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# A Python approach for GRB afterglow analysis: sAGa (Software for AfterGlow Analysis)



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## ABSTRACT

This technical note describes a fully self-consistent code in Python – called sAGA (Software for AfterGlow Analysis) – to cope with the complex landscape of GRB afterglows. sAGA adds up to other pre-existing broadband fitting tools in the literature and provides an independent check, emphasising the broadband study of GRB afterglows over the last two decades.

This code aims to model GRB afterglow data within a self-consistent physically grounded picture. Built adopting a Bayesian approach, all the data set, from radio to gamma-rays, is modelled. By-products are plots of spectra and light-curves, and computation of the break frequencies and normalisations as a function of the shock microphysical parameters, such as the power-law index of the electron energy distribution, the fractions of the blastwave energy delivered to relativistic electrons and magnetic fields, and other parameters such as the kinetic energy of the explosion and the density of the circumburst medium (CBM). Dust extinction of optical along the sightline and scintillation in radio frequencies are also accounted for.

sAGA has been successfully tested on the broadband data of the afterglows of GRB 120521C, GRB 090423, and GRB 050904. Our results are consistent with those reported in the literature within  $\lesssim 2\sigma$ . Moreover, the values of the power-law index of the electron energy distribution obtained from sAGA analysis are compatible with the inferences based on the lines of reasoning based on the observation of the optical/X-ray spectra.



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# 1 Introduction: an analytical approach for broadband modelling of GRB afterglows

The afterglow radiation from gamma-ray bursts (GRBs) – short and intense pulses of gamma-ray radiation, originating from either core collapsing massive stars (e.g. [149]) or binary neutron star (BNS) mergers (e.g. [1]) – takes place when the outflow from the GRB central engine penetrates the circumburst medium (CBM), resulting mainly in synchrotron radiation (for a review see e.g. [102, 83, 31]). It originates in two shock regions: a forward shock (FS) that propagates in the CBM (e.g. [44], hereafter GS02), and a reverse shock (RS) that propagates back into the flow itself and radiates at lower frequencies (e.g. [85, 57, 59, 32]).

GRB afterglows encode a wealth of information on (1) the radiation mechanism, in particular the possible presence of large-scale magnetic fields ploughing the ejecta, which is still one of the main open issues in the field (e.g. [51]); (2) relativistic shock micro-physics; (3) energetics; (4) jet geometry. All these issues can be addressed effectively and uniquely through observations at lower frequencies, especially in the radio band. Observations of radio afterglows are key to diagnose the GRB physics (e.g. [90]), especially for the understanding of the RS component, which links directly to the nature of the outflow and, consequently, to the progenitor itself (e.g. [60]). On the other hand, the detection of radio afterglows has proven challenging with current radio telescopes (e.g. [13]) – especially in single-dish mode [80] – mainly because of their faintness ( $\lesssim$  mJy).

The analysis of GRB afterglow spectra and light curves is made possible using data from radio to X-ray frequencies. The ongoing improvements in sensitivity for broadband facilities, especially at radio frequencies – such as the upgraded Giant Metre-wave Radio Telescope (GMRT, [130, 54, 45])<sup>1</sup>, the Karl G. Jansky Very Large Array (VLA, [133])<sup>2</sup>, the Arcminute Microkelvin Imager Large Array (AMI-LA, [162])<sup>3</sup>, and the NOrthern Extended Millimeter Array (NOEMA, [15])<sup>4</sup> – give the opportunity to gain insight into the microphysical parameters with unprecedented accuracy. In parallel, the continuous evolution of computational resources fosters the development of sophisticated data analysis packages (e.g. [109, 56, 22, 62, 12, 159, 138, 151, 137, 23, 42, 68, 69, 111, 3, 114, 6]), but to date there is no computational tool that is able to fully describe the complex landscape of the GRB afterglows.

In this context we developed a fully self-consistent code in Python called sAGA (Software for AfterGlow Analysis), described in this technical note. sAGA provides an independent tool among other computational packages aimed at broadband modelling of GRB afterglows. Built adopting a Bayesian approach, all the data, from radio to gamma-rays, are modelled. sAGA considers different radiation processes (synchrotron and inverse Compton radiation, Sects. 4 and 9, respectively), and other aspects, described in this technical note (jetted emission and non-relativistic regime, Sect. 5; energy injection phenomenon, Sect. 6; extinction and absorption effects, Sect. 7; scintillation in radio frequencies, Sect. 8), selectable by the user through a simple widget displayed when sAGA is launched.

This application receives in input two text-based files (Sect. 2.2): the “observation data file” (a table containing the epoch of observation, the flux density and its uncertainty, and the observing frequency) and the GRB “parameter file” (such as the sky position and the redshift). Later, sAGA performs a broadband data analysis in a single process through a

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<sup>1</sup><http://www.gmrt.ncra.tifr.res.in/>

<sup>2</sup><https://science.nrao.edu/facilities/vla>

<sup>3</sup><https://www.astro.phy.cam.ac.uk/research/research-projects/AMI>

<sup>4</sup><http://iram-institute.org/EN/noema-project.php>

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new approach that consists in the manipulation of all the data both at each given epoch and given frequency. Finally, in output sAGA provides several plots of light curves and spectra of the GRB afterglow (both for each epoch/observing frequency and global) and a text-based file reporting best-fit values associated with the user’s configuration (selected radiation processes and other aspects).

sAGA determines the break frequencies and normalisations as a function of the shock microphysical parameters, such as the power-law index of the electron energy distribution ( $p$ ), the fractions of the blastwave energy delivered to relativistic electrons ( $\epsilon_e$ ) and magnetic fields ( $\epsilon_B$ ), and other parameters such as the kinetic energy of the explosion ( $E_{K,\text{iso}}$ ), and the CBM density ( $n_0$  for ISM-like CBM; the normalised mass-loss rate  $A_*$  for wind-like CBM). Dust extinction of optical along the sightline is also accounted for in terms of the V-band extinction  $A_V$ .

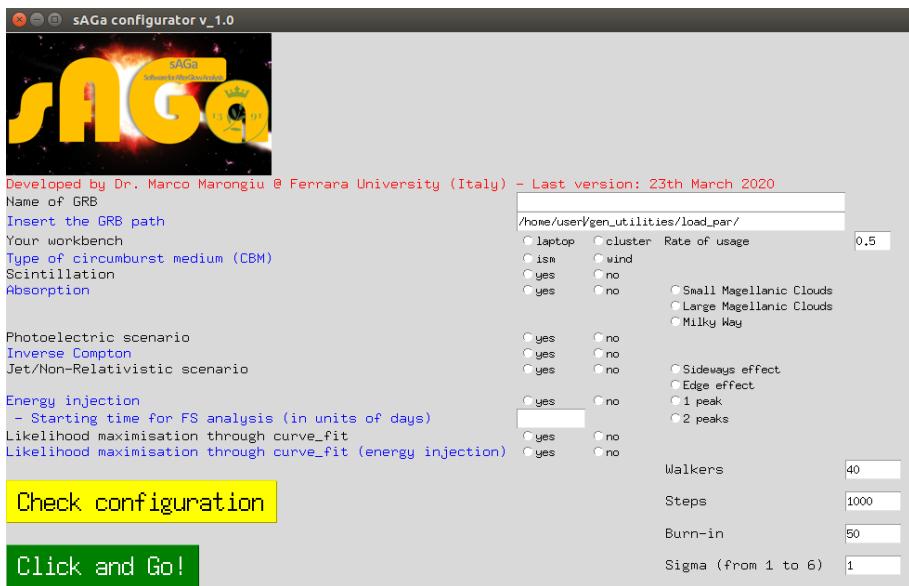
sAGA has been successfully tested on the broadband data of the afterglows of GRB 120521C, GRB 090423, and GRB 050904 for which analogous and independent analyses are available in the literature, where the results obtained with sAGA are consistent with those reported in the literature (especially [67], hereafter L14, who make use of a similar approach for the characterisation of the GRB afterglow) within  $\lesssim 2\sigma$ .

This technical note is organised as follows. Preliminary information about sAGA is reported in Sect. 2; the Markov Chain Monte Carlo (MCMC) analysis in Bayesian approach – crucial in high-dimensional problems (like the present one) – is reported in Sect. 3; the physical aspects of GRB afterglow emission encoded in sAGA are described in Sects. 4, 5, 6, 7, 8, 9. The test phase of sAGA on other GRB afterglows is reported in Sect. 10, and finally we give our conclusions in Sect. 11.

Hereafter, sAGA assumes default  $\Lambda$ CDM cosmological parameters of  $\Omega_m = 0.32$ ,  $\Omega_\Lambda = 0.69$ , and  $H_0 = 67.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$  [103]; the user can use specific tools available in the Python ASTROPY package<sup>5</sup> [5, 104] to customise these parameters.

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<sup>5</sup><https://www.astropy.org/>



**Figure 1:** Widget of sAGA. The user must compile all the boxes before clicking the button “Click and Go!”.

## 2 Preliminary information

sAGA is compatible with the following characteristics:

- Ubuntu 12.04 (x32 or x64-based operating system) or recent versions as operating system;
- 4 GB or more of RAM (16 GB recommended);
- 5 GB or more of free disk space;
- python 3.X.X;
- emcee 3.X.X;
- anaconda 4.X.X or more.

### 2.1 Usage of sAGA

The usage of sAGA is very simple, thanks to a very intuitive widget (Fig 1). After filling the form with the required details for the analysis, the "Check configuration" yellow button allows to verify the configuration on the user's terminal, and eventually to modify the configuration. Once satisfied with the selected configuration, the "Click and Go!" green button launches sAGA.

