extent of the radio halo detected in the SRT+VLA image at  $1.49 \text{ GHz}$  is reassuringly similar to that observed at  $1.4 \text{ GHz}$  by Kim

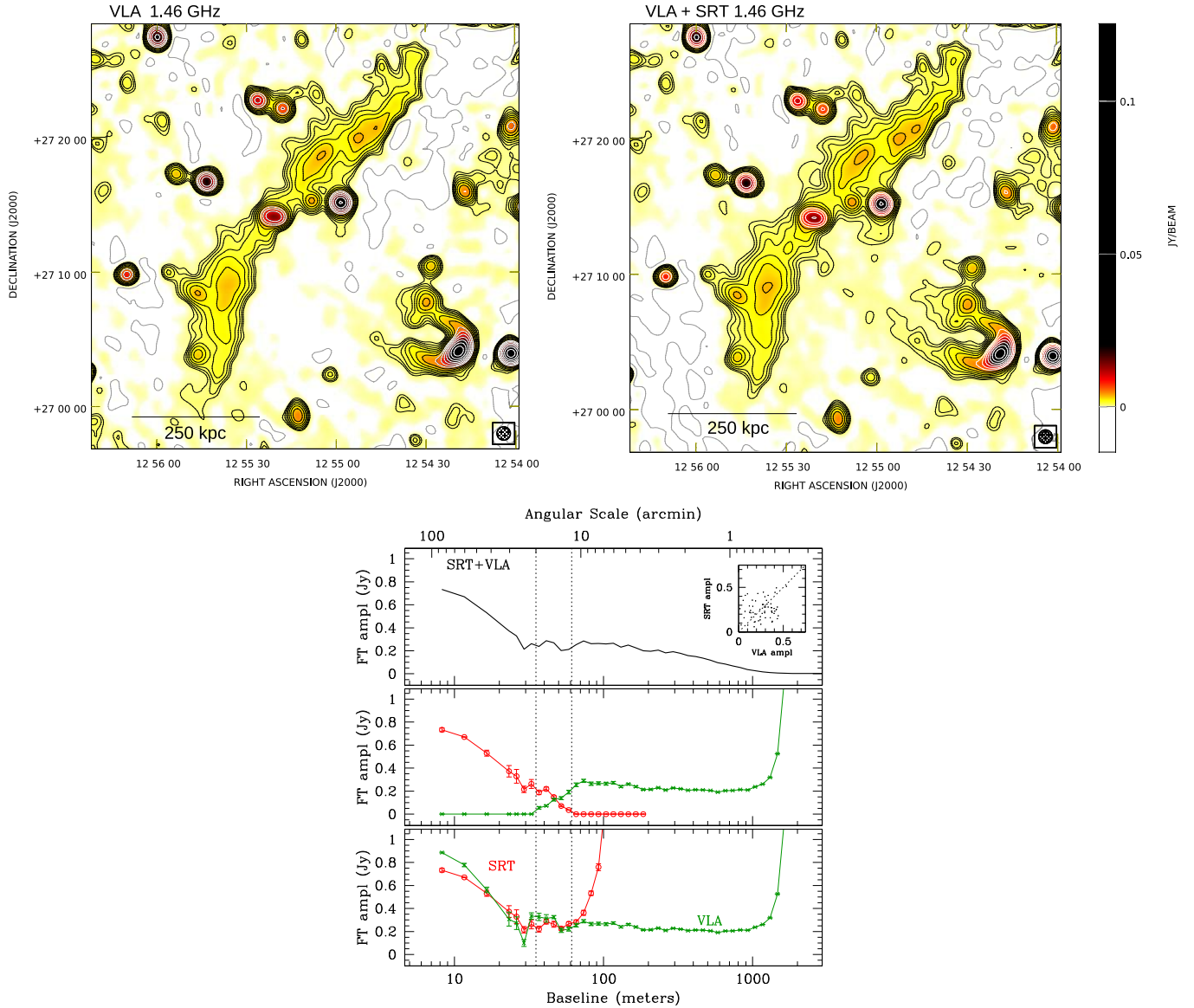


**Figure 3.** Radio images at 1.49 GHz of the centre of the Coma cluster. Top-left: VLA D-configuration image. Top-right: Combination of the SRT and VLA images. In both images, contours start a  $3\sigma_l = 0.45 \text{ mJy beam}^{-1}$  and increase by  $\sqrt{2}$ . The beam FWHM is 60 arcsec. One negative level at  $-3\sigma_l$  is represented in light-grey. Bottom: Plot of the Fourier amplitude as a function of baseline in meters. The lower panel shows the SRT and VLA amplitude deconvolved by the respective point spread functions. The middle panel shows the weighted profiles of the single-dish and interferometer Fourier amplitudes, with a scaling factor of 11 per cent applied to the SRT amplitude. The upper panel shows the combined amplitude re-convolved to the VLA beam of 60 arcsec. The inset shows the consistency of the VLA and SRT flux densities inside the overlapping annulus before the final weighted merging.

et al. (1990) at a resolution of  $71 \text{ arcsec} \times 60 \text{ arcsec}$  (see fig. 2 in that paper). They combined two interferometers, the DRAO Synthesis Telescope and the VLA, to recover the large-scale emission, while we used the SRT single-dish antenna in combination with the VLA. The final results obtained with the two techniques are in excellent agreement.

We produced a combined SRT and VLA image for the radio relic 1253+273 as well. For this, we recovered from the VLA archive four deep D-configuration pointings at 1.46 GHz (projects AA22 and AG200). We combined the four pointings using AIPS task LTESS. We show the resulting image in the top-left panel of Fig. 4. We subtracted the strong point source Coma A from both the VLA mosaic and the SRT image, and we merged the Fourier amplitudes as shown in the bottom panel of Fig. 4. Also in this case, we retained

11 per cent the scale factor of the SRT amplitude, derived from the NVSS. We present the final SRT+VLA image of the radio relic at 1.46 GHz and 60 arcsec resolution in the top-right panel of Fig. 4. Differently from what was observed for the central radio halo, in the case of the relic 1253+273 the addition of SRT data does not reveal the presence of new large-scale emission. Given the morphology of the relic, the VLA does not lose flux density, as its short baselines are sufficient. The Fourier amplitudes for the SRT and VLA data are comparable on the angular scales range from 20 arcmin to 40 arcmin, and consequently the shape of the radio relic is the same, apart from a slight increase in the transverse size. We observe some enhancement of the surface brightness only in the region in between the relic and the head-tail source associated to NGC 4789. Consistent with the LOFAR images at 144 MHz presented in Bonafede et al. (2021) and



**Figure 4.** Radio images at 1.46 GHz of the peripheral relic B1253+275. Top-left: VLA D-configuration image. Top-right: Combination of the SRT and VLA images. In both images, contours start a  $3\sigma_I = 0.45$  mJy/beam and increase by  $\sqrt{2}$ . The beam FWHM is 60 arcsec. One negative level at  $-3\sigma_I$  is represented in light-grey. Bottom: Plot of the Fourier amplitude as a function of baseline in meters. In the lower panel shows the SRT and VLA amplitude deconvolved by the respective point spread functions. Middle panels show the weighted profiles of the single-dish and interferometer Fourier amplitudes, with a scaling factor of 11 per cent applied to the SRT amplitude. The upper panels show the combined amplitude re-convolved to the VLA beam of 60 arcsec. The inset shows the consistency of the VLA and SRT flux densities inside the overlapping annulus before the final weighted merging.

Bonafede et al. (2022), the radio source’s tails appear to be elongated towards the relic and in direct contact with it.

## 4 ANALYSIS – RADIO HALO

### 4.1 Radio halo flux density at 6.6 GHz

We analysed the SRT image at 6.6 GHz to obtain an accurate measurement for the flux density of the radio halo. We integrated the total intensity over a circular aperture of 35 arcmin in diameter, corresponding to about 1 Mpc in linear size. The circumference delimits exactly the  $3\sigma_I$  isophote. We included the contribution of both the discrete radio point sources (PS) and the diffuse emission. We used the accurate beam area of the SRT at 6.6 GHz,  $\Omega_{\text{beam}} =$

9.93 arcmin<sup>2</sup> (see Appendix D), and we found a total (halo+PS) flux density of  $S_{\text{tot}} = 194 \pm 5$  mJy over an area of  $N_{\text{beam}} = 97$ .

We corrected the radio halo flux density for the thermal Sunyaev–Zel’dovich effect (SZE; Sunyaev & Zeldovich 1972). The thermal SZ effect causes a change in the apparent brightness of the cosmic microwave background (CMB) radiation towards the centre of the galaxy cluster. At cm wavelengths, in the Rayleigh–Jeans approximation, the SZ-effect manifests as a decrement in the CMB temperature of  $\Delta T_{\text{RJ}} = -2y \cdot T_{\text{CMB}}$ . The Comptonization parameter,  $y$ , is given by the line-of-sight integral of the product of the thermal electron density,  $n_e$ , and temperature,  $T_e$ :

$$y = \frac{\sigma_T}{m_e c^2} \int_{\text{LOS}} n_e k_B T_e dl. \quad (4)$$

We calculated the intensity decrement at radio frequencies according to

$$\left(\frac{\Delta I_{SZ}}{\text{mJy/beam}}\right) = \frac{1}{340} \left(\frac{\nu}{\text{GHz}}\right)^2 \left(\frac{\Delta T_{RJ}}{\text{mK}}\right) \left(\frac{\Omega_{\text{beam}}}{\text{arcmin}^2}\right) \quad (5)$$

(see Birkinshaw 1999; Basu et al. 2016). Using the image of the Comptonization parameter of the Coma cluster (Planck Collaboration X 2013), we calculated an average value of  $\langle y \rangle \simeq 4.3(\pm 1.0) \times 10^{-5}$  over the radio halo at 6.6 GHz. By using  $\Omega_{\text{beam}} = 9.93 \text{ arcmin}^2$  for the SRT, and  $T_{\text{CMB}} = 2725.5 \text{ mK}$  for the CMB temperature (Fixsen 2009), the expected intensity decrement is  $\Delta I_{SZ} = -0.30 \pm 0.07 \text{ mJy beam}^{-1}$ . The corresponding correction for the SZ decrement at 6.6 GHz in the circular aperture is  $+29 \pm 7 \text{ mJy}$ . We cross-checked the residual base level of the SRT 6.6 GHz image at the external radius of the radio halo using an elliptical annulus of one beam in width. The measured residual base level of the SRT image around the radio halo is  $I_{\text{base}} = -0.25 \pm 0.07 \text{ mJy beam}^{-1}$ . The average Comptonization parameter in the annulus is  $\langle y \rangle = 3.4 \pm 0.9 \times 10^{-5}$ , and the expected SZ signal is  $\Delta I_{SZ} = -0.24 \pm 0.06 \text{ mJy beam}^{-1}$ , which is fully consistent with the measured base level.

A significant fraction of the total flux density is due to the radio galaxies embedded in the radio halo, and their contributions must be carefully removed. In Fig. 5, we show a VLA C-configuration archival image at 1.49 GHz (programme AF196) in gray tones with the SRT radio contours at 6.6 GHz overlaid. We identify ten radio sources with a 6.6 GHz flux density greater than about 1 mJy. We present the integrated spectra of these radio sources in the insets. The dots are the measurements derived from the literature, while the blue line is the best fit of a synchrotron model that is used to estimate the expected flux density at 6.6 GHz (see Table 2). The integrated radio spectra of 5C 4.81 and 5C 4.86 are well described by the Continuous Injection (CI) model. The CI model has three free parameters: the injection spectral index,  $\alpha_{\text{inj}}$ , the break frequency,  $\nu_b$ , and the flux density normalization (Murgia et al. 1999). The spectral index moderately steepens by  $+0.5$  at frequencies above the spectral break,  $\nu_b$ . We fitted the spectra of the remaining point sources with a simple power law with index  $\alpha$ . Adding together the estimated flux densities of all the ten radio sources, we found  $S_{\text{PS}} = 181 \pm 5 \text{ mJy}$ .

