

Does the evolution of the radio luminosity function of star-forming galaxies match that of the star formation rate function?

Matteo Bonato,^{1,2★} Mattia Negrello,³ Claudia Mancuso,¹ Gianfranco De Zotti,^{1,2} Paolo Ciliegi,⁴ Zhen-Yi Cai,⁵ Andrea Lapi,¹ Marcella Massardi,⁶ Anna Bonaldi,⁷ Anna Sajina,⁸ Vernesa Smolčić⁹ and Eva Schinnerer¹⁰

¹SISSA, Via Bonomea 265, I-34136 Trieste, Italy

²INAF – Osservatorio Astronomico di Padova, Vicolo dell'Osservatorio 5, I-35122 Padova, Italy

³School of Physics and Astronomy, Cardiff University, The Parade, Cardiff CF24 3AA, UK

⁴INAF – Osservatorio Astronomico di Bologna, Via Ranzani 1, I-40127 Bologna, Italy

⁵CAS Key Laboratory for Research in Galaxies and Cosmology, Department of Astronomy, University of Science and Technology of China, Hefei, Anhui 230026, China

⁶INAF, Osservatorio di Radioastronomia, Via Gobetti 101, I-40129 Bologna, Italy

⁷Jodrell Bank Centre for Astrophysics, School of Physics and Astronomy, The University of Manchester, Oxford Road, Manchester M13 9PL, UK

⁸Department of Physics & Astronomy, Tufts University, 574 Boston Avenue, Medford, MA 02155, USA

⁹Department of Physics, University of Zagreb, Bijenička cesta 32, HR-10000 Zagreb, Croatia

¹⁰Max Planck Institute for Astronomy, Königstuhl 17, Heidelberg D-69117, Germany

Accepted 2017 April 21. Received 2017 April 18; in original form 2016 March 4

ABSTRACT

The assessment of the relationship between radio continuum luminosity and star formation rate (SFR) is of crucial importance to make reliable predictions for the forthcoming ultra-deep radio surveys and to allow a full exploitation of their results to measure the cosmic star formation history. We have addressed this issue by matching recent accurate determinations of the SFR function up to high redshifts with literature estimates of the 1.4 GHz luminosity functions of star-forming galaxies (SFGs). This was done considering two options, proposed in the literature, for the relationship between the synchrotron emission (L_{synch}), that dominates at 1.4 GHz, and the SFR: a linear relation with a decline of the $L_{\text{synch}}/\text{SFR}$ ratio at low luminosities or a mildly non-linear relation at all luminosities. In both cases, we get good agreement with the observed radio luminosity functions but, in the non-linear case, the deviation from linearity must be small. The luminosity function data are consistent with a moderate increase of the $L_{\text{synch}}/\text{SFR}$ ratio with increasing redshift, indicated by other data sets, although a constant ratio cannot be ruled out. A stronger indication of such increase is provided by recent deep 1.4-GHz counts, down to μJy levels. This is in contradiction with models predicting a *decrease* of that ratio due to inverse Compton cooling of relativistic electrons at high redshifts. Synchrotron losses appear to dominate up to $z \simeq 5$. We have also updated the Massardi et al. evolutionary model for radio loud AGNs.

Key words: galaxies: active – galaxies: evolution – radio continuum: galaxies.

1 INTRODUCTION

In the last several years, deep radio surveys reaching sub-mJy detection limits have been emerging as a powerful tool to investigate the evolution with cosmic time (or redshift) of star-forming galaxies (SFGs), of active galactic nuclei (AGNs) and of their mutual interactions. This is because the radio emission is not affected by

dust obscuration and has straightforward K -corrections, thanks to the simple power-law shape of the spectra. On the other hand, the featureless radio spectra do not provide redshift information. This limitation has been overcome by surveys down to tens of μJy over fields with panchromatic coverage, such as the Cosmic Evolution Survey (COSMOS; Scoville et al. 2007) field and the Extended-Chandra Deep Field-South (E-CDFS; Miller et al. 2013).

The multifrequency data available for these fields include spectroscopic redshifts for a substantial fraction of sources and have allowed accurate photometric redshift estimates for most of the

* E-mail: matteo.bonato@oapd.inaf.it

others, as well as an effective separation of sources whose radio emission is due to star formation from those whose radio emission is powered by an active nucleus (Smolčić et al. 2008; Ilbert et al. 2009; Sargent et al. 2010a; Bonzini et al. 2012, 2013). With this information in hand, radio luminosity functions (RLFs) of both radio source populations have been derived up to high redshifts (Smolčić et al. 2009a,b; Padovani et al. 2011, 2015; Novak et al. 2017).

Another investigation of the evolution of SFGs and of radio loud (RL) AGNs out to $z \sim 2.5$ was carried out by McAlpine, Jarvis & Bonfield (2013) combining a 1 deg² Very Large Array (VLA) radio survey, complete to a depth of 100 μ Jy, with accurate 10 band photometric redshifts from the Visible and Infrared Survey Telescope for Astronomy Deep Extragalactic Observations and the Canada–France–Hawaii Telescope Legacy Survey. Less deep radio surveys are dominated by RL AGNs and were exploited to derive the RLFs of this population at several redshifts (Donoso, Best & Kauffmann 2009; Best et al. 2014). Accurate estimates of the local RLFs of both SFGs and RL AGNs have been presented by Mauch & Sadler (2007).

Identifications of sub-mJy radio sources have also revealed the presence of a third population, the ‘radio-quiet’ (RQ) AGNs (e.g. Padovani et al. 2009; Bonzini et al. 2013). Evidence of nuclear activity in these sources comes from one or more bands of the electromagnetic spectrum (e.g. optical, mid-infrared, X-ray) but the origin of their radio emission is still being hotly debated. High resolution radio observations have provided evidence that some RQ AGNs have components with very high surface brightness, variability, or apparent super-luminal motion, all of which are characteristic of emission driven by a super massive black hole (e.g. Herrera Ruiz et al. 2016; Maini et al. 2016).

However, this does not necessarily prove that the general RQ AGN population possesses radio cores that contribute substantially to the total radio emission. Based on their study of the E-CDFS VLA sample, Padovani et al. (2015) concluded that RQ and RL QSOs are two totally distinct AGN populations, characterized by very different evolutions, luminosity functions and Eddington ratios. The radio power of RQ AGNs evolves similarly to SFGs, consistent with their radio emission being powered by star formation. This conclusion was confirmed by the study of Bonzini et al. (2015), who used deep *Herschel* photometry to determine the FIR emission, hence the SFR, of E-CDFS galaxies. Further support to this view was provided by Kellermann et al. (2016) who, based on 6 GHz Jansky Very Large Array (JVLA) observations of a volume-limited sample of 178 low redshift optically selected QSOs, argued that the bulk of the radio emission of RQ QSOs is powered by star formation in their host galaxies (see also Kimball et al. 2011; Condon et al. 2013). In the following, we will adopt this view and will not consider RQ AGNs as an additional radio source population.

This paper deals with the interpretation of these observational results and especially with their exploitation to assess the relationship between the 1.4 GHz luminosity and the star formation rate (SFR) up to $z \simeq 5$. This relation is of crucial importance to make reliable predictions for the forthcoming ultra-deep surveys and to allow a full exploitation of their results to measure the cosmic star formation history. We have investigated it by comparing the observed RLFs at several redshifts with those expected from the accurate determinations of the SFR functions of galaxies, converted to RLFs using literature relationships between SFR and radio (synchrotron and free–free) luminosity (Section 2). To have a comprehensive view of the outcome of radio surveys, we need to take into account also RL AGNs. This is done using an updated version of the Massardi et al. (2010) model. In Section 3, we discuss our results. The main

conclusions are summarized in Section 4. Throughout this paper, we use a standard flat Λ CDM cosmology with $\Omega_m = 0.32$, $\Omega_\Lambda = 0.68$, $h = 0.67$.

2 MODELING THE EVOLUTION OF THE LUMINOSITY FUNCTION OF STAR-FORMING GALAXIES

The radio continuum emission of SFGs is a well-established SFR diagnostic, unaffected by dust obscuration (Kennicutt & Evans 2012). It thus offers the opportunity to get a comprehensive view of the cosmic star formation history. In contrast, optical/UV surveys miss the heavily dust enshrouded star formation while the far-infrared (FIR) to millimeter-wave observations only measure the dust-reprocessed starlight. This is, in fact, one of the key science drivers of the Square Kilometre Array (SKA) and of its pathfinder telescopes, such as ASKAP and MeerKAT. To achieve this goal, however, it is necessary to set on a firm basis the connection between radio emission and SFR, and to assess whether it depends on redshift.

The radio continuum emission of SFGs consists of a nearly flat-spectrum free–free emission plus a steeper-spectrum synchrotron component. The free–free emission is proportional to the production rate of ionizing photons, with a weak dependence on the electron temperature; thus, it directly traces the formation rate of massive stars. The synchrotron emission, due to the interaction of relativistic electrons, mostly produced by supernovae, with the galactic magnetic field, dominates at low radio frequencies.