### 2.2 Preparation of data files

Before using sAGA, the user must compile three text-based files:

1. The *data tables* – one for each observing frequency – contain the data set of the GRB afterglow under consideration; each table must include (1) the epoch of observation (in units of days), (2) the flux density and (3) its uncertainty (in units of mJy), (4) the

## 2.3 Composition of sAGA

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observing frequency (in units of Hz), and (5) the nature of the measure (0 for upper limit, 1 for detection). These tables are stored in a working directory that the user must type in the "Insert the GRB path" box of the widget (Fig. 1).

2. The "*observation data file*" includes the necessary instructions for reading the data tables from sAGA.
3. The "*parameter file*" contains all the known information about the GRB afterglow under consideration, such as the GRB position and its redshift.

### 2.3 Composition of sAGA

sAGA consists in a sophisticated Python architecture (Fig. 2), composed of several environments:

- **importlibmod.py** ⇒ This part acquires the information from the text-based files described in Sect. 2.2.
- **maths.py** ⇒ Some mathematical/statistical functions are contained in this file.
- **bayesian.py** ⇒ In this file there are the necessary functions for the Bayesian analysis of the data.
- **scint.py** ⇒ This part includes the functions related to the radio scintillation analysis (for further information see Sect. 8).
- **absorp\_opt.py - nh\_photo.py** ⇒ All the functions responsible for the dust extinction in optical and the photoelectric absorption in X-rays (see Sect. 7) are included in this file.
- **jet\_nr.py** ⇒ In this file there is the part regarding the jetted emission and the Newtonian regime (Sect. 5).
- **class\_fs.py - class\_ei.py - class\_rs.py** ⇒ All the functions describing the radiation mechanisms ascribed to forward (FS) and reverse shocks (RS)<sup>6</sup> and the energy injection regime (Sect. 6) are contained in these files.
- **inv\_compton.py** ⇒ This part regards the inverse Compton radiation, nearing completion (Sect. 9).
- **plot\_fit\_synchr.py** ⇒ This is the output of sAGA, containing the functions for the production of spectra and light curves (Sect. 4, both plots and tables), and Bayesian/modelling results (Sect. 3). The output is located in the directory path typed from the user in the "Insert the GRB path" box in the widget (Fig. 1).

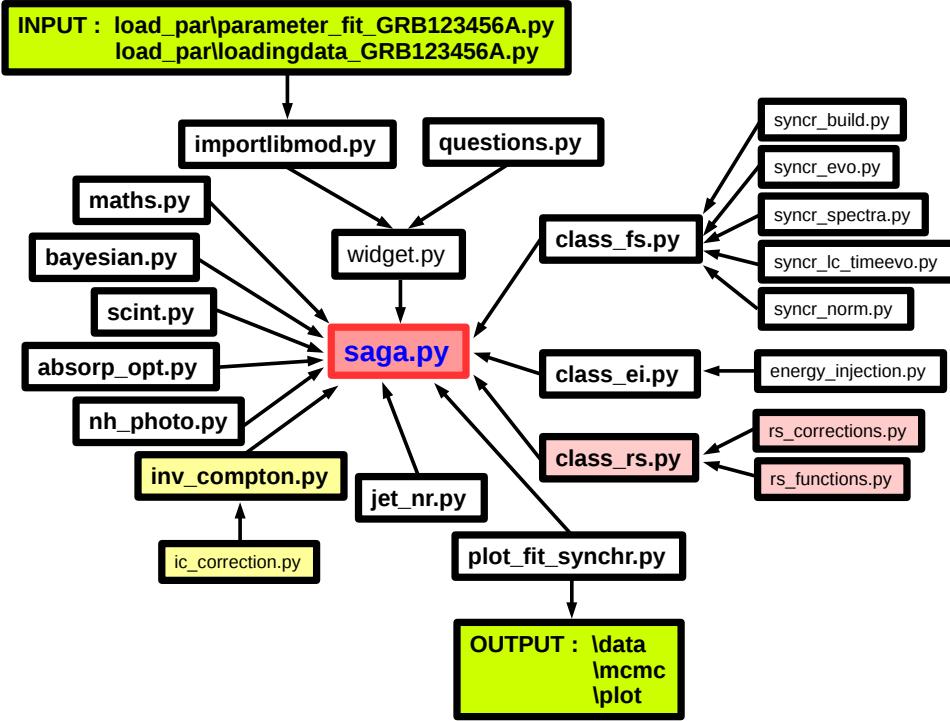
## 3 Markov Chain Monte Carlo

The best-fit solution for a data set sAGA that includes both detections and upper limits, is calculated through the maximisation of the following likelihood function, given by (e.g., L14):

$$\prod p(e_i)^{\delta_i} F(e_i)^{1-\delta_i} \quad (1)$$

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<sup>6</sup>Reverse shock regime is incomplete and currently unavailable.



**Figure 2:** Structure of sAGA. Yellow boxes indicate the sections nearing completion; red boxes indicate the incomplete parts. Input/Output are labeled in green.

where  $e_i$  are the residuals (the difference between either measurement or  $3\sigma$  upper limit and the predicted flux from the model),  $\delta_i$  is the detection parameter (equal to 0 for a  $3\sigma$  upper limit and 1 for a detection),  $p(e_i)$  is the probability density function of the residuals (we assumed a Gaussian error model), and  $F(e_i)$  is the cumulative distribution function of the residuals. In sAGA the maximisation of the likelihood function is calculated by using the sequential least squares programming tool available in the Python SCI PY package<sup>7</sup> [50].

The radiation processes and other additional aspects involved in sAGA inevitably introduce many free parameters (Table 1): in this high-dimensional problem the algorithm would be stuck in local minima. This can be overcome through a Markov Chain Monte Carlo (MCMC) analysis in Bayesian approach (e.g. [125, 81]) using the Python-based code EMCEE<sup>8</sup> [26]: the model parameters are constrained through the definition of prior distributions that encode preliminary and general information; the respective parameter space for each model parameter is derived from accurate modelling of the broadband GRB afterglows (e.g., [124, 68, 117, 100, 126, 64]), and is reported in Table 1. sAGA considers (1) uniform priors for the parameters that describe the exponential terms on the flux densities ( $A_V$ ) and the power-law indices ( $p$  and the injection index  $m$ ; Sect. 6), and (2) Jeffreys priors [49], for the parameters that span different orders of magnitudes ( $E_{K,\text{iso}}$ ,  $n_0$ ,  $A_*$ ,  $\epsilon_e$ ,  $\epsilon_B$  and  $t_j$ ).  $\epsilon_e$  and  $\epsilon_B$  are currently believed to be of the order of a few percent to tens of percent by energy [127]; therefore, their priors are truncated at an upper bound of 1/3, corresponding to their expected equipartition values (e.g. L14)<sup>9</sup>.

<sup>7</sup><http://www.scipy.org/>

<sup>8</sup><https://emcee.readthedocs.io/en/stable/>

<sup>9</sup>This consists in the equal distribution of the internal energy among the magnetic field, the accelerated

**Table 1:** Free parameter space available in sAGA, with relative range of definition (for further details, see Sect. 3).

Parameter	Unit	Description	Range definition
$p$	-	Power-law index of the electron energy distribution	$1.5 - 3.5$
$\epsilon_e$	-	Blastwave energy rate delivered to relativistic electrons	$0 - 1/3$
$\epsilon_B$	-	Blastwave energy rate delivered to magnetic fields	$0 - 1/3$
$E_{K,\text{iso}}$	$10^{52} \text{ erg}$	Kinetic energy of the explosion (in units of $10^{52} \text{ erg}$ )	$10^{-2} - 10^3$
$n_0$	$\text{cm}^{-3}$	Density for ISM-like CBM	$10^{-3} - 10^2$
$A_*$	$5 \times 10^{11} \text{ g cm}^{-1}$	Parameter connected with the wind-like density CBM	$10^{-3} - 10^2$
$A_V$	mag	Extinction in the host galaxy	$0 - 10$
$t_j$	d	Jet break time	According to the case
$t_{ei,1}$	d	Beginning time of the first injection	According to the case
$t_{ei,2}$	d	Beginning time of the second injection	According to the case
$m, m_2$	-	Injection indices ( $m_2$ in case of two bumps)	$0 - 3$ (ISM)
$m, m_2$	-	Injection indices ( $m_2$ in case of two bumps)	$0 - 1$ (wind)

In the MCMC analysis the ensemble sampler is initially run until the convergence of the average likelihood across the chains; the initial (unstable) period, called “burn-in”, is discarded (recommended Markov chains for this phase: 500). The subsequent Markov chains are set up between  $10^3$  and  $10^4$ , depending on both the complexity of the problem and the computational characteristics. As reported by L14, the convergence is checked by verifying the stability (over the length of the chain following burn-in) of the distributions; these distributions frequently exhibit long tails, and hence the quantiles are referred to compute summary statistics and quote 68% credible regions around the median. All these MCMC parameters are selectable with sAGA in the widget (Fig. 1, on the lower right) through the “Walkers”<sup>10</sup>, “Steps”, “Burn-in”, and “Sigma”<sup>11</sup> boxes; the user must be aware that high values of *Steps* ( $> 10^4$ ) correspond to high computational performance<sup>12</sup>.

## 4 GRB synchrotron emission

GRB afterglow radiation is thought to be the result of the relativistic ejecta being slowed down by the surrounding CBM [84] and takes place when a significant rate of the ejecta energy is transferred to the shocked external medium. At the early-stage of the GRB afterglow (about the first few hours), the radiative processes are responsible of the loss of a significant fraction of the kinetic energy; later, in the adiabatic phase, the radiation losses become negligible [102].