We calculated the net radio halo flux density at 6.6 GHz to be

$$\begin{aligned} S_{\text{halo}} &= S_{\text{tot}} - I_{SZ} \cdot N_{\text{beam}} - S_{\text{PS}} \\ &= 194(\pm 5) + 97 \cdot [0.30(\pm 0.07)] - 181(\pm 5) \\ &= 42 \pm 10 \text{ mJy}, \end{aligned} \quad (6)$$

where the final quoted error represents the  $1\sigma$  statistical uncertainty obtained by adding in quadrature the individual errors. We included in quadrature the systematic error on the total halo flux density of 3 per cent. This includes both the systematic uncertainty of the flux density calibrator and the systematic error of the SRT at 6.6 GHz (see Appendix B).

#### 4.2 Radio halo flux density at 1.49 GHz

We derived the radio halo flux density at 1.49 GHz by analyzing the combined SRT+VLA image at 60 arcsec resolution. A mask image is constructed by identifying the discrete sources in the VLA C array image at 1.49 GHz, where the extended emission is not detected. The radio halo at 1.49 GHz fades gradually with radius, therefore we integrated the radio intensity over circular apertures of increasing diameter centred at  $\text{RA}_{J2000}: 12^{\text{h}}59^{\text{m}}35^{\text{s}}$  and  $\text{Dec.}_{J2000}: +27^{\circ}45'50''$ . We computed the flux density as the average intensity times the aperture area, measured in beam units. The halo flux

density increases by increasing the aperture, up to a value of  $S_{\text{halo}} = 424 \pm 7 \text{ mJy}$  at a radius of 650 kpc, beyond that radius the flux density profile stabilizes. The halo flux density is consistent with the residual contribution of the SRT to the extended emission after subtracting the NVSS, shown in the upper right panel of Fig. 2. Note, however, that at larger radii, the noise in the image is affected by the VLA primary beam correction and the integration of the flux density profile is not feasible (see Section 6.1 for an alternative estimate based on the extrapolation of the brightness radial profile).

#### 4.3 Global spectrum of the radio halo

We compared our new measurements of the radio halo flux density at 1.49 and 6.6 GHz with the data in the literature. We list the flux density measurements in Table 3, along with the instruments used to collect the data. The quoted uncertainties refer to the  $1\sigma$  level. However, in the fit procedure, we include a systematic error of 10 per cent to account for the different flux density scales used in these works. By following the procedure used for the SRT measurement at 6.6 GHz, we corrected the measurements at 2.675 and 4.85 GHz for the SZ decrement, by adding respectively 1.9 and 5.9 mJy to the original flux density of 107 and 26 mJy reported by Thierbach, Klein & Wielebinski (2003). At lower frequencies, the correction is negligible. We note that similar approaches to the one used in this work have been followed in the past to correct Effelsberg data for the SZE and to evaluate its impact on the interpretation of the spectral steepening observed in the Coma halo (Enblin 2002; Donnert et al. 2010; Brunetti et al. 2013).

We present the global radio spectrum of the Coma halo in Fig. 6. The spectrum is a collection of measurements taken over more than four decades with very different radio telescopes as well as different procedures to estimate fluxes, and this is reflected in the significant scatter of the data.

We modelled the radio spectrum with a simple modified power law of the form:

$$\log_{10}(S_\nu) = \log_{10}(S_0) - \alpha_0 \cdot \log_{10}(\nu/\nu_0) + k \cdot [\log_{10}(\nu/\nu_0)]^2. \quad (7)$$

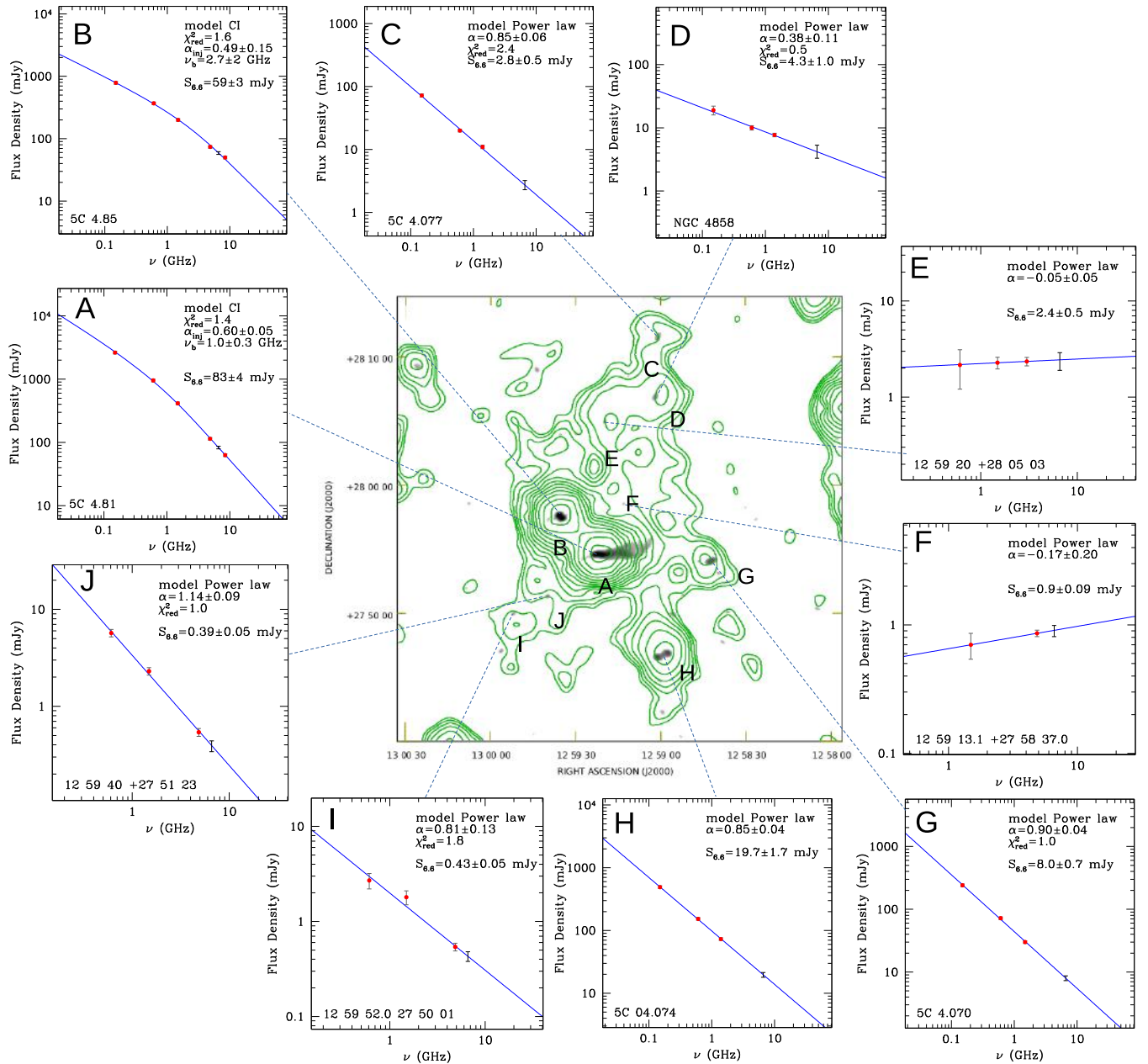
The model has three free parameters. The parameters  $S_0$  and  $\alpha_0$  represent the halo flux density and spectral index at the reference frequency of  $\nu_0$ , respectively. The parameter  $k$  is the spectral curvature. We show the best-fitting model as a continuous line in Fig. 6, where we have used a reference frequency of  $\nu_0 = 1 \text{ GHz}$ . The best fit model yields a normalization of  $S_0 = 743 \pm 55 \text{ mJy}$ . This is a robust estimate for the total radio halo flux density at 1 GHz, given the large scatter of the individual measurements. The radio spectrum is steep. The best-fit spectral index at 1 GHz is  $\alpha_0 = 1.48 \pm 0.07$ . However, the best fit requires a significant curvature in the radio spectrum, with  $k = -0.17 \pm 0.07$ . In this modified power-law model, the spectral index varies with frequency if the curvature  $k \neq 0$ .

We obtain the variation of the model spectral index with frequency,  $\alpha_\nu$ , by differentiating equation (7) with respect to  $\log_{10}(\nu/\nu_0)$ :

$$\alpha_\nu \equiv -\frac{d \log_{10}(S_\nu)}{d \log_{10}(\nu/\nu_0)} = \alpha_0 - 2k \cdot \log_{10}(\nu/\nu_0). \quad (8)$$

This logarithmic derivative can be viewed as the model spectral index calculated between an infinitesimally close pair of frequencies centred at frequency  $\nu$ . The curvature parameter  $k$  can be viewed as the derivative of the spectral index with respect to log frequency:

$$k \equiv -\frac{1}{2} \cdot \frac{d \log_{10} \alpha_\nu}{d \log_{10}(\nu/\nu_0)}. \quad (9)$$



**Figure 5.** VLA C-configuration image at 1.49 GHz and 15 arcsec resolution with the SRT radio contours at 6.6 GHz overlaid. The panels show the spectra of the ten brightest discrete radio sources embedded in the radio halo. The bar shown in each spectrum marks the expected flux density at 6.6 GHz. For the two strongest sources at the centre of the cluster, 5C 4.81 and 5C 4.84, the solid line represents the best fit of the CI model. For the remaining sources, the solid line represents the best fit of a power law.

We represent the variation of the model spectral index with a dashed line in Fig. 6. We observe a progressive steepening of the radio halo spectrum, from a spectral index of 1.1 at 0.1 GHz up to a spectral index of 1.8 at 10 GHz. Indeed, we confirm the halo spectrum is curved, in agreement with previous results obtained with the Effelsberg 100-m telescope (Thierbach, Klein & Wielebinski 2003).

#### 4.4 Radio halo spatially resolved spectra

We extracted the spatially resolved spectra in four independent sectors of the radio halo. We used the LOFAR 144 MHz image

(Bonafede et al. 2022), the WSRT 608 MHz image (Giovannini et al. 1993), the WSRT 326 MHz images (Venturi, Giovannini & Feretti 1990), and the SRT+VLA 1.49 GHz and SRT 6.6 GHz images from this work. We convolved the images to a common angular resolution of 2.9 arcmin. We then extracted the spectra using the circular sectors shown in Fig. 7. The diameter of the circular area (35 arcmin) is the same we used to integrate the total radio halo flux density at 6.6 GHz. We show the radio spectra of the four sectors in the lateral panels. We subtracted the contribution of point sources by masking the areas they occupy. For the calculation of the flux density, we assumed that these blanked area have a total intensity equal to the average in that sector. In practice, we multiplied the total intensity average by the

**Table 2.** Flux density measurements of the discrete radio sources embedded in the halo shown in Fig. 5. The flux densities at 6.6 GHz are estimates.