A calibration of the relation between SFR and free–free emission was derived by Murphy et al. (2011, 2012), based on observations of a sample of local galaxies, mostly with SFR $< 1 M_\odot \text{ yr}^{-1}$. Following Mancuso et al. (2015), we have rewritten it as

$$L_{\text{ff}}(\nu) = 3.75 \times 10^{26} \left(\frac{\text{SFR}}{M_\odot \text{ yr}^{-1}} \right) \left(\frac{T}{10^4 \text{ K}} \right)^{0.3} \times \exp\left(-\frac{h\nu}{kT}\right), \quad (1)$$

where T is the temperature of the emitting plasma, and $g(\nu, T)$ is the Gaunt factor for which we adopt the approximation given by Draine (2011)

$$g(\nu, T) = \ln \left\{ \exp \left[5.960 - \frac{\sqrt{3}}{\pi} \ln \left(Z_i \frac{\nu}{\text{GHz}} \left(\frac{T}{10^4 \text{ K}} \right)^{-1.5} \right) \right] + \exp(1) \right\}, \quad (2)$$

Z_i being the charge of ions. This equation reproduces the Murphy et al. (2012) calibration at the calibration frequency (33 GHz) for a pure hydrogen plasma ($Z_i = 1$) and $T = 10^4 \text{ K}$; we adopt these values in the following. The differences at other radio frequencies, due to the less accurate approximation for the Gaunt factor used by Murphy et al. (2012), are always $\lesssim 3$ per cent.

The calibration of the SFR–synchrotron luminosity relation is a bit more controversial because it involves complex and poorly understood processes such as the production rate of relativistic electrons, the fraction of them that can escape from the galaxy and the magnetic field strength. A calibration of the L_{sync} –SFR relation was obtained by Murphy et al. (2011, 2012) using *STARBURST99* (Leitherer et al. 1999) and observations of the low SFR nearby galaxy samples mentioned above. Following Mancuso et al. (2015), we have slightly modified their relation including a steepening of the synchrotron spectrum by $\Delta\alpha = 0.5$ above a break frequency of 20 GHz, to take into account electron ageing effects (Banday & Wolfendale 1991). The SFR–synchrotron luminosity relation then

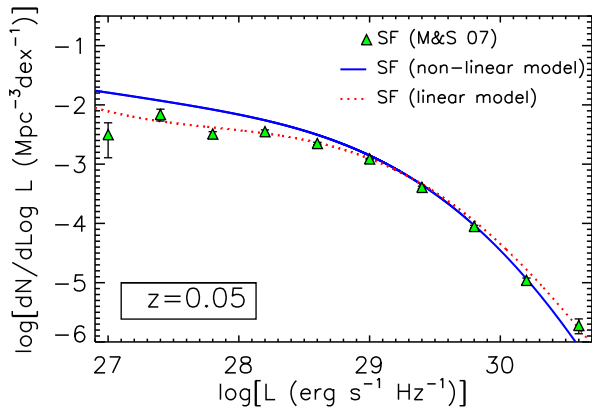


Figure 1. Comparison between the observational determination of the local RLF of SFGs at 1.4 GHz (data points; Mauch & Sadler 2007) and the one obtained from the local SFR function using either equation (4) with a dispersion of 0.4 dex (dotted red curve) or equation (5) with a dispersion of 0.3 dex (solid blue line).

writes

$$L_{\text{sync}} \simeq 1.9 \times 10^{28} \left(\frac{\text{SFR}}{\text{M}_{\odot} \text{yr}^{-1}} \right) \left(\frac{\nu}{\text{GHz}} \right)^{-0.85} \times \left[1 + \left(\frac{\nu}{20 \text{ GHz}} \right)^{0.5} \right]^{-1} \text{ erg s}^{-1} \text{ Hz}^{-1}. \quad (3)$$

The calibration by Murphy et al. (2011, 2012) was adopted in the extensively cited review by Kennicutt & Evans (2012). However, Mancuso et al. (2015) showed that this relation, combined with observational determinations of the local SFR function, leads to an over-prediction of the faint end of the local RLF of SFGs worked out by Mauch & Sadler (2007). A similar conclusion was previously reached by Massardi et al. (2010).

This is in keeping with the argument made by Bell (2003). He pointed out that the FIR emission traces most of the SFR in luminous galaxies but only a minor fraction of it in faint galaxies. Nevertheless, the FIR to radio luminosity ratio is similar for the two galaxy groups, implying that the radio emission from low-luminosity galaxies is substantially suppressed, compared to brighter galaxies.

To recover consistency with the Mauch & Sadler (2007) LF, Mancuso et al. (2015) assumed a deviation from a linear L_{sync} –SFR relation at low radio luminosities close to that proposed by Massardi et al. (2010):

$$L_{\text{sync}}(\nu) = \frac{L_{*,\text{sync}}(\nu)}{\left(L_{*,\text{sync}}/\bar{L}_{\text{sync}} \right)^{\beta} + \left(L_{*,\text{sync}}/\bar{L}_{\text{sync}} \right)}, \quad (4)$$

where $L_{*,\text{sync}} = 0.886 \bar{L}_{\text{sync}} (\text{SFR} = 1 \text{ M}_{\odot} \text{yr}^{-1})$ with \bar{L}_{sync} given by equation (3), and $\beta = 3$; at 1.4 GHz, $L_{*,\text{sync}} \simeq 10^{28} \text{ erg s}^{-1} \text{ Hz}^{-1}$. A different empirical relation was proposed by Bell (2003).

The comparison with the Mauch & Sadler (2007) LF also showed that the bright end of the 1.4 GHz LF is under-predicted unless we allow for a substantial dispersion around the mean L_{sync} –SFR relation. Mancuso et al. (2015) obtained good agreement adopting a dispersion of the synchrotron luminosity at given SFR $\sigma_{\log L} = 0.4$ (see Fig. 1). This dispersion is large compared to the much quoted value of 0.26 reported by Yun, Reddy & Condon (2001), who however pointed out that the dispersion is larger at the high luminosities where it matters most in the present context. Murphy et al. (2012, their table 5) found a scatter of 0.29 dex around the average ratio of the total IR luminosity (usually assumed to be a good SFR estimator) to the SFR inferred from 33 GHz measurements. Since the

latter are dominated by thermal emission, that Murphy et al. (2012) argue to be a robust SFR indicator, it is not implausible that the dispersion around the mean L_{sync} –SFR relation is somewhat larger. A larger dispersion (0.6 dex) of synchrotron luminosity, measured at 610 MHz, and the SFR was reported by Garn et al. (2009) whose sample, however, included galaxies up to $z = 2$; the dispersion may thus have been increased by evolution of the L_{sync} –SFR relation. A dispersion of ~ 0.4 dex is also indicated by figs 6 and 9 of Delhaize et al. (2017).

Thus, although observational indications and theoretical arguments (e.g. Lacki, Thompson & Quataert 2010) converge in suggesting deviations from a linear relation, its shape is uncertain. It is even unclear whether the L_{sync} –SFR relationship becomes non-linear only at low radio luminosities. Price & Duric (1992) and Niklas (1997), from analyses of samples of galaxies for which they were able to separate the free–free and the synchrotron components using the radio continuum spectra, concluded that their data are consistent with a mildly non-linear relation, holding at all radio luminosities: $L_{\text{sync}} \propto \text{SFR}^{1.2}$.

We find that a relation of this kind yields a local RLF of SFGs in reasonably good agreement with the Mauch & Sadler’s one, although slightly steeper both above and below the knee luminosity. An excellent fit at high luminosities is obtained with a milder deviation from linearity ($L_{\text{sync}} \propto \text{SFR}^{1.1}$); at low luminosities, however, the model is still above the data points. This is illustrated by Fig. 1, where the solid blue line, labeled ‘non-linear model’, is obtained with a mean L_{sync} /SFR relationship given by:

$$\bar{L}_{\text{sync}} \simeq 1.51 \times 10^{28} \left(\frac{\nu}{\text{GHz}} \right)^{-0.85} \left(\frac{\text{SFR}}{\text{M}_{\odot} \text{yr}^{-1}} \right)^{1.1} \text{ erg s}^{-1} \text{ Hz}^{-1}, \quad (5)$$

and adopting a dispersion of L_{sync} at given SFR of $\sigma_{\log L} = 0.3$. The normalization is consistent, within the uncertainties, with the Price & Duric (1992) and Niklas (1997) results. The dotted red line shows, for comparison, the fit with the ‘linear model’, with deviations from linearity only at faint luminosities (equation 4). The lower dispersion around the mean L_{sync} –SFR relation obtained for the ‘non-linear’ compared to the ‘linear’ model suggests that the former might be preferred; on the other hand, its fit of the Mauch & Sadler’s local luminosity function is somewhat worse.