The hydrodynamics of the adiabatic phase, and the resulting synchrotron emission, is based on the theory of relativistic blastwaves [11]; this theory consists in a self-similar spherical solution for an adiabatic ultra relativistic blastwave characterised by a Lorentz factor of the shocked fluid (also known as blastwave Lorentz factor)  $\Gamma \gg 1$ . The electrons are accelerated to relativistic speed by the 1st-order Fermi acceleration mechanism, which implies a power-law distribution in terms of energy, given by:

$$N(\gamma_e)d\gamma_e \propto \gamma_e^{-p}d\gamma_e \quad (2)$$

where  $\gamma_e$  is the electron Lorentz factor, and  $p$  is the electron energy distribution power-law index, usually ranging between constrained to 1.5 and 3.5 ([44], hereafter GS02).

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electrons and the baryons (protons/neutrons).

<sup>10</sup>The user must choose an even integer; the minimum value corresponds to twice as the number of parameters, plus 2.

<sup>11</sup>We quoted the uncertainties based on the quantiles – in terms of sigma – of the samples in the marginalised distributions.

<sup>12</sup>For further details, see <https://emcee.readthedocs.io/en/stable/tutorials/line/>.

The minimum injected electron Lorentz factor  $\gamma_m$  ( $< \gamma_e$ ) in this distribution is defined as:

$$\gamma_m = \Gamma \epsilon_e \left( \frac{p - 2}{p - 1} \right) \frac{m_p}{m_e} \quad (3)$$

where  $m_e$  and  $m_p$  are the electron mass and the proton mass, respectively. In the presence of the self-generated magnetic fields, these relativistic particles lose their energy emitting synchrotron radiation. The typical synchrotron frequency of a relativistic electron depends on its Lorentz factor and – in the observer frame – is given by:

$$\nu(\gamma_e) \simeq \Gamma \gamma_e^2 \frac{q_e B}{2\pi m_e c} \quad (4)$$

where  $q_e$  is the electron charge;  $B$  is the comoving magnetic field strength.

The spectral power of a relativistic electron  $P_\nu$  with initial energy  $\gamma_e mc^2$  varies approximately as  $\nu^{1/3}$  for  $\nu < \nu(\gamma_e)$  and cuts off exponentially for  $\nu > \nu(\gamma_e)$ . The total emitted power can be expressed – in the observer frame – as:

$$P(\gamma_e) \simeq \frac{4}{3} \sigma_T c \Gamma^2 \gamma_e^2 \frac{B^2}{8\pi} \quad (5)$$

where  $\sigma_T$  is the electron Thomson cross-section. The total peak spectral power  $P_{\nu, \text{max}} \approx P(\gamma_e)/\nu(\gamma_e)$  is independent of  $\gamma_e$  and occurs at  $\nu(\gamma_e)$ .

This picture is valid only in adiabatic phase, where the electron radiates a negligible fraction of its energy, and hence until  $\gamma_e$  is less than a critical Lorentz factor  $\gamma_c$ :

$$\gamma_c = \frac{6\pi m_e c}{\Gamma \sigma_T B^2 t}, \quad (6)$$

where  $t$  is the timescale (in the observer-frame) within which an electron characterised by an initial Lorentz factor  $\gamma_e > \gamma_c$  cools down to  $\gamma_c$ . Above  $\gamma_c$ , cooling by synchrotron radiation becomes significant, so that the shape of the electron distribution is modified in the  $\gamma_e > \gamma_c$  regime [121, 31]. The electron Lorentz factors  $\gamma_m$  and  $\gamma_c$  – evolving in time – define two characteristic emission frequencies  $\nu_m$  and  $\nu_c$  in the synchrotron spectrum. Depending on the order of  $\gamma_m$  and  $\gamma_c$ , the synchrotron spectrum falls into two broad categories: fast-cooling ( $\nu_m > \nu_c$ , or  $\gamma_m > \gamma_c$ ) and slow-cooling ( $\nu_m < \nu_c$ , or  $\gamma_m < \gamma_c$ ) regimes. In the first case, all electrons with Lorentz factors above  $\gamma_c$  cool rapidly; in the second case, only the most energetic electrons cool rapidly (e.g., GS02, [121, 31]). The prompt phase of GRBs is expected to be in the fast-cooling regime [101], whereas the transition to the slow-cooling regime is expected to take place during the early stages of the afterglow ([84, 147], GS02).

Another characteristic frequency is the synchrotron self-absorption  $\nu_{sa}$ , below which the synchrotron photons are self-absorbed (e.g. [119, 58]). During the afterglow phase,  $\nu_{sa}$  is usually the smallest among the three frequencies. In particular, only in fast-cooling regime the self-absorption frequency splits in  $\nu_{ac}$  and  $\nu_{sa}$ , where an optical depth of unity is produced by noncooled electrons and all electrons, respectively ([43], GS02). When  $\nu_{sa} > \nu_c$ , the electron energy distribution may be significantly modified, resulting in inaccurate analytical models [31].

## 4.1 Evolution of GRB synchrotron spectra and light curves in sAGA

The synchrotron spectrum evolves with time as the blastwave expands, with spectral transitions occurring when two or more break frequencies cross each other. For the case of

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FS emission, sAGA modelled the synchrotron broadband spectrum with smoothly connected power-law segments, following the prescriptions described in GS02. Such a model includes synchrotron cooling and self-absorption for both ISM and wind-like CBM, resulting in 5 different spectral regimes at any given time with 11 definitions of the break frequencies – corresponding to different combinations of the synchrotron frequencies – with the time-independent micro-physics parameters  $E_{K,iso}$ ,  $p$ ,  $n_0$  (or  $A_*$ ),  $\epsilon_e$  and  $\epsilon_B$  as free parameters (see Fig. 1 in GS02).

The synchrotron light curve at a given  $\nu_{obs}$  evolves with time, undergoing temporal transitions (or power-law breaks) whenever a characteristic frequency crosses  $\nu_{obs}$ . This translates in smoothly connected power-law segments: for example,  $t_m$  and  $t_c$  are the times at which  $\nu_m$  and  $\nu_c$  cross  $\nu_{obs}$ , respectively, that is  $\nu_m(t_m) = \nu_c(t_c) = \nu_{obs}$ . As described in [121], the possible orderings of break times depend on the comparison between  $\nu_{obs}$  and  $\nu_0 = \nu_c(t_0) = \nu_m(t_0)$ , where  $t_0$  is the transition time between fast and slow cooling regimes. The regime  $\nu_{obs} > \nu_0$  defines the high-frequency light curve, where  $t_0 > t_m > t_c$ ; on the other hand, the regime  $\nu_{obs} < \nu_0$  defines the low-frequency light curve, characterised by  $t_0 < t_m < t_c$ . In sAGA light curves are calculated through a specific time-dependent weighting scheme described in L14; the transition time  $t_{trans}$  between different spectral regimes is calculated through geometric average, since sometimes in GS02 the same  $t_{trans}$  is defined by different equations.

## 5 Jetted emission and non-relativistic transition

In their work, the hydrodynamics presented by GS02 assumes isotropic expansion; however, the GRB outflow usually shows evidence for the presence of a jetted emission in the form of an achromatic break in the temporal power-law decay of the afterglow light curves. This is usually interpreted as the edge of the jet becoming visible to the observer.

In the literature there are two broad families of jets: uniform and structured. The first assumes an uniform distribution of energy and Lorentz factor within a jet cone with a sharp edge (the so-called "top-hat jet"), the second assumes an angular distribution in energy and Lorentz factor (e.g. [37, 152]). sAGA considers the uniform jet regime, because is simpler than structured jet model, based on special relativistic hydrodynamics (e.g. [23, 40, 18]); although in the latest years the growing evidence has been found that favours the structured jet, as in the case of the GRB 170817A associated to GW 170817 [4]<sup>13</sup>

The uniform jet scenario, based on purely geometrical or dynamical effects, assumes a simplified conical jet blastwave, with a half opening angle  $\theta_j$  and  $\Gamma$ , where only the emission inside the  $1/\Gamma$  cone is detectable due to relativistic beaming. During the deceleration phase – for an observer in the jet sightline –  $\Gamma$  decreases gradually until  $1/\Gamma > \theta_j$  in the form of an achromatic jet break at the jet break time  $t_j$ <sup>14</sup>. The light curve steepening can arise from two effects: the pure edge effect (e.g. [97]) and the sideways expansion effect [109, 120]. In the pure edge effect, the blastwave dynamics does not change during the jet break transition; the degree of steepening at  $t_j$  for the flux densities is defined as  $\Delta\alpha = \alpha_{post,jet} - \alpha_{pre,jet} = (3 - k)/(4 - k)$ , where  $k$  is the exponent of the density profile

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<sup>13</sup>Recently, the open-source Python package AFTERGLOWPY is available for on-the-fly computation of structured jet afterglows with arbitrary viewing angle [114].

<sup>14</sup>However, afterglow observations in the Swift era have shown a lack of achromatic breaks compared to the pre-Swift era [24]. Missing breaks are attributed to far off-axis observations [142], to poor quality of data [20], or to the break time falling beyond the end of Swift/XRT follow-up. Another possible interpretation is that the X-ray afterglow of many GRBs does not originate from external shocks but from a long-lasting central engine [86], suggesting that only the optical light curve may be suitable to identify jet breaks.

$n = A r^{-k}$  ( $k = 0$  for ISM-like CBM,  $k = 2$  for wind-like CBM, [37]). The sideways expansion effect of a conical jet, as opposed to the pure edge effect, implies that the jet exponentially decelerates when  $\Gamma \sim \theta_j^{-1}$ ; this feature translates in the change of the evolution of both the spectral break frequencies and flux densities at  $t_j$ , as described in several papers (e.g. [120, 122, 96]) and summarised in Table 5. Several numerical simulations and sophisticated analytical treatments suggest that the contribution of sideways expansion is significant up to  $\Gamma \gtrsim 2$  [38, 62, 12, 159, 42, 23, 140], even if  $\alpha = -p$  post-jet-break decay could be a reasonable rough approximation [152].