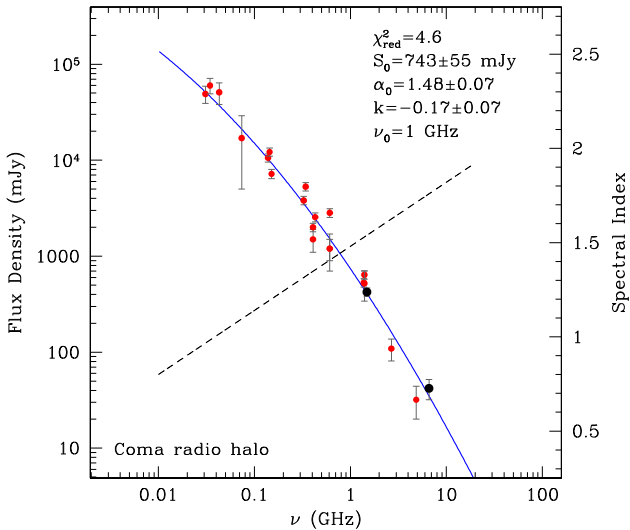
Source	Label	Frequency (MHz)	$S_\nu$ (mJy)	Instrument	Reference
5C 4.81	A	150	$2633 \pm 81$	TGSS	Intema et al. (2017)
		608	$955 \pm 2.6$	WSRT	Giovannini et al. (1993)
		1490	$415 \pm 12$	VLA	VLA project AF196
		4860	$114 \pm 3$	VLA	VLA project AF196
		6600	$83 \pm 4$	<i>Estimate</i>	this work
5C 4.84	B	8440	$63 \pm 2$	VLA	VLA project AF196
		150	$776 \pm 24$	TGSS	Intema et al. (2017)
		608	$369 \pm 1.3$	WSRT	Giovannini et al. (1993)
		1490	$200 \pm 6$	VLA	VLA project AF196
		4860	$74 \pm 2$	VLA	VLA project AF196
5C 4.077	C	6600	$59 \pm 3$	<i>Estimate</i>	this work
		8440	$50 \pm 2$	VLA	VLA project AF196
		150	$72 \pm 4$	TGSS	Intema et al. (2017)
		608	$20 \pm 0.7$	WSRT	Giovannini et al. (1993)
		1400	$11 \pm 0.7$	NVSS	Condon et al. (1998)
NGC 4858	D	6600	$2.8 \pm 0.5$	<i>Estimate</i>	this work
		150	$19 \pm 3$	TGSS	Intema et al. (2017)
		608	$10 \pm 0.8$	WSRT	Giovannini et al. (1993)
		1490	$7.7 \pm 0.5$	VLA	VLA project AF196
12 59 20 +28 05 03	E	6600	$4.3 \pm 1.0$	<i>Estimate</i>	this work
		608	$2.16 \pm 0.95$	WSRT	Giovannini et al. (1993)
		1490	$2.28 \pm 0.32$	VLA	VLA project AF196
		3000	$2.35 \pm 0.24$	VLA	VLA project AF196
12 59 13 +27 58 37	F	6600	$2.4 \pm 0.5$	<i>Estimate</i>	this work
		1490	$0.70 \pm 0.16$	VLA	VLA project AF196
		4860	$0.86 \pm 0.05$	VLA	VLA project AF196
		6600	$0.90 \pm 0.09$	<i>Estimate</i>	this work
5C 4.070	G	150	$241 \pm 9$	TGSS	Intema et al. (2017)
		608	$72 \pm 1$	WSRT	Giovannini et al. (1993)
		1490	$30 \pm 1$	VLA	VLA project AF196
		6600	$8.0 \pm 0.7$	<i>Estimate</i>	this work
5C 4.074	H	150	$491 \pm 16$	TGSS	Intema et al. (2017)
		608	$153 \pm 1.7$	WSRT	Giovannini et al. (1993)
		1400	$73 \pm 2$	NVSS	Condon et al. (1998)
		6600	$19.7 \pm 1.7$	<i>Estimate</i>	this work
12 59 52 +27 50 01	I	608	$2.7 \pm 0.5$	WSRT	Giovannini et al. (1993)
		1490	$1.8 \pm 0.3$	VLA	VLA project AF196
		4860	$0.54 \pm 0.05$	VLA	VLA project AF196
		6600	$0.43 \pm 0.05$	<i>Estimate</i>	this work
12 59 40 +27 51 23	J	608	$5.7 \pm 0.5$	WSRT	Giovannini et al. (1993)
		1490	$2.3 \pm 0.2$	VLA	VLA project AF196
		4860	$0.54 \pm 0.05$	VLA	VLA project AF196
		6600	$0.39 \pm 0.05$	<i>Estimate</i>	this work

number of beams contained in the entire sector. We also subtracted the flux densities at 6.6 GHz of point sources labelled F for sector NW, and sources I and J for sectors SE. The contribution of these sources is relevant only at 6.6 GHz, and thus we decided not to blank them in the images at 2.9 arcmin resolution. We fit the local spectra of the NE, SE, and SW sectors, with the modified power-law model in equation (7). The local spectrum has in general a negative curvature, consistently with the integrated global spectrum. However, the NW sector is an exception. In the NW sector, the spectrum is best fit by a simple power law with no curvature. The simple power-law fit still yields a better fit with a reduced  $\chi^2 = 2.1$ , while the curved power law has reduced  $\chi^2 = 2.5$ . We note that radio halo intensity at 6.6 GHz is also, on average, higher in the NW sector. There may be a connection between the spectral and polarization properties observed in the NW

sector. In fact, the polarized spot shown in Fig. 1 is located exactly within the NW sector, where no significant evidence of spectral curvature is observed. We do not have a definitive explanation for this coincidence. The power-law spectrum may suggest the possibility that the polarized emission is an external structure projected onto the halo, similar to what was found by Rajpurohit et al. (2021) for the case of MACS J0717.5+374. However, if existing, this elusive structure is probably diffuse and no easily distinguishable from the halo, as no obvious discrete sources associated with the polarized spot are found (see Appendix C). Another possibility could be found in the SRG/e-Rosita X-ray data presented by Churazov et al. (2021) showing the presence of a prominent secondary shock west of the core of the Coma cluster. The NW sector is located in the downstream part of the shock. Therefore, the spectral and polarization properties we observe

**Table 3.** Flux density measurements of the radio halo in the Coma cluster. All measurements have the point sources subtracted. Column 1: Frequency [MHz]; Column 2: Flux density [mJy]; Column 3: Type of instrument: Int = image produced from interferometric observations, SD = image produced from single dish observations; Column 4: Flux density reference.

Frequency (MHz)	$S_\nu$ (mJy)	Instrument	Reference
30.9	$49000 \pm 10000$	Int – Clark Lake	Henning (1989)
34.5	$60000 \pm 11000$	Int – Gauribinadur	Sastry & Shevgaonkar (1983)
43.0	$51000 \pm 13000$	Int – Clark Lake	Hanisch & Erickson (1980)
73.8	$17000 \pm 12000$	Int – Clark Lake	Hanisch & Erickson (1980)
139	$10600 \pm 600$	Int – WSRT	Pizzo (2010)
144	$12200 \pm 40$	Int – LOFAR	Bonafede et al. (2022)
151	$7200 \pm 800$	Int – Cambridge Low-Frequency Synthesis Telescope	Cordey (1985)
326	$3810 \pm 30$	Int – WSRT	Venturi, Giovannini & Feretti (1990)
342	$5300 \pm 100$	Int – WSRT	Bonafede et al. (2022)
408	$1500 \pm 400$	Int – Northern Cross	Ballarati, et al. (1981)
408	$2000 \pm 200$	DRAO+Effelsberg	Kim et al. (1990); Flux density from Giovannini et al. (1993)
430	$2550 \pm 280$	SD – Arecibo	Hanisch (1980)
608	$1200 \pm 300$	Int – WSRT	Giovannini et al. (1993)
610	$2830 \pm 300$	SD – GBT	Jaffe & Rudnick (1979)
610	$1200 \pm 500$	Int – WSRT	Valentijn (1978)
1380	$530 \pm 50$	Int – DRAO+VLA	Kim et al. (1990); Flux density from Giovannini et al. (1993)
1400	$640 \pm 35$	SD – Effelsberg	Deiss et al. (1997)
1400	$520 \pm 180$	SD – Arecibo	Hanisch (1980)
1490	$424 \pm 7$	Int+SD – VLA+SRT	This work
2675	$109 \pm 28$	SD – Effelsberg	Thierbach, Klein & Wielebinski (2003), SZ corrected
4850	$32 \pm 12$	SD – Effelsberg	Thierbach, Klein & Wielebinski (2003), SZ corrected
6600	$42 \pm 10$	SD – SRT	This work, SZ corrected



**Figure 6.** Global radio spectrum of the Coma halo. Black dots are measurements from this work, while red dots are the measurements from the literature. The modified power-law best fit is shown as a solid blue line. The dashed line represents the model spectral index as function of frequency (left axis scale).

in this region could be related to the shock passage that possibly influenced both the magnetic field and the spectrum of the synchrotron emission.

We note that the spectral index  $\alpha_0$ , measured for the spectra of the four sectors, is flatter than the global one. However, while the global spectrum is a set of inhomogeneous measurements, the flux densities in the four sectors are obtained from images at the same resolution, in the same regions, and with the point sources subtracted.

## 5 ANALYSIS – RADIO RELIC

### 5.1 Radio relic flux density at 6.6 GHz

We measured the flux density of the radio relic at 6.6 GHz by integrating the total intensity above the  $3\sigma$  isophote. We found a total flux density of  $S_{\text{tot}} = 39.8 \pm 1.2$  mJy, over an area of  $N_{\text{beam}} = 12.7$ . We identified three point sources in the relic: 5C 04.024, 5C 04.029, and J125508+271520 (see Fig. 8). We list the flux densities of these sources in Table 4, and we show their radio spectra in the insets of Fig. 8. We fitted the radio spectra using a power law, and we estimated the expected flux density at 6.6 GHz. Considering all the three sources together, their contributions are  $S_{\text{PS}} = 15.9 \pm 2.1$  mJy.

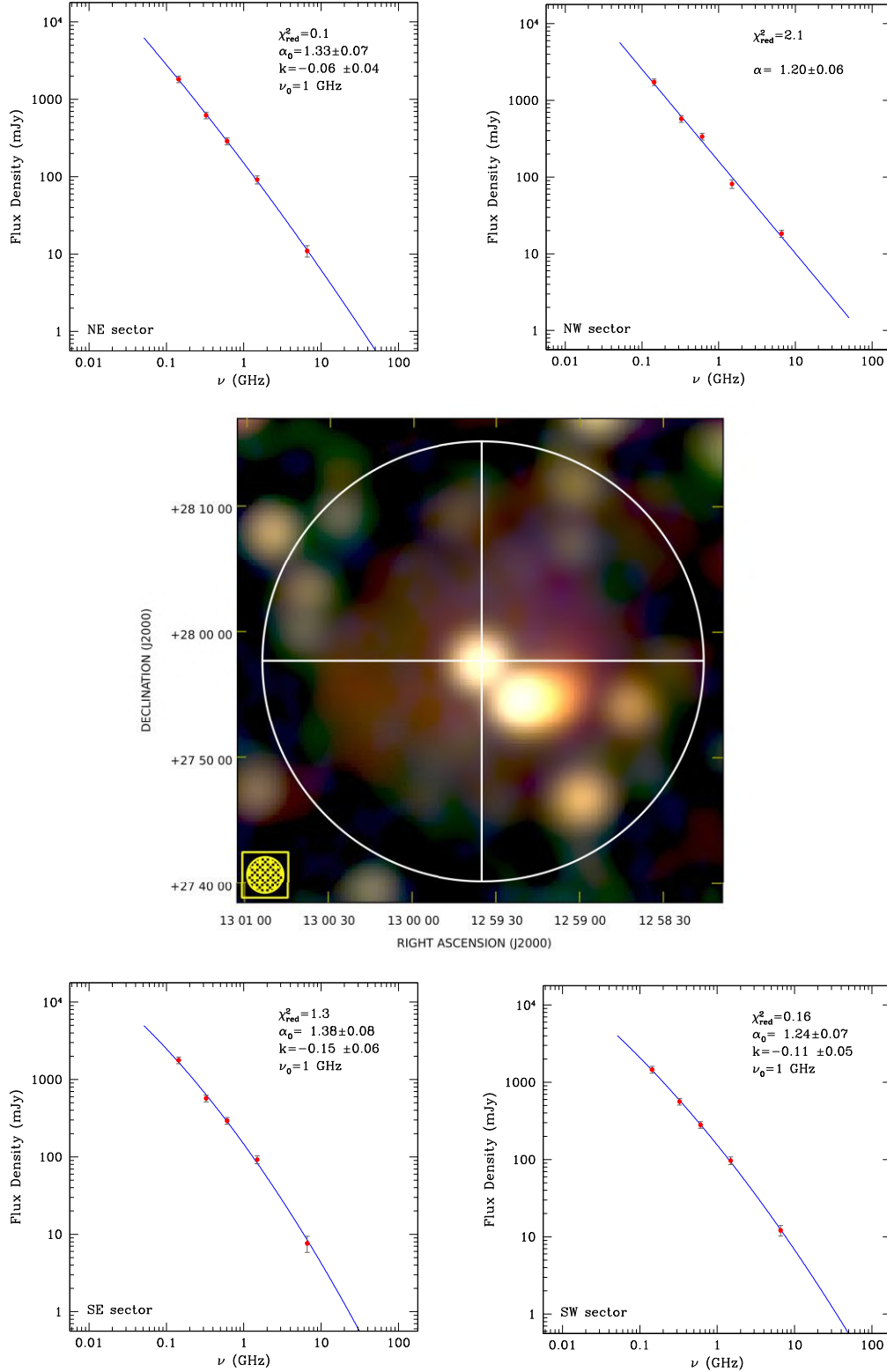
We calculated that the SZ signal at the relic location is  $\Delta I_{\text{SZ}} = -0.04 \pm 0.01$  mJy beam $^{-1}$ . By correcting for the SZ negative signal and by subtracting the point sources contribution, we found for the net radio relic flux density at 6.6 GHz:

$$\begin{aligned}
 S_{\text{relic}} &= S_{\text{tot}} - I_{\text{SZ}} \cdot N_{\text{beam}} - S_{\text{PS}} \\
 &= 39.8(\pm 1.2) + 12.7 \cdot [0.04(\pm 0.01)] - 15.9(\pm 2.1) \\
 &= 24.4 \pm 2.4 \text{ mJy},
 \end{aligned} \tag{10}$$