Fig. 2 compares the radio emission spectra of SFGs yielded by equation (4) and by equation (5) for two values of the SFR, 100 and $1 \text{ M}_{\odot} \text{yr}^{-1}$. For both values of the SFR, equation (5) gives higher radio luminosities. Equation (4) substantially lowers the synchrotron contribution for low SFRs to the point that the free–free emission of these sources may become dominant, even at 1.4 GHz (in the observer’s frame), especially for high- z sources. Hence, determinations of the radio emission spectrum of SFGs with moderate to low SFRs ($\text{SFR} \lesssim 1 \text{ M}_{\odot} \text{yr}^{-1}$) over a sufficiently broad frequency range would allow one to discriminate between the ‘linear’ and the ‘non-linear’ model.

All these studies however are limited to local galaxies with moderate luminosities/SFRs. Do their conclusions extend to high redshifts when SFRs reach much larger values? The applicability at high redshift of the local L_{sync} –SFR relation was not firmly demonstrated yet. From a theoretical point of view, it may be expected that the mean L_{sync} /SFR ratio decreases at high redshifts when the cooling of relativistic electrons via inverse Compton scattering off the cosmic microwave background, whose energy density increases as $(1+z)^4$, dominates over synchrotron cooling (e.g. Murphy 2009; Lacki & Thompson 2010; Schleicher & Beck 2013;

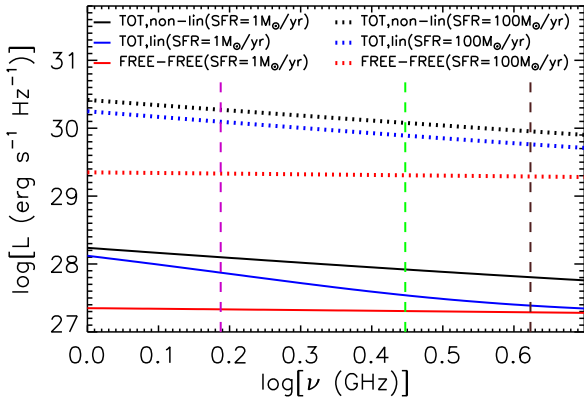


Figure 2. Radio emission spectrum of SFGs for two values of the SFR (100 and $1 M_{\odot} \text{ yr}^{-1}$, dotted and solid lines, respectively). For each value of the SFR, the lowest dotted and solid red lines show the free–free contributions, while the two upper lines show the total, including the synchrotron contribution, computed using either equation (5), uppermost black line of each type, or equation (4), middle blue lines. The vertical dashed lines show the rest-frame frequencies corresponding to the observed frequency of 1.4 GHz for $z = 0.1, 1, 2$ (from left- to right-hand side).

Schober, Schleicher & Klessen 2016). On the other hand, under some circumstances, the ratio might rather increase with redshift (Lacki & Thompson 2010; Schleicher & Beck 2013).

Observational studies concerned the relation between radio luminosity and FIR luminosity, generally believed to be a reliable measure of the SFR. In the relevant redshift range, the considered, relatively high, radio luminosities are dominated by synchrotron emission (cf. Fig. 2), so that the conclusions concern, more specifically, the relation between synchrotron luminosity and SFR. The results have been controversial. Some studies found that the FIR–radio relation is unchanged or suffers only minor variations at high redshift (e.g. Ibar et al. 2008; Sargent et al. 2010b; Bourne et al. 2011; Mao et al. 2011; Pannella et al. 2015), while others have found significant, albeit weak, evolution (e.g. Seymour et al. 2009; Ivison et al. 2010a,b; Magnelli et al. 2015; Basu et al. 2015). Magnelli et al. (2015) based on FIR and radio observations of the most extensively studied extragalactic fields (GOODS-N, GOODS-S, ECDFS and COSMOS) reported evidence of a weak redshift evolution of the parameter

$$q_{\text{FIR}} = \log \left(\frac{L_{\text{FIR}}[\text{W}]}{3.75 \times 10^{12}} \right) - \log (L_{1.4\text{GHz}}[\text{W Hz}^{-1}]), \quad (6)$$

where L_{FIR} is the FIR luminosity integrated from rest-frame 42 to 122 μm and $L_{1.4\text{GHz}}$ is the rest-frame 1.4 GHz luminosity. They found

$$q_{\text{FIR}} = (2.35 \pm 0.08) \times (1+z)^{\alpha_{\text{M}}}, \quad (7)$$

with $\alpha_{\text{M}} = -0.12 \pm 0.04$.

A new investigation of the evolution of the infrared–radio correlation has been recently carried out by Delhaize et al. (2017). Using highly sensitive 3 GHz VLA observations and *Herschel/Spitzer* infrared data in the 2 deg² COSMOS field, they were able to push the study of the correlation up to $z \simeq 5$. Their results confirm a weak but statistically significant trend of q_{FIR} with redshift. The fitted redshift dependence of q_{FIR} has a slightly higher normalization and steeper slope than that found by Magnelli et al. (2015): $q_{\text{FIR}} = (2.88 \pm 0.03) \times (1+z)^{-0.19 \pm 0.01}$.

These results are in striking contradiction with the inverse Compton scenario envisioned by several models, as mentioned above.

A full investigation of this issue is beyond the scope of this paper. Various possibilities have been discussed by Magnelli et al. (2015) and Delhaize et al. (2017), including possible biases introduced by simplifying approximations used in their analyses. The choice of radio spectral index used for the K -correction was found to affect the normalization and the redshift dependence of q_{FIR} : A steeper spectral index lowers the normalization and steepens the dependence on $(1+z)$. However, only marginal differences were found varying the spectral indices in the observed range. A flattening of the effective spectral index is produced by the increasing contribution of free–free emission towards higher radio frequencies; this translates in a flatter trend with $(1+z)$. However, a substantial flattening of the average effective radio spectral index with increasing redshift is inconsistent with their data.

The rapid increase with redshift of the AGN population hosted by SFGs might suggest that the evolution of $L_{\text{synch}}/\text{SFR}$ ratio is due to an increasing contribution of RQ AGNs to the radio luminosity. To weed out the AGN contamination, Magnelli et al. (2015) removed from their sample X-ray AGNs and AGNs selected by the *Spitzer* Infrared Array Camera (IRAC) colour–colour criteria of Lacy et al. (2007). Excluding AGNs did not change their results; they concluded that the evolution is most likely not driven by AGN contamination. The analysis by Delhaize et al. (2017) led to a more open conclusion: it is possible that AGN contributions only to the radio regime could be influencing the trend found for their sample.

A physically based prediction of the negative evolution of q_{FIR} was put forward by Lacki & Thompson (2010). They argued that high- z starburst galaxies have much higher cosmic-ray vertical scaleheights than local starbursts ($h \sim 1$ kpc instead of $h \sim 0.1$ kpc). Then energy losses of cosmic rays (free–free, ionization, pion production), competing with synchrotron cooling, are weaker because they depend on the volume density. If, moreover, the magnetic field strength, B , increases with the SFR surface density, Σ_{SFR} , cosmic rays lose most of their energy via synchrotron emission before escaping from the galaxy and suffering inverse Compton cooling. Taking also into account that the other competing cooling processes are weaker it is then expected that q_{FIR} decreases at high redshifts. According to Magnelli et al. (2015), this scenario might account for the observed trend, although some difficulties remain.

We investigate the possible evolution of q_{FIR} (or, equivalently, of the $L_{\text{synch}}/\text{SFR}$ ratio) combining the accurate determinations of the redshift-dependent SFR functions that are presently available with the information on the RLFs of SFGs provided by the deep surveys mentioned in Section 1. Detailed studies of the evolution of the SFR function across the cosmic history were carried out by Cai et al. (2013) focusing on FIR data and by Cai et al. (2014) focusing on UV and Ly α data, properly corrected for dust attenuation. The latter study, however, was limited to $z \gtrsim 2$. These authors built a model that fits a broad variety of data¹: multifrequency and multi-epoch luminosity functions of galaxies and AGNs, redshift distributions, number counts (total and per redshift bins). It also accurately predicted the counts and the redshift distribution of strongly lensed galaxies detected by the South Pole Telescope (Mocanu et al. 2013; Weiß et al. 2013) as shown by Bonato et al. (2014).

The model was extended by Mancuso et al. (2015) and further successfully tested against observational determinations of the H α luminosity function at several redshifts. The combination of dust extinction corrected UV/Ly α /H α data with FIR data yielded

¹ See http://people.sissa.it/~zcaigalaxy_agn/ or http://staff.ustc.edu.cn/~zcaigalaxy_agn/index.html.

accurate determinations of the SFR function up to $z \simeq 6-7$, some estimates being available up to $z \sim 10$ (see also Aversa et al. 2015).

3 COMPARISON BETWEEN MODEL AND DATA

Fig. 3 compares the model luminosity functions of SFGs obtained from the SFR functions using equation (1) plus equation (4) with the observational determinations at several redshifts available in the literature. Note that, the model parameters were fixed to fit the Mauch & Sadler (2007) local luminosity function. No free parameters were introduced to fit the luminosity functions at higher redshifts.