$\theta_j$  is computed, both for ISM-like and wind-like CBM, from  $t_j$  (expressed in units of days) [147, 109, 120, 16, 145] as:

$$\theta_{j,\text{ISM}} = 9.25 \left( \frac{n_0}{E_{52,k,\text{iso}}} \right)^{1/8} \left( \frac{t_j}{1+z} \right)^{3/8} \text{ deg} \quad (7)$$

$$\theta_{j,\text{wind}} = 11.55 \left[ \frac{t_j A_*}{(1+z) E_{52,k,\text{iso}}} \right]^{1/4} \text{ deg}, \quad (8)$$

where  $z$  is the redshift of the source,  $E_{52,k,\text{iso}}$  is the isotropic-equivalent kinetic energy expressed in units of  $10^{52}$  erg,  $n_0$  is the number density in units of  $\text{cm}^{-3}$ , and  $A_*$  in units of  $5 \times 10^{11} \text{ g/cm}^{15}$ . For long GRBs,  $\theta_j$  usually ranges between  $3^\circ$  and  $10^\circ$  (e.g., [10]): this results in a beaming correction factor  $f_b = 1 - \cos \theta_j$  between  $\sim 10^{-3}$  and  $\sim 10^{-2}$ , suggesting that the true released energy is two or three orders of magnitude lower than the measured  $E_{\text{iso}}$  (with a typical value of a few  $10^{51}$  erg). On the other hand, measurements of  $\theta_j$  for short GRBs are less frequent, mainly because of the faintness of their afterglows; the average  $\theta_j$  of short GRBs seems to be larger than that of long GRBs [10, 25], with beaming-corrected energies usually lower than  $10^{50}$  erg.

This picture is valid only for an on-axis observer, but the light curve behaviour also depends on the direction of the observer. Fitting X-ray data at late-time with numerical jet models suggests that the sightline for most GRBs is misaligned from the jet axis [113, 156]. For an off-axis observer, an orphan afterglow (characterised by the absence of the high-energy component) could in principle be observed at late-times. Several authors discussed the possibility of detecting orphan afterglows (e.g., [110, 92, 134, 161]). Recently [77] discovered a good candidate for an orphan afterglow of a long GRB in the radio transient source FIRST J1419+3940, characterised by decreasing brightness over the last few decades.

Finally, besides these two forms of jets, more complicated structured jets have been discussed in the literature, such as the two-component jet model. According to this model, the GRB outflow consists in a narrow jet component (usually characterised by a higher  $L_{\gamma,\text{iso}}$  and a larger  $\Gamma$ ), surrounded by a wider jet component (with a lower  $L_{\gamma,\text{iso}}$  and a smaller  $\Gamma$ ). Depending on the viewing angle, the two-component jet predicts some light curve features, such as an early jet break and late-time re-brightening [48, 99, 150]. This model was used to interpret the afterglow data for several GRBs, such as GRB 030329 [9] and GRB 080319B [105]. Moreover, this can be accommodated with the collapsar model, where a narrow and highly relativistic jet emerging from a star is surrounded by a wider, less relativistic cocoon [106, 153].

The relativistic blastwave, thanks to the interaction with the CBM, gradually decelerates, reaching the non-relativistic/Newtonian (NR) phase, when  $\gamma < \sqrt{2}$  and the electrons should

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<sup>15</sup>In the density profile  $\rho(r) = Ar^{-2}$ ,  $r$  is the radius,  $A = \dot{M}_w 4\pi V_w \equiv 5 \times 10^{11} A_* \text{ g cm}^{-1}$  is a constant proportional to the progenitor mass-loss rate  $\dot{M}_w$  (assumed constant), for a given wind velocity  $V_w = 10^3 \text{ km s}^{-1}$  and  $\dot{M}_w = 10^{-5} \text{ M}_\odot \text{ yr}^{-1}$  [16].

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be in the slow cooling scenario ( $\nu_m < \nu_c$ ), at the transition time

$$t_{\text{NR,ISM}} = 84(1+z) \left( \frac{E_{52,k,\text{iso}}}{n_0} \right)^{1/3} \text{ days} \quad (9)$$

for ISM-like CBM [147], and

$$t_{\text{NR,wind}} = 694(1+z) \left( \frac{E_{52,k,\text{iso}}}{A_*} \right) \text{ days} \quad (10)$$

for wind-like CBM [16].

In the deep Newtonian phase, the blastwave dynamics can be derived from simple scaling relations (e.g. [148]). The light curves in the NR phase are steeper than those in the relativistic phase, but are shallower than the post-jet-break phase in the relativistic regime [152]. This feature suggests that the transition from relativistic to NR phase occurs after the jet break, probably in timescales of years (e.g. [74, 159]). This holds for ISM-like environment at the late stage of the blastwave evolution, since a stellar wind ends at a termination shock beyond which the medium is already of ISM type [31, 152].

Observationally, in the optical band it is very difficult to observe the NR phase in the light curves, since the afterglow emission is strongly contaminated by the host galaxy light before reaching the NR phase. On the other hand, this transition may be more easily observed in the radio band at late-time (timescales of years), especially in the case of nearby sources (e.g. GRB 030329, [136]).

SAGA is configured so that, at the beginning of the analysis, the user can select the jet/NR regime; this choice modifies the evolution of the spectral break frequencies and flux densities at  $t_j$  (free parameter) and  $t_{NR}$ , smoothing over the transition with a fixed smoothing parameter ( $s = 5$ , [38]). For completeness, the post-break (sideways expansion) and Newtonian evolution of the spectral break frequencies are reported in Table 5, following prescriptions reported in several works ([120, 30, 96, 122, 139, 70], GS02).

## 6 Energy injection

As the shock propagates into the CBM, the blastwave decelerates: this is observed through the decay evolution in the observed light curves of GRB afterglows. Sometimes, these light curves are characterised by plateaus, probably due to the re-brightening of the GRB afterglow (e.g. [93, 73, 78, 47]). This effect consists of the energy injection into the blastwave shock, the nature of which is explained through different possible mechanisms (e.g. [158, 41, 33]).

In the models based on the long-lasting central engine, such as a spinning-down millisecond magnetar [21, 157], the blastwave is fed by a long-lasting Poynting-flux-dominated wind, defined by the power-law decay with time:

$$L(t) = L_0 \left( \frac{t}{t_0} \right)^{-q} \quad (11)$$

where  $t$  is the central engine time (corresponding to the observer time of GRB afterglow),  $L_0$  is the luminosity at the reference time  $t_0$ , and  $q \geq 0$ <sup>16</sup>. This corresponds to the temporal evolution of the blastwave energy  $E \propto t^{1-q} = t^m$ , where  $m = 1 - q$  is the “injection index”.

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<sup>16</sup>The same approach sometimes is based on  $L(t) = L_0(t/t_0)^q$  and  $q \leq 0$  (e.g. [87, 82, 141, 66]).

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An alternative type of energy injection occurs when the central engine injects a stratified ejecta with a continuous distribution of bulk Lorentz factor  $\gamma$ , defined as the ejecta mass above a certain Lorentz factor [107, 118, 135]:

$$M(> \gamma) = \gamma^{-s}. \quad (12)$$

The ejecta is moving between a maximum  $\gamma_{max}$  – corresponding to the Lorentz factor of the blastwave at the onset of energy injection  $t_{0,ei}$ ,  $\Gamma(t_{0,ei})$  – and a minimum Lorentz factor  $\gamma_{min}$ . As the blastwave decelerates, energy injection takes place when  $\Gamma(t_{0,ei}) \approx \gamma_{max}$  and hence the slower ejecta shells begin depositing energy into the blastwave. This regime lasts until the lowest energy ejecta located at  $\gamma_{min}$  have transferred their energy to the blastwave. Later, the afterglow proceeds like a standard regime, but powered by a blastwave with increased energy and Lorentz factor  $\gamma_{min}$ .

These two energy injection mechanisms can be considered equivalent through the connection between two injection parameters  $s$  and  $q$  as follows [154]:

$$s = \frac{10 - 3k - 7q + 2kq}{2 + q - k} \quad (13)$$

$$q = \frac{10 - 2s - 3k + ks}{7 + s - 2k}. \quad (14)$$

where  $k$  is the exponent of the density profile  $n = A r^{-k}$  ( $k = 0$  for ISM-like CBM, and  $k = 2$  for wind-like CBM). From Eq. (14) follows that

$$m = \frac{(3 - k)(s - 1)}{7 + s - 2k}, \quad (15)$$

where  $m$  ranges between 0 and 3 for ISM-like CBM (between 0 and 1 for wind-like CBM). Moreover,  $s$  is bounded 1 and  $\infty$  for both ISM-like CBM and wind-like CBM. In the absence of energy injection, the standard hydrodynamic evolution requires that  $m = 0$ ,  $s = 1$  or  $q = 1$  in the above expressions (e.g. [31]).