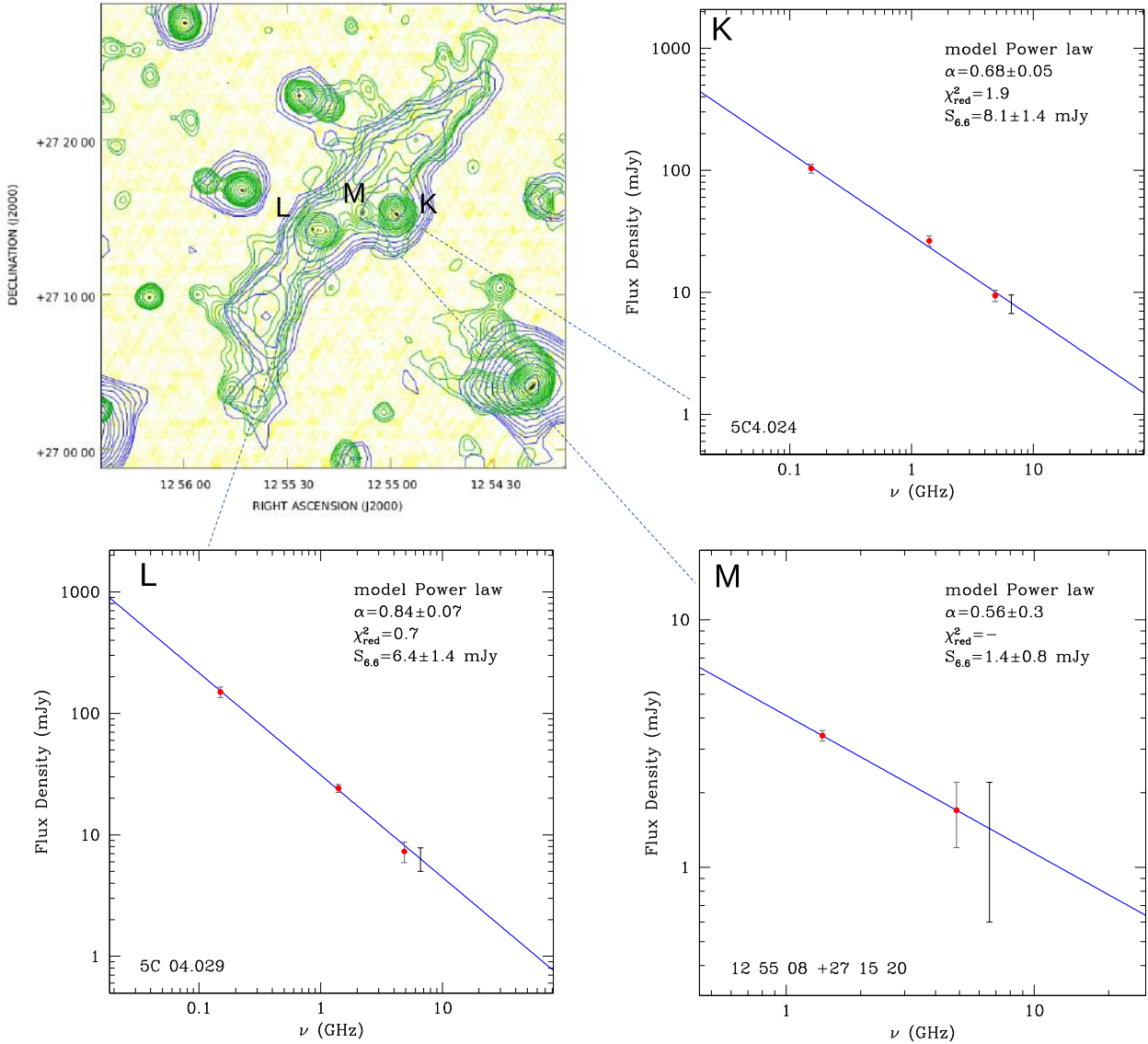
The quoted error refers to the statistical  $1\sigma$  uncertainty, we neglected the systematic uncertainty because it is negligible given the relatively low flux density of the radio relic.

### 5.2 Radio relic flux density at 1.46 GHz

We measured the radio relic flux density at 1.46 GHz using the SRT+VLA image by integrating the total intensity down to the  $3\sigma_I$  isophote. We found a total flux density of  $S_{\text{tot}} = 230 \pm 2$  mJy, over an area of  $N_{\text{beam}} = 121.7$ . We subtracted from this value the point sources contribution of  $S_{\text{PS}} = 49 \pm 4$  mJy. We estimated a net relic flux density at 1.46 GHz of  $S_{\text{relic}} = 181 \pm 4$  mJy. The relic flux density is consistent with the residual contribution of the SRT to the



**Figure 7.** Tricolor radio halo image of the Coma radio halo obtained by superposing images at 0.608 GHz (red), 1.49 GHz (green), and 6.6 GHz (blue) at a resolution of 2.9 arcmin. The lateral panels show the halo spectra in the four sectors represented in the central picture, where we also included the LOFAR flux densities at 0.144 GHz. The blue lines are the best fit of the modified power-law model, except for the NW sector, where it represents the fit of a simple power law with no curvature. We corrected the 6.6 GHz flux density for the SZ decrement. The diameter of the circular region is the same we used to integrate the total flux density of the radio halo. Note that we have masked the regions occupied by discrete radio sources so that the radio spectra refer only to the diffuse emission.



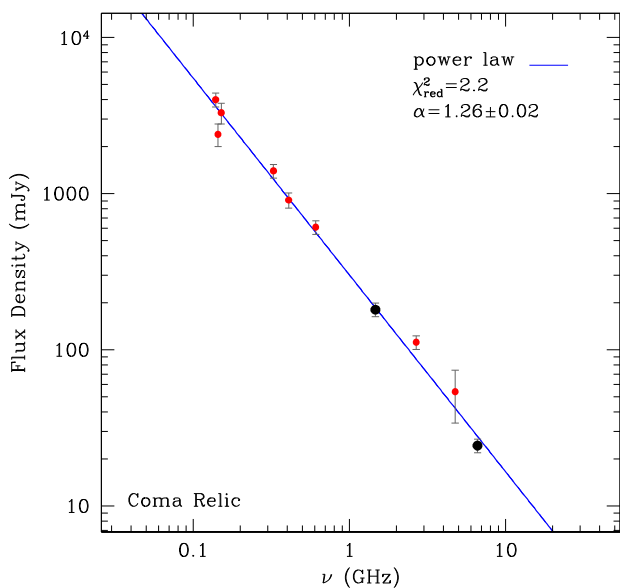
**Figure 8.** VLA FIRST image at 1.4 GHz and 6 arcsec resolution of the relic 1253+273, with the SRT+VLA radio contours at 1.46 GHz (green) and the SRT contours at 6.6 GHz (blue) overlaid. The panels show the spectra of three discrete radio sources embedded in the radio relic. The bar shown in each spectrum marks the expected flux density at 6.6 GHz. The blue line is the best fit of a power-law model.

**Table 4.** Flux density measurements of the discrete radio sources embedded in the relic, shown in Fig. 8. The flux densities at 6.6 GHz are estimates.

Source	Label	Frequency (MHz)	$S_\nu$ (mJy)	Instrument	Reference
5C 04.024	K	150	$104 \pm 9$	TGSS	Intema et al. (2017)
		1400	$26 \pm 3$	NVSS	Condon et al. (1998)
		4860	$9.4 \pm 1$	VLA	VLA project AG194
		6600	$8.1 \pm 1.4$	<i>Estimate</i>	this work
5C 04.029	L	150	$150 \pm 15$	TGSS	Intema et al. (2017)
		1400	$24 \pm 2$	NVSS	Condon et al. (1998)
		4860	$7.3 \pm 1.4$	VLA	VLA project AG194
		6600	$6.4 \pm 1.4$	<i>Estimate</i>	this work
J12 55 08 +27 15 20	M	1400	$3.4 \pm 0.2$	FIRST	Becker, White & Helfand (1995)
		4860	$1.7 \pm 0.5$	VLA	VLA project AG194
		6600	$1.4 \pm 0.8$	<i>Estimate</i>	this work

**Table 5.** Flux density measurements of the relic shown in Fig. 9. All measurements are with embedded point sources subtracted. Column 1: frequency (MHz); Column 2: flux density (mJy); Column 3: type of instrument: Int = image produced from interferometric observations, SD = image produced from single dish observations; Column 4: flux density reference.

Frequency (MHz)	$S_\nu$ (mJy)	Instrument	Reference
139	$4000 \pm 200$	Int – WSRT	Pizzo (2010)
144	$2400 \pm 400$	Int – LOFAR	Bonafede et al. (2022)
151	$3300 \pm 500$	Int – Cambridge Low-Freq. Synth.Tel.	Cordey (1985); Flux density from Giovannini, Feretti & Stanghellini (1991)
326	$1400 \pm 30$	Int – WSRT	Giovannini, Feretti & Stanghellini (1991)
408	$910 \pm 100$	Int – Northern Cross	Ballarati, et al. (1981); Flux density from Giovannini, Feretti & Stanghellini (1991)
608	$611 \pm 50$	Int – WSRT	Giovannini, Feretti & Stanghellini (1991)
1465	$181 \pm 4$	Int+SD – VLA + SRT	This work
2675	$112 \pm 10$	SD – Effelsberg	Thierbach, Klein & Wielebinski (2003)
4750	$54 \pm 20$	SD – Effelsberg	Andernach, Feretti & Giovannini (1984)
6600	$24.4 \pm 2.4$	SD – SRT	This work, SZ corrected



**Figure 9.** Flux density of the Coma relic as a function of the frequency. Red dots are measurements from the literature, while black dots are the new 1.46 GHz and 6.6 MHz measurements presented in this work. The blue line represents the best fit of a power-law model.

extended emission after subtracting the NVSS, shown in the upper right panel of Fig. 2.

### 5.3 Global spectrum of the radio relic

We collected the flux density at different frequencies, available in the literature for the relic. These are listed in Table 5, along with the measurements taken in this work. We present the global spectrum of the relic in Fig. 9. The data set is made up by a collection of inhomogeneous flux density measurements taken over various decades with different instruments by different authors, and in the fitting procedure we considered for each data point a systematic error of 10 per cent error to account for the different calibration scales involved. Furthermore, we only included in Table 5 those measurements in which point sources have been subtracted from the flux density of the relic. The best fit of a power-law model gives a global spectral index  $\alpha = 1.26 \pm 0.02$  with a reduced  $\chi^2_{\text{red}} = 2.2$ . We found a spectral index of the radio relic that is slightly steeper than

the early value reported by Thierbach, Klein & Wielebinski (2003),  $\alpha = 1.18 \pm 0.02$ .