The figure compares the luminosity functions obtained without evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio (solid blue lines) with those given by the same model but allowing for the best-fitting evolution from Magnelli et al. (2015, solid dark-brown lines). With these data alone, it is hard to discriminate among the two possibilities, although the Magnelli et al. prediction provides a somewhat better description of the highest luminosity bins, especially at high redshift.

The main discrepancies between model (with and without evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio) and observational estimates, particularly with those by Smolčić et al. (2009a) at $z = 0.8$ and 1.1 and by McAlpine et al. (2013) at $z = 2.2$, occur at the highest radio luminosities ($\log(L_{1.4\text{GHz}}/\text{erg s}^{-1}\text{Hz}^{-1}) \gtrsim 31.5$), where the observational determinations tend to exceed expectations from the model. To check whether this may be due, at least in part, to our model for the SFR function falling short at high luminosity, we have replaced it with the analytic formulae given by Mancuso et al. (2016). These formulae provide an accurate empirical fit of the observed SFR functions. The discrepancy was not significantly mitigated.

Note that, the mean SFR of galaxies with 1.4 GHz luminosity of $10^{31.5}\text{ erg s}^{-1}\text{Hz}^{-1}$ is $\simeq 2800 M_{\odot}\text{ yr}^{-1}$ according to equation (4) or $\simeq 1355 M_{\odot}\text{ yr}^{-1}$ according to equation (5). Even in the latter case, we are dealing with extreme SFRs that occur rarely. While the model predictions are, by construction, consistent with the space densities of galaxies with the corresponding SFRs, derived primarily from *Herschel* data (Gruppioni et al. 2013), space densities derived from radio data are well above them. A contribution to the high luminosity excess may be due to strongly lensed SFGs. However, according to the estimates by Mancuso et al. (2015), this contribution is of order of 10 per cent or less in the relevant redshift and luminosity ranges.

Are radio surveys detecting SFGs with extreme SFRs missed by FIR/sub-mm surveys? A more likely explanation is that the radio emission of galaxies with $\log(L_{1.4\text{GHz}}/\text{erg s}^{-1}\text{Hz}^{-1}) \gtrsim 31.5$ has a substantial, perhaps dominant, contribution of nuclear origin. A contamination of SFG samples by RL AGNs is not surprising. In fact, both the Smolčić et al. (2009a) and the McAlpine et al. (2013) SFG samples were built using an optical colour-based method to separate SFGs from AGNs. The latter were identified in the radio population as sources associated with galaxies with predominantly old stellar populations, i.e. with redder colours. But studies of FIR properties of RL AGNs have found that their host galaxies show a strong evolution as a function of redshift, from predominantly quiescent at low z , except for the highest AGN powers (Gürkan et al. 2015), to predominantly dusty, with active star-formation at $z \gtrsim 1$ (e. g. Kalfountzou et al. 2014; Magliocchetti et al. 2014, 2016; Rees et al. 2016). Based on the results of McAlpine et al. (2013), Magliocchetti et al. (2016) argue that the radio luminosity beyond which the radio emission is predominantly AGN-powered increases from $\log(L_{1.4\text{GHz}}/\text{erg s}^{-1}\text{Hz}^{-1}) \simeq 29.8$ at $z = 0$ to $\log(L_{1.4\text{GHz}}/\text{erg s}^{-1}\text{Hz}^{-1}) \simeq 31.6$ at $z = 1.8$, and remains constant at higher redshifts. This is consistent with the luminosity

ranges where the excess over the expected SFG contribution shows up (see Fig. 3).

A clear indication that the contamination of the bright tail of the RLFs of SFGs is due to RL AGNs comes from Figs 4 and 5. The former figure shows that the observed space densities of the highest luminosity SFGs are akin to those of RL AGNs. RL AGNs are modelled following Massardi et al. (2010, see Appendix A for an upgraded version of such models). The second shows that the total (SFG+RL AGN) RLFs above $\log(L_{1.4\text{GHz}}/\text{erg s}^{-1}\text{Hz}^{-1}) \simeq 31.5$ can indeed be entirely accounted for by RL AGNs.

Strong support to this conclusion comes from the very recent analysis of the VLA-COSMOS 3 GHz survey data by Novak et al. (2017). The increased sensitivity of the 3 GHz survey compared to the 1.4 GHz survey used by Smolčić et al. (2009a) and the different method used to select SFGs yielded ~ 10 times more SFG detections in the same redshift range. The new, statistically more robust determinations of the SFG RLFs do not show indications of excesses over the model predictions at any redshift (cf. Fig. 3).

The ‘non-linear’ model with slope 1.1 (equation 5) yields luminosity functions hardly distinguishable from those of the ‘linear’ model; therefore, we chose not to plot them. The use of either equation (4) or (5) yields reasonably good matches of the data. The quality of the fit looks quite similar by eye. A χ^2 test gives a slight preference to the linear model, but the possibility of systematic errors due to, for example, contamination by nuclear emission or errors on photometric redshift estimates makes it difficult to reach a definite conclusion. However, the quality of the fit worsens rapidly as the slope on the $L_{\text{synch}}/\text{SFR}$ relation increases. Already for a slope of 1.2, the value suggested by Price & Duric (1992), the χ^2 increases by more than a factor of 2. Thus, although a deviation from linearity at all luminosities cannot be ruled out, the data on the luminosity functions of SFGs imply that the slope cannot be significantly larger than 1.1.

Note that a contamination by RL AGNs, which flattens the brightest portion of the RLFs, mimics the effect of a slope larger than 1: The flattening could be misinterpreted as evidence for a ‘non-linear’ relation. In the presence of a significant AGN contamination, the minimum χ^2 associated with the ‘non-linear’ model would be underestimated and the upper limit to the slope would be overestimated.

As shown by Fig. 3, the available estimates of the RLFs of SFGs cover limited luminosity ranges. At $z > 1$, they are restricted to luminosities well above the RLF ‘knee’ i.e. well above the luminosity, L_* , below which the slope of the RLF flattens substantially. But the largest contribution to the counts at any flux density S comes from redshifts at which $L(S, z) \sim L_*$. It follows that the counts constrain the redshift-dependent SFG luminosity function at luminosities below those at which direct determinations have been obtained. The sensitivity of the counts to the detailed shape of the luminosity function is illustrated by Fig. 6: Models that fit similarly well the available luminosity function data yield markedly different counts.

Fig. 7 compares the observed 1.4 GHz Euclidean normalized counts below 10 mJy with those yielded by the model for RL AGNs and SFGs. The counts of RL AGNs include the contributions of both steep- and flat-spectrum sources, the former being the dominant population. The counts of SFGs computed using the non-evolving ‘linear’ model are lower than those by Bondi et al. (2008), Vernstrom et al. (2016) and Smolčić et al. (2017), and then the estimate based on the $P(D)$ analysis by Vernstrom et al. (2014). The ‘non-linear’ model with a slope of 1.1 (not shown) yields counts barely higher; the difference is almost indiscernible by eye.