SAGA accounts for energy injection – ranging between  $t_{ei,i}$  and  $t_{ei,f}$ <sup>17</sup> (in units of days) – selecting the number of “bumps” of injected energy from the central engine (1 or 2)<sup>18</sup>. The kinetic energy in the standard afterglow regime (e.g. GS02) is modified in time according to the following broken power-law function [66]:

$$E_{52,k,iso}(t) = \begin{cases} E_{52,k,iso,f} & t \geq t_{ei,f} \\ E_{52,k,iso,f} \left( \frac{t}{t_{ei,f}} \right)^m & t_{ei,i} < t < t_{ei,f} \\ E_{52,k,iso,i} \equiv E_{52,k,iso,f} \left( \frac{t_{ei,i}}{t_{ei,f}} \right)^m & t \leq t_{ei,i} \end{cases} \quad (16)$$

for one bump of energy injection, where  $E_{52,k,iso,i}$  and  $E_{52,k,iso,f}$  are the initial and final blastwave energy (in units of  $10^{52}$  erg), respectively, and

$$E_{52,k,iso}(t) = \begin{cases} E_{52,k,iso,f} & t \geq t_{ei,f} \\ E_{52,k,iso,f} \left( \frac{t}{t_{ei,f}} \right)^{m_1} & t_{ei,i_2} < t < t_{ei,f} \\ E_{52,k,iso,f} \left( \frac{t_{ei,i_2}}{t_{ei,f}} \right)^{m_1} \left( \frac{t}{t_{ei,i_2}} \right)^{m_2} & t_{ei,i_1} < t \leq t_{ei,i_2} \\ E_{52,k,iso,f} \left( \frac{t_{ei,i_2}}{t_{ei,f}} \right)^{m_1} \left( \frac{t_{ei,i_1}}{t_{ei,i_2}} \right)^{m_2} & t \leq t_{ei,i_1} \end{cases} \quad (17)$$

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<sup>17</sup>This parameter is fixed by the observer and obtained by independent modelling of broadband light curves.

<sup>18</sup>This number will be implemented for higher values.

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for two consecutive bumps of energy injection, where  $m_1$  and  $m_2$  are the injection indices referred to the first and second bump, respectively, and  $t_{ei,i_1}$  is the beginning time (in units of days) of the first injection, lasting up to  $t_{ei,i_2}$ .

Through Eqs. 16 and 17, the temporal evolution  $t$  (in units of days) of  $\Gamma$  is assumed from the standard afterglow regime (GS02, [66]):

$$\Gamma(t)_{ISM} = 3.65 \left( \frac{E_{52,k,iso}(t)}{n_0} \right)^{1/8} \left( \frac{t}{z+1} \right)^{-3/8} \quad (18)$$

for ISM-like CBM and

$$\Gamma(t)_{wind} = 3.72 \left( \frac{E_{52,k,iso}(t)}{A_*} \right)^{1/4} \left( \frac{t}{z+1} \right)^{-1/4} \quad (19)$$

for wind-like CBM.

If the energy injection switch is enabled, sAGA works in iterative mode: the first step consists in the MCMC analysis (Sect. 3) of the simple FS (eventually with absorption and/or jet approach) for the data set after  $t_{ei,f}$  to determine the micro-physics parameters of the GRB afterglow ( $E_{52,k,iso,f}$  included). Successively, these values are assumed as starting point for the energy injection regime at  $t < t_{ei,f}$  to obtain the free parameters  $t_{ei,i}$  and  $m$  (and hence  $q$ ).

## 7 Extinction and absorption processes

sAGA accounts for possible dust extinction in optical and photoelectric absorption caused in X-rays (e.g., [72]).

The typical size of dust grains in ISM is comparable to the frequency of blue light. This results in a strong absorption and scattering by the dust grains of the blue light coming from distant objects, making (for an observer on Earth) these objects dimmer (extinction) and redder (reddening) than they really are. GRB afterglows are subject to optical extinction, which is caused by the contribution of (1) the Galactic dust along the line of sight (Galactic) and (2) the dust within the host galaxy (intrinsic). A detailed knowledge of the latter is crucial for (1) determining the intrinsic luminosity of GRB afterglows from X-ray to near-IR frequencies; (2) constraining the nature of the GRB progenitors and their environments; and (3) probing the ISM of high-redshift galaxies and the cosmic star formation history [72]. Nevertheless, dust extinction in GRB host galaxies is still poorly known, and there are different extinction curves that can be assumed to properly model optical afterglow SEDs (e.g. [52, 71, 128, 160]).

sAGA, to determine the extinction  $A_V$  (measured in the V band), adopts the extinction curves as parametrised by [98], modelled using Milky Way (MW), or the dust models for Small and Large Magellan Clouds (SMC and LMC, respectively). The extinction correction is not applied to the data set, but only to the modelling and plotting phase.

UV frequencies often are affected by the absorption by neutral hydrogen, from  $z \gtrsim 1$ . sAGA accounts for this effect through a sight-line-averaged model for the optical depth of the intergalactic medium (IGM) as described by [75], to compute the IGM transmission as a function of wavelength at the redshift of the GRB; this model considers the Ly $\alpha$  absorption by neutral hydrogen along the line of sight and photoelectric absorption by intervening systems. This effect is contained in ETAU\_MADAU library of SYNPHOT Python package [129].

Where the X-ray data set are subject to photoelectric absorption, sAGA accounts for this effect through the related hydrogen-equivalent column density  $N_H$  (in units of  $10^{22} \text{ cm}^{-2}$ ),

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obtained by a polynomial fit of the effective absorption cross-section per hydrogen atom as a function of energy in the 0.03–10 keV range assuming a given abundance pattern [89].

## 8 Radio interstellar scintillation

Inhomogeneities in the electron density distribution in the MW along the GRB line of sight scatter the flux at low frequencies ( $\lesssim 10$  GHz), causing variations in measured flux density of the source. This effect, called interstellar scintillation (ISS), is significant when the source size subtended at the scattering screen is comparable to the size of the inhomogeneities and becomes negligible as the blastwave expands [112, 35, 143, 34, 39]. Usually GRBs show a similar behaviour in their radio light curves, with variations taking place between observations on timescales ranging between hours and days (e.g. [35, 29, 27]). In the standard (and easy) picture, ISS is assumed to take place at a single “thin screen” at some intermediate distance  $d_{\text{scr}}$  (in units of kpc), typically  $\sim 1$  kpc for high Galactic latitudes.

The strength of the scattering is quantified by a dimensionless parameter, defined as [144]

$$\xi = 7.9 \times 10^3 \text{SM}^{0.6} d_{\text{scr}}^{0.5} \nu_{\text{GHz}}^{-1.7}. \quad (20)$$

where SM indicates the scattering measure (in units of  $\text{kpc m}^{-20/3}$ ).

There are in general two types of ISS: weak and strong scattering. The weak scattering occurs when  $\xi \ll 1$ , and the strong scattering regime – in turn divided into refractive and diffractive scintillation – occurs when  $\xi \gg 1$  [39]. The transition frequency  $\nu_{\text{trans}}$  between strong and weak ISS is defined as the frequency at which  $\xi = 1$  [35]:

$$\nu_{\text{trans}} = 10.4 \text{ SM}_{-3.5}^{6/17} d_{\text{scr}}^{5/17} \text{ GHz} \quad (21)$$

where  $\text{SM}_{-3.5} = (\text{SM}/10^{-3.5} \text{ m}^{-20/3} \text{ kpc})$ . ISS depends strongly on frequency: at high radio frequencies only modest flux variations are expected, while at low frequencies strong ISS effects are important. In the strong ISS regime, diffractive scintillation can produce large flux variations on timescales of minutes to hours but is only coherent across a bandwidth  $\Delta\nu = (\nu/\nu_{\text{trans}})^{3/4}$  [35, 143].

In all regimes,  $\xi$  decreases with time at all frequencies as the size of the emitting region expands, with diffractive ISS suppressing before refractive ISS. The source expansion also increases the typical timescale of the variations for both diffractive and refractive ISS [108]. In this complex situation, the contribution of ISS for each regime is measured by the modulation index  $m_{\text{scint}}$ , defined as the rms fractional flux density variation. Accurate prescription about the behaviour of  $m_{\text{scint}}$  is described in [143] and [39], only in the asymptotic regimes ( $\xi \ll 1$  for weak ISS and  $\xi \gg 1$  for strong ISS), and allows to analyse ISS only in weak/strong refractive or weak/strong diffractive scenario.

SAGA considers the ISS effect through another approach to compute  $m_{\text{scint}}$ , based on a dedicated fitting function that includes both diffractive and refractive contributions [34]. The values of  $\nu_{\text{trans}}$  and SM are estimated through the NE2001<sup>19</sup> model for the Galactic electron distribution [17]. The expected ISS contribution in the model-predicted flux density  $F_{\text{model}}$  is defined as (L14):

$$\Delta F_{\text{scint}} = m_{\text{scint}} F_{\text{model}}. \quad (22)$$

$\Delta F_{\text{scint}}$  is summed to the uncertainty of flux densities before the MCMC optimisation (Sect. 3); usually this action influences the quality of the radio data set, especially in the

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<sup>19</sup><http://www.astro.cornell.edu/~cordes/NE2001/>

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C-band (4–8 GHz; e.g. [88]), but it is extremely useful to account for the ISS effect in the modelling. Moreover, Eq. (22) is used to highlight the ISS interested range in the spectra and light curves produced by sAGA at the end of the analysis.

## 9 Inverse-Compton regime

Recently, TeV emission has first been observed from a couple of bright GRB afterglows (190114C, [76]; 180720B, [2]). The SEDs showed a double-peaked shape, with the TeV emission best explained in terms of inverse Compton (IC) up-scattering of synchrotron photons by high-energy electrons. The energies involved in the IC emission – generally occurring when  $\epsilon_B \ll \epsilon_e$  – are very large, and hence the ejecta is in a regime in which the IC cross-section decreases rapidly; as a result, a photon undergoes only a single scattering [11, 115, 97, 95, 123].