## 6 DISCUSSION

### 6.1 The Coma radio halo in the $I_0$ – $r_e$ plane

We compared the basic morphological properties of the radio halo in the Coma cluster with those of other similar sources known in the literature. In particular, we used the SRT+VLA image at 1.49 GHz to determine the central intensity and the e-folding radius of the diffuse emission.

In order to investigate the morphological properties of the diffuse radio emission in clusters of galaxies, Murgia et al. (2009) proposed to fit their azimuthally averaged intensity profile with an exponential of the form:

$$I(r) = I_0 e^{-r/r_e}. \quad (11)$$

By fitting the observed intensity profile one obtains the central brightness,  $I_0$ , and the e-folding radius,  $r_e$ , from which the average radio halo emissivity can be calculated as

$$\langle J \rangle \simeq 7.7 \times 10^{-41} (1+z)^{3+\alpha} \cdot \frac{I_0}{r_e} \quad (\text{erg s}^{-1} \text{cm}^{-3} \text{Hz}^{-1}), \quad (12)$$

or, in more convenient units:

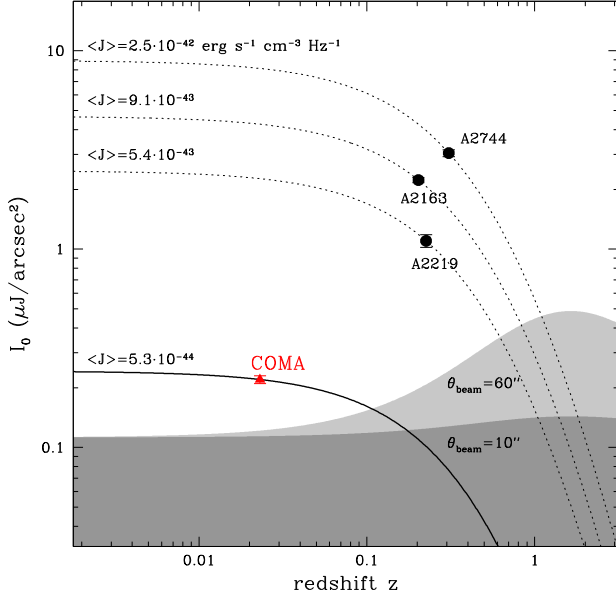
$$\langle J \rangle \simeq 2.3 \times 10^{26} (1+z)^{3+\alpha} \cdot \frac{I_0}{r_e} \quad (\text{W Hz}^{-1} \text{Mpc}^{-3}), \quad (13)$$

where  $I_0$  and  $r_e$  are, respectively, measured in  $\mu\text{Jy arcsec}^{-2}$  and kpc. The term  $(1+z)^{3+\alpha}$  takes into account of both the  $k$ -correction and cosmological dimming of the surface brightness with redshift.

In the bottom-left panel of Fig. 10, we show the modelling of the azimuthally averaged radial profile of the Coma radio halo at 1.49 GHz. We obtained the profile using the circular annuli shown in the bottom-right panel of Fig. 10. We masked all the point sources, implicitly assuming for the blanked regions the same halo average brightness as in the rest of the annulus. By a fit of the exponential law, we obtained  $I_0 = 0.22 \pm 0.01 \mu\text{Jy arcsec}^{-2}$  and  $r_e = 350 \pm 50$  kpc. The flux density obtained by extrapolating the surface brightness profile up to  $3r_e$  is of  $S_{3r_e} = 650 \pm 95$  mJy.

In the top-left panel of Fig. 10, we show the Coma cluster in the  $I_0$ – $r_e$  plane at 1.4 GHz along with a sample of 15 known radio haloes presented in Murgia et al. (2009), Murgia et al. (2010), and





**Figure 11.** The Coma radio halo in the  $I_0$ -redshift plane in comparison with much brighter haloes of similar e-folding radius. The lines represent the dimming of the radio halo surface brightness as a function of redshift for a constant emissivity. The shaded areas indicate the minimum intensity below which the radio halo would be undetectable at 1.4 GHz because of the confusion limit. Light and dark grey areas correspond to angular resolutions of 60 and 10 arcsec, respectively (see the text).

floor is equal to the FWHM beam:

$$I_{\min}(z) = 3\sigma_c \cdot \exp\left[\frac{\theta_{\text{beam}}''}{r_e(z)''}\right], \quad (14)$$

where  $\theta_{\text{beam}}$  is the FWHM beam and  $r_e(z)''$  is the (redshift dependent) angular size of the e-folding radius in arcseconds, while for the confusion noise we adopted the formula by Condon (2002):

$$\sigma_c = 0.05 \cdot (\nu/\text{GHz})^{-0.8} (\theta_{\text{beam}}/60 \text{ arcsec})^2 \mu\text{Jy arcsec}^{-2}. \quad (15)$$

In practice, we require that, to be detectable as such, a radio halo must have a minimum angular diameter, measured using the  $3\sigma_c$  isophote, of at least two times the FWHM beam.

In Fig. 11, we show the Coma radio halo in the  $I_0$ -redshift plane in comparison with the much brighter haloes, of similar size, hosted in the galaxy clusters A2219, A2163, and A2744. The average  $r_e$  of these radio haloes is about 340 kpc, that is comparable to that of the Coma radio halo. The lines represent the dimming of the radio halo brightness as a function of redshift for a constant emissivity. We estimate that a Coma-like radio halo could be detectable only up to maximum redshift  $z \lesssim 0.1$ , beyond this distance it would be hardly observable at 1.4 GHz and 60 arcsec resolution. This region of parameter space is represented by the light-grey area. The interferometers of the new generation (such as MeerKAT, ngVLA, and SKAO) may allow for confusion limited images of radio haloes at even higher angular resolution. For example, in Fig. 11 we show in dark-grey the predicted undetectable region for a radio halo observed at 1.4 GHz and 10 arcsec resolution. In this case, it would be possible to observe a Coma-like radio halo up to a redshift  $z \lesssim 0.2$ .

The Coma radio halo could be representative of a class of intrinsically large radio haloes with low surface brightness that are visible only at very low redshifts. We speculate that the gap, in the  $I_0$ - $r_e$  plane shown in the top panel of Fig. 10, between the Coma

and the other radio haloes of comparable size could be due to this observational bias.

We compare our estimate for the halo central brightness of  $I_0 = 0.22 \pm 0.01 \mu\text{Jy arcsec}^{-2}$  at 1.49 GHz, with the value of  $I_0 = 5.42 \pm 0.04 \mu\text{Jy arcsec}^{-2}$  at 0.144 GHz, estimated using LOFAR by Bonafede et al. (2022). The two values are indeed in excellent agreement if one considers for the radio halo a spectral index of  $\alpha = 1.4$  between 0.144 and 1.49 GHz. This is the same spectral index value that is deduced using the model fit shown in Fig. 6. The e-folding radius at 1.49 GHz,  $r_e = 350 \pm 35$  kpc, is slightly larger than that at 0.144 GHz,  $r_e = 310 \pm 1$  kpc.

## 6.2 The Coma radio relic shock wave

Radio relics are associated with cosmological shock waves produced by accretion and merging phenomena in galaxy clusters (Enßlin et al. 1998). In the context of the diffusive shock acceleration theory (Drury 1983), the shock-wave compression ratio,  $R$ , is related to the stationary radio spectral index by

$$R = \frac{\alpha + 1}{\alpha - 1/2}, \quad (16)$$

where  $\alpha = \alpha_{\text{inj}} + 0.5$ , and the injection spectral index is related to  $\delta$ , the index of the energy distribution of accelerated particles in the shock, by  $\alpha_{\text{inj}} = (\delta - 1)/2$ . The stationary spectral index refers to the asymptotic power-law regime that is reached when the number of particles that leave a given energy bin because of the radiative losses is equally replaced by the newly accelerated particles. If the integrated radio spectrum of the Coma relic represents the steady state, then the observed high-frequency spectral index  $\alpha = 1.26 \pm 0.02$  implies a compression factor  $R = 3.0 \pm 0.1$ . From the shock theory (see e.g. Hoeft & Brüggén 2007), we can relate the compression factor,  $R$ , to the upstream Mach number defined as

$$M = \frac{v_u}{c_u}, \quad (17)$$

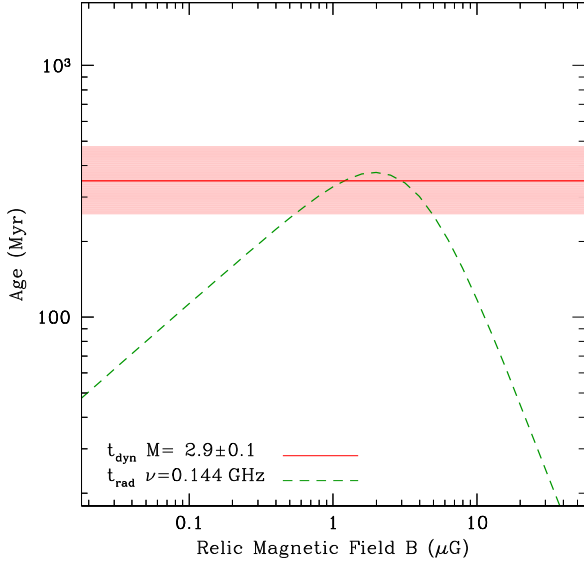
where  $v_u$  and  $c_u$  are, respectively, the upstream gas velocity and sound speed. By assuming a polytropic index  $\gamma_{\text{gas}} = 5/3$ , we have

$$M^2 = \frac{\alpha + 1}{\alpha - 1}, \quad (18)$$

which gives  $M = 2.9 \pm 0.1$ . The relic spectral index is in fact steeper than the canonical value of  $\alpha = 1$  that would be expected for hypersonic shock waves,  $M \gtrsim 10$ .

The Mach number we derived from the radio spectrum is marginally consistent, within the uncertainties, with the values deduced from the analysis of the SZE caused by the pressure discontinuity in proximity of the relic:  $M = 2.9^{+0.8}_{-0.6}$  (Erler et al. 2015) and  $M = 2.2 \pm 0.3$  (Basu et al. 2016). However, as for many other relics in the literature, for the relic in Coma we also found that the radio Mach number is larger than values inferred from X-ray temperature discontinuity based on XMM data  $M = 1.9^{+0.16}_{-0.40}$  (Ogrea & Brüggén 2013), Suzaku data  $M = 2.2 \pm 0.5$  (Akamatsu et al. 2013), and SRG/e-Rosita  $M = 1.9 \pm 0.2$  (Churazov et al. 2023). Note that Churazov et al. (2023) derived a radio Mach number of  $M = 3.5$  from a spectral index  $\alpha = 1.18 \pm 0.02$  (Thierbach, Klein & Wielebinski 2003). Based on the new radio data presented in this work, we find the integrated spectrum is better described by a steeper spectral index  $\alpha = 1.26 \pm 0.02$ , which results in a radio Mach number slightly closer to the SZE and X-rays estimates.

From the mass conservation at the shock front, the downstream gas velocity is  $v_d = v_u/R$ . If the ICM behaves like an ideal polytropic



**Figure 12.** Confinement time ( $t_{\text{dyn}}$ , red colour) and radiative age ( $t_{\text{rad}}$ , green colour and dashed line) of the electrons in the relic as a function of the magnetic field strength. The confinement time is calculated from a relic width of  $D = 220 \pm 30$  kpc by considering a Mach number  $M = 2.9 \pm 0.1$  and an upstream sound speed  $c_u = 640 \pm 88$  km s $^{-1}$ . The profile of the radiative time is calculated for a spectral break  $\nu_b = 144$  MHz.

gas,  $c_u^2 = \gamma_{\text{gas}} k_B T_u / (\mu m_p)$ , and we consider a mean molecular weight  $\mu = 0.6$ , then  $c_u \simeq 516 (T_u / \text{keV})^{1/2}$  km s $^{-1}$ . By considering a temperature of  $T_u = 1.54_{-0.39}^{+0.45}$  keV (Akamatsu et al. 2013), the upstream ICM sound speed is  $c_u = 640 \pm 88$  km s $^{-1}$ . A radio Mach number of  $M = 2.9 \pm 0.1$  implies that the upstream and downstream gas velocities are respectively of  $v_u = 1860 \pm 260$  km s $^{-1}$  and  $v_d = 620 \pm 110$  km s $^{-1}$ .