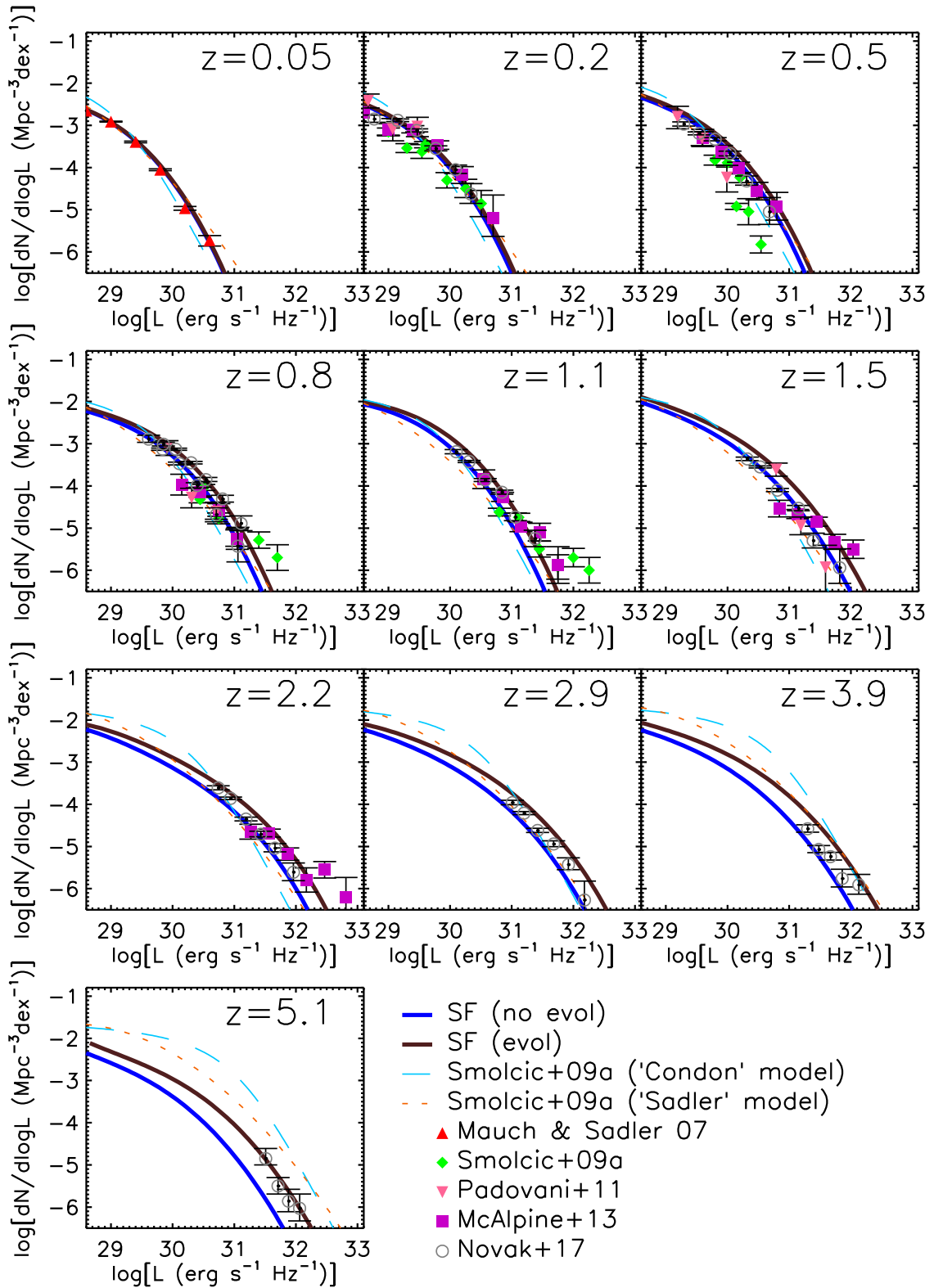


Figure 3. Model RLFs (at 1.4 GHz) of SFGs compared with observational determinations specified in the inset. The solid blue lines show the model RLFs inferred from the SFR functions, summing the free-free (equation 1) and the synchrotron contribution for the ‘linear’ model [equation (4)], without evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio. The solid dark-brown lines show the same model but with the best-fitting evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio from Magnelli et al. (2015). Also shown, for comparison, are the Condon (1989, ‘Condon’ model, dashed cyan lines) and the Sadler et al. (2002, ‘Sadler’ model, orange short dashes) parameterizations of the RLF (Smolčić et al. 2009a).

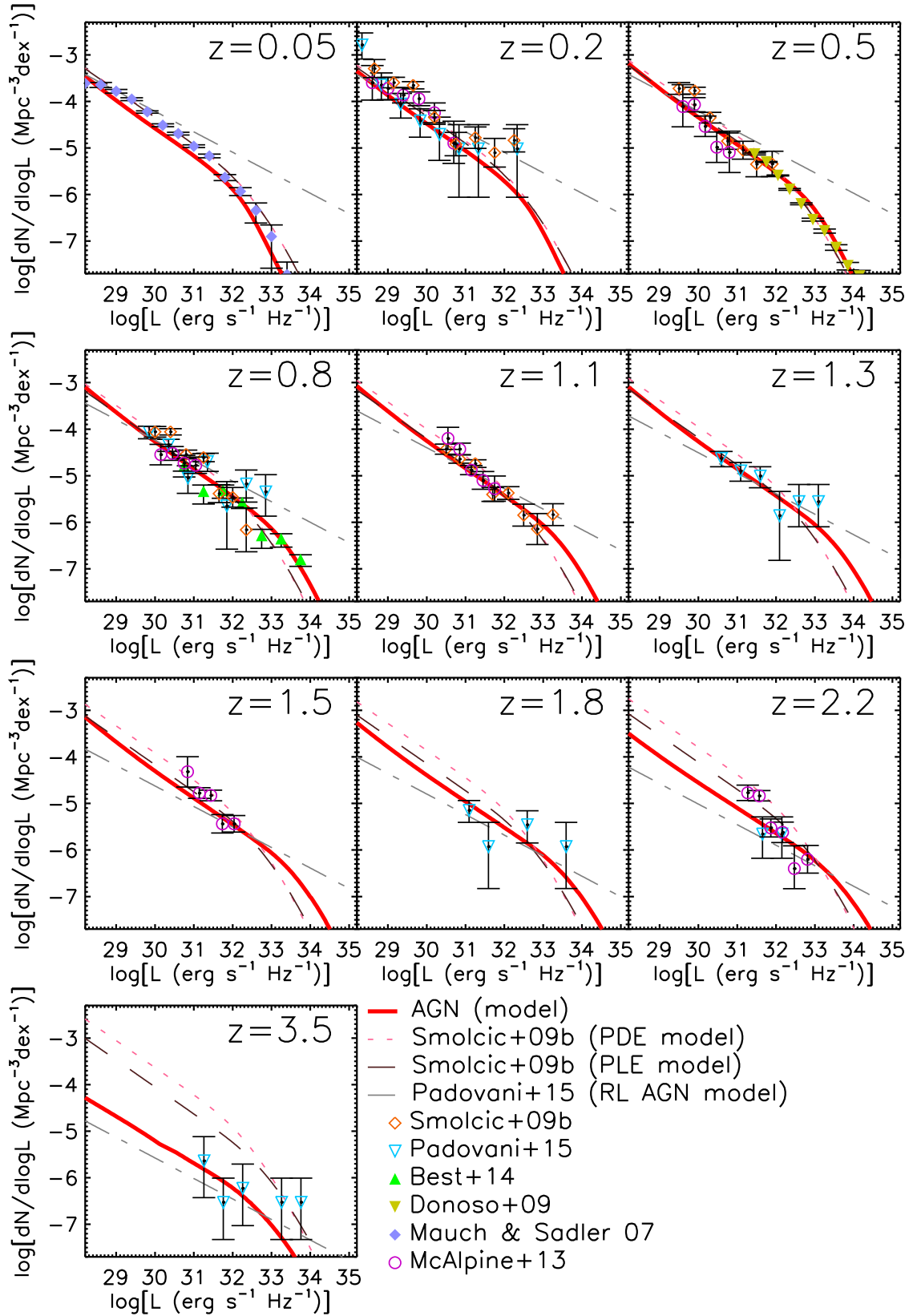


Figure 4. RLFs (at 1.4 GHz) of RL AGNs yielded by the model described in Appendix A (solid red lines) compared with the observational estimates specified in the inset. Also shown, for comparison, are the Smolčić et al. (2009b) pure density evolution (PDE, pink short dashes) and pure luminosity evolution (PLE, dashed brown lines) models and the best-fitting ‘ z_{peak} density evolution’ (ZDE) model with single power-law LF of Padovani et al. (2015, dot-dashed grey lines).