The contribution of IC emission – in terms of flux density – is typically negligible compared with synchrotron radiation, but the IC mechanism can influence the cooling for the shock-accelerated electrons and hence dominate the total cooling rate (e.g. [123, 155]). The effects of IC depend on the Compton  $y$ -parameter<sup>20</sup>, defined as

$$y = \frac{-1 + \sqrt{1 + 4\eta\epsilon_e/\epsilon_B}}{2} \quad (23)$$

where  $\eta$  is the fraction of energy that has been radiated away due both to synchrotron and IC radiation. At early-time, during the fast cooling stage of the GRB afterglow, where most of the electron energy is lost,  $\eta = 1$  and IC emission dominates over synchrotron; during the slow cooling stage at late-time,  $\eta$  decreases because  $\eta = (\nu_c/\nu_m)^{-(p-2)/2}$ , and hence the synchrotron component begins to dominate over IC scattering component [123]. Moreover, if  $y < 1$ , the IC regime can be neglected; otherwise a high-energy component (of the order of 10 MeV) appears in the spectrum and the cooling timescale is shortened by a factor  $y$  [123, 102]. As in the case of synchrotron emission, since temporal evolution of the GRB afterglow emission depends on the CBM, IC radiation is different in the case of the ISM-like and wind-like CBM.

sAGA accounts for IC emission by computing  $y$  from the FS parameters<sup>21</sup>, and hence scaling the spectral break frequencies and flux densities of the synchrotron spectrum by the appropriate powers of  $1 + y$  ([123], L14, GS02).

## 10 Test cases for sAGA

sAGA has been successfully tested on the broadband data of the afterglows of some well studied GRBs (GRB 120521C, GRB 090423, and GRB 050904). Hereafter, we briefly compare the sAGA results with what is reported the literature; our results are consistent with those reported in the literature within  $\lesssim 2\sigma$ .

### 10.1 GRB 120521C

GRB 120521C was discovered with the SWIFT/BAT [7] on 2012 May 21 at 23:22:07 UT [8]. This burst is characterised by a duration  $T_{90} = (26.7 \pm 0.4)$  s [79] and a high redshift

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<sup>20</sup>Note that this equation does not take the Klein–Nishina correction into account [91, 146, 33, 65]. This frequency-dependent correction is expected to be important only at very high frequencies,  $\nu \gtrsim 10^{18}$  Hz at  $t \gtrsim 1$  d (e.g. [155]). We therefore do not consider this effect further in this analysis.

<sup>21</sup>At the time of writing, this implementation is still work in progress.

**Table 2:** Summary statistics from MCMC analysis obtained through the analysis of L14 (first column) and sAGA (second column) with broadband data (from radio to X-ray frequencies) of GRB 120521C for a model based on a jetted (sideways-regime) FS emission with optical absorption, in ISM-like CBM. sAGA makes use of the  $\chi^2$  test to quantify the goodness of fit. Since L14 do not report any statistic that quantifies the goodness of the fit, for comparison we report for L14 the  $\chi^2_r$  obtained by fixing the parameter set found by those authors. All the uncertainties are reported at 68% ( $1\sigma$ ).

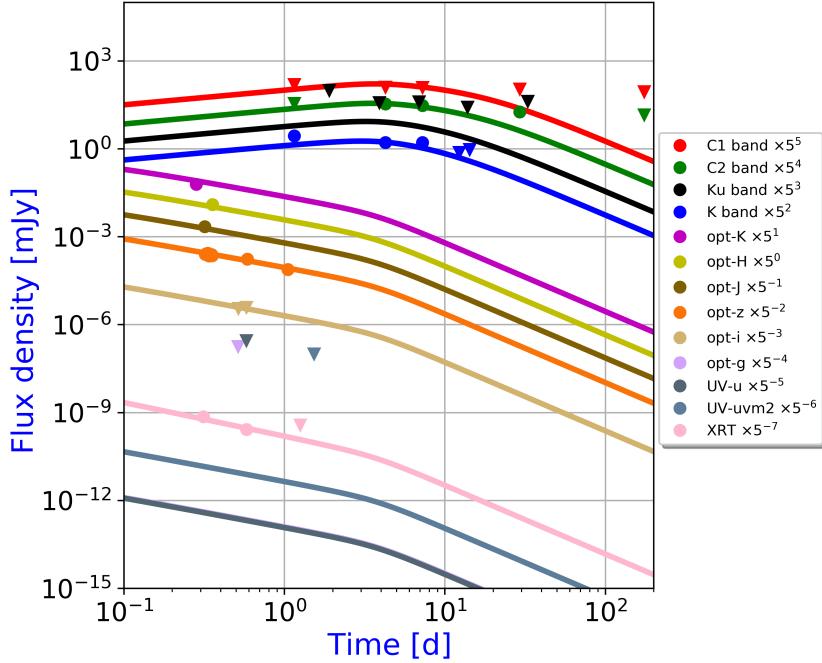
Parameter	Unit	L14	sAGA
$p$	-	$2.17^{+0.09}_{-0.07}$	$2.34 \pm 0.07$
$\epsilon_e$	-	$(4.5^{+6.7}_{-2.4}) \times 10^{-2}$	$(5.4^{+1.7}_{-1.3}) \times 10^{-2}$
$\epsilon_B$	-	$(7.0^{+0.2}_{-6.0}) \times 10^{-3}$	$(2.4^{+1.3}_{-1.1}) \times 10^{-3}$
$n_0$	$\text{cm}^{-3}$	$(2.0^{+1.0}_{-0.7}) \times 10^{-3}$	$(6.8^{+4.4}_{-2.8}) \times 10^{-2}$
$E_{52}$	$10^{52} \text{ erg}$	$(2.2^{+3.7}_{-1.4}) \times 10^1$	$(2.6^{+4.8}_{-5.9}) \times 10^1$
$A_v$	mag	$< 0.05$	$(3.1^{+2.1}_{-2.0}) \times 10^{-2}$
$t_j$	d	$6.8^{+3.8}_{-2.4}$	$3.2^{+2.3}_{-1.3}$
$\theta_j$	deg	$3.0^{+2.3}_{-1.1}$	$3.2^{+0.8}_{-0.6}$
$\nu_m^{\text{a}}$	Hz	$5.5 \times 10^{11}$	$7.6 \times 10^{11}$
$\nu_c^{\text{a}}$	Hz	$1.2 \times 10^{16}$	$7.4 \times 10^{16}$
$\nu_{sa}^{\text{a}}$	Hz	$\lesssim 5.0 \times 10^9$	$4.5 \times 10^8$
$\nu_{ac}^{\text{a}}$	Hz	-	$1.8 \times 10^{10}$
$\chi^2_r$	-	1.4	1.1

<sup>a</sup> Measured at  $t_{obs} = 1$  d.

( $z \approx 6$ , L14). The afterglow of GRB 120521C was observed with several facilities from radio to X-rays (VLA, optical/NIR telescopes, SWIFT/XRT) between  $\sim 10^{-3}$  d to  $\sim 200$  d after the GRB trigger time, and it is described in terms of FS emission with jet break and dust extinction.

As reported by L14, data prior to 0.25 d are ignored because the X-ray light curve displays a steep decline before  $\sim 0.01$  d, possibly connected to the high-latitude component of the prompt emission (e.g. [63]), followed by a plateau phase extending up to  $\sim 0.25$  d, usually attributed to the energy injection (e.g. [93, 154]). The broadband analysis of the GRB 120521C data after 0.25 d with sAGA, the best-fit model of which is shown in Fig. 3, is compared with the results by L14: in both treatments, an ISM model provides a good fit to the broadband data. As displayed in Table 2, several parameters are consistent with those reported by L14 within  $\sim 1\sigma$  ( $\epsilon_e$ ,  $\epsilon_B$ ,  $E_{52}$ ,  $A_V$ ,  $t_j$  and  $\theta_j$ ), and  $\sim 2\sigma$  ( $p$ ). The self-absorption frequency obtained with sAGA lies below the VLA frequencies, and is therefore not fully constrained; this conclusion is compatible with L14, who also constrained this frequency between  $1.75 \times 10^8$  Hz and  $2.7 \times 10^9$  Hz, with our value lying in between ( $4.5 \times 10^8$  Hz).

Finally, the two values of  $p$  (Table 2) are also compatible with the one inferred from the optical/X-ray SEDs alone. In this approach, an empirical power-law fit of the optical/X-ray SED at  $\sim 0.3$  d after the explosion yields  $\beta = -0.58^{+0.08}_{-0.06}$ . At this time the afterglow spectrum is in slow cooling regime ( $\nu_m < \nu_c$ ), resulting in  $\beta = (1 - p)/2$ , and hence  $p = 1 - 2\beta = 2.16^{+0.12}_{-0.16}$ , compatible with both analyses.



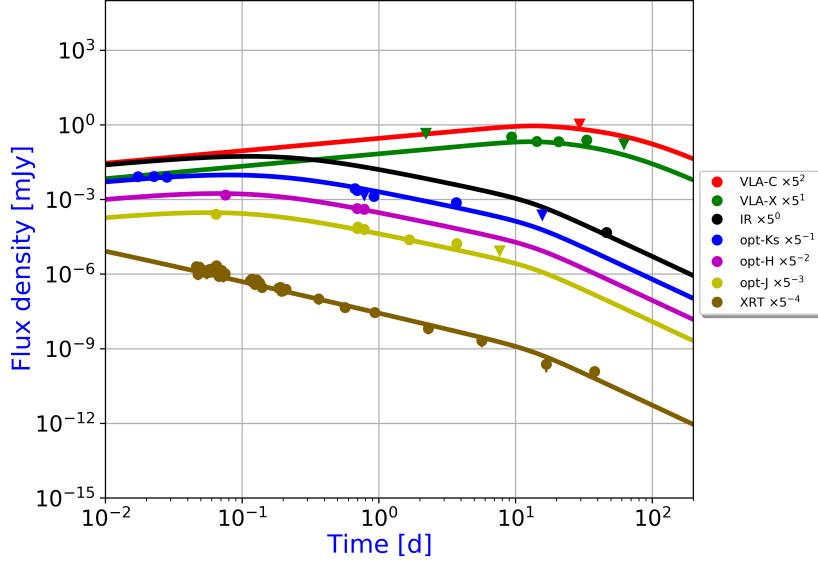
**Figure 3:** Broadband modelling of GRB 120521C for a FS model with an ISM-like CBM (GS02). Filled circles indicate detections, and upside down triangles indicate  $3\sigma$  upper limits. The physical parameters of the burst derived from the best-fit solution are listed in Table 2 (fourth column).