Following the reasoning of Markevitch et al. (2005), we relate the width of the synchrotron-emitting region,  $D$ , with the velocity of the down-stream flow that carries the relativistic electrons away from the shock. The relic transverse size change with frequency. In line with what is usually observed, the width is significantly larger at low frequencies. In the LOFAR image at 144 MHz we measure a width  $D = 220 \pm 30$  kpc from the  $3\sigma$  isophote. In the SRT 6.6 GHz image, the width is 80 kpc. In the analysis, we decided to adopt the width measured in the LOFAR image at 144 MHz because this is the one less subject to the effect of the radiative losses of the synchrotron electrons. The confinement time of the radio electrons within this thickness from the shock front is estimated as  $t_{\text{dyn}} = D/v_d \simeq 350 \pm 110$  Myr, where  $v_d$  is the downstream velocity.

According to Enßlin et al. (1998), we then compare confinement time of the radio electrons in the relic to the radiative age due to synchrotron and inverse Compton energy losses:

$$t_{\text{rad}} = 1590 \frac{B_{\mu\text{G}}^{0.5}}{(B_{\mu\text{G}}^2 + B_{\text{IC}}^2)[(1+z)\nu_b/\text{GHz}]^{0.5}} \text{ Myr}, \quad (19)$$

where  $\nu_b$  is the break frequency in GHz,  $B$  is the relic magnetic field in  $\mu\text{G}$ , and  $B_{\text{IC}} = 3.25(1+z)^2 \mu\text{G}$  is the inverse-Compton equivalent magnetic field whose energy density is equal to that of the CMB photons. In Fig. 12, we show the confinement time  $t_{\text{dyn}}$  and the synchrotron age,  $t_{\text{rad}}$ , as a function of the magnetic field strength,  $B$ . The radiative age is computed from equation (19) using a break frequency of  $\nu_b = 144$  MHz, meaning that due to the radiative losses the spectral break shifted to the low end of the observed frequency range. This is the condition necessary to observe

an integrated spectrum consistent with the stationary spectral index  $\alpha = \alpha_{\text{inj}} + 0.5$ . We note that  $t_{\text{rad}}$  is generally lower than  $t_{\text{dyn}}$ , except for  $B$  in the range from 0.5 to 5  $\mu\text{G}$ , where the two time-scales are comparable within the uncertainties. The closest match between the two time-scales is obtained around  $B \simeq 2 \mu\text{G}$ . This is the magnetic field strength ( $B = B_{\text{IC}}/\sqrt{3}$ ) that maximizes the radiative age of the synchrotron electrons, i.e.  $t_{\text{rad}} \simeq 380 \pm 70$  Myr. Note that Bonafede et al. (2013) inferred from Faraday rotation data that the magnetic field in the relic region is  $\sim 2 \mu\text{G}$ .

A simple estimate of the energy dissipated in the relic can be obtained by considering the change in the kinetic energy flux across the shock:

$$\Delta F_{\text{KE}} = \frac{1}{2} \rho_u v_u^3 \left(1 - \frac{1}{R^2}\right) \text{ erg s}^{-1} \text{ cm}^{-2}, \quad (20)$$

where  $\rho_u$  is the upstream gas mass density (Finoguenov et al. 2010). Taking for the part of the shock-front directly associated with the radio relic a perpendicular circular area of 0.5 Mpc $^2$ , the rate of kinetic energy dissipation is estimated as

$$\frac{dE_{\text{KE}}}{dt} \simeq 1.3 \times 10^{45} \text{ erg s}^{-1}, \quad (21)$$

where we take  $\rho_u = n_e m_p$ , with  $m_p$  the proton mass and  $n_e = 5.6 \times 10^{-5} \text{ cm}^{-3}$  is the thermal electrons density at the radial distance of the Coma relic from the cluster centre (Churazov et al. 2021).

The total non-thermal luminosity,  $L_{\text{NT}} = L_{\text{radio}} + L_{\text{IC}}$ , of the relativistic electron radiating by synchrotron and inverse-Compton processes in the observed radio band (0.144–10 GHz) is

$$L_{\text{NT}} = 1.5 \times 10^{40} \left[1 + \left(\frac{B_{\text{IC}}}{B_{\mu\text{G}}}\right)^2\right] \text{ erg s}^{-1}. \quad (22)$$

If this luminosity is sustained by the kinetic energy dissipated in the shock, then the efficiency of the electron acceleration is given by the ratio

$$\epsilon \equiv \frac{L_{\text{NT}}}{\frac{dE_{\text{KE}}}{dt}}. \quad (23)$$

By inserting equations (21) and (22), we get for the Coma relic:

$$\epsilon \simeq 1.1 \times 10^{-5} \left[1 + \left(\frac{B_{\text{IC}}}{B_{\mu\text{G}}}\right)^2\right]. \quad (24)$$

Indeed, considering the new value for the radio Mach number of  $M = 2.9 \pm 0.1$ , we find that a relatively small acceleration efficiency ( $\epsilon \lesssim 1$  per cent) is required to match the radio luminosity observed for the Coma relic if  $B > 0.1 \mu\text{G}$ . A similar result to what we find was obtained by Finoguenov et al. (2010) for the A3376 relic. However, the required shock acceleration efficiency increases if the relic's power-law spectrum extends to frequencies much lower than those observed so far. In particular, for others well-studied radio relics Botteon et al. (2020) estimated that significantly higher values of acceleration efficiency are needed to explain the observed radio luminosity if the electrons are accelerated directly from the thermal pool. An alternative scenario often considered in the literature is the one in which the shock wave has accelerated a population of electrons that are already at relativistic energies. In the case of the Coma relic, there is a convincing evidence that plasma injected into the ICM from the head–tail source associated with NGC 4789 could provide the seed relativistic electrons that the low Mach number shock wave would reaccelerate (see the discussion in Bonafede et al. 2022).

## 7 CONCLUSIONS

In this paper, we present deep total intensity and polarization observations of the Coma cluster of galaxies at 1.4 and 6.6 GHz performed with the SRT. Our results are summarized as follows:

(i) By combining the single-dish 1.4 GHz data with archival VLA observations we obtain new images of the central radio halo and of the peripheral radio relic where we properly recover the flux density from the large-scale structures.

(ii) In the halo, we find a localized spot of polarized signal at 6.6 GHz, with fractional polarization of about 45 per cent, and a hint of polarized emission that extends along the north-east side of the diffuse emission.

(iii) The radio relic at 6.6 GHz is highly polarized, up to 55 per cent, and the projected direction of the  $\vec{E}$ -field is perpendicular to the relic ridge line, as usually found for these sources.

(iv) The integrated halo spectrum shows evidence of spectral curvature, with a frequency spectral index of  $\alpha = 1.48 \pm 0.07$  at a reference frequency of 1 GHz. However, because of the spectral curvature, the halo spectral index increases from  $\alpha \simeq 1.1$ , at 0.1 GHz, up to  $\alpha \simeq 1.8$ , at 10 GHz.

(v) We modeled the integrated spectrum of the radio relic using a power law, and we find for the stationary spectral index  $\alpha = 1.26 \pm 0.02$ . From the shock theory, we inferred a radio Mach number  $M = 2.9 \pm 0.1$ , which is higher than the estimates based on the SZE and the X-rays present in the literature. The radiative lifetime of the electrons emitting at low frequency is comparable with the confinement time in the relic if the magnetic field in the emitting region is of the order of  $B \simeq 2 \mu\text{G}$ .

(vi) We calculated that in the case of the Coma relic, the non-thermal luminosity of the relativistic electrons radiating in the radio band can be supported by a few percent of the kinetic energy dissipated in the shock wave if the magnetic field strength is  $B > 0.1 \mu\text{G}$ .

(vii) We compared the Coma radio halo surface brightness profile at 1.4 GHz (central brightness,  $I_0$ , and e-folding radius,  $r_e$ ) with the same properties of the other haloes. We find that the Coma radio halo is peculiar in that while its radius is comparable to the intrinsically larger haloes, its central brightness is one order of magnitude fainter. This means that the Coma radio halo has one of the lowest emissivities at 1.4 GHz observed so far:  $\langle J \rangle \simeq 5.3 \times 10^{-44} \text{ erg s}^{-1} \text{ cm}^{-3} \text{ Hz}^{-1}$ , or equivalently  $\langle J \rangle \simeq 1.6 \times 10^{23} \text{ W Hz}^{-1} \text{ Mpc}^{-3}$ .

(viii) We calculated that a diffuse radio source with the properties of the Coma radio halo would be undetectable, at 1.4 GHz and 60 arcsec resolution, beyond a redshift  $z \lesssim 0.1$  due to the confusion limit and the cosmological dimming of the surface brightness. At 10 arcsec resolution, the redshift limit is  $z \lesssim 0.2$ .

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## DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

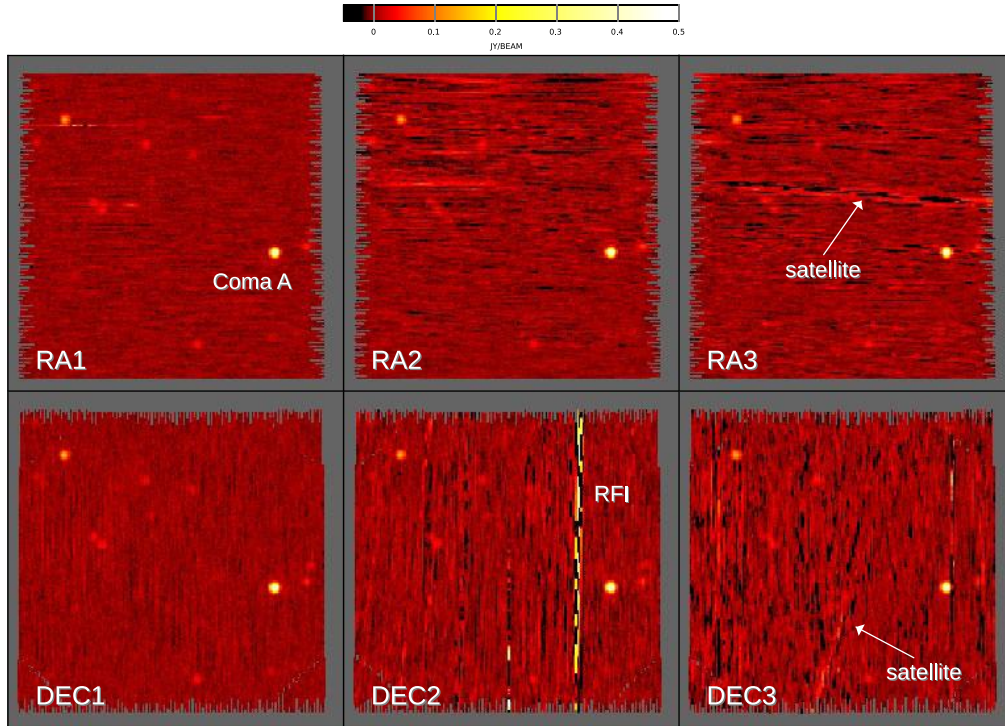
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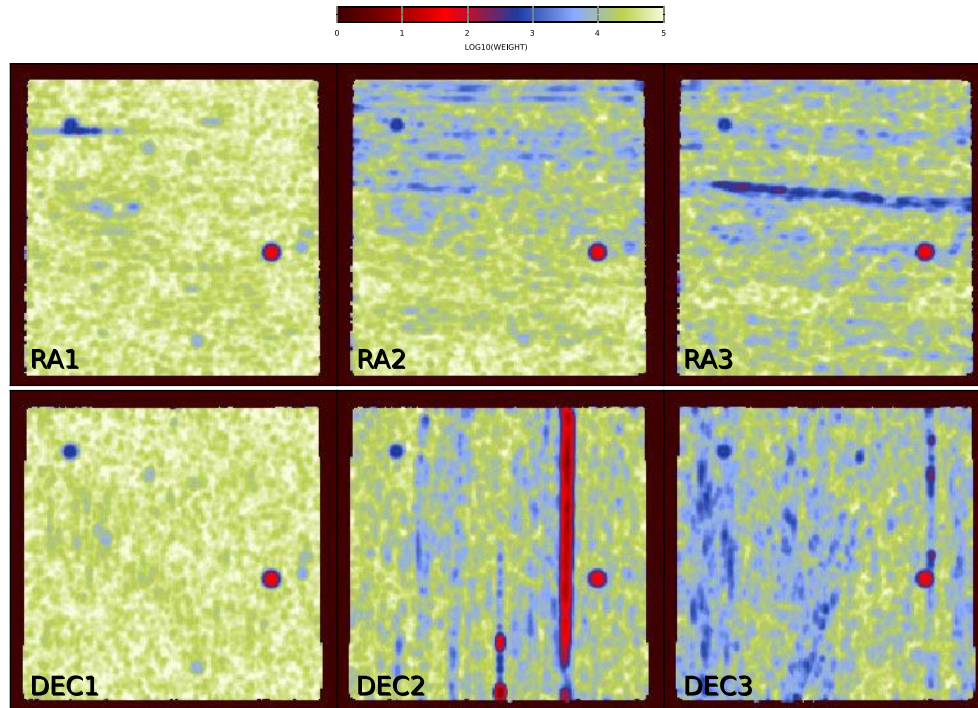
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## APPENDIX A: IMAGING STACKING