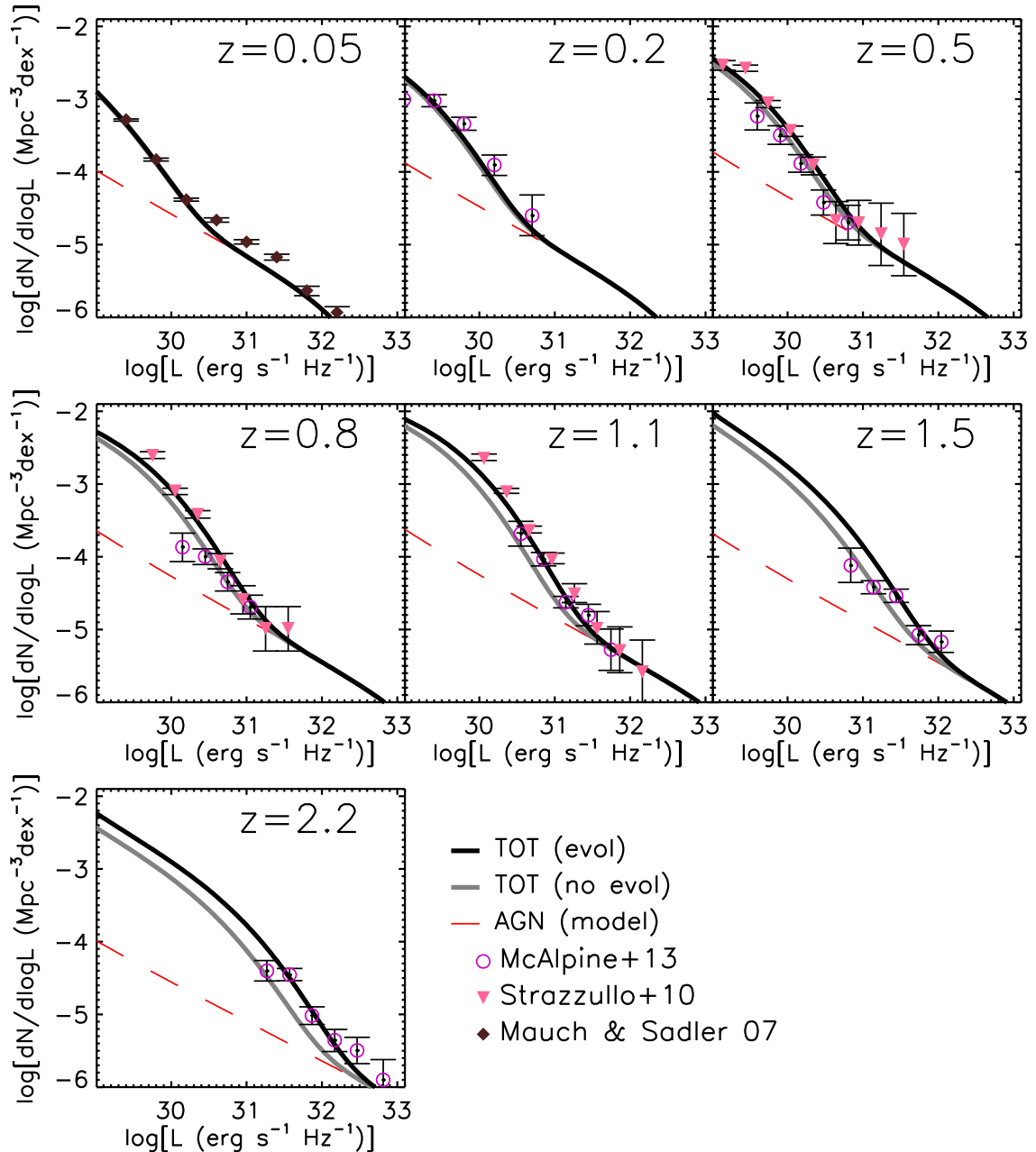


Figure 5. Total (SFG plus RL AGN) RLFs (at 1.4 GHz) derived using the ‘linear’ model for the synchrotron emission, with and without evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio (solid black and grey lines, respectively), compared with estimates from the literature at several redshifts. The dashed red lines show the contributions of RL AGNs.

Much better agreement with the observed counts is obtained with the ‘linear’ model, adopting the evolution of the $L_{\text{synch}}/\text{SFR}$ ratio based on the results of Magnelli et al. (2015, cf. equations 6 and 7; solid black line in Fig. 7):

$$\log L_{\text{synch},1.4\text{ GHz}}(z) = \log L_{\text{synch},1.4\text{ GHz}}(0) + 2.35[1 - (1+z)^{-0.12}]. \quad (8)$$

$L_{\text{synch},1.4\text{ GHz}}(0)$ is given by equation (4), and L_{FIR} has been converted to SFR using the calibration by Kennicutt & Evans (2012). The source counts thus lend support to the case for an increase with z of the $L_{\text{synch}}/\text{SFR}$ ratio, for which the Magnelli et al. (2015) data yielded a significance at the 3σ level only. A comparison with

Fig. 6 shows that such good fit, obtained without playing with any free parameter, is a highly non-trivial result.

The dashed black line in Fig. 7 illustrates the sensitivity of the counts to the evolution of the $L_{\text{synch}}/\text{SFR}$ ratio. Already with the coefficient of equation (6) and α_M at their 1σ limits (2.43 and -0.16 , respectively), the evolution yields counts at hundreds of μJy flux densities at the upper limits of observational determinations. The ‘non-linear’ model with slope 1.1 [equation (5)] gives counts very close to those of the latter case, i.e. requires a slightly weaker evolution to match the counts. Thus the counts, while supporting the evolution of the $L_{\text{synch}}/\text{SFR}$ ratio, also provide tight constraints on its strength.

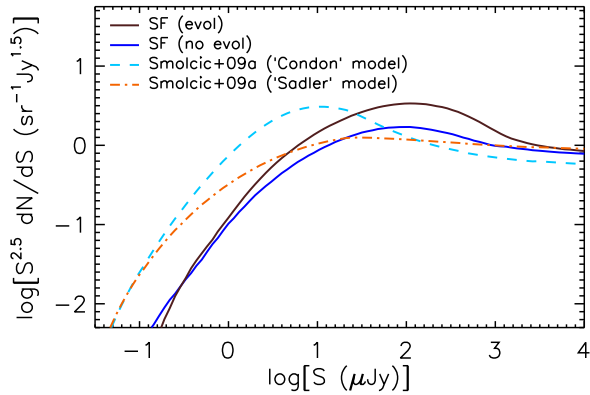


Figure 6. SFG counts yielded by the ‘linear’ model for the synchrotron emission, with and without evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio (solid brown and blue line, respectively), compared with those given by the empirical models from Smolčić et al. (2009a): the ‘Condon’ model (dashed cyan line) and the ‘Sadler’ model (dot–dashed orange line).

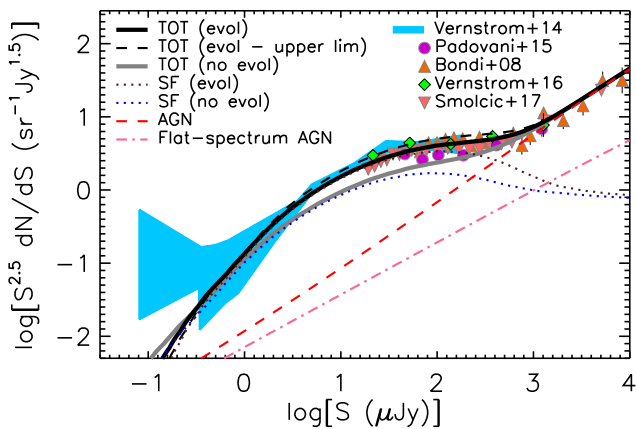


Figure 7. Comparison between the observed faint 1.4 GHz Euclidean normalized counts and those yielded by the model. The counts of RL AGNs (dashed red line) are dominated by steep-spectrum sources; the contribution of the flat-spectrum ones is shown by the dot–dashed pink line. The dotted lines show the counts of SFGs yielded by the ‘linear’ model, with (upper line) and without evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio, for the best-fitting value of the evolutionary parameter given by Magnelli et al. (2015). The total counts for the two cases, obtained adding the RL AGN contribution, are shown by the solid black and grey lines, respectively. The evolution brings the model counts to agreement with the observational estimate by Bondi et al. (2008), by Vernstrom et al. (2016) and by Smolčić et al. (2017), and with the results of the $P(D)$ analysis by Vernstrom et al. (2014, shaded light blue area). The ‘non-linear’ model with slope of 1.1 yields counts (not shown) imperceptibly higher than those from the ‘linear’ model. The dashed black line shows the model counts for an evolution of the mean $L_{\text{synch}}/\text{SFR}$ ratio at the 1σ limit of Magnelli et al. (2015). In this case, the counts are at the upper boundary of the observational determinations.

4 CONCLUSIONS

We have exploited the observational estimates of the 1.4 GHz RLFs of SFGs at several redshifts, up to $z \simeq 5$, to investigate the relationship between the 1.4 GHz luminosity and the SFR over a wider luminosity and redshift range than done so far. The assessment of such a relationship is crucial on one hand to enable a full exploitation of surveys from the SKA and its precursors to measure the cosmic star formation history, and on the other hand to provide reliable predictions for future deep radio surveys. To this end, we have exploited recent accurate determinations of the SFR functions

up to high redshifts obtained by combining data from optical, UV, $H\alpha$ and FIR/sub-mm surveys.

At the low radio frequencies ($\lesssim 5$ GHz) at which deep large area surveys are preferentially carried out or planned, the dominant emission process is synchrotron radiation, whose connection to the SFR is not well understood, although very well established observationally. Several observational indications and theoretical arguments point to deviations from a linear relation between the synchrotron emission, L_{synch} , and SFR. However, the parameters defining such a relation are fraught with a considerable uncertainty. It is even unclear whether the deviations from linearity are limited to low luminosities/SFRs (Bell 2003; Lacki et al. 2010; Massardi et al. 2010; Mancuso et al. 2015) or extend to all luminosities (Price & Duric 1992; Niklas 1997; Basu et al. 2015).

We have derived 1.4 GHz luminosity functions from the SFR functions both in the case of deviations from a linear relation limited to low luminosities (‘linear’ model) and in the case of a mildly non-linear relation at all luminosities (‘non-linear’ model). In both cases, the model parameters were fixed fitting the local luminosity function of SFGs by Mauch & Sadler (2007).

The quality of the fit of observational determinations of the 1.4 GHz luminosity function at several redshifts is similarly good in both cases. A χ^2 analysis slightly favours the ‘linear’ model, but we must be aware of systematics that are difficult to quantify. Thus with the data at hand, we cannot clearly discriminate among the two options. However, the RLF data reject ‘non-linear’ models with a slope ≥ 1.2 .

The ‘linear’ and ‘non-linear’ options differ most markedly at the highest and at the lowest luminosities. Current surveys are not deep enough to reach sufficiently low luminosities at high redshifts to allow for a clear discrimination. At the highest luminosities, the observed luminosity functions of SFGs may be contaminated by nuclear radio emission and must therefore be dealt with caution. Much larger and deeper samples, and better ancillary data to allow a more solid classification are necessary to accurately determine the parameters of the $L_{\text{synch}}/\text{SFR}$ relation.