## 10.2 GRB 090423

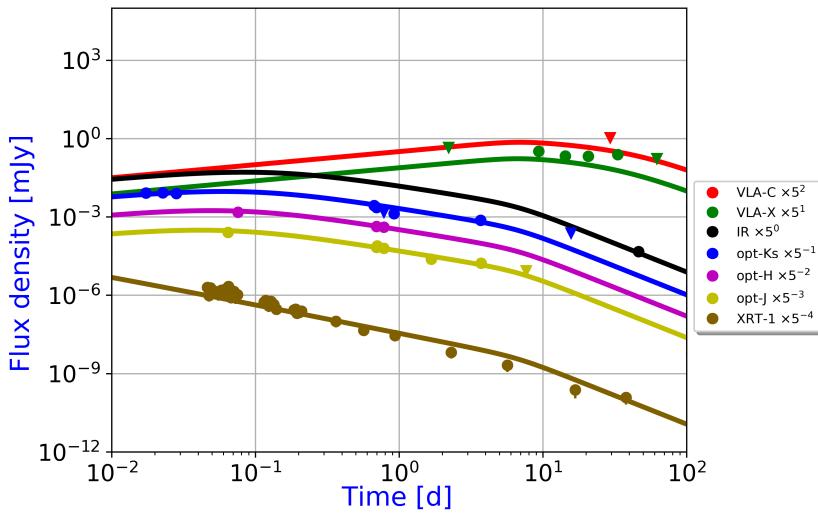
GRB 090423 was discovered with the SWIFT/BAT [7] on 2009 April 23 at 7:55:19 UT [61]. This burst is characterised by a duration  $T_{90} = 10.3 \pm 1.1$  s [94] and a high redshift ( $z = 8.26$ , [116, 132]). The afterglow of GRB 090423 was observed with several facilities from radio to high-energies (VLA, CARMA, optical/NIR telescopes, SWIFT/XRT) between  $\sim 10^{-2}$  d to  $\sim 280$  d after the GRB triggering, and it is described in terms of FS, jet break, and dust extinction.

The millimeter data are ignored because they are probably affected by RS radiation (L14). sAGA results are found to agree with those of L14, obtaining a very good fit with an ISM model. We followed the same approach as those authors and fixed the power-law index of the electron energy distribution ( $p = 2.56$ , based on their best-fit value); our result is in good accordance. Our best-fit model in ISM-like CBM is shown in Fig. 4 and the corresponding physical parameters are listed in Table 3 (third column). Both solutions are consistent with each other within  $\sim 1\sigma$ . Moreover, thanks to sAGA we estimated that the non-relativistic regime occurs at  $t_{NR} = (5.1^{+1.7}_{-1.3}) \times 10^4$  d since the GRB. Finally, the self-absorption frequency  $\nu_{sa}$  obtained with sAGA is not fully constrained because it lies below the VLA frequencies, compatibly with L14, who also constrained this frequency between  $6.8 \times 10^6$  Hz and  $3.1 \times 10^8$  Hz, with my value being  $3 \times 10^7$  Hz.

The fixed parameter  $p = 2.56$  is also compatible with what inferred from optical/X-ray SEDs alone. In this approach, the empirical power-law fit of the optical/X-ray SEDs at 0.07 d and 0.7 d implies  $\beta = -0.7 \pm 0.2$ . Since the synchrotron spectrum is in slow cooling regime ( $\nu_m < \nu_c$ ) at these epochs,  $\beta = (1-p)/2$ , and hence  $p = 1 - 2\beta = 2.4 \pm 0.4$ . Therefore, we analysed the broadband data from GRB 090423 with  $p$  as a free parameter, obtaining the results reported in Table 3 (fourth column). Fig. 5 shows our best-fit model in ISM-like



**Figure 4:** Broadband modelling of GRB 090423 for a FS model with an ISM-like CBM (GS02), with  $p = 2.56$ . See the caption of Fig. 3 for a full description of the symbols. The physical parameters of the burst derived from the best-fit solution are listed in Table 3 (fourth column).



**Figure 5:** Broadband modelling of GRB 090423 for a FS model with an ISM-like CBM (GS02), with  $p$  as free parameter. See the caption of Fig. 3 for a full description of the symbols. The physical parameters of the burst derived from the best-fit solution are listed in Table 3 (fifth column).

**Table 3:** Summary statistics from the modelling obtained through the analysis of L14 (first column), and sAGA (second and third columns) with broadband data (from radio to X-ray frequencies) of GRB 090423 for a model based on a jetted (sideways-regime) FS emission with optical absorption, in ISM-like CBM. The uncertainties are reported at 68% ( $1\sigma$ ).

Parameter	Unit	L14	sAGA	sAGA
$p$	-	2.56 (fixed)	2.56 (fixed)	$2.31_{-0.09}^{+0.17}$
$\epsilon_e$	-	$(2.7_{-0.7}^{+2.0}) \times 10^{-2}$	$(5.1_{-0.8}^{+1.0}) \times 10^{-2}$	$(3.0_{-0.4}^{+1.0}) \times 10^{-2}$
$\epsilon_B$	-	$(4.8_{-3.9}^{+9.5}) \times 10^{-2}$	$(6.7_{-3.1}^{+5.9}) \times 10^{-3}$	$(2.2_{-1.7}^{+0.8}) \times 10^{-1}$
$n_0$	$\text{cm}^{-3}$	$(2.5_{-0.3}^{+0.6}) \times 10^{-5}$	$(0.6_{-0.4}^{+0.8}) \times 10^{-5}$	$(4.4_{-3.1}^{+6.4}) \times 10^{-5}$
$E_{52}$	$10^{52} \text{ erg}$	$(3.4_{-1.4}^{+1.1}) \times 10^2$	$(1.8 \pm 0.4) \times 10^2$	$(1.3_{-0.6}^{+2.1}) \times 10^2$
$A_v$	mag	$0.15 \pm 0.02$	$0.11 \pm 0.02$	$(8.8_{-1.9}^{+2.7}) \times 10^{-2}$
$t_j$	d	$14.6_{-2.3}^{+2.7}$	$13.5 \pm 2.7$	$7.6_{-1.5}^{+5.5}$
$\theta_j$	deg	$1.5_{-0.3}^{+0.7}$	$2.2 \pm 0.3$	$1.3 \pm 0.5$
$\nu_m^{\text{a}}$	Hz	$7.7 \times 10^{12}$	$8.1 \times 10^{12}$	$3.9 \times 10^{12}$
$\nu_c^{\text{a}}$	Hz	$4.5 \times 10^{17}$	$4.9 \times 10^{17}$	$1.3 \times 10^{16}$
$\nu_{sa}^{\text{a}}$	Hz	$\lesssim 8.0 \times 10^9$	$3.0 \times 10^7$	$1.8 \times 10^8$
$\nu_{ac}^{\text{a}}$	Hz	-	$1.0 \times 10^9$	$2.3 \times 10^9$
$\chi_r^2$	-	1.2	0.9	1.3

<sup>a</sup> Measured at  $t_{obs} = 1$  d.

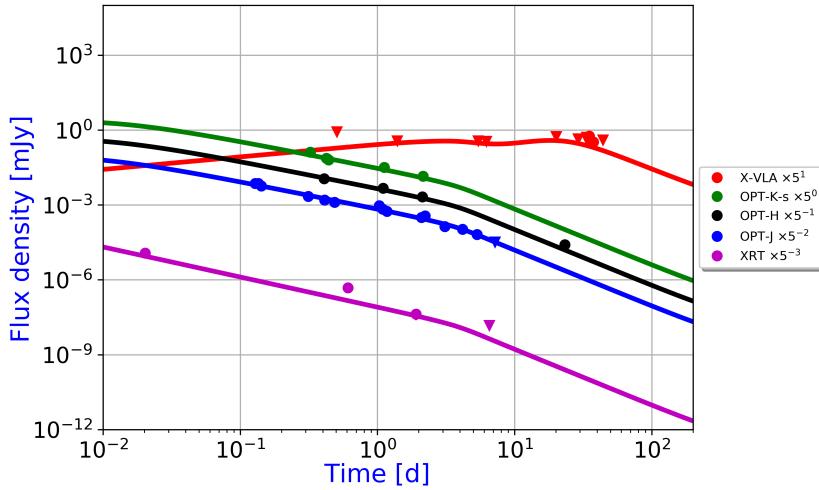
CBM. Both solutions are consistent with each other within  $\sim 1\sigma$ . The non-relativistic regime sets in at  $t_{NR} = (1.1 \pm 0.3) \times 10^5$  d after the GRB. Finally, the different value of  $t_j$  (and  $\theta_j$ ) obtained through this approach is part of a debate about the presence of jetted emission for this GRB: for example, a previous analysis of GRB 090423 claimed no jet break up to  $\sim 45$  d [14].