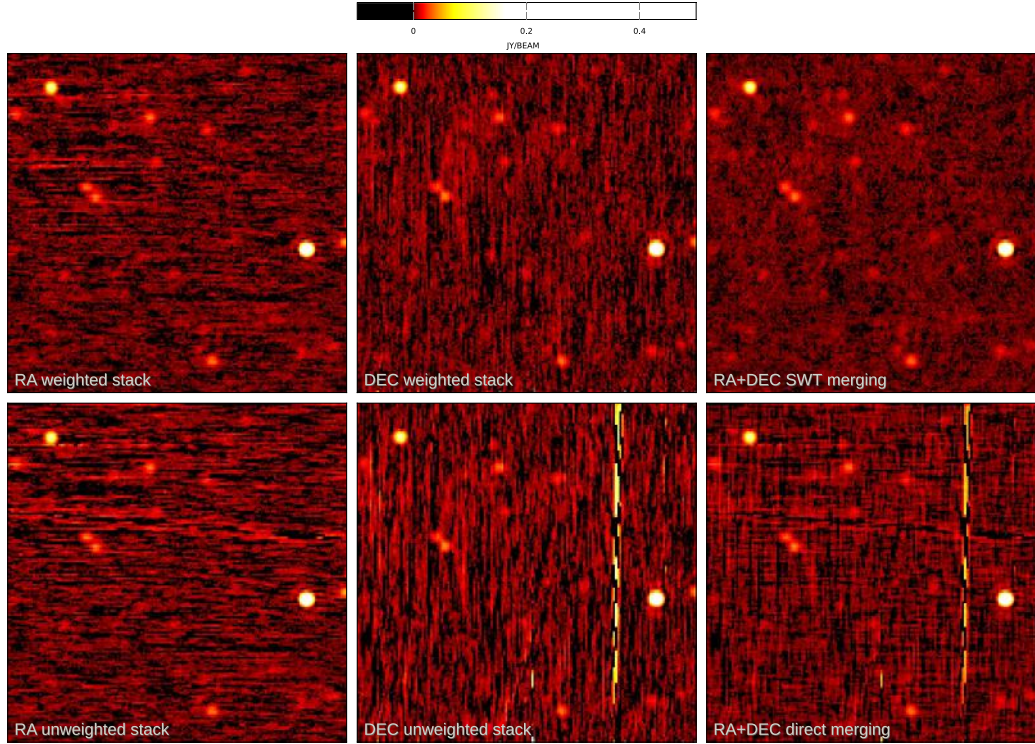
The SCUBE data reduction pipeline implements a weighted stacking imaging. For each polarization and Stokes parameter, spectral cubes are combined to increase the signal-to-noise ratio using a weighted average (Murgia & Fatigoni 2023). First, the channel-0 (spectral average) is smoothed with a Gaussian kernel of 4 pixels in FWHM and then the local intensity variance is calculated for each pixel over a patch of  $3 \times 3$  FWHM in size. The weight at pixel  $(x, y)$  is calculated as  $w_{(x,y)} = 1/\sigma_{(x,y)}^2$ . In Fig. A1, we show the spectral average of polarization R for six spectral cubes acquired on Feb-06-2016. The scans along RA1 and Dec.1 are clearly better in terms of noise rms. Moreover, a strong RFI is present in the Dec. 2 scan and satellites streaks are visible in the RA3 and Dec. 3 scans. In Fig. A2, we show the corresponding weights for these cubes calculated as described above. The isolated RFI and the noisy regions are down-weighted, as desired. Strong real sources, like Coma A, are down-weighted, but this does not represent a problem because the weights are nearly the same for all images and thus the average is consistently computed when dividing for the local sum of weights. The parameters used in the weighting procedure can be adjusted by the user, and also various weighting schemes can be selected. For instance, it is possible to weight both the channel-0 and the single-channels and then consider the minimum weight in order to suppress both broad-band and narrow-band RFI. In any case, the weights are always applied to all frequency channels in the spectral cubes before averaging them. In the top-left and top-middle panels of Fig. A3, we show the weighted stack of the three RA and Dec. scans, respectively. The procedure is very effective in suppressing the RFI signals. The top-right panel shows the merging of the orthogonal RA and Dec. averages, obtained by mixing the SWT detail coefficients (Murgia et al. 2016). This last step filters out the correlated noise along the scan direction, and the final image is noticeably cleaner. For comparison, in the bottom panels we show the unweighted stack of the RA (bottom-left) and Dec. (bottom-middle) scans along with their directed average (bottom-right). The noise of the R-pol image obtained with the weighted SWT merging is  $\sigma_R = 1.06$  mJy beam<sup>-1</sup> (base level 0.03 mJy beam<sup>-1</sup>), while the noise of the direct merging image is  $\sigma_R = 3.74$  mJy beam<sup>-1</sup> (base level 0.46 mJy beam<sup>-1</sup>).



**Figure A1.** Spectral average of polarization  $R$  for the C-band scans acquired on 06 February 2016. Top panels: scans along the RA. Bottom panels: scans along Dec. RFI from satellites appear as oblique streaks while the RFI aligned with the scan direction, like in the Dec. 2 scan, originating most probably from ground sources.



**Figure A2.** Images of the weights used for the stacking of the spectral cubes. The channel-0 image is smoothed with a Gaussian kernel of 4 pixels, and then weights are calculated as the inverse of the local variance of the brightness:  $w_{(x,y)} = 1/\sigma_{(x,y)}^2$ . Note that isolated RFI and noisy regions are down weighted. Strong point sources are also down weighted but, since this occurs equally in all the images, the weighted average is unaffected in these pixels.

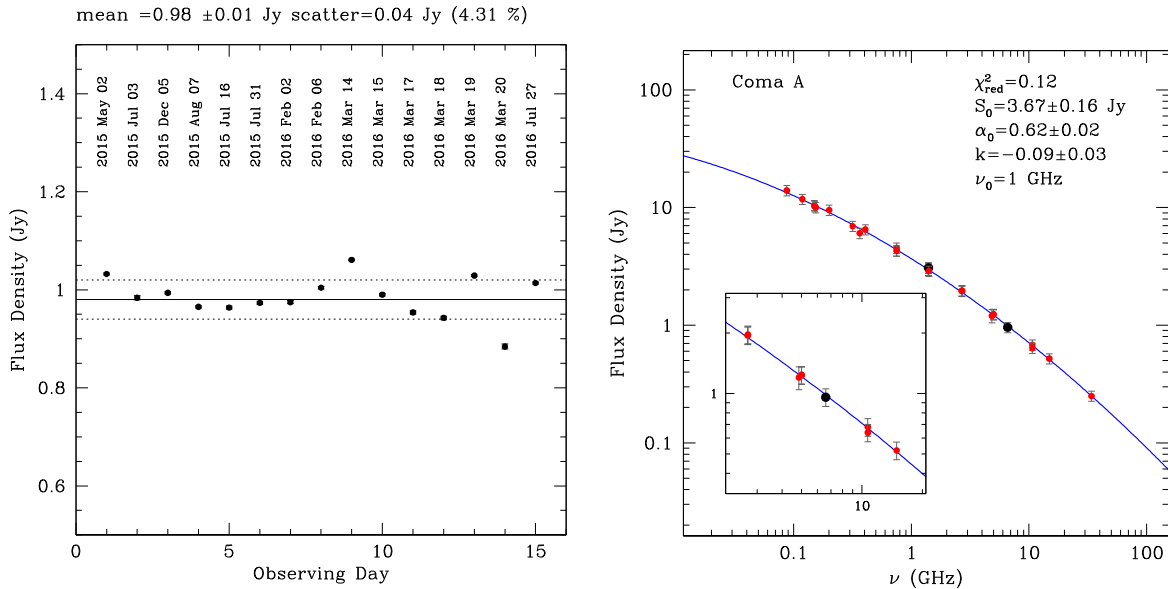


**Figure A3.** Top panels: weighted stacking of the RA (left) and Dec. (middle) for polarization  $R$  scans, shown in Fig. A1. The combination of the RA and Dec. images obtained from the SWT merging is shown in the top-right panel. The unweighted stacking is shown in the bottom panels for comparison. The direct average of the unweighted RA and Dec. scans shown in the bottom-right panel is evidently noisier than the SWT merging.

## APPENDIX B: SRT C-BAND FLUX DENSITY CONSISTENCY CHECK.

We evaluated the consistency of the SRT flux density scale at 6.6 GHz by measuring the flux density of Coma A that we assume to be constant in time during the period of our observations. In the left

panel of Fig. B1, we show the flux density of Coma A at 6.6 GHz measured during the campaign of observations. The mean value is of  $0.98 \pm 0.01$  Jy with a scatter of 0.04 Jy. The larger deviations, such as in the 20MAR16 session, are mostly due to higher RFI levels. The degree of reproducibility of the Coma A flux density can be



**Figure B1.** Left: Coma A Stokes I flux density at 6.6 GHz measured for the different observing days. The scatter around the average (solid line) is of about 4 per cent, and it is represented by the dotted lines. Right: the SRT flux density measurements of Coma A at 1.4 and 6.6 GHz (black dots) are compared with the literature data (red dots). The continuous blue line is the best fit of the modified power-law model. The inset shows a zoom of the spectrum around 6.6 GHz.

**Table B1.** Flux density measurements of Coma A (3C 277.3) taken from the literature using the NED. We obtained flux densities from the GLEAM (Wayth et al. 2015; Hurley-Walker et al. 2017) with AIPS task JMFTT.