We have modelled the source counts with two components, one accounting for SFGs and one for RL AGNs (i.e. we have assumed that the radio emission from RQ AGNs is dominated by star formation). Under this assumption, both the ‘linear’ and the ‘non-linear’ cases, without evolution of the $L_{\text{synch}}/\text{SFR}$ ratio, yield sub-mJy counts substantially below the observational determinations by Bondi et al. (2008), Vernstrom et al. (2016) and Smolčić et al. (2017), and the $P(D)$ estimate from Vernstrom et al. (2014). Good consistency is achieved, for the ‘linear’ case, adopting the best-fitting evolution derived by Magnelli et al. (2015). A similarly good fit is obtained, for the ‘non-linear’ case, with a slightly weaker evolution. This strengthens the case for evolution that Magnelli et al. (2015) found to be significant only at the 3σ level. At the same time, the counts provide a tight upper limit to the strength of the evolution. Already, the 1σ limits of the Magnelli et al. (2015) evolutionary parameters yield counts at the upper boundary of observational determinations at hundreds of μJy flux densities.

The increase with redshift of the $L_{\text{synch}}/\text{SFR}$ ratio, supported by our results, is in contradiction with models predicting a decrease of such ratio at high redshifts as a consequence of the increase of the energy losses of relativistic electrons via inverse Compton scattering off the cosmic microwave background (e.g. Murphy 2009; Lacki & Thompson 2010; Schleicher & Beck 2013; Schober et al. 2016).

As for RL AGNs, we find good consistency between the observational determinations of the redshift-dependent RLFs and our update of the Massardi et al. (2010) model, without any

adjustment of the parameters. This lends support to the description of downsizing built in the model.

ACKNOWLEDGEMENTS

We are grateful to Marco Bondi for useful clarifications on the VLA–COSMOS catalogue. The comments of the anonymous referees have helped us to better focus our paper and to clarify several points. Work supported in part by PRIN–INAF 2014 ‘Probing the AGN/galaxy co-evolution through ultra-deep and ultra-high resolution radio surveys, by PRIN–INAF 2012 ‘Looking into the dust-obscured phase of galaxy formation through cosmic zoom lenses in the Herschel Astrophysical Large Area Survey’ and by ASI/INAF agreement n. 2014-024-R.1. Z-YC is supported by the National Science Foundation of China (grant No. 11503024). AB acknowledges support from the European Research Council under the EC FP7 grant number 280127. VS acknowledges the European Union’s Seventh Framework programme under grant agreement 337595. PC thanks the support of the Ministry of Foreign Affairs and International Cooperation, Directorate General for the Country Promotion (Bilateral Grant Agreement ZA14GR02 - Mapping the Universe on the Pathway to SKA). MN acknowledges financial support from the European Union’s Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 707601.

REFERENCES

- Aversa R., Lapi A., de Zotti G., Shankar F., Danese L., 2015, *ApJ*, 810, 74
 Banday A. J., Wolfendale A. W., 1991, *MNRAS*, 248, 705
 Basu A., Wadadekar Y., Beelen A., Singh V., Archana K. N., Sirothia S., Ishwara-Chandra C. H., 2015, *ApJ*, 803, 51
 Bell E. F., 2003, *ApJ*, 586, 794
 Best P. N., Ker L. M., Simpson C., Rigby E. E., Sabater J., 2014, *MNRAS*, 445, 955
 Bonato M. et al., 2014, *MNRAS*, 438, 2547
 Bondi M., Ciliegi P., Schinnerer E., Smolčić V., Jahnke K., Carilli C., Zamorani G., 2008, *ApJ*, 681, 1129
 Bonzini M. et al., 2012, *ApJS*, 203, 15
 Bonzini M., Padovani P., Mainieri V., Kellermann K. I., Miller N., Rosati P., Tozzi P., Vattakunnel S., 2013, *MNRAS*, 436, 3759
 Bonzini M. et al., 2015, *MNRAS*, 453, 1079
 Bourne N., Dunne L., Ivison R. J., Maddox S. J., Dickinson M., Frayer D. T., 2011, *MNRAS*, 410, 1155
 Cai Z.-Y. et al., 2013, *ApJ*, 768, 21
 Cai Z.-Y., Lapi A., Bressan A., De Zotti G., Negrello M., Danese L., 2014, *ApJ*, 785, 65
 Condon J. J., 1989, *ApJ*, 338, 13
 Condon J. J., Kellermann K. I., Kimball A. E., Ivezić Ž., Perley R. A., 2013, *ApJ*, 768, 37
 De Zotti G., Massardi M., Negrello M., Wall J., 2010, *A&AR*, 18, 1
 Delhaize J. et al., 2017, preprint ([arXiv:1703.09723](https://arxiv.org/abs/1703.09723))
 Donoso E., Best P. N., Kauffmann G., 2009, *MNRAS*, 392, 617
 Draine B. T., 2011, *Phys. Interstellar Intergalactic Medium*
 Garn T., Green D. A., Riley J. M., Alexander P., 2009, *MNRAS*, 397, 1101
 Gruppioni C. et al., 2013, *MNRAS*, 432, 23
 Gürkan G. et al., 2015, *MNRAS*, 452, 3776
 Herrera Ruiz N., Middelberg E., Norris R. P., Maini A., 2016, *A&A*, 589, L2
 Ibar E. et al., 2008, *MNRAS*, 386, 953
 Ilbert O. et al., 2009, *ApJ*, 690, 1236
 Ivison R. J. et al., 2010a, *MNRAS*, 402, 245
 Ivison R. J. et al., 2010b, *A&A*, 518, L31
 Kalfountzou E. et al., 2014, *MNRAS*, 442, 1181
 Kellermann K. I., Condon J. J., Kimball A. E., Perley R. A., Ivezić Ž., 2016, *ApJ*, 831, 168
 Kennicutt R. C., Evans N. J., 2012, *ARA&A*, 50, 531
 Kimball A. E., Kellermann K. I., Condon J. J., Ivezić Ž., Perley R. A., 2011, *ApJ*, 739, L29
 Lacki B. C., Thompson T. A., 2010, *ApJ*, 717, 196
 Lacki B. C., Thompson T. A., Quataert E., 2010, *ApJ*, 717, 1
 Lacy M., Petric A. O., Sajina A., Canalizo G., Storrie-Lombardi L. J., Armus L., Fadda D., Marleau F. R., 2007, *AJ*, 133, 186
 Leitherer C. et al., 1999, *ApJS*, 123, 3
 McAlpine K., Jarvis M. J., Bonfield D. G., 2013, *MNRAS*, 436, 1084
 Magliocchetti M. et al., 2014, *MNRAS*, 442, 682
 Magliocchetti M., Lutz D., Santini P., Salvato M., Popesso P., Berta S., Pozzi F., 2016, *MNRAS*, 456, 431
 Magnelli B. et al., 2015, *A&A*, 573, A45
 Maini A., Prandoni I., Norris R. P., Giovannini G., Spitler L. R., 2016, *A&A*, 589, L3
 Mancuso C. et al., 2015, *ApJ*, 810, 72
 Mancuso C., Lapi A., Shi J., Gonzalez-Nuevo J., Aversa R., Danese L., 2016, *ApJ*, 823, 128
 Mao M. Y., Huynh M. T., Norris R. P., Dickinson M., Frayer D., Helou G., Monkiewicz J. A., 2011, *ApJ*, 731, 79
 Massardi M., Bonaldi A., Negrello M., Ricciardi S., Raccanelli A., de Zotti G., 2010, *MNRAS*, 404, 532
 Mauch T., Sadler E. M., 2007, *MNRAS*, 375, 931
 Miller N. A. et al., 2013, *ApJS*, 205, 13
 Mocanu L. M. et al., 2013, *ApJ*, 779, 61
 Murphy E. J., 2009, *ApJ*, 706, 482
 Murphy E. J. et al., 2011, *ApJ*, 737, 67
 Murphy E. J. et al., 2012, *ApJ*, 761, 97
 Niklas S., 1997, *A&A*, 322, 29
 Novak M. et al., 2017, preprint ([arXiv:1703.09724](https://arxiv.org/abs/1703.09724))
 Padovani P., Mainieri V., Tozzi P., Kellermann K. I., Fomalont E. B., Miller N., Rosati P., Shaver P., 2009, *ApJ*, 694, 235
 Padovani P., Miller N., Kellermann K. I., Mainieri V., Rosati P., Tozzi P., 2011, *ApJ*, 740, 20
 Padovani P., Bonzini M., Kellermann K. I., Miller N., Mainieri V., Tozzi P., 2015, *MNRAS*, 452, 1263
 Pannella M. et al., 2015, *ApJ*, 807, 141
 Price R., Duric N., 1992, *ApJ*, 401, 81
 Rees G. A. et al., 2016, *MNRAS*, 455, 2731
 Sadler E. M. et al., 2002, *MNRAS*, 329, 227
 Sargent M. T. et al., 2010a, *ApJS*, 186, 341
 Sargent M. T. et al., 2010b, *ApJ*, 714, L190
 Schleicher D. R. G., Beck R., 2013, *A&A*, 556, A142
 Schober J., Schleicher D. R. G., Klessen R. S., 2016, *ApJ*, 827, 109
 Scoville N. et al., 2007, *ApJS*, 172, 1
 Seymour N., Huynh M., Dwelly T., Symeonidis M., Hopkins A., McHardy I. M., Page M. J., Rieke G., 2009, *MNRAS*, 398, 1573
 Smolčić V. et al., 2008, *ApJS*, 177, 14
 Smolčić V. et al., 2009a, *ApJ*, 690, 610
 Smolčić V. et al., 2009b, *ApJ*, 696, 24
 Smolčić V. et al., 2017, preprint ([arXiv:1703.09713](https://arxiv.org/abs/1703.09713))
 Vernstrom T. et al., 2014, *MNRAS*, 440, 2791
 Vernstrom T., Scott D., Wall J. V., Condon J. J., Cotton W. D., Kellermann K. I., Perley R. A., 2016, *MNRAS*, 462, 2934
 Weiß A. et al., 2013, *ApJ*, 767, 88
 Yun M. S., Reddy N. A., Condon J. J., 2001, *ApJ*, 554, 803