### 10.3 GRB 050904

This GRB was discovered with SWIFT/BAT on 2005 September 4 at 1:51:44 UT [19] and it is characterised by a high redshift ( $z = 6.29$ , [131, 46, 55]). Broadband data (at radio, optical and X-ray frequencies) are taken from the papers of [36] (hereafter G07) and L14, which describe the GRB afterglow emission in terms of FS, jet break, and dust extinction. Our results are compared with G07 and L14; as in previous studies of this burst ([28], G07 and L14), we find that an ISM model works better than a wind one. Our best-fit model is shown in Fig. 6 and the corresponding physical parameters are listed in Table 4 (third column).

Almost all the parameters obtained with sAGA are consistent with those in the literature within  $\sim 1\sigma$  ( $\epsilon_e$ ,  $A_V$ , and  $\theta_j$ ) and  $\sim 2\sigma$  ( $\epsilon_B$ ,  $E_{k,iso,52}$ ); moreover, we estimated that the non-relativistic regime occurs at  $t_{NR} = (4.3_{-0.9}^{+1.1}) \times 10^2$  d after the GRB. The jet break time of  $t_j = 3.6$  d inferred by my analysis is later than different values reported in the literature ( $t_j = 2.6 \pm 1$  d, [131];  $t_j = 2.63 \pm 0.37$  d, [53]; Table 4), but it is consistent with them within  $\sim 2\sigma$ .

Finally, our derived value of the  $p$  is compatible with the value obtained by G07 within  $\sim 2\sigma$ , and apparently incompatible with the value obtained by L14. This value, as reported by G07, is explainable through the achromatic break interpretation of GRB afterglow light curves, where the post-jet-break decay index is predicted to be  $\alpha = -p$  (Sect. 5); as reported by [131], in the jetted scenario the multiple NIR light curves of the afterglow after  $t_j$  are



**Figure 6:** Broadband modelling of GRB 050904 for a FS model with an ISM-like CBM (GS02). See the caption of Fig. 3 for a full description of the symbols. The physical parameters of the burst derived from the best-fit solution are listed in Table 4 (fifth column).

described by a decay with power-law index  $\alpha = p = 2.4 \pm 0.4$ , consistent with the values of  $p$  reported in Table 4.

**Table 4:** Summary statistics from the modelling obtained through the analysis of G07 (first column), L14 (second column), and sAGA (third column) with broadband data (from radio to X-ray frequencies) of GRB 050904 for a model based on a jetted (sideways-regime) FS emission with optical absorption, in ISM-like CBM. All the uncertainties are reported at 68% ( $1\sigma$ ).

Parameter	Unit	G07	L14	sAGA
$p$	-	$2.15 \pm 0.04$	$2.07 \pm 0.02$	$2.29 \pm 0.03$
$\epsilon_e$	-	$(3.1^{+2.5}_{-1.8}) \times 10^{-2}$	$(1.2^{+1.5}_{-0.5}) \times 10^{-2}$	$(2.5^{+0.6}_{-0.5}) \times 10^{-2}$
$\epsilon_B$	-	$(2.0^{+1.9}_{-1.5}) \times 10^{-1}$	$(1.3^{+2.2}_{-1.1}) \times 10^{-2}$	$(1.3^{+0.5}_{-0.2}) \times 10^{-3}$
$n_0$	$\text{cm}^{-3}$	$84.4^{+188.6}_{-58.4}$	$(6.3 \pm 0.1) \times 10^2$	$(9.5^{+7.5}_{-3.8}) \times 10^2$
$E_{52}$	$10^{52} \text{ erg}$	$(2.2^{+3.1}_{-0.9}) \times 10^1$	$(1.7^{+1.2}_{-1.0}) \times 10^2$	$(3.5^{+1.1}_{-0.9}) \times 10^1$
$A_v$	mag	$3.4^{+4.6}_{-1.6} \times 10^{-2}$	$< 0.05$	$(7.5^{+37.6}_{-5.7}) \times 10^{-4}$
$t_j$	d	$3.2 \pm 0.2$	$1.5^{+0.2}_{-0.1}$	$3.6^{+0.7}_{-0.4}$
$\theta_j$	deg	$7.3^{+3.0}_{-0.5}$	$6.2^{+3.3}_{-1.4}$	$8.2^{+1.1}_{-0.9}$
$\nu_m^{\text{a}}$	Hz	-	-	$3.7 \times 10^{12}$
$\nu_c^{\text{a}}$	Hz	-	-	$3.5 \times 10^{14}$
$\nu_{sa}^{\text{a}}$	Hz	-	-	$7.8 \times 10^{10}$
$\nu_{ac}^{\text{a}}$	Hz	-	-	$3.4 \times 10^{11}$
$\chi^2_r$	-	$1.4^{\text{b}}(1.02)^{\text{c}}$	1.4	0.73

<sup>a</sup> Measured at  $t_{obs} = 0.1$  d.

<sup>b</sup> Value reported in [36].

<sup>c</sup> This value is obtained with sAGA fixing the parameters to those of G07.

Break frequency	Spectrum	Evolution of break frequency, $\nu \propto t^\alpha$				Evolution of flux density, $F_{\nu,b,ext} \propto t^\beta$			
		Spherical model		$t > t_{jet}$	$t > t_{NR}$	Spherical model	$t > t_{jet}$	$t > t_{NR}$	
		ISM	Wind	ISM	Wind	ISM	Wind	ISM	Wind
1 - $\nu_{sa}$	1	0	-3/5	-1/5	6/5	2/15	-1/5	-2/5	2/5
2 - $\nu_m$	1	-3/2	-3/2	-2	-3	-7/3	0	-1/2	-1
3 - $\nu_c$	1,2	-1/2	1/2	0	-1/5	-	$\frac{1-p}{2}$	$\frac{1-p}{2}$	$\frac{3-p}{5}$
4 - $\nu_m$	2,3	-3/2	-3/2	-2	-3	-7/3	$\frac{-5/2}{2}$	-2	$\frac{-p}{5}$
5 - $\nu_{sa}$	2	$-\frac{3p+2}{2(p+4)}$	$-\frac{3(p+2)}{2(p+4)}$	$-\frac{2(p+1)}{p+4}$	$-\frac{3p-2}{p+4}$	$-\frac{7p+6}{3(p+4)}$	$-\frac{5p-5}{2(p+4)}$	-4	-4
6 - $\nu_{sa}$	3	$-\frac{3(p+1)}{2(p+5)}$	$-\frac{3p+5}{2(p+5)}$	$-\frac{2(p+1)}{p+5}$	$-\frac{3p-2}{p+4}$	$-\frac{5(p-1)}{2(p+5)}$	$-\frac{4p+1}{2(p+5)}$	$\frac{47-32p}{5(p+4)}$	$\frac{7-12p}{3(p+4)}$
7 - $\nu_{ac}$	4,5	3/10	0	2/5	-	-	11/10	1	$\frac{4p+1}{p+5}$
8 - $\nu_{sa}$	4	-1/2	-2/3	-2/3	6/5	-	0	1/12	-2/3
9 - $\nu_m$	4,5	-3/2	-3/2	-2	-3	-	1/2	1/2	0
10 - $\nu_{sa}$	5	-1/2	-8/5	-6/5	6/5	-	0	-8/5	-7/5
11 - $\nu_c$	5	-1/2	1/2	0	-1/5	-	0	-1/2	-1

**Table 5:** Evolution of spectral break frequencies and peak flux densities – connected with the spectra showed in Fig. ?? – before (GS02) and after [120, 122, 96] the jet break and the transition to non-relativistic expansion [30, 139, 70].

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## 11 Conclusions and future development

This technical note illustrates the Python code sAGA (Software for AfterGlow Analysis), which aims to broadband modelling of GRB afterglows based on an analytical approach.

Built adopting a Bayesian statistics, our code adds up to other pre-existing broadband fitting packages in the literature (e.g. [56, 12, 138, 151, 23, 68, 69, 111, 3, 114, 6]) and provides an independent tool, concerning the broadband study of GRB afterglows over the last two decades. sAGA performs simultaneously a broadband data analysis – from radio to gamma-rays frequencies – in a single iteration through a new approach that consists in the manipulation of all the data both at each observing epoch  $t_{obs}$  and observing frequency  $\nu_{obs}$ , considering different radiation processes and other aspects, described in this technical note. This approach allows the user to estimate in one fell swoop the micro-physics parameters of the GRB afterglow and other physical information that characterises the explosion.

sAGA has been successfully tested on the broadband data set of the afterglows of GRB 120521C, GRB 090423, and GRB 050904. Our results are consistent with those reported in the literature (especially L14, who make use of a similar approach for the characterisation of the GRB afterglow) within  $\lesssim 2\sigma$ . Moreover, the values of  $p$  are compatible with the inferences based on the lines of reasoning based on the observation of the optical/X-ray SEDs.

Another successful application of sAGA concerned the rich and challenging data set of GRB 160131A (Marongiu et al., submit.). Furthermore, the ISS tool has been applied to the radio data set of GRB 190114C [88].

Upon a specific computational improvement and more robust test phase with other sources, sAGA could be even more competitive among the other broadband fitting tools thanks to future implementation of other radiation mechanisms that could contribute to GRB afterglows (IC emission is nearing completion and RS regime is incomplete and currently unavailable). Moreover, other physical aspects could be added, such as more complex jet structures (e.g., either the so-called structured or two-component jet models), and more bumps for energy injection regime (currently sAGA accepts up to two bumps). These improvements are crucial for a future sharing of sAGA with the international community; for further information and collaboration, the reader is encouraged to contact the authors of this technical note.

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