Frequency (MHz)	$S_\nu$ (Jy)	Reference
87.5	$13.96 \pm 0.1$	GLEAM 72-103
118.5	$11.78 \pm 0.05$	GLEAM 103-134
150	$10.4464 \pm 1.0449$	TGSS (Intema et al. 2017)
151	$10.24 \pm 0.4$	7C (Waldram et al. 1996)
154.5	$10.013 \pm 0.04$	GLEAM 139-170
200.5	$9.5144 \pm 0.1$	GLEAM 170-231
318	$6.94 \pm 0.31$	Kuehr et al. (1981)
365	$6.047 \pm 0.133$	TEXAS (Douglas et al. 1996)
408	$6.49 \pm 0.55$	Kuehr et al. (1981)
750	$4.3 \pm 0.20$	Kuehr et al. (1981)
750	$4.53 \pm 0.09$	Kuehr et al. (1981)
750	$4.28 \pm 0.08$	Pauliny-Toth, Wade & Heeschen (1966)
1400	$3.08 \pm 0.05$	SRT this work
1400	$3.06 \pm 0.11$	Pauliny-Toth, Wade & Heeschen (1966)
1400	$2.925 \pm 0.0978$	NVSS (Condon et al. 1998)
1400	$2.933 \pm 0.082$	Laing & Peacock (1980)
1410	$2.88 \pm 0.03$	Witzel et al. (1979)
2695	$1.95 \pm 0.04$	Kuehr et al. (1981)
2695	$1.951 \pm 0.04$	Laing & Peacock (1980)
2700	$1.97 \pm 0.1$	Kuehr et al. (1981)
4850	$1.202 \pm 0.158$	87GB (Gregory & Condon 1991)
5000	$1.23 \pm 0.06$	Kuehr et al. (1981)
5000	$1.24 \pm 0.04$	Laing & Peacock (1980)
6600	$0.958 \pm 0.001$	SRT this work
10700	$0.68 \pm 0.03$	Kellermann & Pauliny-Toth (1973)
10700	$0.638 \pm 0.028$	Laing & Peacock (1980)
14900	$0.52 \pm 0.03$	Laing & Peacock (1980)
34000	$0.250 \pm 0.003$	Lancaster et al. (2005)

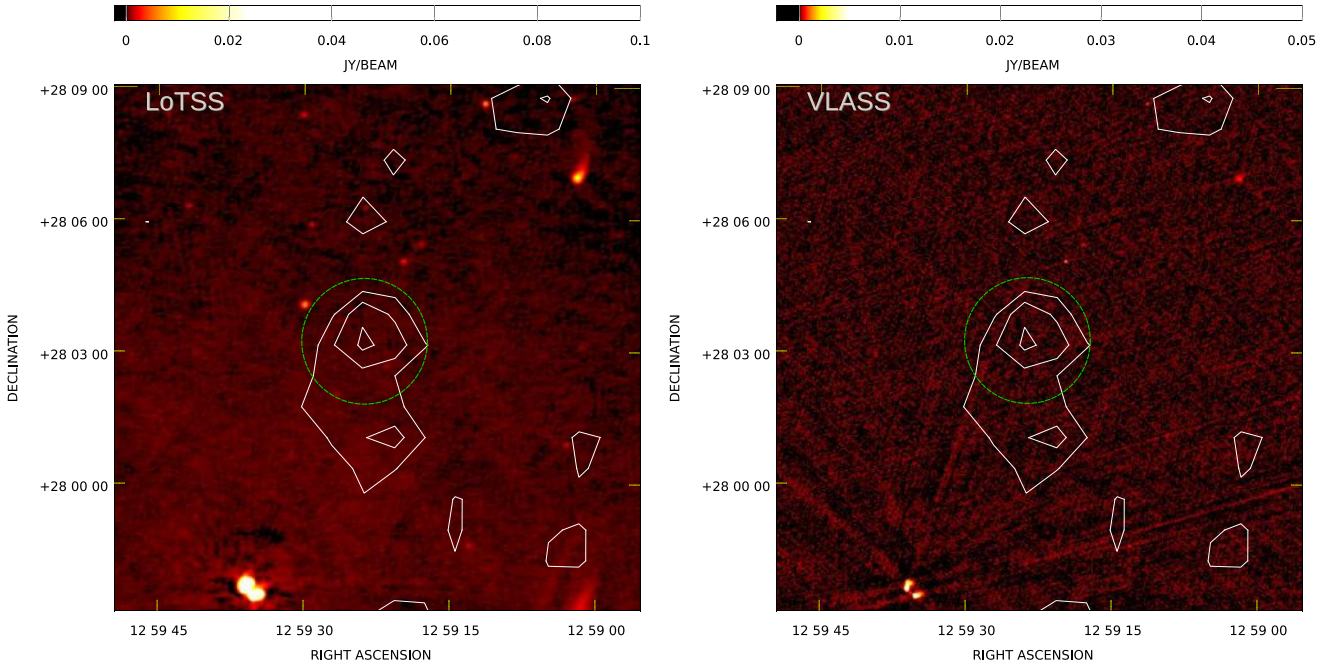
considered as an estimate of the systematic error for a single-day SRT observation of about  $\simeq 4$  per cent. However, by combining all the 15 observing days, the systematic error is expected to decrease by a factor of about  $1/\sqrt{15}$  (assuming a Gaussian scatter).

In the right panel of Fig. B1, we show the consistency of the Coma A flux density at 6.6 GHz compared with the other measurement available in the literature (see Table B1). We modelled the global spectrum of Coma A with a modified power law (see Section 4.3) characterized by three free parameters: the flux density at 1 GHz,  $S_0$ , the spectral index at 1 GHz,  $\alpha$ , and the spectral curvature,  $k$ . Using a reference frequency  $\nu_0 = 1$  GHz, we found for the best-fitting parameters:  $S_0 = 3.67 \pm 0.16$  Jy,  $\alpha_0 = 0.62 \pm 0.02$ , and  $k = -0.09 \pm 0.03$ . The inset shows that the SRT data point is in remarkable agreement with both the measurements at nearby frequencies and the best fit of the modified power-law model represented by the blue line. The difference between the model and the SRT measurement is indeed of about 2.5 per cent. This is somewhat larger than the systematic error of the flux density calibrator, which is about 1 per cent (Perley & Butler 2017). Indeed, we assume a total systematic uncertainty of 3 per cent for the SRT observations at 6.6 GHz.

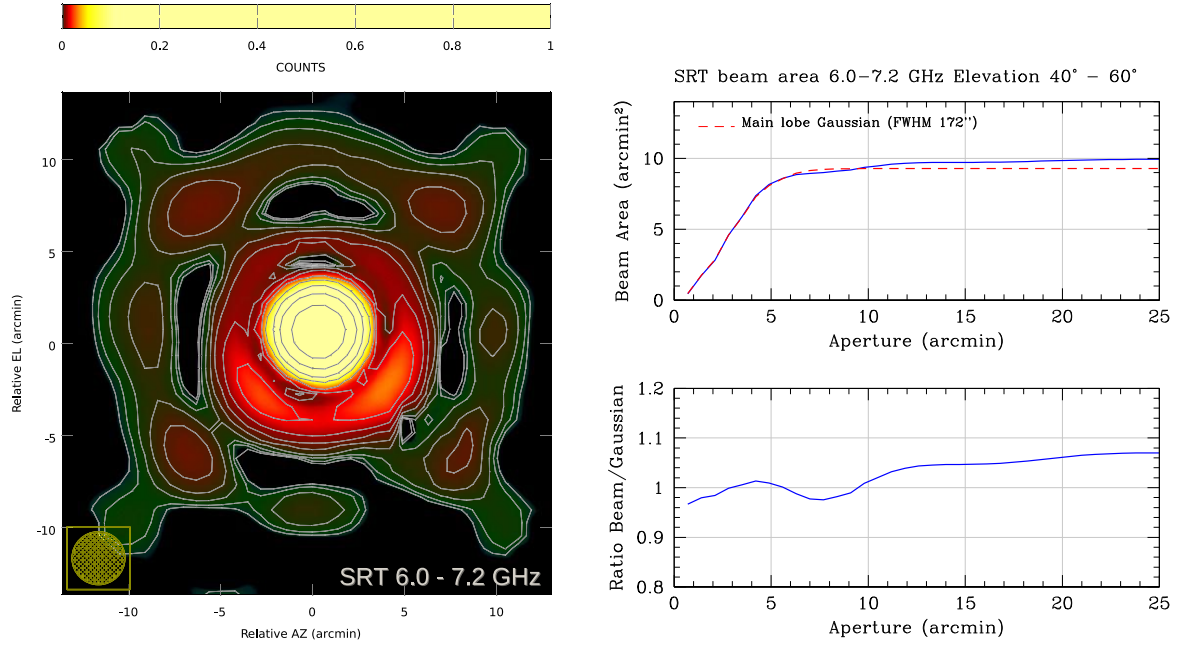
We also checked the SRT data point at 1.4 GHz,  $S_\nu = 3.08 \pm 0.05$  Jy. This data measurement is based on two observing days and at this frequency the difference between the model and the SRT measurement is indeed of about 11 per cent.

### APPENDIX C: HALO POLARIZED SPOT

We tested whether the polarized spot detected in the Coma radio halo could be due to a discrete radio source indistinguishable from the diffuse emission in the 6.6 GHz SRT total intensity image. We inspected both the LoTSS at 144 MHz and the high-frequency



**Figure C1.** Coma radio halo. The SRT polarization contours at 6.6 GHz are overimposed to the LoTSS image at 144 MHz (left) and to the VLASS image at 2–4 GHz (right). The green dash circle represents the FWHM beam of the SRT observation at 6.6 GHz.



**Figure D1.** Left: SRT C-band beam in the band from 6.0 to 7.2 GHz. Contours range from 0 to  $-40$  dB and are spaced by  $-3$  dB. Right: Top panel shows the beam area as a function of the diameter of a circular aperture centred in the beam (continuous line). The dashed line is the area of a Gaussian fit to the main lobe of the beam. The bottom panel shows the ratio of the beam area to the Gaussian model as a function of the aperture diameter.

VLASS images at 2–4 GHz. The spot has a peak polarized intensity of  $1.6 \text{ mJy beam}^{-1}$  at 6.6 GHz. If the source is a 100 per cent polarized with an inverted spectral index  $\alpha_{\text{thick}} = -2.5$  (the canonical value for a synchrotron self-absorption) then it would not be detectable in the total intensity at 144 MHz, given the noise level of the LoTSS which is equal to  $1\sigma$  of  $80 \text{ } \mu\text{Jy beam}^{-1}$ . On the other hand, the source would still be detectable in total intensity in the VLASS at a significance of  $3\sigma$ , since the  $1\sigma$  noise level in the VLASS mosaic is  $70 \text{ } \mu\text{Jy beam}^{-1}$ . However, there are no sources on the location of the polarized signal in either survey (see Fig. C1). Also, the polarization level of this supposed source most likely should be less than 100 per cent, resulting in a higher total intensity signal. We therefore exclude the possibility the polarized spot is caused by a contamination from a source with an inverted spectrum unresolved in total intensity by the SRT beam at 6.6 GHz.

#### APPENDIX D: SRT BEAM AREA

The beam area is a relevant parameter for an accurate photometry of extended radio sources. In Fig. D1, we show the SRT beam in the 6.0–7.2 GHz band, determined in the elevation range from  $40^\circ$  to  $60^\circ$  by observing strong point-like quasars. In the image are visible the main lobe, the second lobe ( $-20$  dB), and the third lobe ( $-30$  dB). The diagonal stripes are caused by the struts of the support structure of the secondary mirror of the telescope. A two-dimensional Gaussian fit to the beam main lobe results in an FWHM of 172 arcsec. In the top-right panel of Fig. D1, we present the profile of the beam area integrated over circular apertures of increasing diameter for both the observed beam (continuous line) and the Gaussian model (dotted line). The Gaussian model beam area tends asymptotically to  $\Omega_{\text{beam}} = 2\pi/(8\ln 2) \cdot \text{FWHM}^2 \simeq 1.133 \cdot \text{FWHM}^2$ , or  $9.28 \text{ arcmin}^2$ . However, due to the contribution of the side-lobes the effective beam

area is larger than the Gaussian beam area by about 7 per cent for apertures larger than 20 arcmin, see bottom-right panel of Fig. D1. The full beam area we consider for the aperture photometry is indeed  $\Omega_{\text{beam}} = 9.93 \text{ arcmin}^2$ .

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