APPENDIX A: EVOLUTION OF RADIO LOUD AGNS

To describe the cosmological evolution of RL AGNs, we adopted the Massardi et al. (2010) model, which successfully fitted a large amount of data on LFs of steep- and flat-spectrum sources, multifrequency source counts and redshift distributions. The model includes two flat-spectrum populations with different evolutionary

Table A1. Best-fitting values of the parameters of the evolutionary model for RL AGNs (see equations A1, A2, A3 and A4).

Parameters	FSRQ	BLLac	SS-AGNs
a	0.743	0.786	0.487
b	3.293	1.750	2.410
$\log n_0$	-11.262	-7.683	-5.866
$\log L_*(0)$	34.285	33.223	32.472
k_{evo}	-0.976	0.582	1.244
$z_{\text{top},0}$	1.749	1.054	1.063
δz_{top}	0.001	-	0.772
m_{ev}	-0.207	1	0.278

properties (flat-spectrum radio quasars, FSRQs, and BL Lacs) and a single steep-spectrum population. For sources of each population, a simple power-law spectrum is adopted: $S \propto \nu^{-\alpha}$, with $\alpha_{\text{FSRQ}} = \alpha_{\text{BLLac}} = 0.1$ and $\alpha_{\text{steep}} = 0.8$.

The epoch-dependent comoving LFs (in units of $\text{Mpc}^{-3} (\text{d log } L)^{-1}$) were modelled as double power laws:

$$\Phi(L(z), z) = \frac{n_0}{(L(0)/L_*(0))^a + (L(0)/L_*(0))^b} \frac{d \log L(0)}{d \log L(z)}. \quad (\text{A1})$$

Massardi et al. (2010) worked out, for each population, an analytic luminosity evolution model entailing a high- z decline of the comoving LF:

$$L_*(z) = L_*(0) \text{dex} \left[k_{\text{evo}} z \left(2z_{\text{top}} - 2z_{\text{top}}^{m_{\text{ev}}} z_{\text{top}}^{(1-m_{\text{ev}})/(1+m_{\text{ev}})} \right) \right], \quad (\text{A2})$$

where z_{top} is the redshift at which $L_*(z)/L_*(0)$ reaches its maximum and $|m_{\text{ev}}| \leq 1$. The data further required a luminosity dependence of z_{top} , that was parametrized as

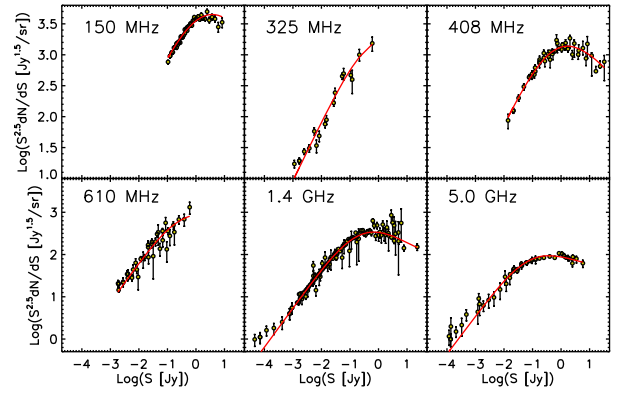
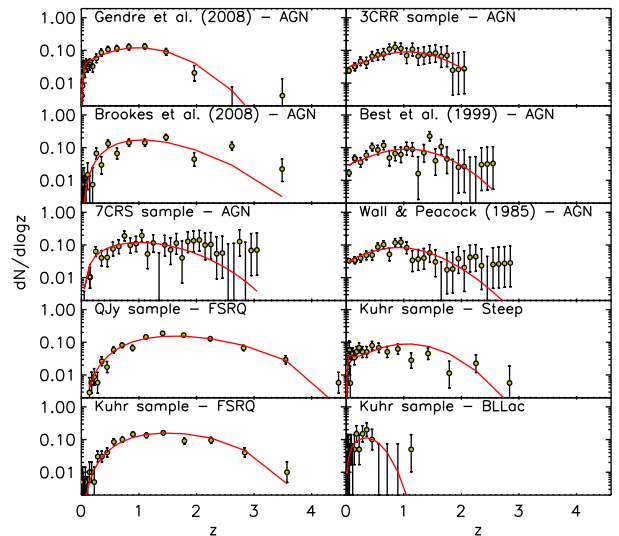
$$z_{\text{top}} = z_{\text{top},0} + \frac{\delta z_{\text{top}}}{1 + L_*(0)/L}. \quad (\text{A3})$$

The fit gave positive values for the parameters, $z_{\text{top},0}$ and δz_{top} , implying that the high- z decline of the space density is more pronounced and starts at lower redshifts for less powerful sources. This behaviour is qualitatively similar to the *downsizing* observed for galaxies and optically and X-ray selected quasars. We included the Jacobian term

$$\begin{aligned} \frac{d \log L(0)}{d \log L(z)} &= 1 + 2k_{\text{evo}} \delta z_{\text{top}} \ln 10 \frac{L_*(0)/L(0)}{(1 + [L_*(0)/L(0)])^2} \\ &\quad - \frac{2 \ln 10 (1 - m_{\text{ev}})}{1 + m_{\text{ev}}} \times \delta z_{\text{top}} \times \frac{L_*(0)}{L(0)} \\ &\quad \times \frac{[z_{\text{top},0} + \delta z_{\text{top}} / (1 + L_*(0)/L(0))]^{-m_{\text{ev}}}}{(1 + L_*(0)/L(0))^2}, \end{aligned} \quad (\text{A4})$$

inadvertently omitted in the code used by Massardi et al. (2010). We have recomputed the best-fitting values of the parameters using the same method and comparing the model to the same data sets. The global minimum χ^2 decreases by about 10 per cent and the best-fitting values of the parameters change a little. The new values are listed in Table A1.

As found by Massardi et al. (2010), the luminosity dependence of the peak redshift required by the data is substantial for the steep-spectrum population but is weak ($\delta z_{\text{top}} \ll 1$) for FSRQs. This is expected since the contributions to the observables (source counts and redshift distributions) of moderate to low luminosity flat-spectrum sources are dominated by BL Lacs, so that the evolution of low luminosity FSRQs is poorly constrained. In the case of BL Lacs,


Figure A1. Comparison of our best-fitting evolutionary model for RL AGNs with Euclidean normalized differential counts at several frequencies. Data points are from the compilation by De Zotti et al. (2010). As is well known, AGNs become sub-dominant compared to SFGs at sub-mJy flux density levels.

Figure A2. Comparison of our best-fitting evolutionary model for RL AGNs with observational determinations of the redshift distributions for several source samples. See Massardi et al. (2010) for a description of the samples and for references.

the data are not enough to constrain the parameters governing the luminosity dependence of the evolution. Thus, following Massardi et al. (2010), for this population, we have set $m_{\text{ev}} = 1$ and $\delta z_{\text{top}} = 0$.

Figs A1 and A2 compare the outcome of the revised model with the observed source counts at different frequencies and with the observational determinations of the redshift distributions for 10 source samples at different frequencies, at different flux density limits and for different populations of RL AGNs. The agreement of the model with the data is always satisfactory.

Our model for RL AGNs is quite successful at accounting for the evolution of the RLFs of these objects (see Fig. 4). As mentioned above, the dominant AGN population is made of steep-spectrum sources for which evidence of downsizing was inferred from integrated data (primarily source counts). The adopted description of the downsizing turns out to be nicely consistent with the more direct information provided by the redshift dependent luminosity functions.

Figs 3 and 4 also show that our model is highly competitive with the most recent models found in the literature. This is a non-trivial result because the other models shown were tuned to fit specifically the observational determinations of the 1.4 GHz luminosity functions while our model is not. In fact, our redshift-dependent RLFs of

SFGs are directly extrapolated from the SFR functions and those of RL AGNs come from fits of other data sets, without any adjustment of the parameters.

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